Centre No.					Pape	er Refer	ence			Surname	Initial(s)
Candidate No.			6	6	6	5	/	0	1	Signature	

Paper Reference(s)

6665/01

Edexcel GCE

Core Mathematics C3

Advanced

Wednesday 20 January 2010 - Afternoon

Time: 1 hour 30 minutes

Materials required for examination
Mathematical Formulae (Pink or

Items included with question papers

- \overline{N}

Mathematical Formulae (Pink or Green)

Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions to Candidates

In the boxes above, write your centre number, candidate number, your surname, initials and signature. Check that you have the correct question paper.

Answer ALL the questions.

You must write your answer to each question in the space following the question.

When a calculator is used, the answer should be given to an appropriate degree of accuracy.

Information for Candidates

A booklet 'Mathematical Formulae and Statistical Tables' is provided.

Full marks may be obtained for answers to ALL questions.

The marks for individual questions and the parts of questions are shown in round brackets: e.g. (2).

There are 9 questions in this question paper. The total mark for this paper is 75.

There are 28 pages in this question paper. Any blank pages are indicated.

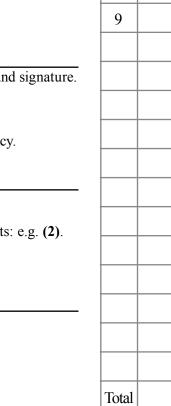
Advice to Candidates

You must ensure that your answers to parts of questions are clearly labelled. You should show sufficient working to make your methods clear to the Examiner. Answers without working may not gain full credit.

This publication may be reproduced only in accordance with Edexcel Limited copyright policy.

Printer's Log. No. N35381A W850/R6665/57570 5/5/5/4/3/3





Examiner's use only

Team Leader's use only

1

3

4

5

6

7

8

Turn over



Leave
blank

	$\frac{x+1}{3x^2-3} - \frac{1}{3x+1}$	
as a single fraction in its		
as a single fraction in its	simplest form.	(4)

Question 1 continued	Leave blank
	01
(Total 4 marks)	Q1

2.

$$f(x) = x^3 + 2x^2 - 3x - 11$$

(a) Show that f(x) = 0 can be rearranged as

$$x = \sqrt{\left(\frac{3x+11}{x+2}\right)}, \quad x \neq -2.$$

(2)

Leave blank

The equation f(x) = 0 has one positive root α .

The iterative formula $x_{n+1} = \sqrt{\left(\frac{3x_n + 11}{x_n + 2}\right)}$ is used to find an approximation to α .

- (b) Taking $x_1 = 0$, find, to 3 decimal places, the values of x_2 , x_3 and x_4 .
- (c) Show that $\alpha = 2.057$ correct to 3 decimal places.

(3)

(3)

Question 2 continued	Leav blan	re k
	_	
	_	
	_	
	_	
	_	
	_	
	_	
	_	
	_	
	_	
	_	
	_	
	_	
	_	
	_	
	_	
	Q2	
(Total 8 marl	ks)	

(a) Express $5\cos x - 3\sin x$ in the form $R\cos(x + \alpha)$, where $R > 0$ and $0 < \alpha < \frac{1}{2}\pi$	5.
	(4)
(b) Hence, or otherwise, solve the equation	
$5\cos x - 3\sin x = 4$	
for $0 \le x < 2\pi$, giving your answers to 2 decimal places.	
	(5)

Question 3 continued	Leave blank
	Q3
(Total 9 marks)	

Leave)
blank	1

(i) Given that $y = \frac{\ln(x^2 + 1)}{x}$, find $\frac{dy}{dx}$.	
	(4)
(ii) Given that $x = \tan y$, show that $\frac{dy}{dx} = \frac{1}{1+x^2}$.	
$dx = 1 + x^2$	(5)
	(3)

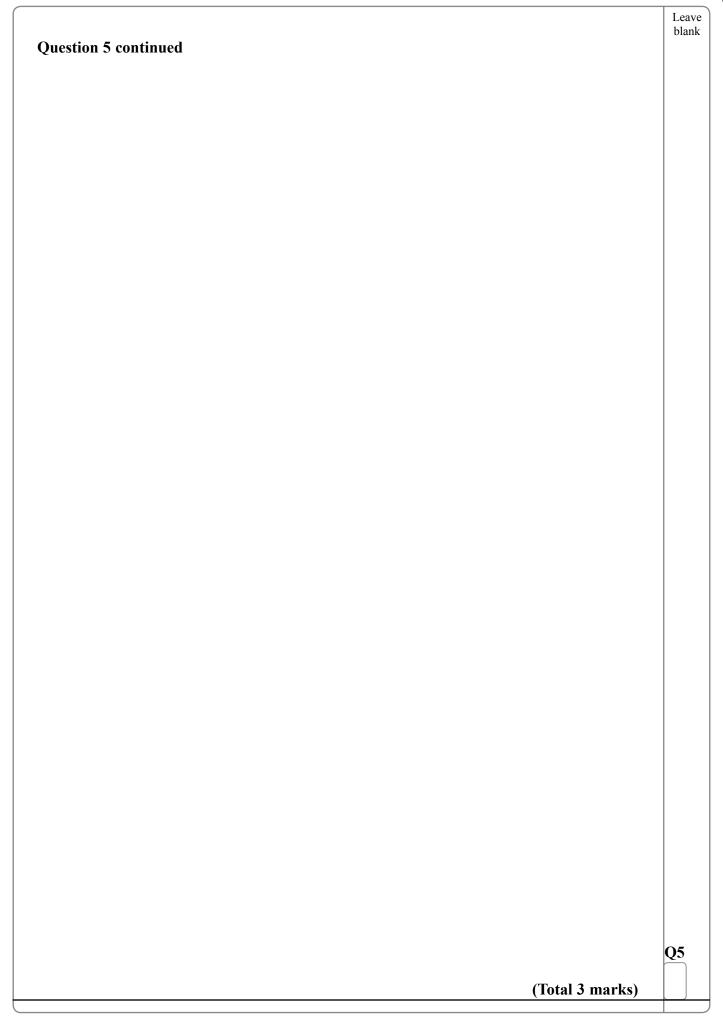
Question 4 continued	Leave blank

uestion 4 continued	

Question 4 continued		Leav
	(Total 9 marks)	Q4

Sketch the graph of $y = \ln x $, stating the coordinates of any points of intersection with axes.	
	(3)

Leave blank



6.

Leave blank

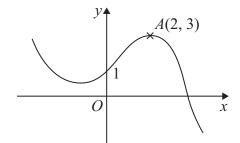


Figure 1

Figure 1 shows a sketch of the graph of y = f(x).

The graph intersects the y-axis at the point (0, 1) and the point A(2, 3) is the maximum turning point.

Sketch, on separate axes, the graphs of

(i)
$$y = f(-x) + 1$$
,

(ii)
$$y = f(x+2) + 3$$
,

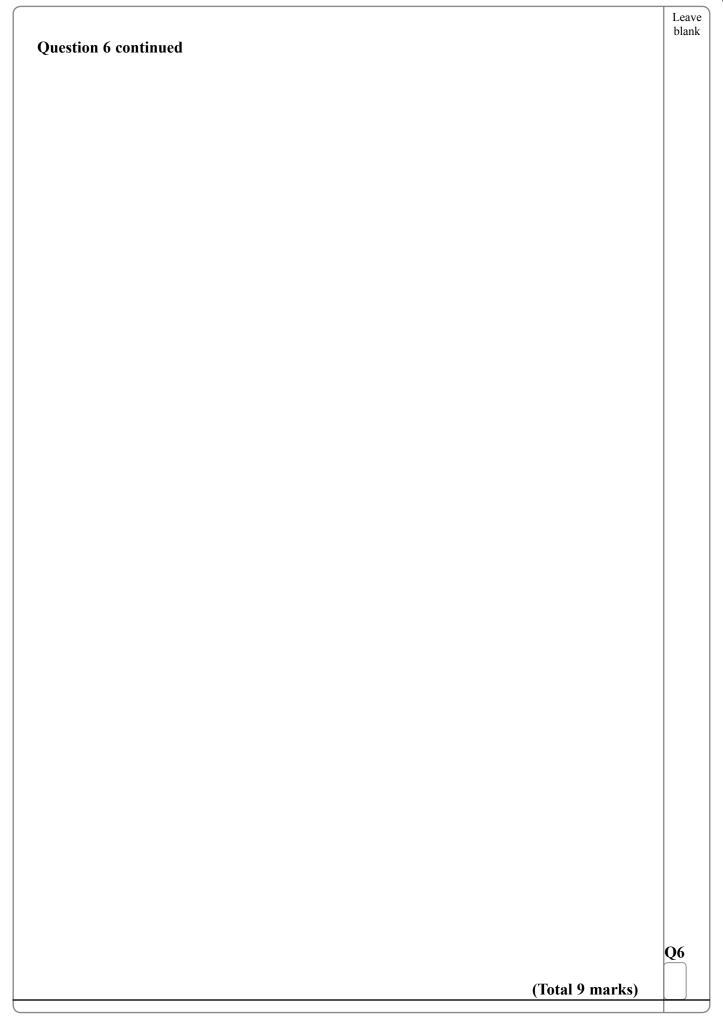
(iii)
$$y = 2f(2x)$$
.

On each sketch, show the coordinates of the point at which your graph intersects the y-axis and the coordinates of the point to which A is transformed.

(9)

Question 6 continued	blank

Question 6 continued	Leave blank



(a) By writing $\sec x$ as $\frac{1}{\cos x}$, show that $\frac{d(\sec x)}{dx} = \sec x \tan x$	<i>X</i> .
cos a ua	(3)
Given that $y = e^{2x} \sec 3x$,	
(b) find $\frac{dy}{dx}$.	
dx	(4)
	(4)
The curve with equation $y = e^{2x} \sec 3x$, $-\frac{\pi}{6} < x < \frac{\pi}{6}$, has a mit (a, b) .	nimum turning point at
(c) Find the values of the constants a and b, giving you figures.	ur answers to 3 significant
1.541.441	(4)

	Leave blank
Question 7 continued	

Question 7 continued	

Question 7 continued	Leave blank
	_
	_
	_
	_
	_
	_
	_
	_
	_
	_
	_
	_
	_
	_
	_
	Q7
(Total 11 mar)	ks)

		$\csc^2 2x - \cot 2x = 1$
for ($0 \leqslant x \leqslant 180^{\circ}$.	
		(7

Question 8 continued	Lea bla
	Q8
(Tot	al 7 marks)

Leave	
blank	

9. (i) Find the exact solutions to the equations	
(a) $\ln(3x - 7) = 5$	(3)
(b) $3^x e^{7x+2} = 15$	
$(0) \ \ 3 \ \ -13$	(5)
(ii) The functions f and g are defined by	
$f(x) = e^{2x} + 3, \qquad x \in \mathbb{R}$	
$g(x) = \ln(x - 1), \qquad x \in \mathbb{R}, \ x > 1$	
(a) Find f^{-1} and state its domain.	(4)
	(4)
(b) Find fg and state its range.	(3)

Question 9 continued	Leave blank

Question 9 continued	l

Question 9 continued	Leave blank

Question 9 continued		blan
	(Total 15 marks)	Q
	(IULAI IS IIIAI KS)	