Algorithm $\overline{1 \text{ A}^*}$

```
1: procedure MAIN()
        open := closed := \phi;
 3:
        g(s_{start}) := 0;
        parent(s_{start}) := s_{start};
 4:
        open.Insert(s_{start}, g(s_{start}) + h(s_{start}));
 5:
        while open \neq \phi \ \mathbf{do}
 6:
            s := open.Pop();
 7:
 8:
            if s = s_{goal} then return "success";
            closed := closed \cup \{s\};
 9:
            for each s' \in nghbr(s) do
10:
                if s' \notin closed then
11:
                    if s' \notin open then
12:
                        g(s') := \infty;
13:
                        parent(s') := NULL;
14:
                    UpdateVertex(s, s');
15:
        {\bf return}\ "fail";
16:
17:
    procedure UPDATEVERTEX(S, S')
18:
        g_{old} := g(s');
19:
        ComputeCost(s, s');
20:
        if g(s') < g_{old} then
21:
            if s' \in open then
22:
                open.Remove(s');
23:
            open.Insert(s^{'},g(s^{'})+h(s^{'});
24:
25:
    procedure ComputeCost(s, s')
26:
        if g(s) + c(s, s') < g(s') then
27:
            parent(s') := s;
28:
            g(s') := g(s) + c(s, s');
29:
```

Algorithm 2 Theta*

```
1: procedure MAIN()
2:
       open := closed := \phi;
       g(s_{start}) := 0;
3:
       parent(s_{start}) := s_{start};
4:
       open.Insert(s_{start}, g(s_{start}) + h(s_{start}));
5:
       while open \neq \phi \ \mathbf{do}
6:
           s := open.Pop();
7:
           if s = s_{qoal} then return "success";
8:
           closed := closed \cup \{s\};
9:
           for each s^{'} \in nghbr(s) do
10:
               if s' \notin closed then
11:
                   if s' \notin open then
12:
13:
                       g(s') := \infty;
                       parent(s') := NULL;
14:
                   UpdateVertex(s, s');
15:
       return "fail";
16:
17:
   procedure UPDATEVERTEX(S, S')
18:
       g_{old} := g(s');
19:
        ComputeCost(s, s');
20:
       if g(s') < g_{old} then
21:
           if s' \in open then
22:
               open.Remove(s');
23:
           open.Insert(s', g(s') + h(s');
24:
25:
    procedure ComputeCost(s, s')
26:
       if lineOfSight(parent(s), s') then
27:
            /*Path2*/
28:
           if g(parent(s)) + c(parent(s), s') < g(s') then
29:
               parent(s') := parent(s);
30:
               g(s') := g(parent(s)) + c(parent(s), s');
31:
32:
       else
            /*Path1*/
33:
           if g(s) + c(s, s') < g(s') then
34:
               parent(s') := s;
35:
               g(s') := g(s) + c(s, s');
36:
```

Algorithm 3 Lazy Theta*

```
1: procedure MAIN()
 2:
        open := closed := \phi;
 3:
        g(s_{start}) := 0;
        parent(s_{start}) := s_{start};
 4:
        open.Insert(s_{start}, g(s_{start}) + h(s_{start}));
 5:
        while open \neq \phi do
 6:
            s := open.Pop();
 7:
 8:
           SetVertex(s);
           if s = s_{qoal} then return "success";
 9:
            closed := closed \cup \{s\};
10:
           for each s' \in nghbr(s) do
11:
                if s' \notin closed then
12:
                   if s' \notin open then
13:
                       g(s') := \infty;
14:
                       parent(s^{'}) := NULL;
15:
                    UpdateVertex(s, s');
16:
        return "fail";
17:
18:
19: procedure UPDATEVERTEX(S, S')
20:
        g_{old} := g(s');
        ComputeCost(s, s');
21:
22:
        if g(s') < g_{old} then
           if s' \in open then
23:
                open.Remove(s');
24:
            open.Insert(s', g(s') + h(s');
25:
26:
    procedure ComputeCost(s, s')
        /*Path2*/
28:
        if g(parent(s)) + c(parent(s), s') < g(s') then
29:
           parent(s') := parent(s);
30:
           g(s') := g(parent(s)) + c(parent(s), s');
31:
32:
   procedure SetVertex(s)
33:
        if !lineOfSight(parent(s), s) then
34:
            /*Path1*/
35:
           parent(s) := argmin_{s' \in nghbr(s) \cap closed}(g(s') + c(s', s));
36:
           g(s) := min_{s^{'} \in nghbr(s) \cap closed}(g(s^{'}) + c(s^{'},s));
37:
```