## Computer Science 260

## Assignment 5

Due October 19, 2016

- 1. Give a proof by cases to prove that for all integers x,  $x^2 x$  is an even integer.
- 2. Give a proof by contraposition that for  $a \in \mathbb{Z}$ , if  $a^2 + 3$  is odd, then a is even.
- 3. Give a proof by contradiction for real numbers a and b that  $\frac{a+b}{2} < b \Rightarrow a < b$ .
- 4. Give a proof by contradiction that given integers j and k where  $j \ge 2$  that then  $j \not\mid k \lor j \not\mid (k+1)$ .