



# Functions and generators

June 19, 2021

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# Review HW



# Sum of multiples

Sum of all #s below 1000 that are divisible by 3 and 5.

```
c = 0
for i in range(1000):
    if i %3 ==0 or i %5 ==0:
        c += i
print(c)
```



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c = 0           initializing a counter  
                    variable set to 0  
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```



# Sum of multiples

Sum of all #s below 1000 that are divisible by 3 and 5.

?



c = 0

initializing a counter  
variable set to 0

```
for i in range(1000):
```

```
    if i %3 ==0 or i %5 ==0:
```

```
        c += i
```

```
print(c)
```



# Sum of multiples

Sum of all #s below 1000 that are divisible by 3 and 5.

assignment statement

↓  
c = 0      initializing a counter  
                 variable set to 0  
for i in range(1000):  
    if i %3 ==0 or i %5 ==0:  
        c += i  
print(c)



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```

Looping through a range  
(sequence type, object)  
of 1000



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if statement used for  
conditional execution

conditional expression:  
if the remainder of i  
divided by 3 is 0 or i  
divided by 5 is 0


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equality operator

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print function to  
print-out output



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    if i %3 ==0 or i %5 ==0:
        c += i
print(c)
```

print function to  
print-out output

print() is a f(x), *not* a method ..  
difference is b/c method belongs to a  
class object whereas print is a block of  
code



We build up a silent  
understanding first, then  
vocalize it.

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What if I wanted to make 'Sum of multiples' a function that takes in a given stopping integer?



# Where to start?

What do we want? Inputs & Outputs





# Where to start?

What do we want? Inputs & Outputs

```
def name( __inputs__ ):
```

```
...
```

```
outputs!
```



# Now you!

What' s our input? Output?

```
def name( __inputs__ ):
```

```
...
```

```
outputs!
```



# Now you!

What' s our input? Output?

```
def name( n ):
```

```
...
```

```
    counter!
```



# Question!!

What do we do to get to our output  
form our input?

```
def name( n ):
```



counter!



# Question!!

def keyword used to  
define a f(x) inputs!  
def name( n ):

f(x) name

Inside of the function

counter!

outputs!



## Same code as b4!

We' ve been doing the “...” this whole time. Now we' re just putting it into a function to get from a dynamic input to an output

```
def name( n ):

    counter = 0

    for i in range(1000):

        if i %3 ==0 or i %5 ==0:

            counter += i

    counter
```



# There's a problem.

Can you spot it?

```
def name( n ):

    counter = 0

    for i in range(1000):

        if i %3 ==0 or i %5 ==0:

            counter += i

    counter
```



# Outputs can't just be variables

They must be `returned` or `yielded`

```
def name( n ):

    counter = 0

    for i in range(1000):

        if i %3 ==0 or i %5 ==0:

            counter += i

    return counter

    yield counter
```



What' s the big deal btwn return  
and yield?

First, a silent understanding.  
Let' s just see for ourselves.

---

```
def sum_multiples(n):  
    '''  
    Returns the sum of all multiples of 3 and 5 below input n  
    '''  
  
    #Initialize a counter  
    counter = 0  
  
    #Cycle through all numbers up to n  
    for i in range(n):  
        #Get multiples  
        if i % 3 == 0 or i % 5 == 0:  
            counter += i  
  
    return counter  
  
print(sum_multiples(1000))
```

gives/outputs:

233168

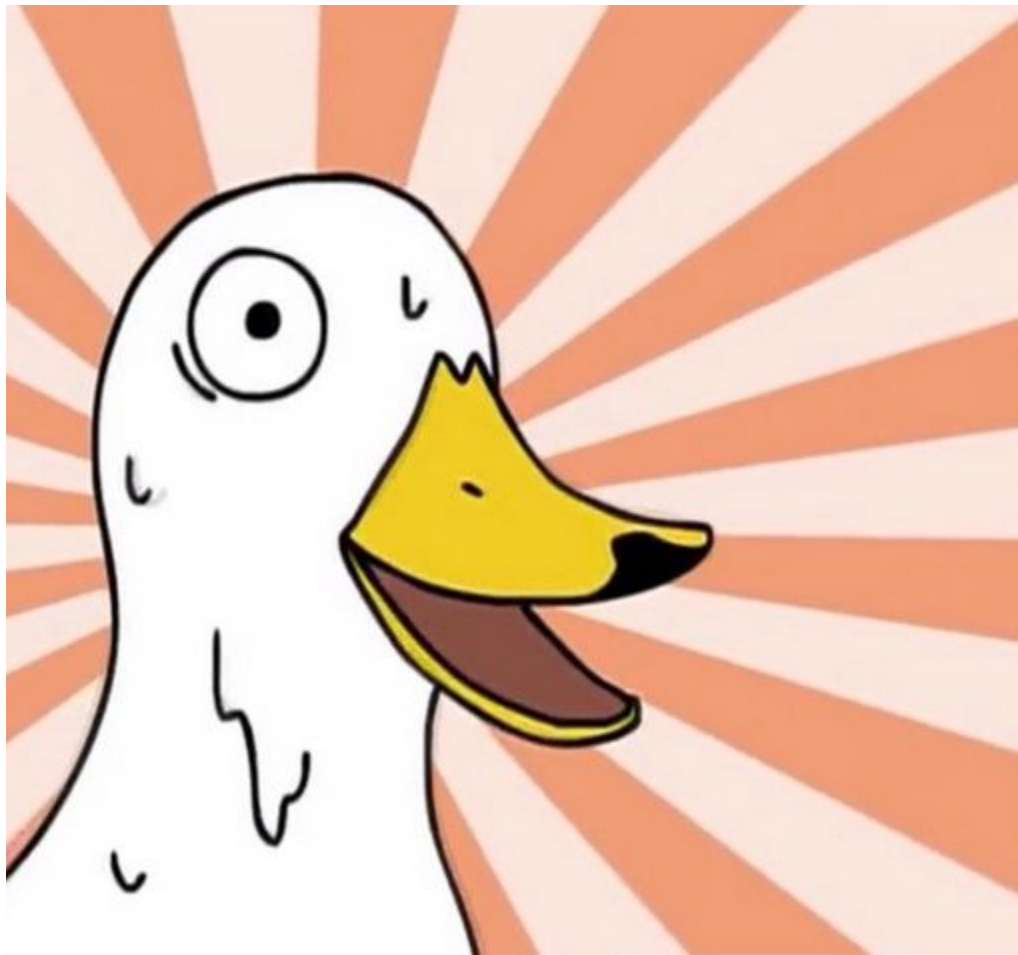
```
def sum_multiples(n):  
    '''  
    Returns the sum of all multiples of 3 and 5 below input n  
    '''  
  
    #Initialize a counter  
    counter = 0  
  
    #Cycle through all numbers up to n  
    for i in range(n):  
        #Get multiples  
        if i % 3 == 0 or i % 5 == 0:  
            counter += i  
  
    yield counter  
  
print(sum_multiples(1000))
```

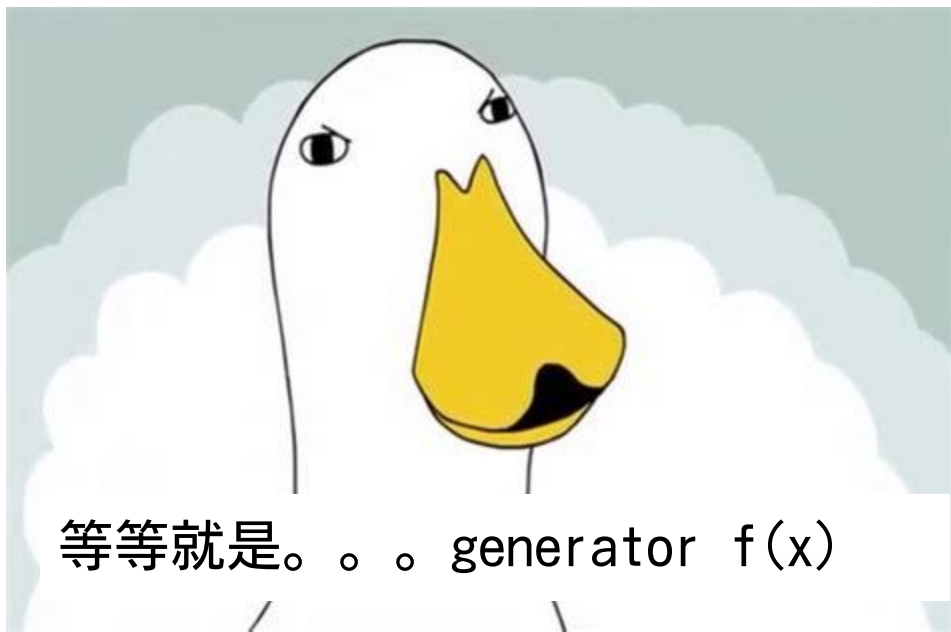
gives/outputs:

```
<generator object sum_multiples at  
0x7f8aa8071ac0>
```

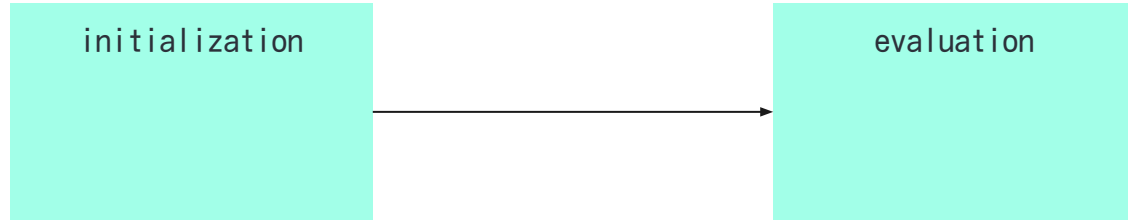


完全看  
不懂啊  
求助啊

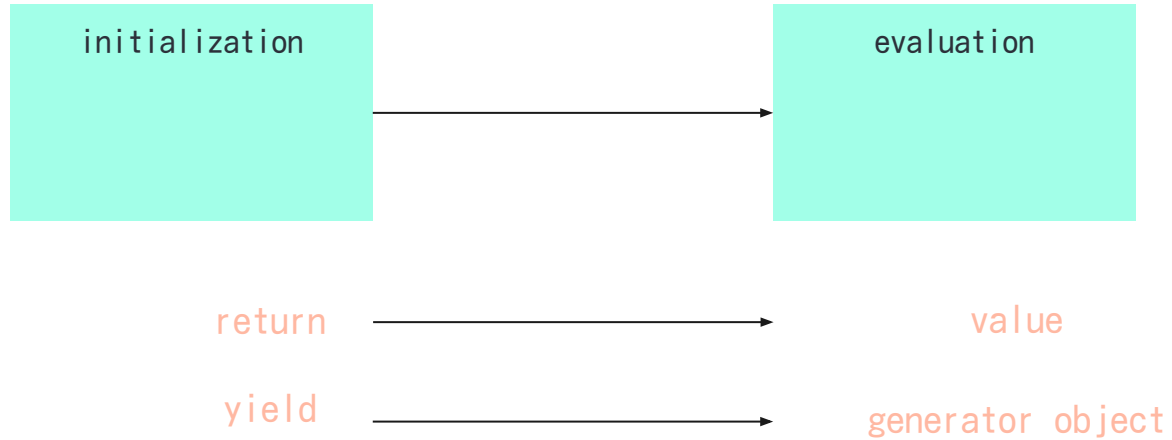




等等就是。。。generator  $f(x)$

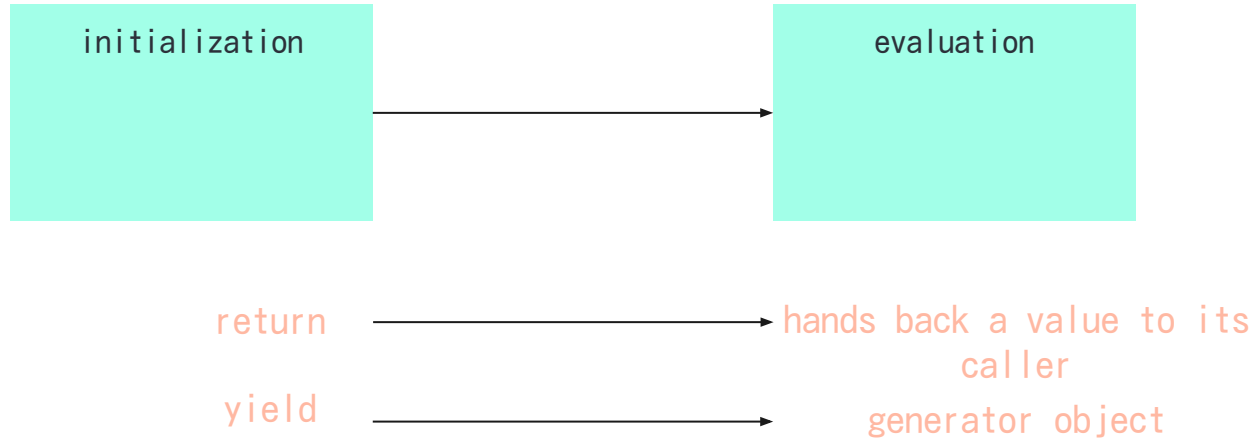


Functions have two steps: (1) initialization and (2) evaluation

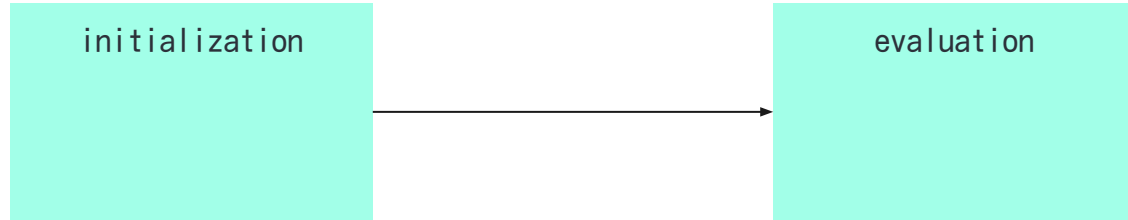


Return keyword:  $f(x)$ ; yield keyword: converts  $f(x)$  to **generator**





Return keyword:  $f(x)$ ; yield keyword: converts  $f(x)$  to **generator**



return → hands back a value to its caller

yield → Starts from where it was paused

Return has to start from the start; yield starts from the pause

---

So when it is useful to use  
generators?

---

So when it is useful to use  
generators?

Sequences!!

0, 1, 1, 2, 3, 5, 8, 13, 21, 34

The Fibonacci sequence

a, b

0, 1, 1, 2, 3, 5, 8, 13, 21, 34

The Fibonacci sequence

a, b  
0, 1, 1, 2

The Fibonacci sequence

a,      b  
0,    1,    1,    2  
a → b,    b → a + b

The Fibonacci sequence



a,      b  
1,    2,    3,    5  
a → b,    b → a + b

If only I could just remember the previous 2 values!

0, 1, 1, 2, 3, 5

a, b

a → b, b → a + b

If only I could just remember the previous 2 values!



# Fibonacci sequence

Want a  $f(x)$  that yields  $a$  and assigns  $a, b$

- Only remember the last 2 entries in sequence while yielding current value & assigning next 2 entries

```
def fib(limit):  
    'initialize' current_val, next_val  
  
    so long as < limit:  
        yield current_val  
  
        assign next two values
```

---

Keep this in mind.

First, we have to cover “so long  
as”



## So long as

Want a condition that is just “so long as this is True”

```
bean = 0  
  
beans = [ 'beans' , 'beans' , 'beans' ]  
  
so long as bean < all_beans:  
    bean += 1  
  
print(bean)
```



## So long as

Want a condition that is just “so long as this is True”

```
bean = 0
```

```
beans = [ 'beans' , 'beans' , 'beans' ]
```

```
so long as bean < all_beans:
```

```
    bean += 1
```

```
print(bean)
```

Gonna start calling this  
“while”



# While

Want a condition that is just “so long as this is True”

```
bean = 0
```

```
beans = [ 'beans' , 'beans' , 'beans' ]
```

```
while bean < all_beans:
```

What is all\_beans?

```
    bean += 1
```

```
print(bean)
```



# While

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```
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```

```
while bean < all_beans:
```

The length of beans!

```
    bean += 1
```

```
print(bean)
```



# While

Want a condition that is just “so long as this is True”

```
bean = 0
```

```
beans = [ 'beans' , 'beans' ]
```

```
while bean < len(beans):  The length of beans!
```

```
    bean += 1
```

```
print(bean)
```



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```

```
while bean < len(beans):
```

```
    bean += 1
```

```
print(bean)
```

built-in f(x) that  
returns number of items  
in an object



# While

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beans = [ 'beans' , 'beans' ]  
  
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```
while bean < len(beans):
```

```
    bean += 1
```

```
    print(bean)
```

Iteratively incrementing  
a counter variable  
initialized @ 0



# While LOOP!

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```
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```

```
while bean < len(beans):
```

```
    bean += 1
```

```
    print(bean)
```

Iteratively incrementing  
a counter variable  
initialized @ 0

We are looping!



# While LOOP!

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```

```
while bean < len(beans):
```

```
    bean += 1
```

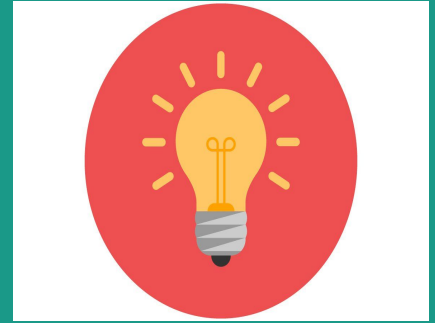
```
    print(bean)
```

Iteratively incrementing  
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initialized @ 0

We are looping!

---

Check for understanding:



Sum all even numbers below 10000  
using a while loop iterator.





# Fibonacci sequence

Want a  $f(x)$  that yields  $a$  and assigns  $a, b$

- Only remember the last 2 entries in sequence while yielding current value & assigning next 2 entries

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        assign next two values
```

a, b  
0, 1, 1, 2  
a → b, b → a + b

The Fibonacci sequence



# Fibonacci sequence

Crap! Why doesnt this work!

```
def fib(limit):  
    current_val = 0  
    next_val = 1  
    while current_val < limit:  
        yield current_val  
        a = b  
        b = a+b
```



# Fibonacci sequence

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```
    a = b
```

```
    b = a+b
```



# Fibonacci sequence

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```
    b = a+b
```





# Fibonacci sequence

This happens one after the other. We need it to happen at the same time.

```
def fib(limit):  
    current_val = 0  
    next_val = 1  
    while current_val < limit:  
        yield current_val  
        a = b  
        b = a+b
```



# Fibonacci sequence


This happens one after the other  
(**synchronously**). We need it to happen  
at the same time (**asynchronously**).

```
def fib(limit):  
    current_val = 0  
    next_val = 1  
    while current_val < limit:  
        yield current_val
```

1  
↓  
2

a = b

b = a+b



```
def fib(n):  
    a, b = 0, 1  
    while a < n:  
        yield a
```

```
1  a = b  
  ↓  
2  b = a+b
```

code diagram of fib(10):

```
a=0, b=1
```

```
a=0 < n=10:
```

```
yield a=0
```

```
a=1
```

```
b=1+1
```

a is being set to  
1, then referenced  
in the next line

a,      b  
0,    1,    1,    2

a → b,    b → a + b

---

This happens @  
the same time.

The Fibonacci sequence



# Fibonacci sequence

This happens one after the other  
(**synchronously**). We need it to happen  
at the same time (**asynchronously**).

```
def fib(limit):  
    current_val = 0  
    next_val = 1  
    while current_val < limit:  
        yield current_val  
        temp = b  
        a = temp  
        b = a+b
```



# Fibonacci sequence

This happens one after the other  
(**synchronously**). We need it to happen  
at the same time (**asynchronously**).

```
def fib(limit):  
    current_val = 0  
    next_val = 1  
    while current_val < limit:  
        yield current_val  
        a, b = b, a+b
```

```
def fib(limit):  
    a, b = 0, 1  
    while a < limit:  
        yield a  
        a, b = b, a+b  
  
print(fib(4e6))
```

gives/outputs:

<generator

object fib at

0x7fd2e80cfb30>

```
def fib(limit):  
    a, b = 0, 1  
    while a < limit:  
        yield a  
        a, b = b, a+b  
  
print(sum(fib(4e6)))
```

gives/outputs:

9227464

4613732 higher than  
the right answer..



```
def fib(limit):  
    a, b = 0, 1  
    while a < limit:  
        yield a  
        a, b = b, a+b  
  
print(sum(fib(4e6)))
```

gives/outputs:

9227464

4613732 higher than  
the right answer..

Sums everything, not just the even  
numbers!!!

---

Use a for loop to iterate over  
the generator object!



# Fibonacci sequence

Iterating over a generator object

```
def fib(limit):  
    current_val = 0  
    next_val = 1  
    while current_val < limit:  
        yield current_val  
        a = b  
        b = a+b  
  
sum = 0  
  
for i in fib(4e6):  
    if i %2 ==0:  
        sum += i  
  
print(sum)
```

---

## A faster way

```
print(sum(a for a in fib(4e6) if not (a % 2)))
```

---

Check for understanding:



Try to use this same pattern to sum all even numbers below 1000.

```
print(sum(a for a in fib(4e6) if not (a % 2)))
```

---

This is called a: List  
comprehension!

```
print(sum(a for a in fib(4e6) if not (a % 2)))
```



### First pass

1, 10, 9, 4  
1, 10, 9, 4      $10 > 9$   
1, 9, 10, 4     swap places  
1, 9, 10, 4      $10 > 4$   
1, 9, 4, 10     swap places  
                  10 is done

### Second pass

1, 9, 4, 10  
1, 9, 4, 10      $9 > 4$   
1, 4, 9, 10     swap places  
1, 4, 9, 10  
1, 4, 9, 10     9, 10 done

### Third pass

1, 4, 9, 10  
1, 4, 9, 10  
1, 4, 9, 10  
1, 4, 9, 10  
1, 4, 9, 10     4, 9, 10 done

### Fourth pass

1, 4, 9, 10  
1, 4, 9, 10  
1, 4, 9, 10  
1, 4, 9, 10  
1, 4, 9, 10     1, 4, 9, 10 done