

# Biomedical Informatics 260

## Visualization of Medical Images

### Lecture 2

David Paik, PhD

Spring 2017

# Last Lecture: Imaging Modalities

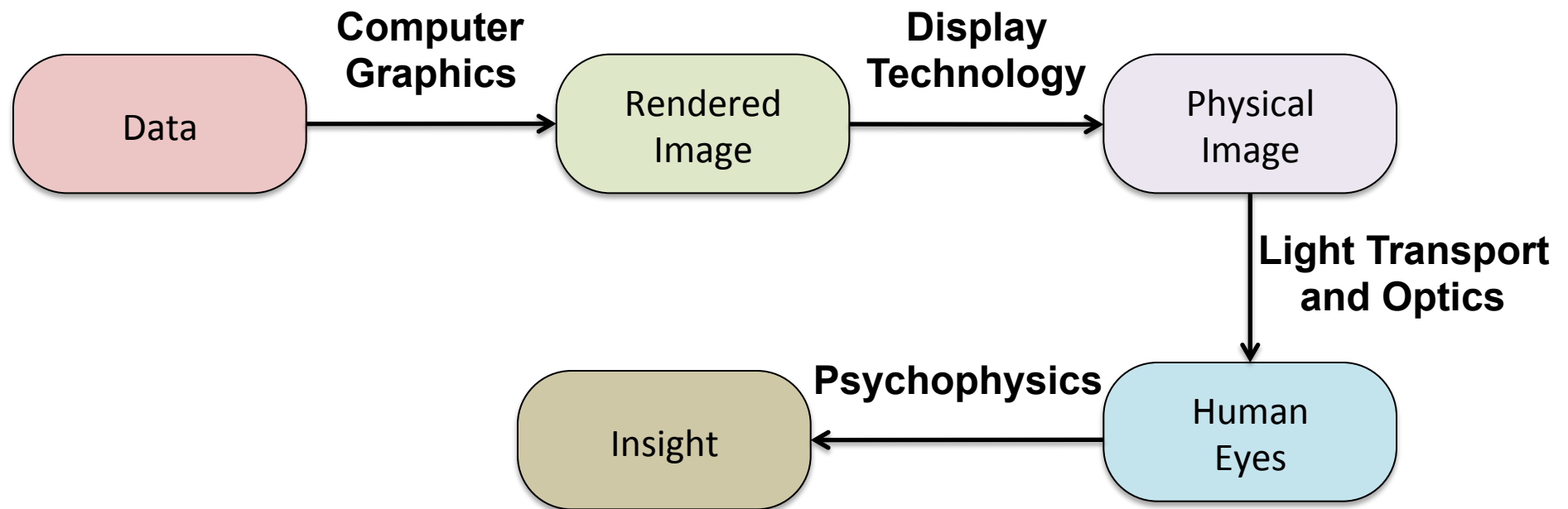
1. How images are acquired
2. Meaning of pixel values



# Today: Visualization

- How do we go from an array of pixel values to a displayed image to human insight about image content?
- Processing images always starts with visualization
- Methods covered today:
  - 2D Computer Graphics
  - 3D Computer Graphics
  - Image Fusion
  - Perception

# Visualization: From Data to Insight

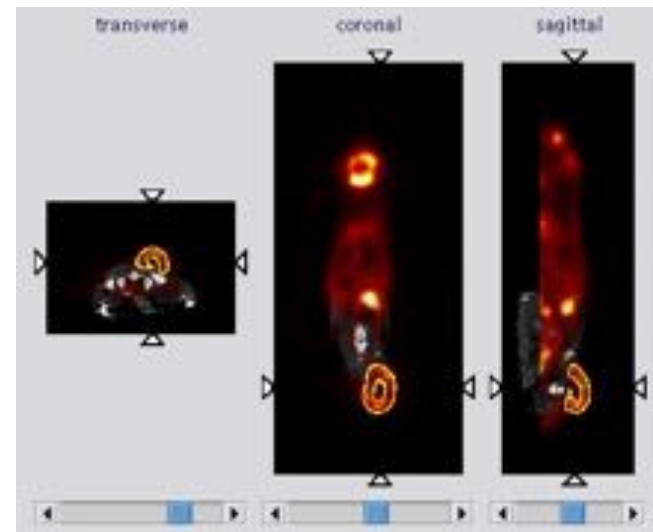


# 2D Computer Graphics

# Image Viewing Environments



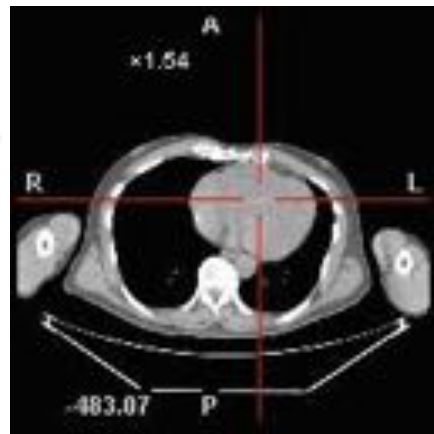
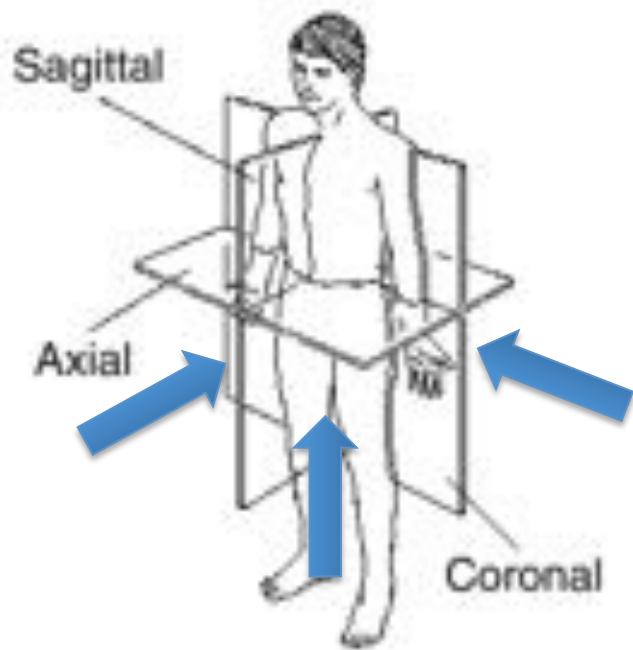
**Typical PACS Workstation**



**Typical Research Software**

**PACS = Picture Archiving and Communication System**

# Multipplanar Reconstruction (MPR)



Axial  
(transverse)

*Radiologist convention:*

*View from the bottom*



Coronal

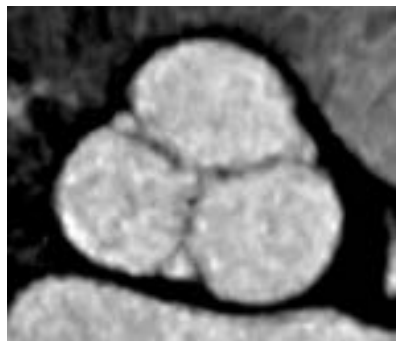
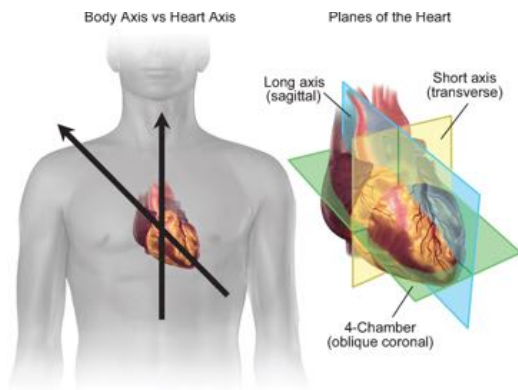
*View from the front*  
Note R-L flipping!



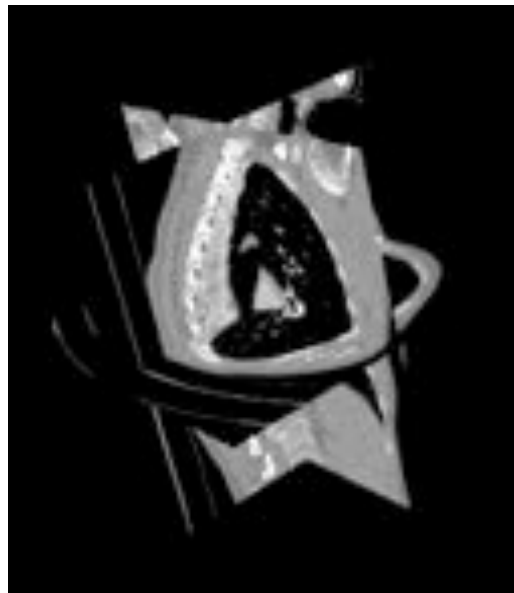
Sagittal

*View from left*

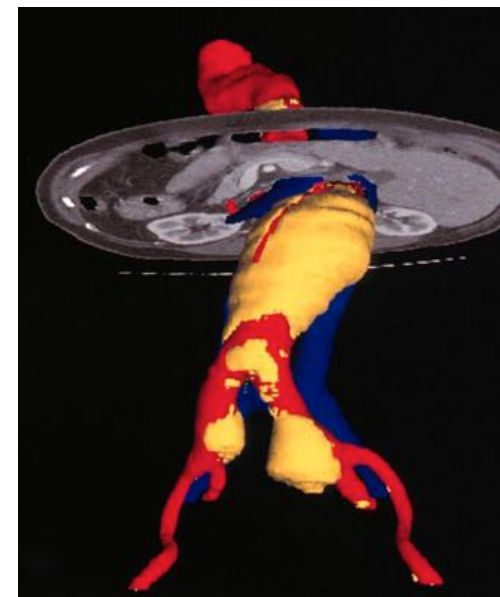
# Multiplanar Reconstruction (MPR)



Oblique



Multiple Planes



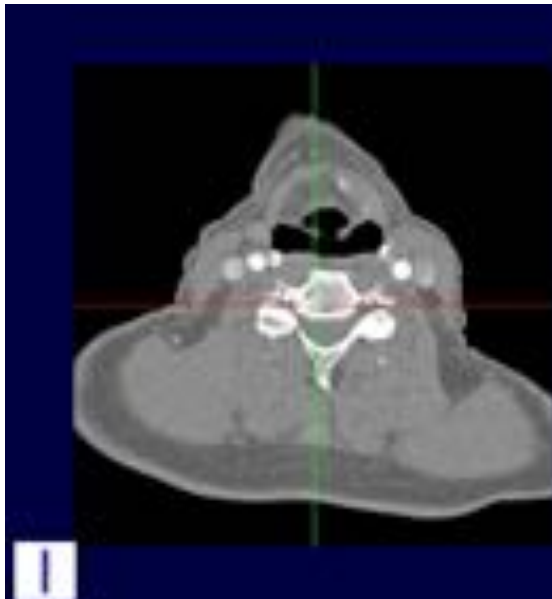
2D+3D

*(often linked to the axis of an organ)*



# MPR

Axial



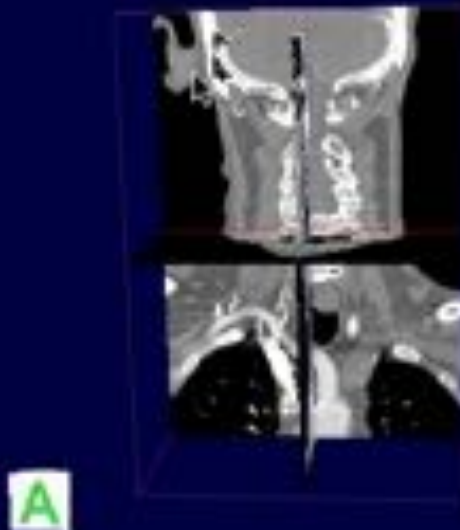
Coronal



Sagittal



3D

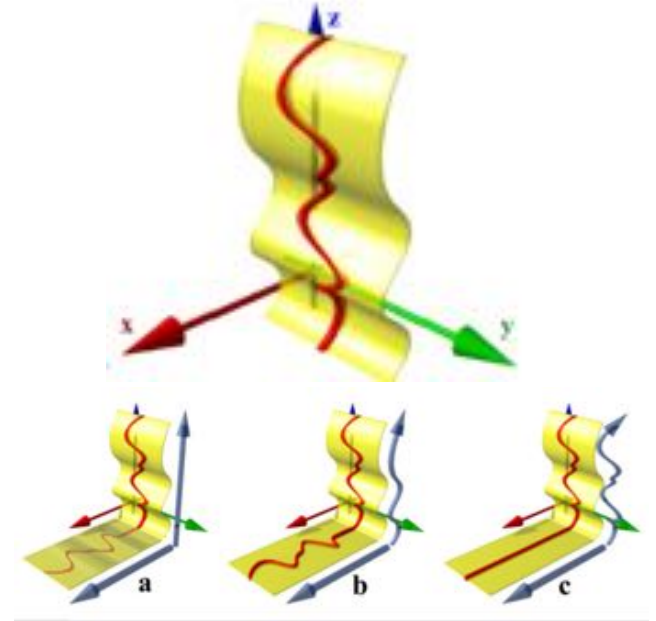


# Oblique Plane

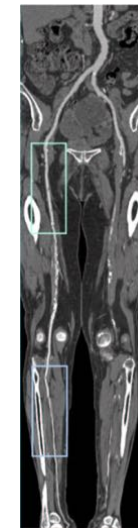
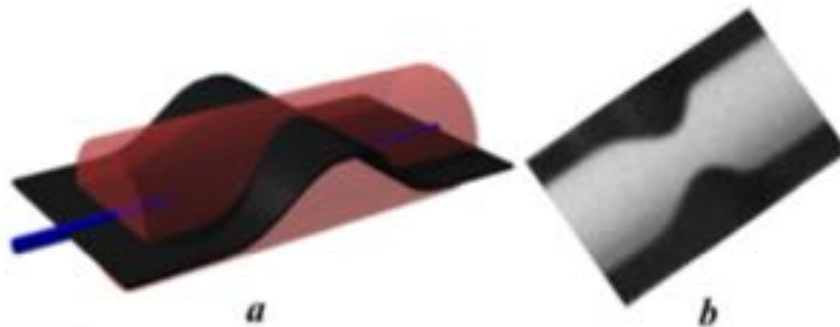


# Curved Planar Reformations (CPR)

- Centerline is determined
  - Manually or automatically
- Sampling along parallel lines
- Various methods for assembling sampled lines into final image
- Pros and Cons
  - Single image to show a long region
  - Artificial stenosis artifact possible

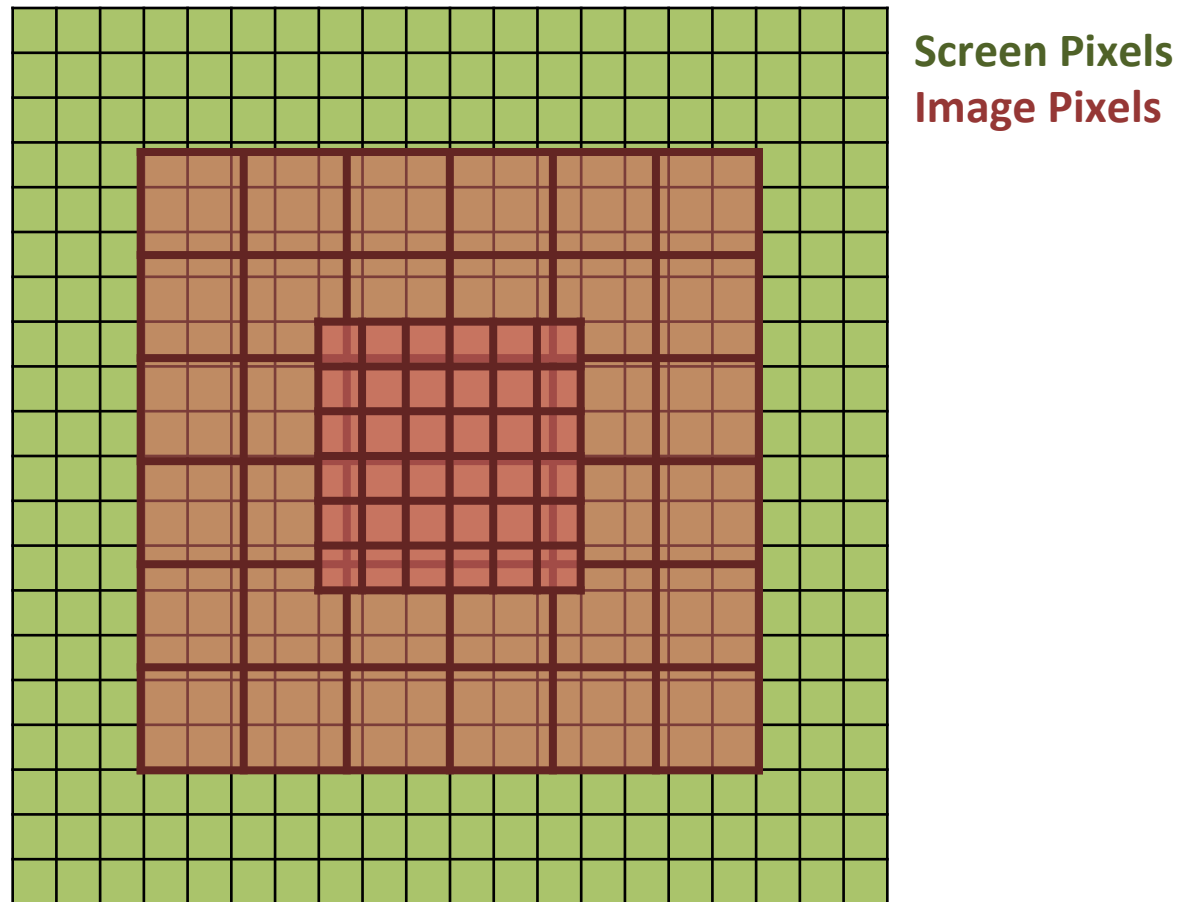


Potential  
Pitfall of  
CPR:

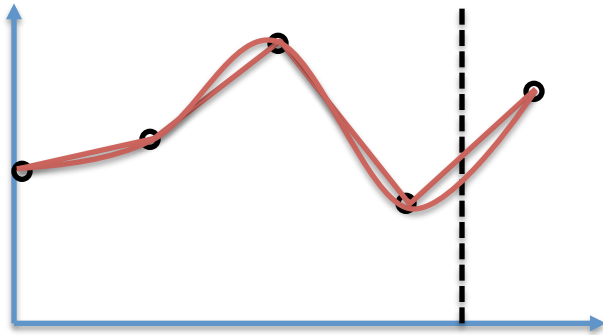


Kanitsar et al., IEEE Viz 2003

# Image Pixels Don't Always Align With Screen Pixels

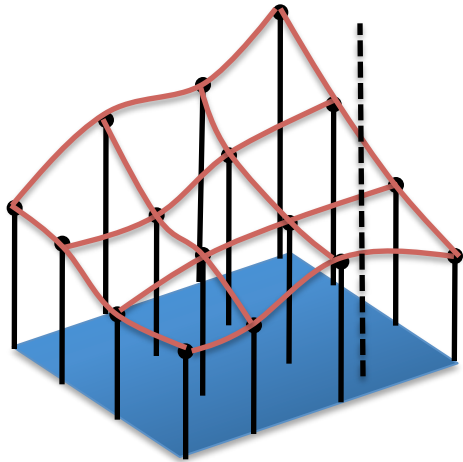


# Interpolation



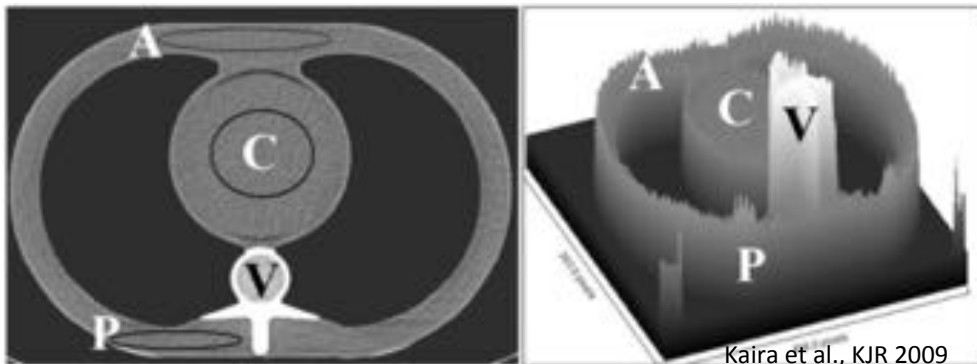
Linear Interpolation (“connect the dots”)

Higher Order Interpolation (smooth)



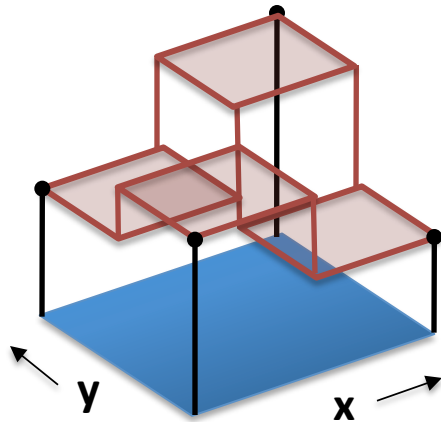
2D images are just two dimensional surface plots where height is image intensity

This naturally extends to 3D



***Thinking of image intensity  
as a height will be a recurring  
theme in this course***

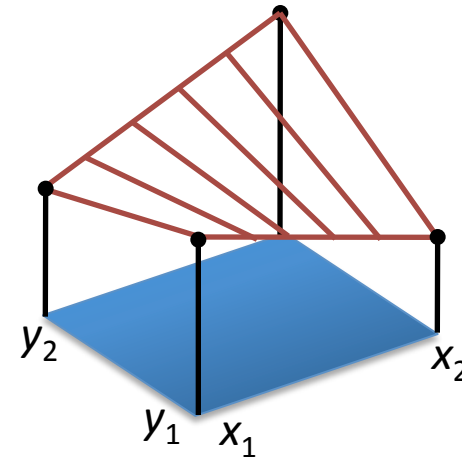
# Image Interpolation



Nearest Neighbor  
Interpolation

$$f(\mathbf{x}, \mathbf{y}) = f([\mathbf{x}], [\mathbf{y}])$$

$[ \ ]$  is rounding function

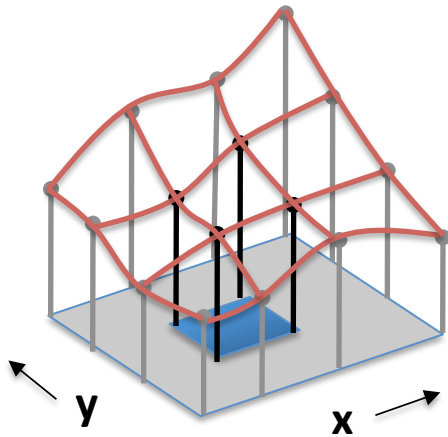


Bilinear  
Interpolation

$$f(\mathbf{x}, \mathbf{y}) = \frac{x_2 - \mathbf{x}}{x_2 - x_1} \cdot \frac{y_2 - \mathbf{y}}{y_2 - y_1} f(x_1, y_1) + \frac{\mathbf{x} - x_1}{x_2 - x_1} \cdot \frac{y_2 - \mathbf{y}}{y_2 - y_1} f(x_2, y_1) + \frac{x_2 - \mathbf{x}}{x_2 - x_1} \cdot \frac{\mathbf{y} - y_1}{y_2 - y_1} f(x_1, y_2) + \frac{\mathbf{x} - x_1}{x_2 - x_1} \cdot \frac{\mathbf{y} - y_1}{y_2 - y_1} f(x_2, y_2)$$



# Image Interpolation

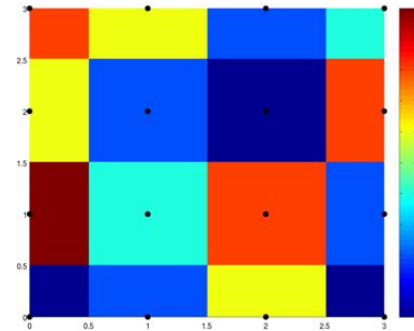


Bicubic  
Interpolation

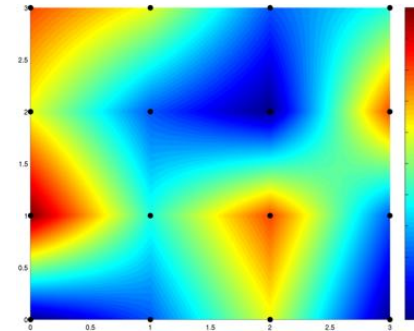
$$f(\mathbf{x}, \mathbf{y}) = \sum_{i=0}^3 \sum_{j=0}^3 a_{ij} \mathbf{x}^i \mathbf{y}^j$$



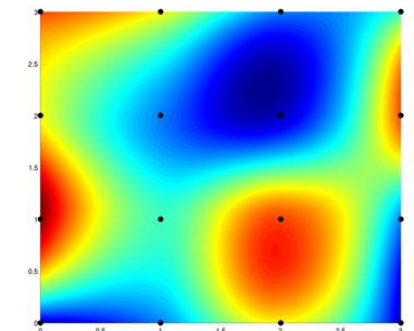
Nearest  
Neighbor



Bilinear

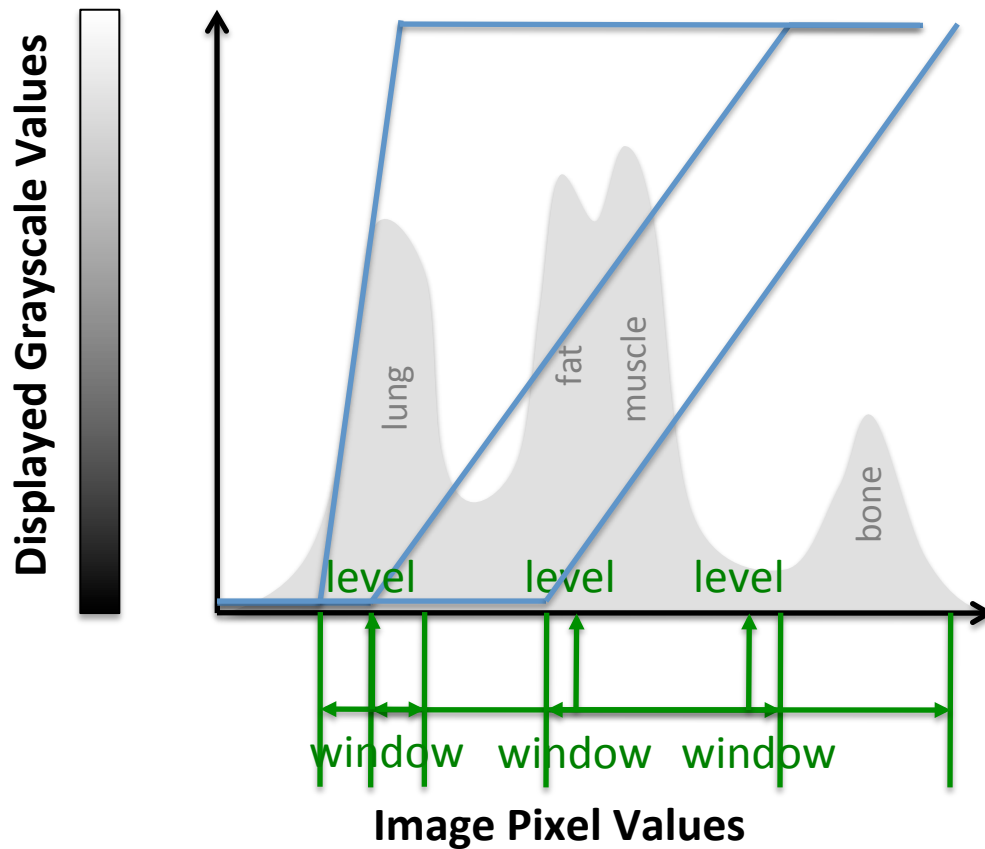


Bicubic



# Intensity Scale Mapping

“Window Leveling”



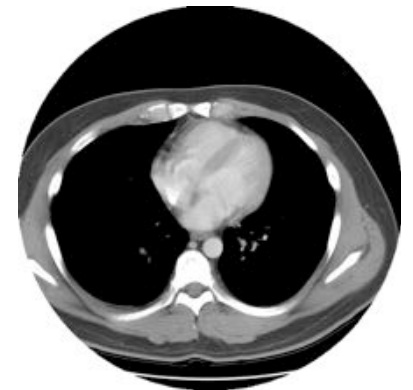
**Most imaging modalities: 16 bits (65,536 values)**  
**Most displays (and human eye): 8 bits (256 values)**

(color mapping is complicated, more on this later)

Original



High Level



Low Level,  
Narrow Window

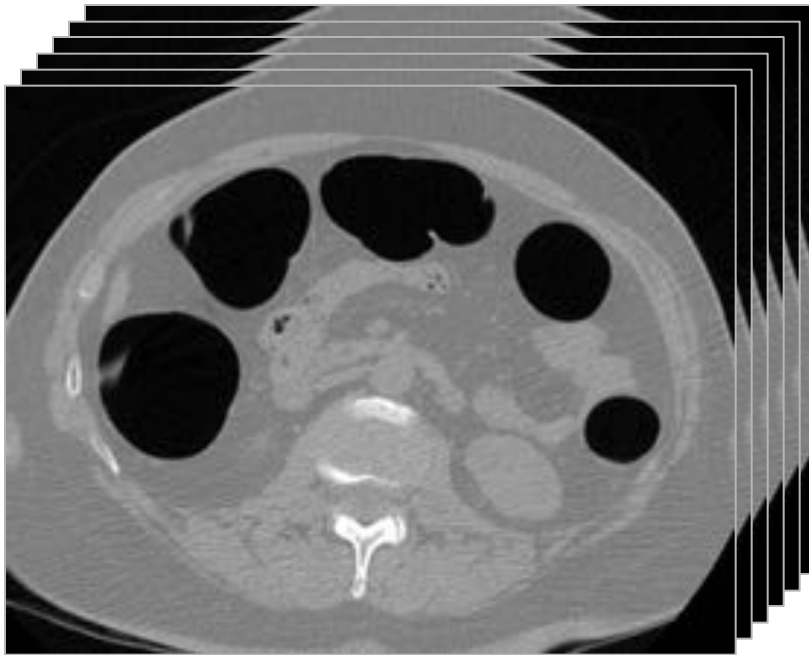




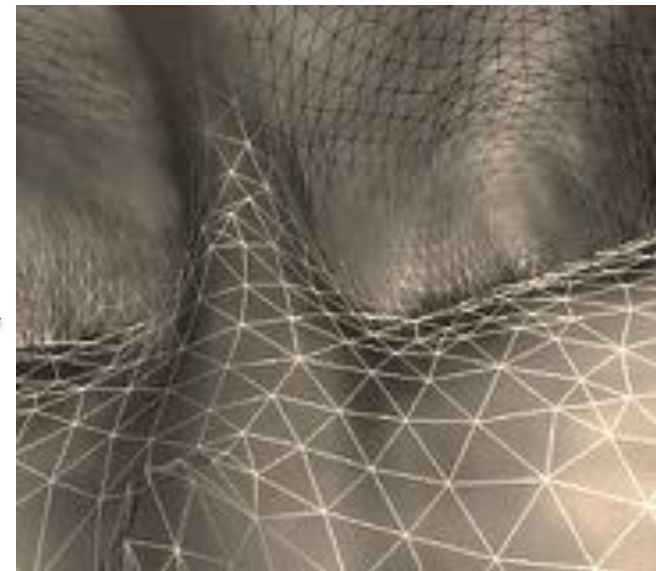
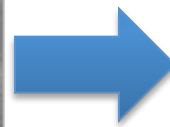
# 3D Computer Graphics

# Marching Cubes Algorithm

- The goal is to take a 3D array of scalar values, find an iso-intensity surface, and then make a triangulated mesh surface of it



**3D Image Dataset**

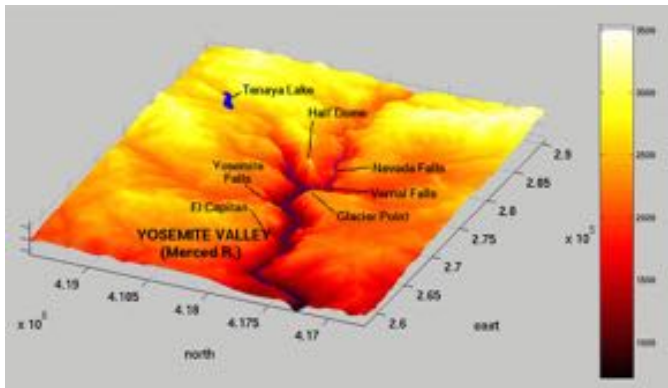


Radetzky et al., AIM 2002

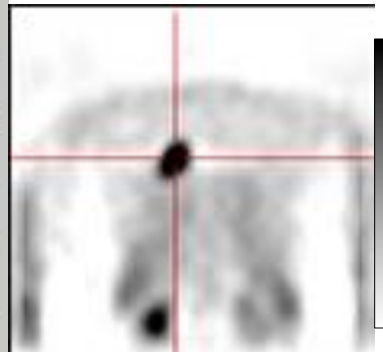
**Triangular Mesh**

# Marching Cubes Algorithm

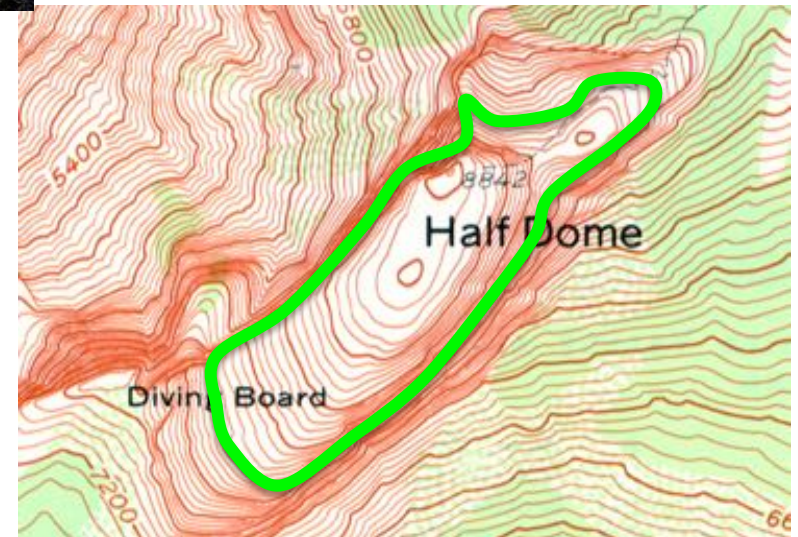
- But first, let's look at the simpler case of "Marching Squares" for 2D images



Yosemite Valley



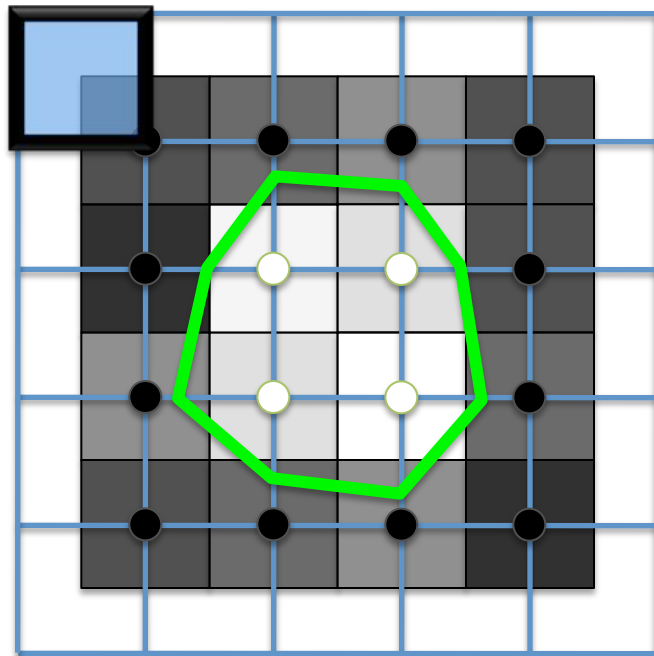
PET Scan



8000 ft iso-contour

(assume altitude data is sampled on a grid)

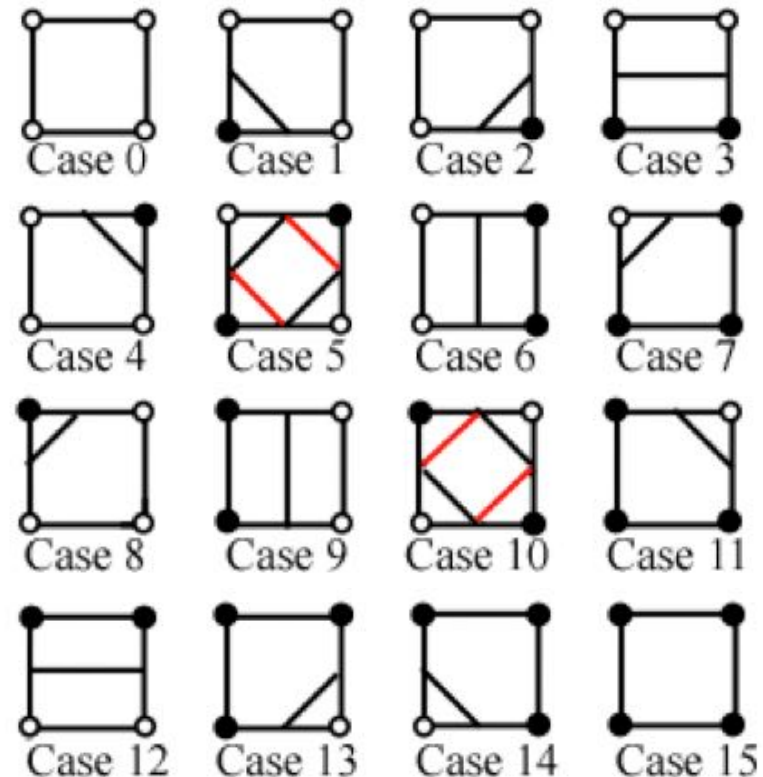
# Marching Squares (in 2D)



- White vertices  $\geq$  threshold
- Black vertices  $<$  threshold

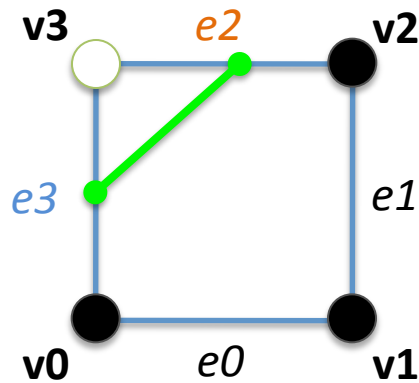
*Examine squares connecting 4 pixel centers*

Placement of line segment vertices on the edges done by linear interpolation  
(note that Case 5 and Case 10 are ambiguous)



**All 16 possibilities**

# Marching Squares Algorithm Details



Case 7

square\_index is a 4-bit number showing which vertices are black (which of the 16 cases)

$$\text{square\_index} = \begin{array}{|c|c|c|c|} \hline \mathbf{v3} & \mathbf{v2} & \mathbf{v1} & \mathbf{v0} \\ \hline \end{array} = 0111_2$$

$$\_\_ + 4 + 2 + 1 = 7$$

edge\_table is a pre-defined lookup table for all 16 cases and returns a 4-bit number indicating which of the 4 cube edges are intersected by the contour

$$\text{edge\_table}[7] = 12 = 1100_2 = \begin{array}{|c|c|c|c|} \hline \mathbf{e3} & \mathbf{e2} & \mathbf{e1} & \mathbf{e0} \\ \hline \end{array}$$

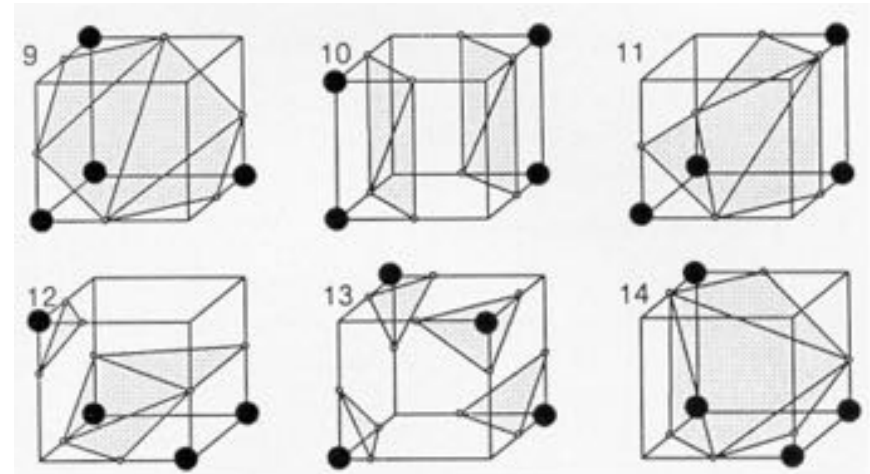
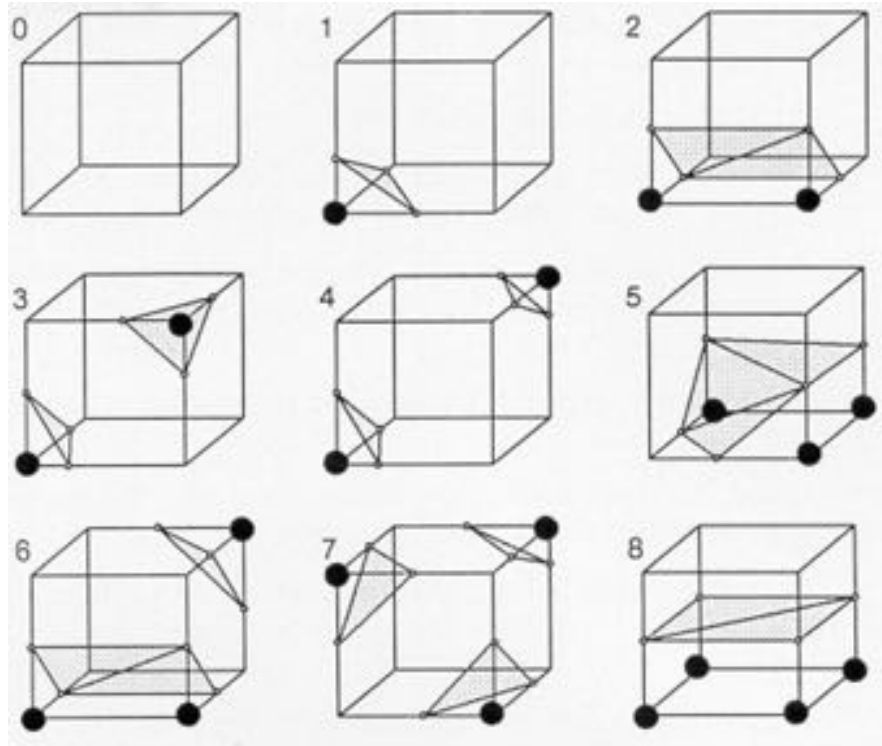
thus **e3** and **e2** are intersected by line segments

line\_table is a pre-defined lookup table of all 16 cases and returns a list of pairs of intersected edges that make line segments

$$\text{line\_table}[7] = \{ \mathbf{3}, \mathbf{2}, -1, -1, -1 \}$$

**e3-to-e2** is a line segment (2 line segments max;  
-1 indicates end of list)

# Marching Cubes (in 3D)



Lorensen and Cline, Comp Graph 1987

256 cases total  
15 unique cases shown here

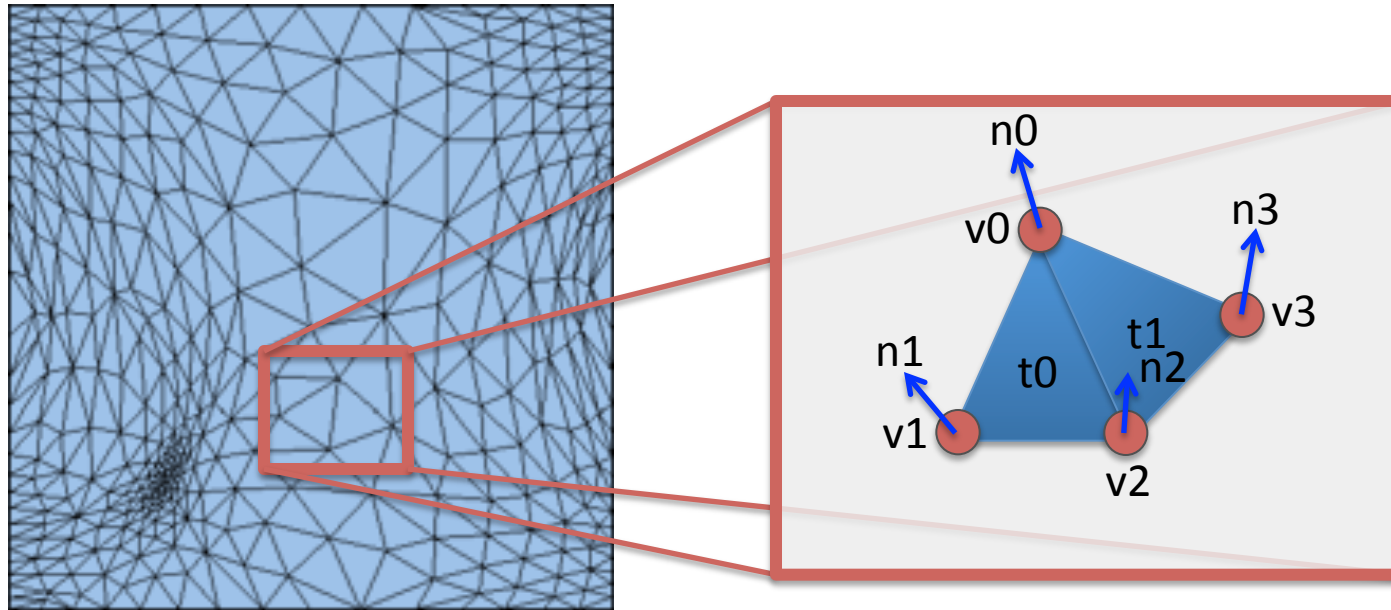
Cases 3,4,6,7,10,12,13 are ambiguous

cube\_index, edge\_table and triangle\_table are directly analogous to marching squares except:

- there are 256 cube cases (instead of 16 square cases)
- there are 12 cube edges (instead of 4 square edges)
- triangles are triplets of intersected edges (instead of line segments as pairs)
- there is a maximum of 5 possible triangles per cube (instead of max 2 line segments per square)



# Mesh Data Structure



## Vertex List

$v0 = (91.3, 32.4, 14.8)$   
 $v1 = (90.1, 31.3, 14.3)$   
 $v2 = (91.9, 31.2, 14.9)$   
 $v3 = (93.2, 31.8, 14.7)$

...

*(Must be careful not to  
redundantly add vertices)*

## Triangle List

$t0 = (v0, v1, v2)$   
 $t1 = (v0, v2, v3)$

...

*(order of vertices determines  
inside vs. outside direction)*

## Normal List

$n0 = (0.11, -0.08, 0.91)$   
 $n1 = (0.13, -0.03, 0.90)$   
 $n2 = (-0.03, 0.05, 0.95)$   
 $n3 = (0.01, -0.02, 0.99)$

...

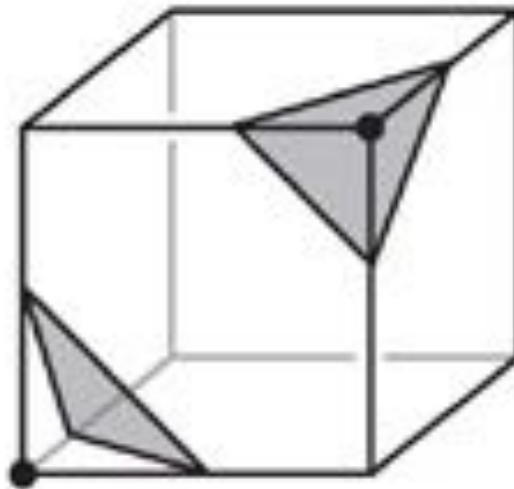
*(Marching Cubes doesn't tell  
you how to calculate normals  
at each vertex; needed for  
smooth surface shading)*

## Questions:

What would be an alternative way  
to triangulate this case?

How might you choose one vs. the other?

Why might you choose one vs. the other?





# Shaded Surface Display

- Triangle mesh made from images
  - Marching cubes is the classic method but isn't the only method
  - Meshes can be decimated, smoothed, adaptively refined
- Surface mesh can be rendered into an image using standard graphics routines
- Pros and Cons
  - Very fast
  - Surface geometry visualized well
  - Only as good as meshing routine
  - Inner structures obscured

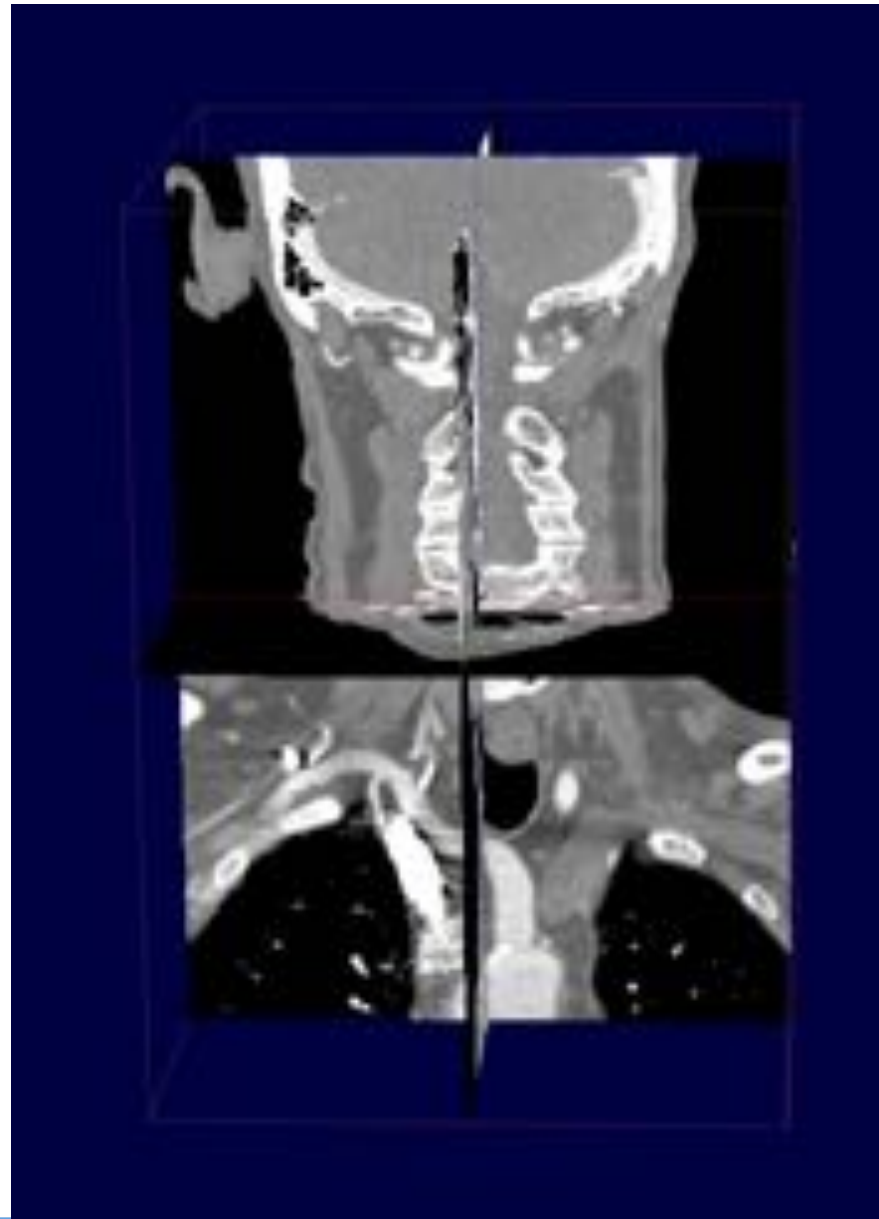


Example rendering of human lungs from CT

Typical game character: 2k-20k triangles

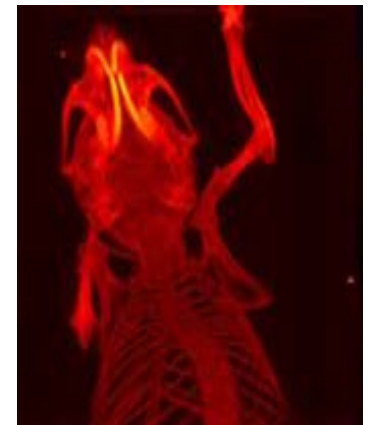
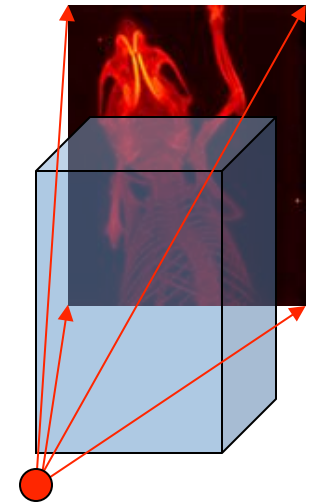
Typical medical image: 500k-10M triangles

# Shaded Surface Display



# Maximum/Minimum/Mean Intensity Projection

- Rays are mathematically cast through the 3D image and the maximum/minimum/mean (interpolated) intensity encountered is put into that 2D image pixel
- Rays may be divergent for perspective or parallel for an orthographic view
- Viewpoint may be rotated around dataset
- Pros and Cons
  - Bright objects well visualized
  - May have overlap (e.g., spine & aorta)
  - Simple, fast, pseudo-3D
  - Rendered 2D image is semi-quantitative



# Maximum/Minimum/Mean Intensity Projection

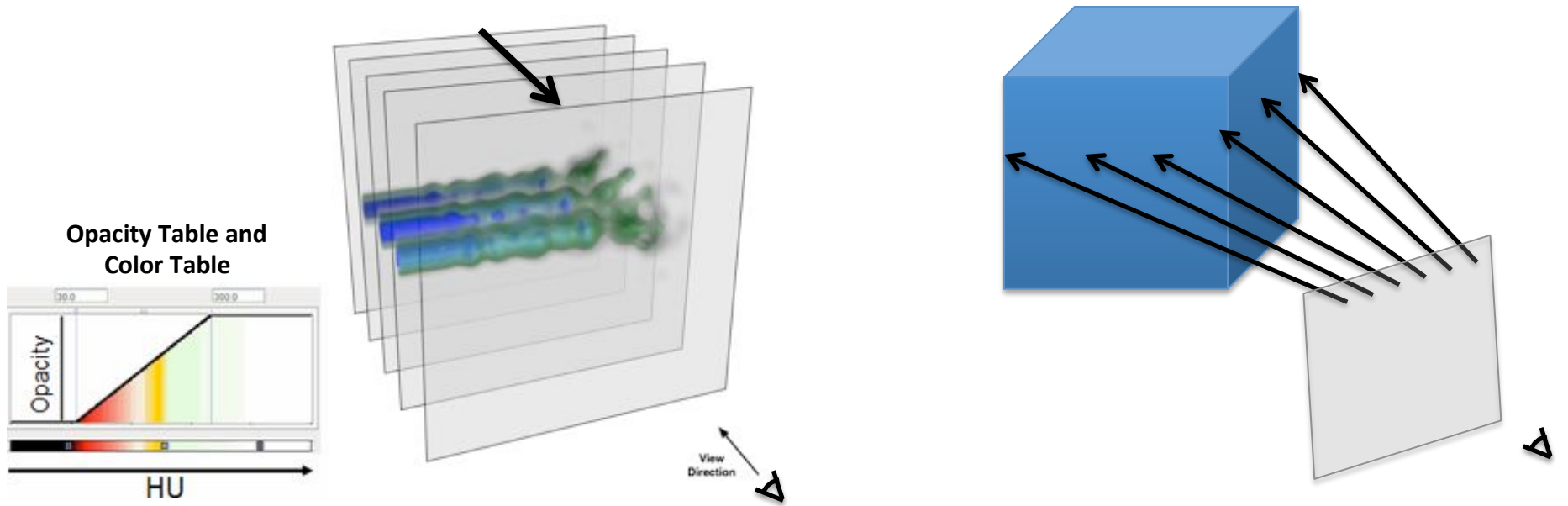


**Mean Intensity Projection**



**Maximum Intensity Projection**

# Direct Volume Rendering



$$\begin{array}{c}
 C_{in}, \alpha_{in} \\
 \downarrow \\
 C, \alpha \\
 \downarrow \\
 C_{out}, \alpha_{out}
 \end{array}
 \quad
 \begin{array}{l}
 C_{out} = (1 - \alpha) \cdot C_{in} + C \\
 \alpha_{out} = (1 - \alpha) \cdot \alpha_{in} + \alpha
 \end{array}$$

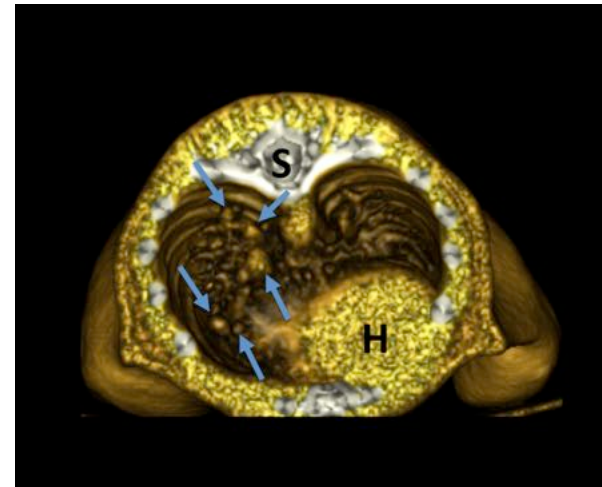
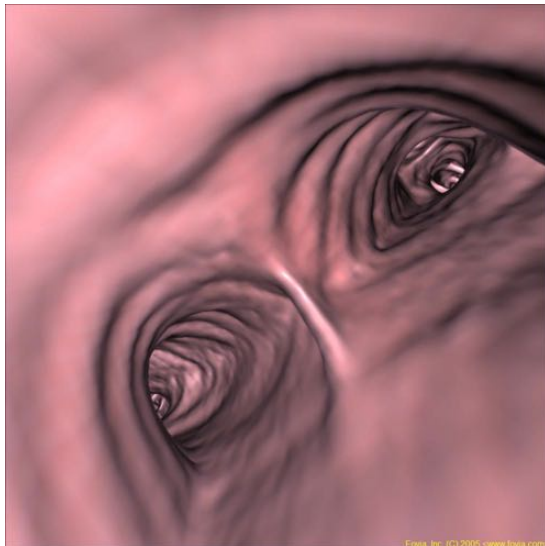
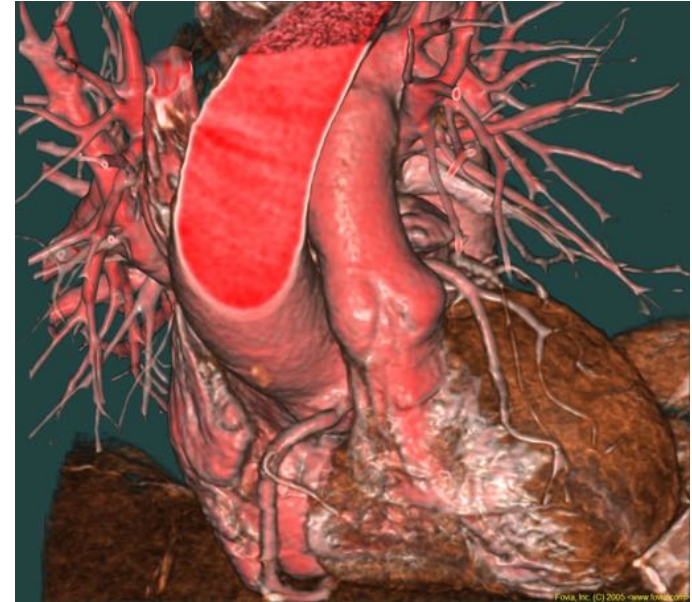
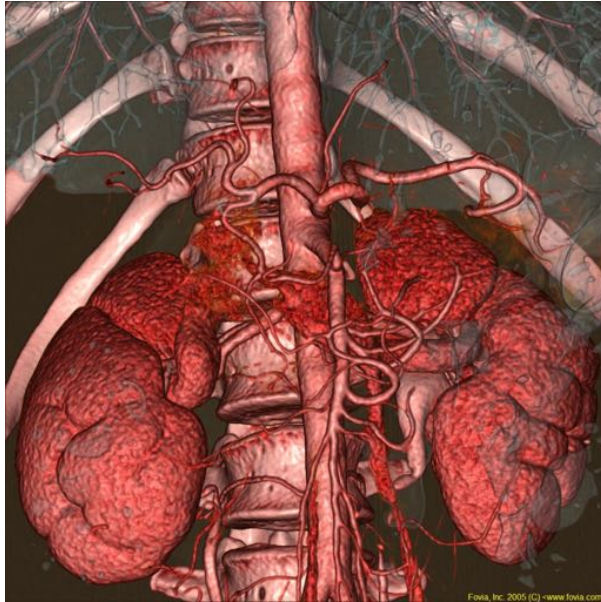
**Object Order Volume Rendering  
(back-to-front)**

$$\begin{array}{c}
 C_{out}, \alpha_{out} \\
 \uparrow \\
 C, \alpha \\
 \uparrow \\
 C_{in}, \alpha_{in}
 \end{array}
 \quad
 \begin{array}{l}
 C_{out} = C_{in} + (1 - \alpha_{in}) \cdot C \\
 \alpha_{out} = \alpha_{in} + (1 - \alpha_{in}) \cdot \alpha
 \end{array}$$

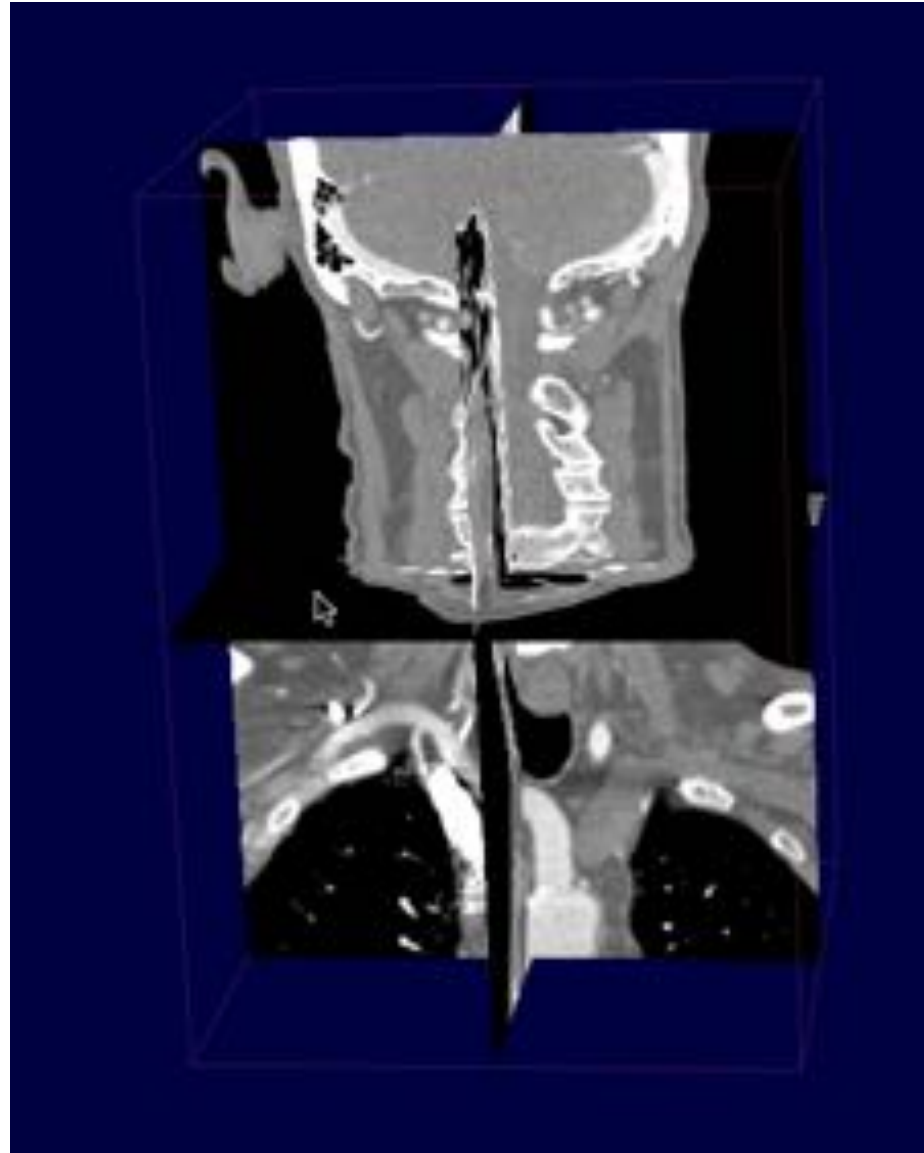
**Image Order Volume Rendering  
(front-to-back)**



# Volume Rendering



# Volume Rendering

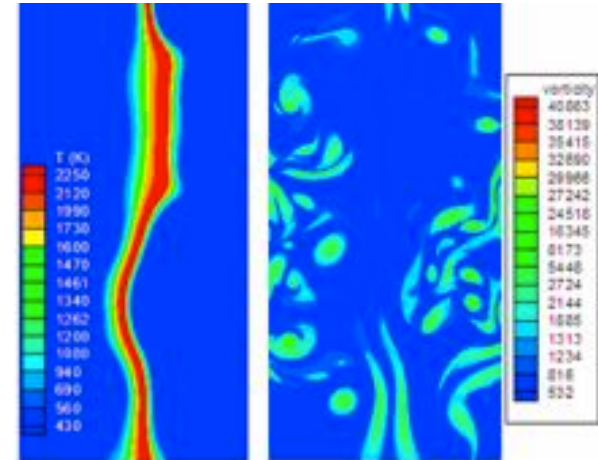
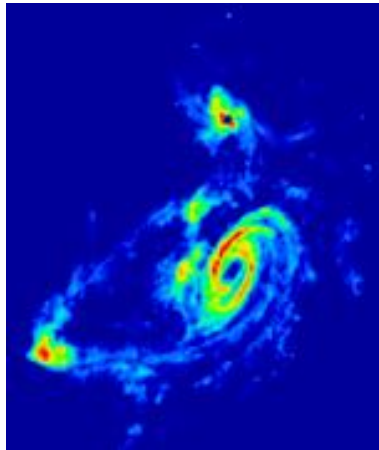


# Image Fusion



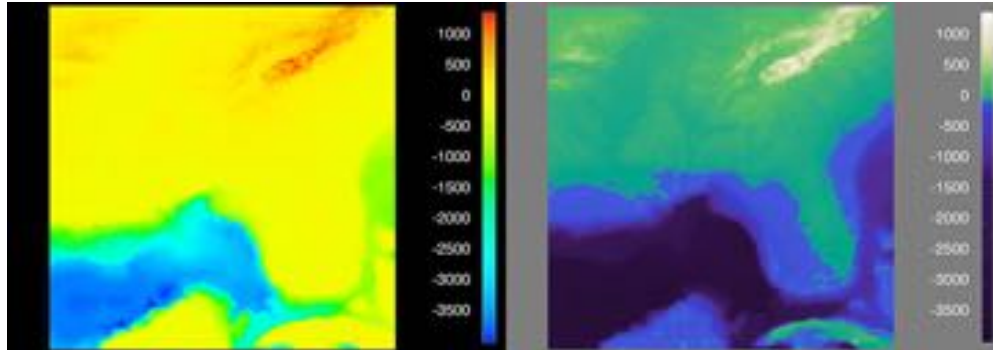
# Image Fusion

- Pseudocoloring used in many fields
  - Assigns 3-component color to 1-component scalar data by using a color lookup table
  - Astronomy, geography, fluid simulations, etc.

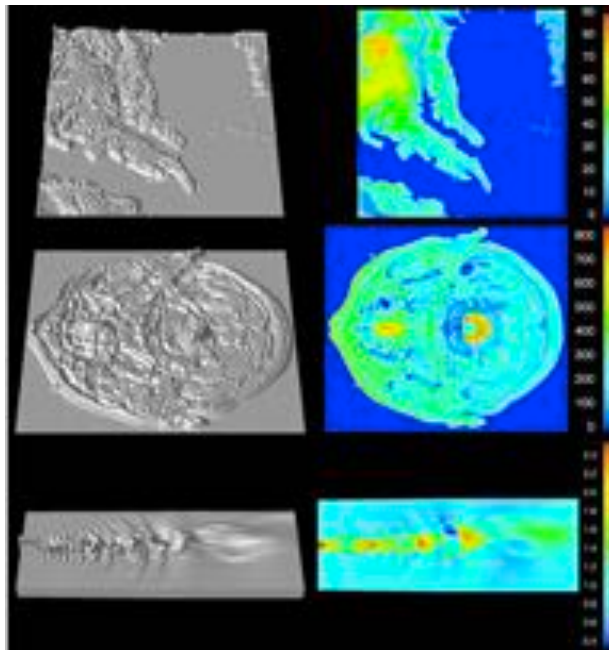


- What kind of information is to be revealed?
  - Metric: quantity at each point
  - Form: shape and structure
- Combine anatomic (e.g., CT) and functional (e.g., PET)

# Pseudocoloring Artifacts

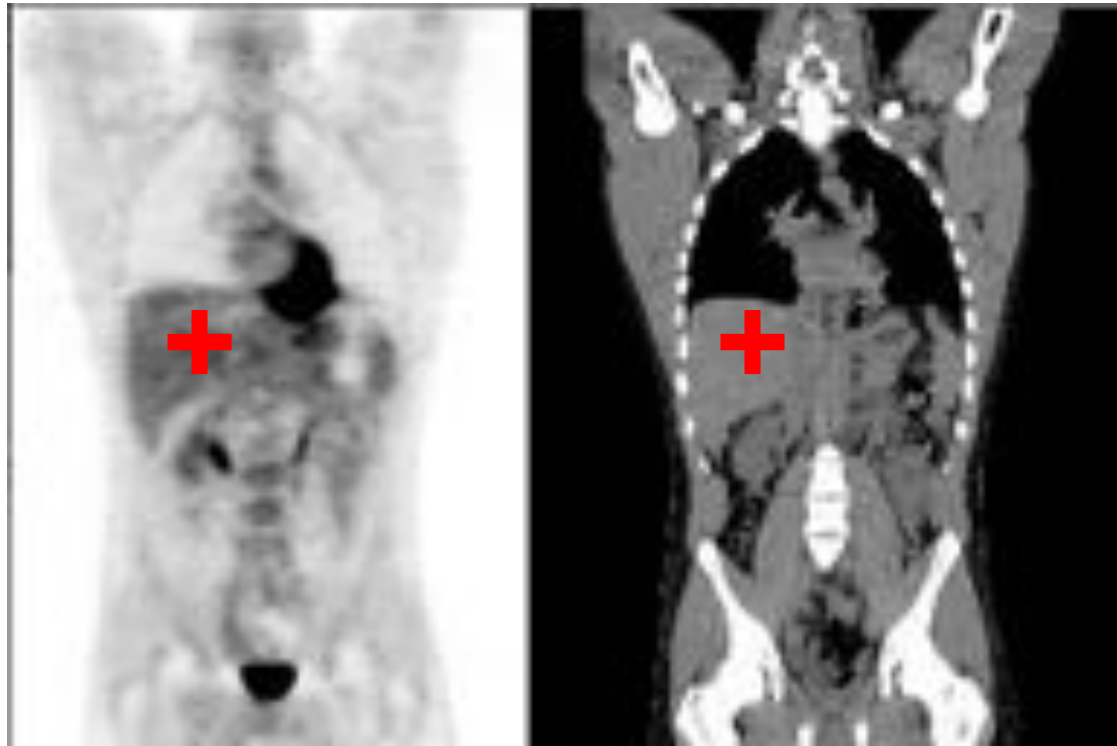


False Negative  
Artifacts



False Positive  
Artifacts

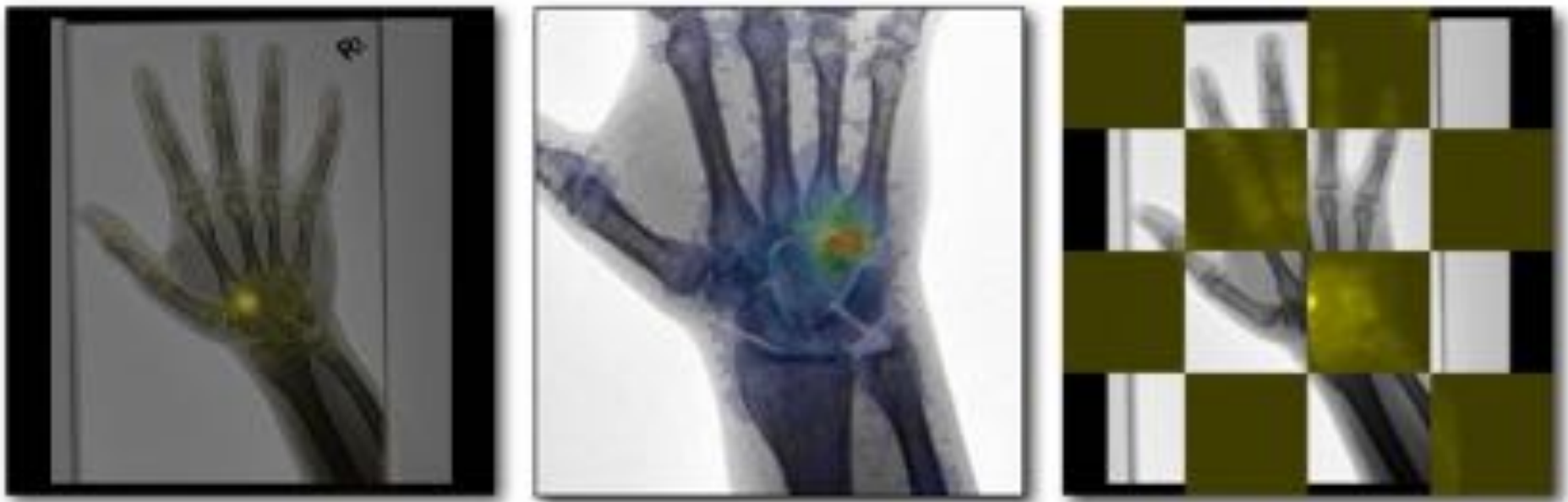
# Parallel Display



Linked cursor to match up locations

# Alternate Pixel Display

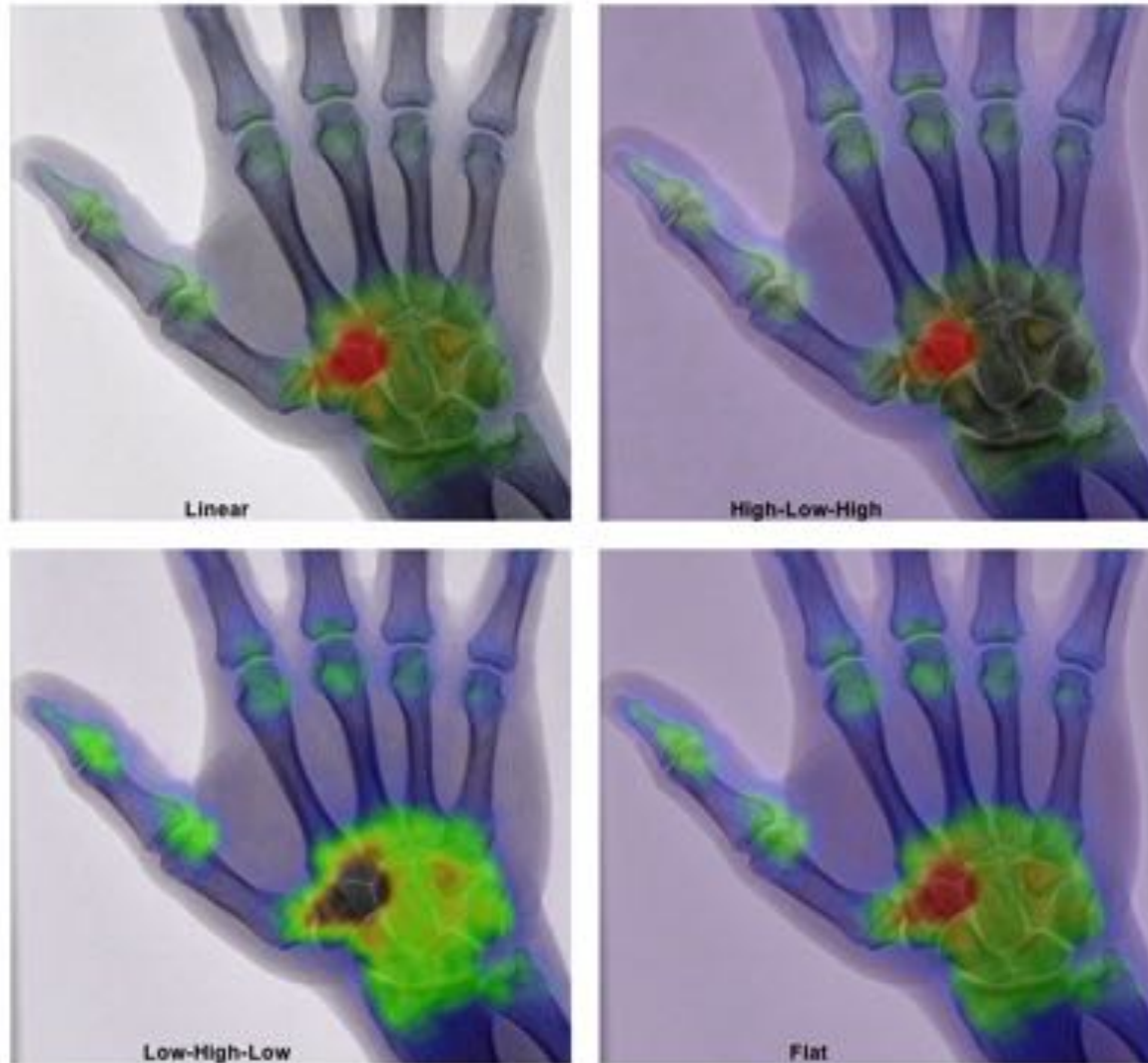
“Screen Door Transparency”



Generated by Kieran Maher, Nov 2006

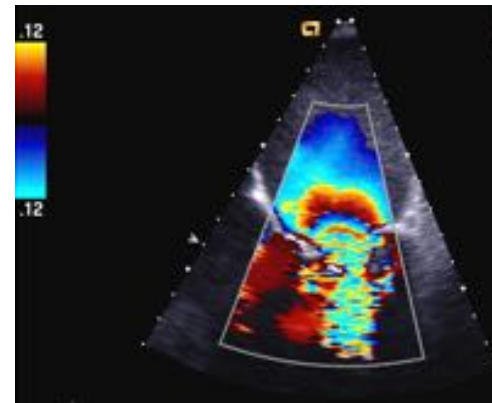
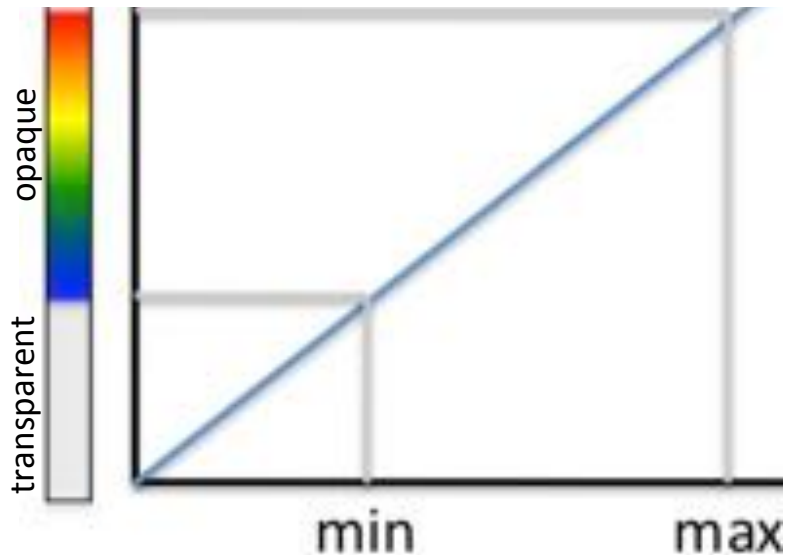
Varying the size of the checkerboard to get different effects

# Alpha Blending

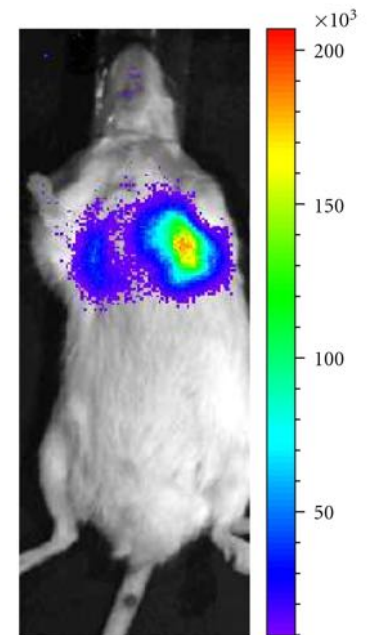


$$I = \alpha I_1 + (1 - \alpha) I_2$$

# Alpha Blending



Doppler Ultrasound



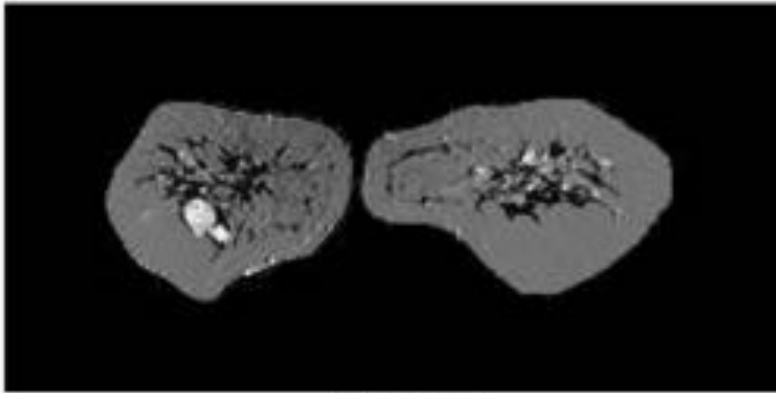
BLI

Chen et al, Circulation 2011

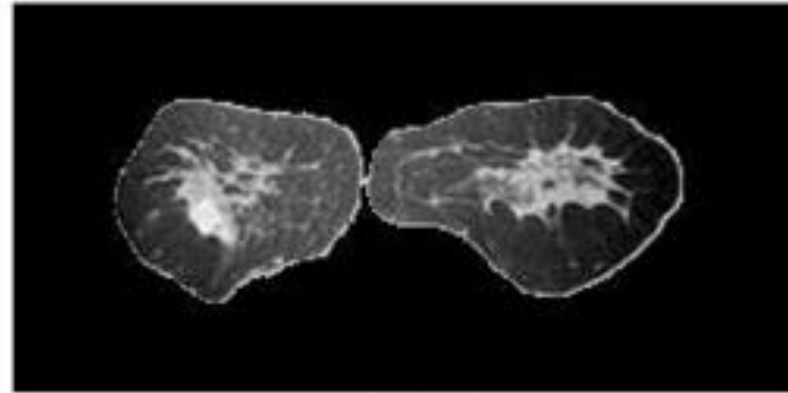
$\alpha$  (opacity or 1-transparency) can be a function of pixel intensity

Typically, functional information shown in color, overlaid on anatomy in grayscale

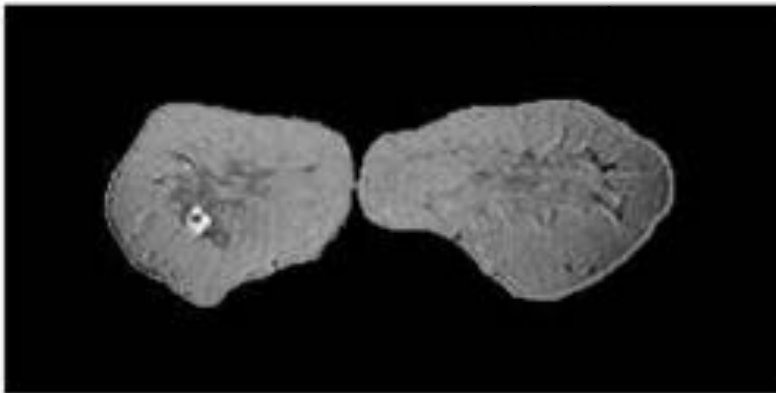
# RGB Fusion



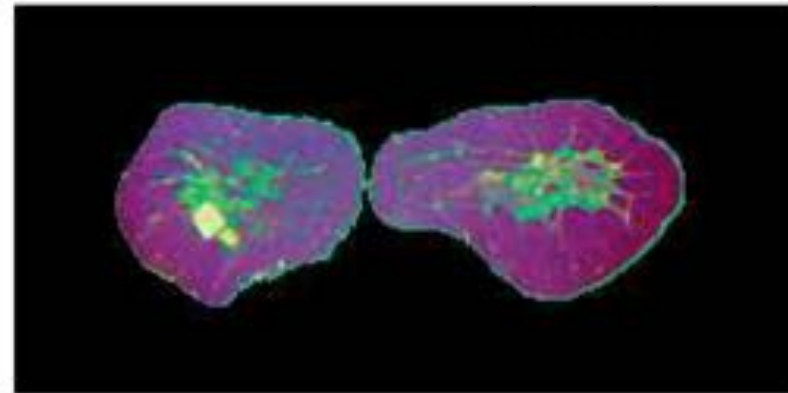
KPCA  $I_1$  (red)



KPCA  $I_2$  (green)



KPCA  $I_3$  (blue)



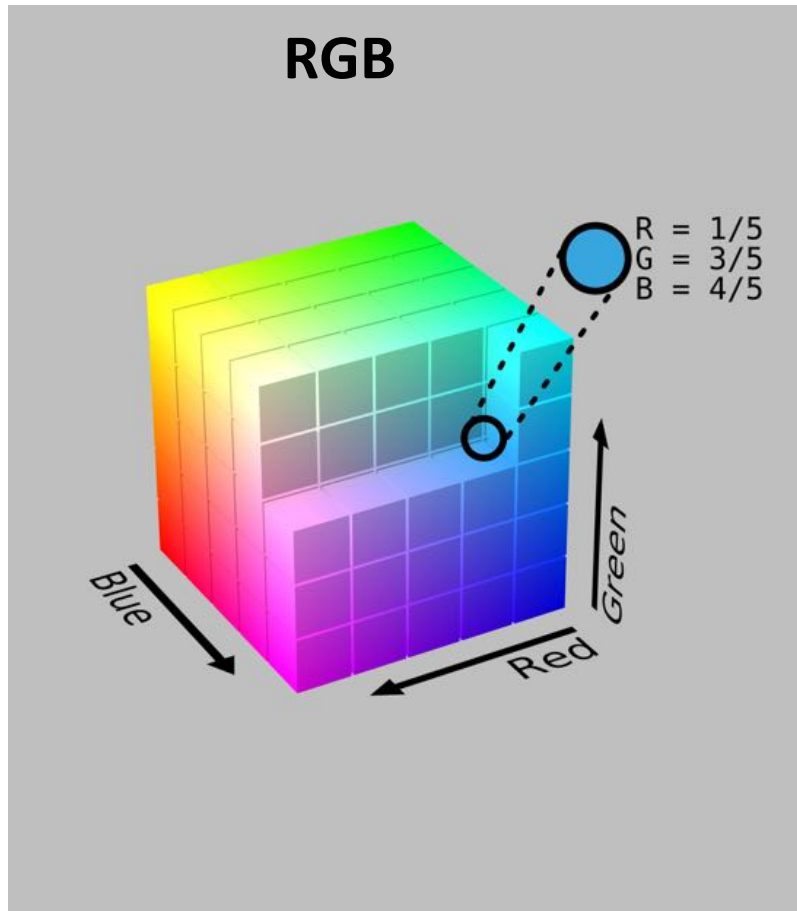
KPCA  $I_{RGB}$

Twelmann et al., Biomed Eng Onl 2004

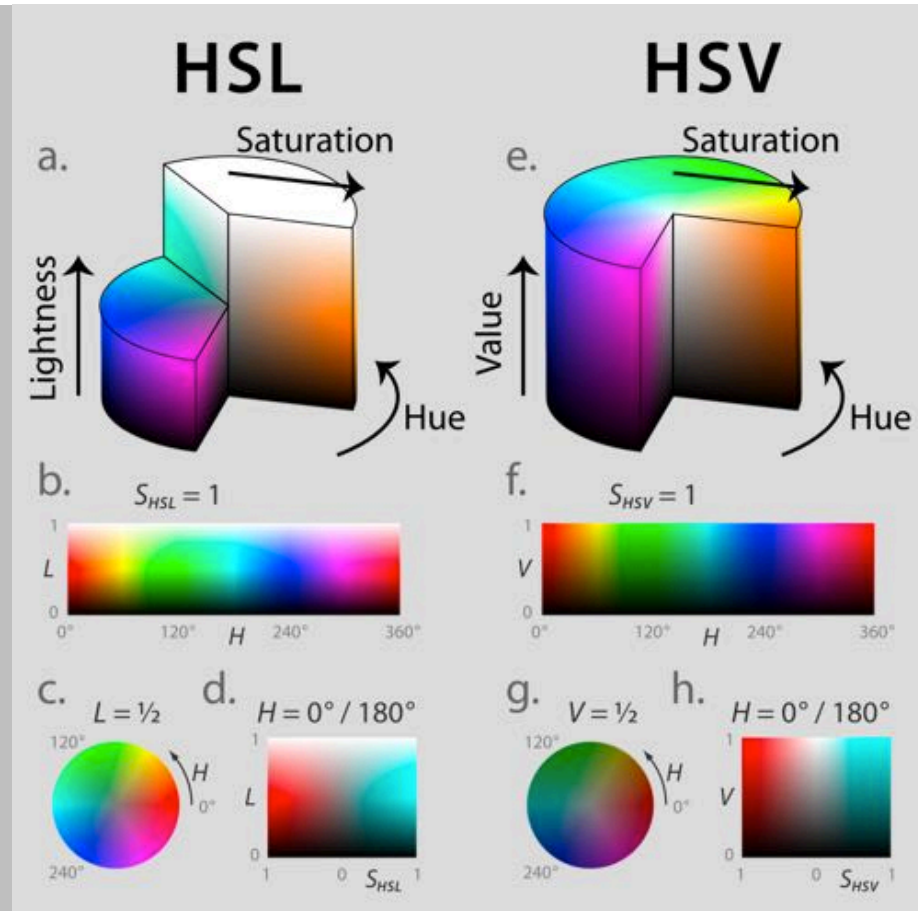
Assigning a color channel (red, green, blue) to each of three images but perception of three channels is intertwined



# Color Spaces



Red  
Green  
Blue



Hue  
Saturation  
Lightness

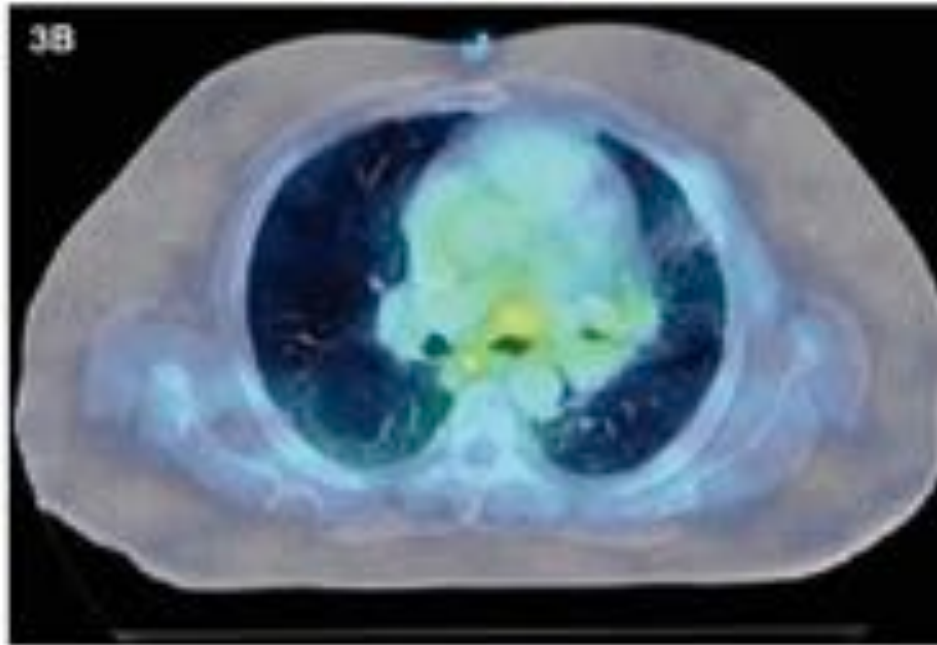
Hue  
Saturation  
Value

wikipedia.org



# Lightness/Hue Encoding

- CT rendered in lightness channel
- PET rendered in hue channel

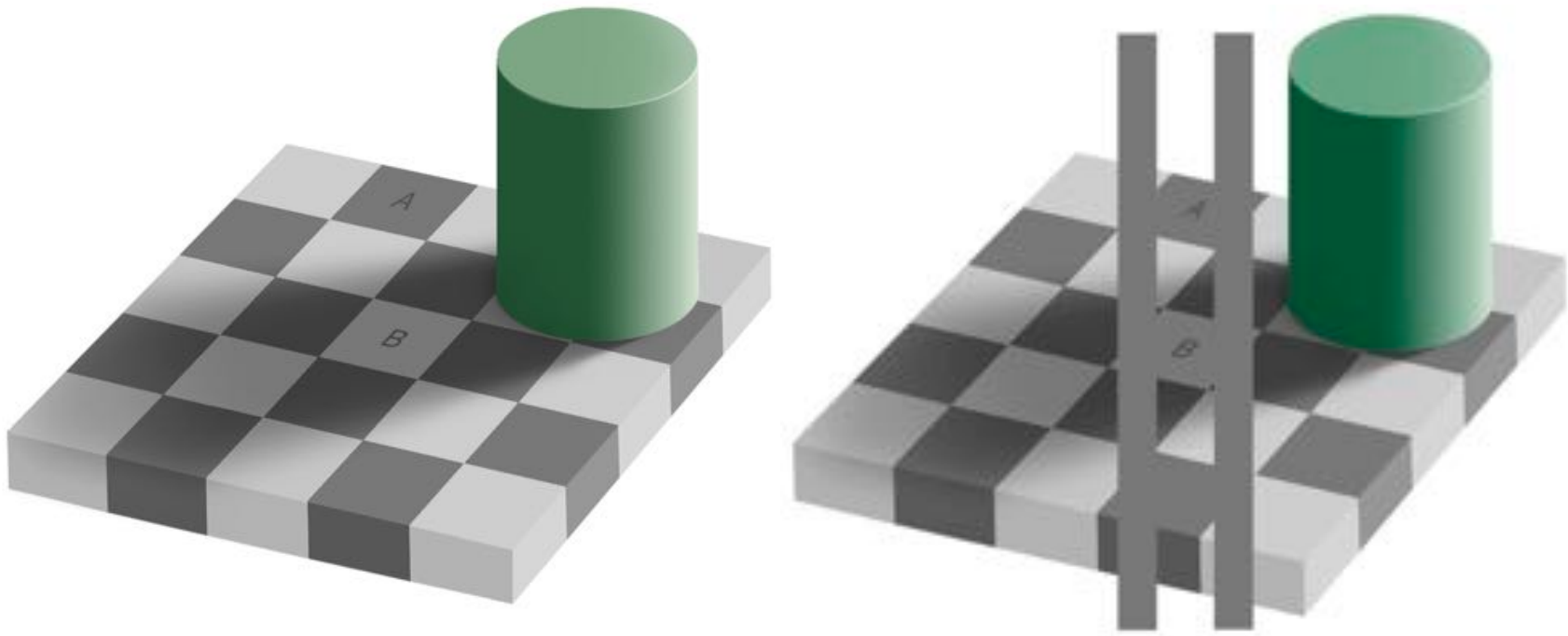


Thomas et al., Mol Im Bio 2003

**Assumption: Lightness and hue can be perceived more or less independently  
(at least better than RGB)**

# Visual Perception

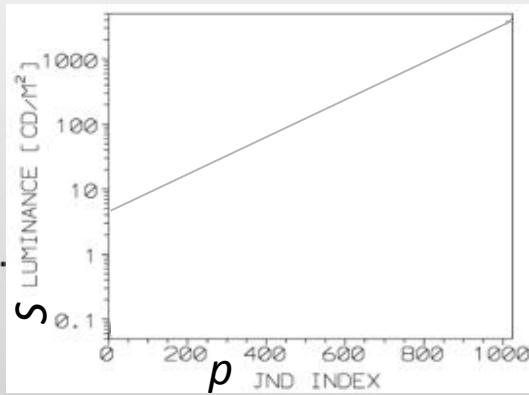
# Perception of Luminosity



# Perception of Luminosity

## Weber Fechner Law

$$dp = k \frac{dS}{S},$$
$$p = k \ln \frac{S}{S_0}$$

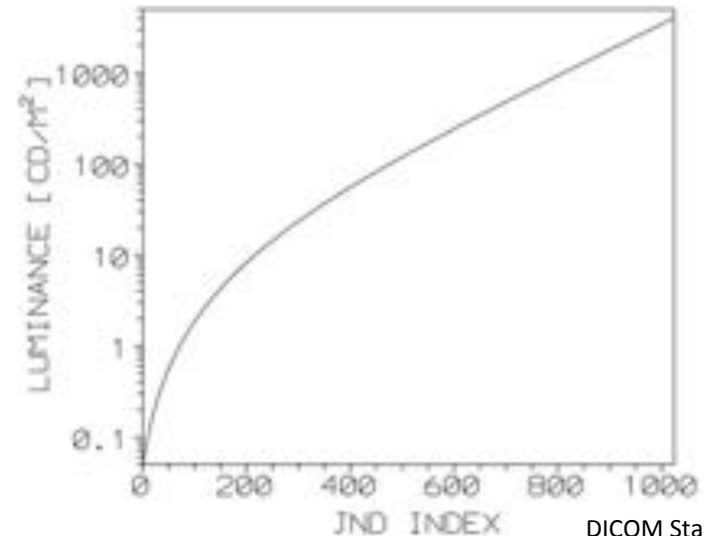


Minimally perceptible ( $p$ ) difference proportional to a percentage of overall stimulus ( $S$ )

First order approximation but it doesn't hold at low stimulus

## DICOM GSDF

(Digital Imaging and Communications in Medicine Grayscale Standard Display Function)



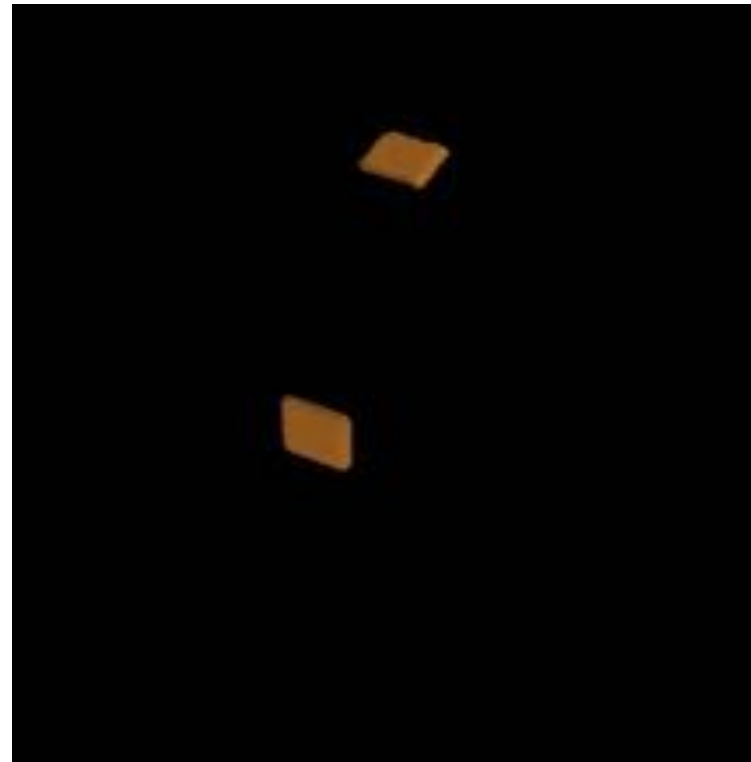
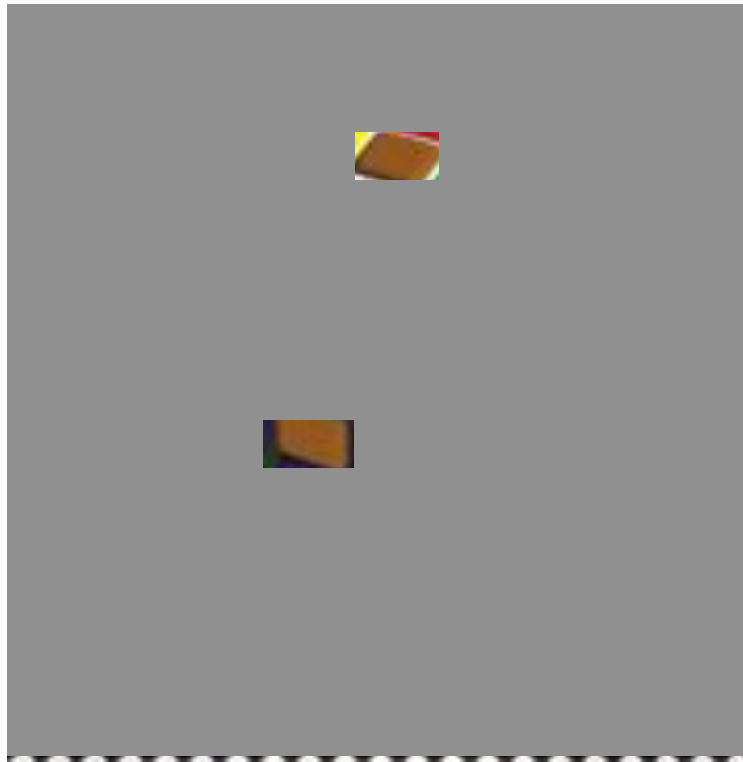
DICOM Standard 3.14

$$\log_{10} L(j) = \frac{a + c \cdot \text{Ln}(j) + e \cdot (\text{Ln}(j))^2 + g \cdot (\text{Ln}(j))^3 + m \cdot (\text{Ln}(j))^4}{1 + b \cdot \text{Ln}(j) + d \cdot (\text{Ln}(j))^2 + f \cdot (\text{Ln}(j))^3 + h \cdot (\text{Ln}(j))^4 + k \cdot (\text{Ln}(j))^5}$$

JND = Just Noticeable Difference

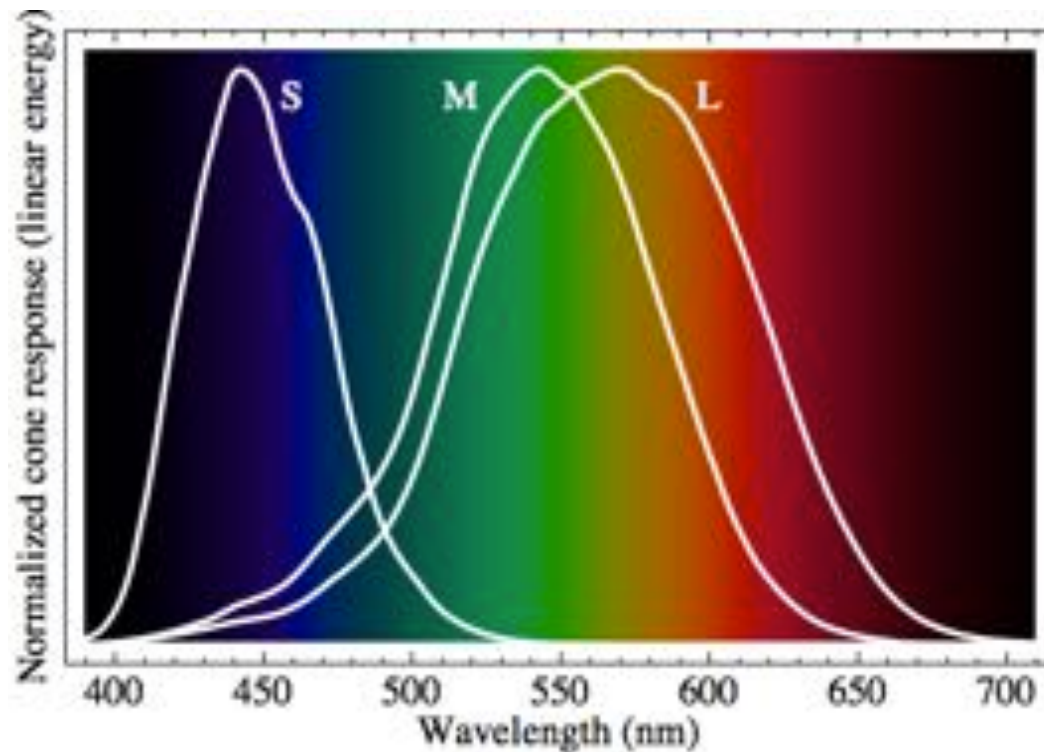
**DICOM GSDF is used to calibrate clinical image displays to transform pixel values to a perceptually uniform gamut of grayscale values**

# Perception of Color

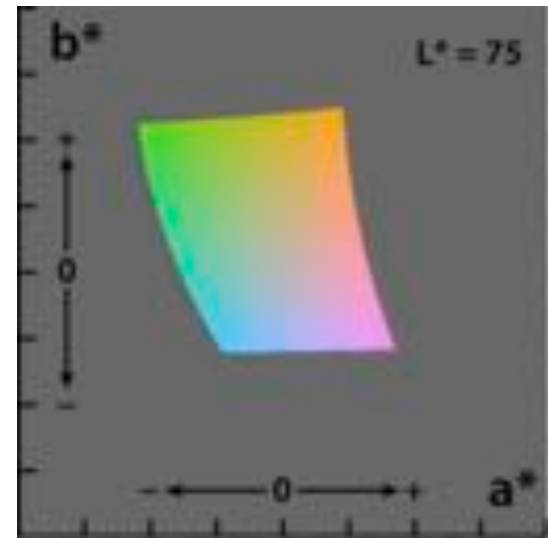


<http://www.moillusions.com/2008/02/color-tile-illusion-new-aspect.html>

# Perception of Color



Human trichromat vision



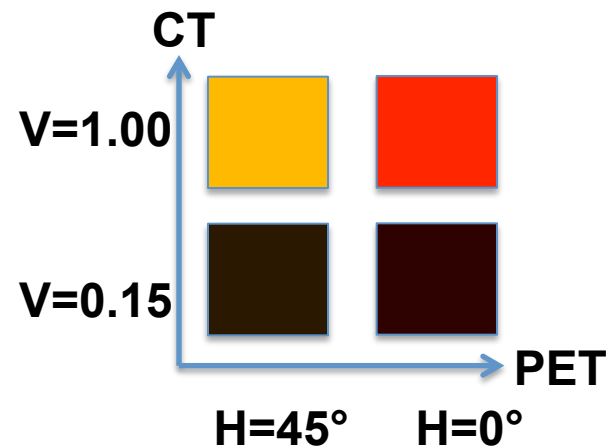
CIE  $L^*a^*b^*$  color space  
approximates perceptual uniformity

(Note: spectral properties of visible light is not inherently limited three degrees of freedom, this is just a limitation of the human visual system)

# Bezold-Brücke Effect

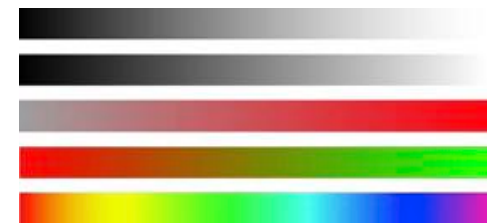
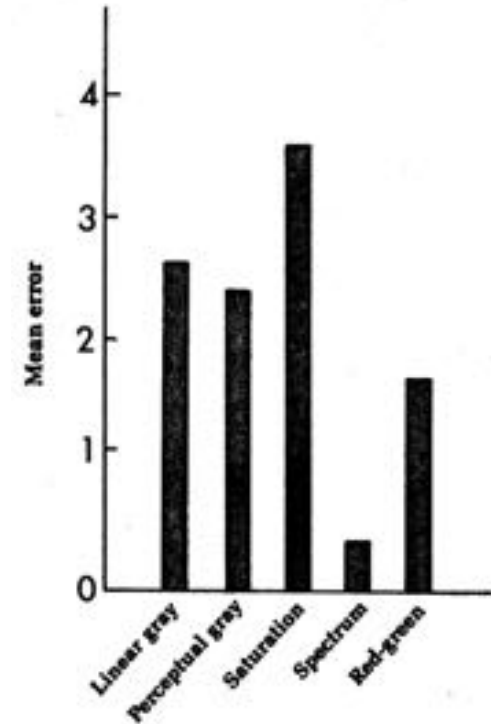
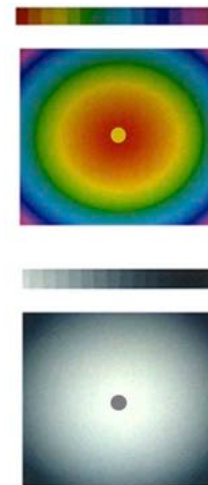
ca. 1874

- Perception of lightness and hue are not independent
  - Still better than RGB
- As lightness changes (at constant hue), the perception of hue changes
  - Very difficult to determine the hue of a nearly black pixel
  - e.g., perceived PET value depends on the underlying CT value



# Metric Information

- Simultaneous Contrast

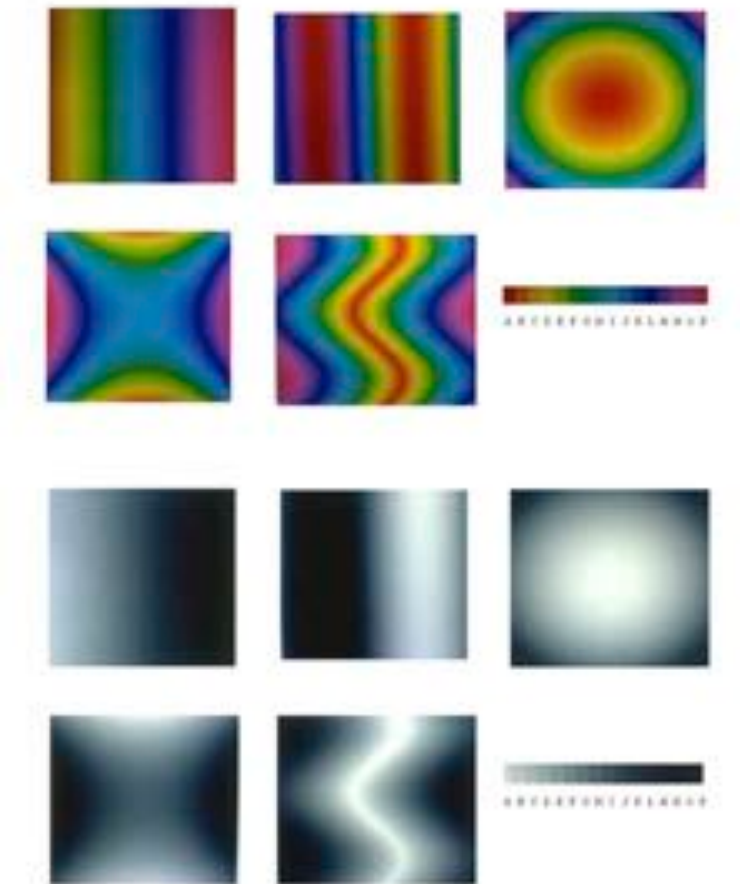


Metric quantities best shown by hue (e.g., spectrum)

Ware et al., IEEE CG&A 1988

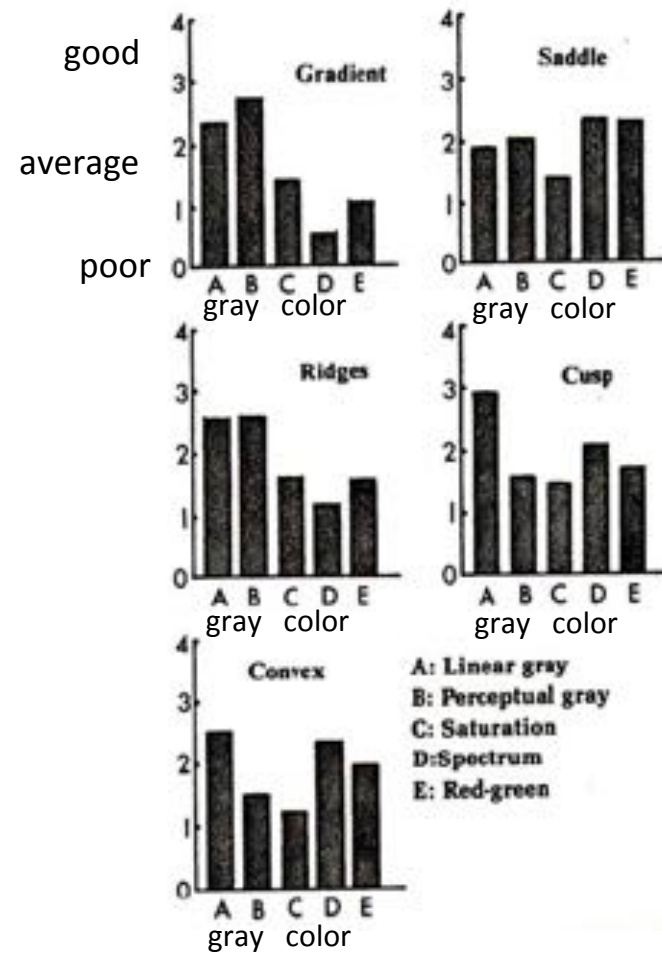


# Form Information

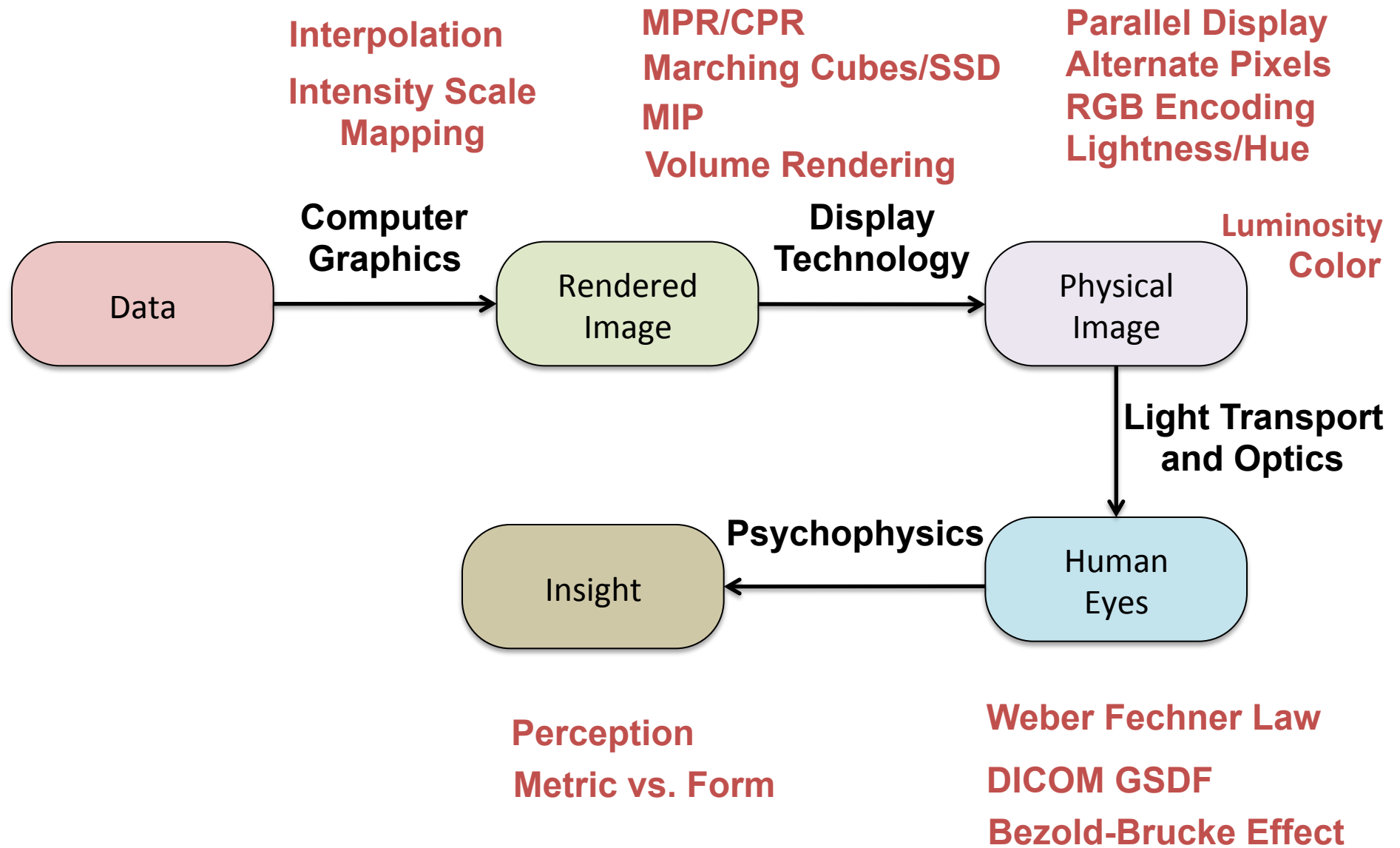


Form best shown by luminance (e.g., grayscale)

“How effective was the color sequence?”



# Visualization: From Data to Insight



# What does it mean for you?

- You now understand the pipeline from an array of pixel values to human insight
- Visualization covers a wider topics than just computer graphics
- Human perception is a critical consideration

**Next Lecture:**  
**Image Segmentation**

