# **CSCE 156 – Computer Science II**

Lab 08 - Recursion

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#### Prior to Lab

- 1. Review this laboratory handout prior to lab.
- 2. Review the lecture notes on recursion.

### Lab Objectives & Topics

Following the lab, you should be able to:

- Be familiar with recursive methods in the Java programming language
- Be able to evaluate and empirically analyze recursive methods

#### Recursion

Recursion is a programming approach common to a "divide and conquer" algorithm strategy where a problem is deconstructed into smaller sub-problems until a "base case" is reached and the problem is solved directly. This lab will get you familiar with recursive algorithms by taking you through several exercises to design and analyze recursive algorithms.

Clone the starter code for this lab from GitHub using the following url: https://github.com/yi-xia/CSCE156-Lab08-Recursion.git.

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## 1 Analyzing the Fibonacci Sequence

Recall that the Fibonacci sequence is a recursively defined sequence such that each term is the sum of the sequence?s two previous terms. That is, the sequence

$$1, 1, 2, 3, 5, 8, 13, 21, 34, 55, \dots$$

A recursive method to compute the Fibonacci sequence has been provided for you (see unl.cse.recursion.Fibonacci). The main() method of this class also provides code to compute the execution time of the recursive method. Run the program for several input instances.

This recursive method is highly inefficient: the method is called many times on the same input. Your task will be to directly observe this by adding code to count the exact number of times the method is called for each input n.

To do this, declare a private integer array and increment entries on each call to the recursive method depending on the input n. You may assume that an array no larger than 50 will be needed.

#### 2 Palindromes

A palindrome is a string of characters that is the same string when reversed. Examples of palindromes: kayak, abba, noon. An empty string and any string of length one is a palindrome by definition.

Your task will be to design and implement a recursive algorithm to determine if a given string is a palindrome or not. Implement the method in the class unl.cse.recursion.Palindrome. You may find that Java's String class has several useful methods such as charAt(int) and substring(int, int).

## 3 Sierpinski Triangle

A fractal is a geometric object that is self-similar. That is, if you zoom in on the object, it retains the same appearance or structure. One such fractal is the Sierpinski Triangle which is formed by drawing a triangle and removing an internal triangle drawn by connecting the midpoints of the outer triangle's sides. This process is repeated recursively ad infinitum. This process is illustrated for the first four iterations in Figure 1.

A Java applet has been provided to you ( unl.cse.recursion.SierpinskiTriangle ) that recursively draws the Sierpinski Triangle for a specified number of recursive iterations. Since this is an applet, you can run it without having a main() method. The

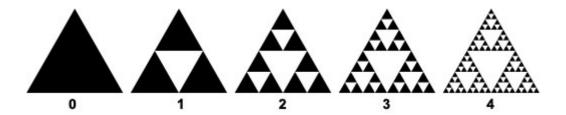


Figure 1: Sierpinski Triangle, 4 iterations

depth of the recursion is specified in the <code>paint()</code> method. It will be your task to modify this program to count the total number of triangles that a recursion of depth n will ultimately render.

#### 4 Pell Numbers

Another recursively defined sequence similar to the Fibonacci sequence are the Pell Numbers, defined as follows.

$$P_n = \begin{cases} 0 & \text{if } n = 0\\ 1 & \text{if } n = 1\\ 2P_{n-1} + P_{n-2} & \text{otherwise} \end{cases}$$

A program has been provided (PellNumbers) that computes the n-th Pell Number using a recursive function. The method has been defined using Java?s BigInteger class, a class that supports arbitrary precision integers. If we were to use this implementation to compute the 1000-th Pell Number, the computation would take not just centuries, but billions and billions of years!!

One alternative to such inefficient recursion is to use *memoization*. Memoization typically involves defining and filling a tableau of incremental values whose values are combined to compute subsequent values in the table.

For this exercise, we will instead use a Java HashMap to store values. A map is a data structure that allows you to define and retrieve key-value pairs. For this exercise, define a (static) HashMap that maps Integer types to BigInteger types (n to  $P_n$ ) and use it in the PellNumber method as follows. If the value  $P_n$  is already defined in the map, use it as a return value. Otherwise, compute the value using recursion, but also place the result into the HashMap so that it will be available for subsequent recursive calls.

Answer the questions in your worksheet and demonstrate your working programs to a lab instructor.

## 5 Another Fibonacci

Bonus Activity 1: The Fibonacci method in Case Study 1 returns a primitive Java int value which has a maximum possible value of 2,147,483,647. Find the maximum value n such that this method returns an accurate value (the value n such that calling Fibonacci (n+1) results in overflow). Hint: you probably cannot use the recursive version provided (why?). Write an alternative method to compute the Fibonacci sequence that returns a Java BigInteger (an arbitrary-precision number class). Also use memoization to eliminate repeated recursive calls.