

DSA
PS1, due Wed 21 8:00 PM

See notes for review of sliding window algorithm.

1. Read up through Chapter 5 (skip Chapter 2) of the textbook.
2. First duplicate. Given a string S return the index of the first repeated character. $S = \text{"abca"}$ returns 3, since the first duplicate is "a" at index 3.
3. Longest increasing subsequence of an array. Given an array L return the length of the longest *increasing* subsequence. $L = [1, 2, 3, 2, 5]$ --> return 3, as $[1, 2, 3]$ longer than $[2, 5]$; $[1, 1, 1, 1, 1]$ --> return 1, as $[1]$ is the longest increasing subsequence; $[1, 0, 1, 0, 1, 0]$ --> return 2, as $\text{len}([0, 1])$ is 2.
4. Longest substring containing unique characters. Given a string S return the length of the longest substring with only non-repeating characters. $S = \text{"aaaa"}$ --> 1, as "a" is the longest substring – "aa" or "aaa" or "aaaa" all have the repeating character "a". $S = \text{"xyz"}$ --> 3, as "xyz" is the longest substring without repeating characters.
5. Longest substring with unique characters of k length. Given a string S and integer k return the string of longest length that contains k distinct characters. $S = \text{"aaa"}$, $k = 1$ --> "a", as "a" is the longest substring that contains 1 distinct character. $S = \text{"eeefg"}$, $k = 3$ --> "efg", as "efg" is the longest substring that contains 3 distinct characters.
6. Subarrays with k different integers. Given an array L return the number of subarrays that can be formed with k distinct integers. $L = [1, 2, 1, 2, 3]$, $k=2$ --> 7, as the # of subarrays with 2 different integers is 7: we can make $[1, 2]$, $[2, 1]$, $[1, 2]$, $[2, 3]$, $[1, 2, 1]$, $[2, 1, 2]$, $[1, 2, 1, 2]$. $L = [1, 2, 1, 3, 4]$, $k = 3$ --> 3, as we can make $[1, 2, 1, 3]$, $[2, 1, 3]$, $[1, 3, 4]$, or 3 subarrays with 3 different integers in them.