High-level image interpretation using logical and morphological approaches

Yifan YANG

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1 Introduction

High-level semantics extraction from an image is an interesting research area for automatic image understanding in artificial intelligence. Many related fields like image annotation, activity recognition and decision-support systems take advantage of semantic content. As advanced as AI has become, it still remains a big challenge for computers to accomplish complex understanding tasks as humans do. Digital image itself is a numerical representation which does not represent explicitly semantic information. Moreover, beyond a single object understanding based on low level features such as colors and forms, we focus on a complex description which relies on context information like spatial relations between diverse objects as well as prior knowledge on the application domain. For instance, in the context of medical applications, the understanding task can be formulated as giving an abstract description of a pathological brain volume, such as in Figure 1. According to different levels of anatomical prior knowledge on brain pathology, two possible descriptions could be given:

- an abnormal structure is present in the brain,

- a peripheral non-enhanced tumor is present in the right hemisphere.

In this thesis, a high-level interpretation is regarded as an explanation of what we have seen in the image. This process is an inference based on prior knowledge to link the abstract description and the observed context of the scene.
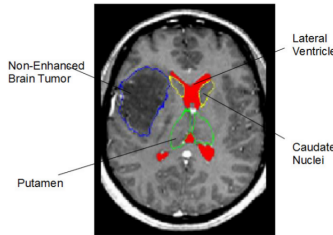

Figure 1: A slice of a pathological brain volume (MRI acquisition), where some structures are annotated.

1.1 Problem formulation

According to the objective pointed out in the previous part, the aim is to extract high-level semantic information from a given image and translate it at a linguistic level. Concretely, we are interested in the interpretation of cerebral images with tumors. The high-level information corresponds to the presence of diverse types of pathologies as well as descriptions of brain structures and spatial relations among them in a brain image. In the context of this thesis, the decision process is modeled as an abductive reasoning [2] using a logical formalism, which is an inference mechanism from facts to explanations. The objective of this thesis is to build a generic logic based formalism as well as to develop an appropriate reasoning process for image

interpretation, allowing us to extract a set of suitable candidates as potential hypotheses for a given image and to select the "best" one by a defined criterion. In image interpretation, spatial relationships are important when objects of similar appearance are present in the image, especially in magnetic resonance imaging (MRI). Such relationships have then to be included in the representation and in the reasoning process.
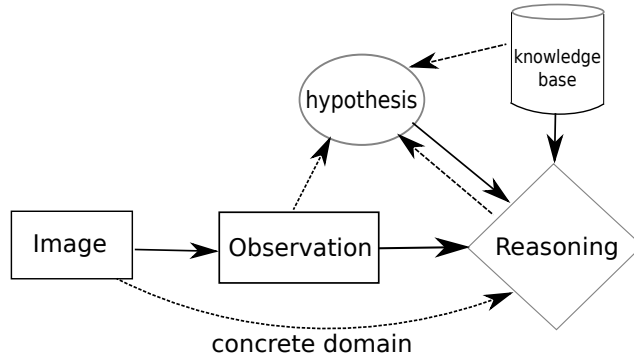
Figure 2:   A general schema of image interpretation task in the thesis.

Figure 2 shows the major components of our framework in this thesis. The given image is translated into symbolic representations in terms of logical form at the beginning. The image can also serve as the concrete domain in both the knowledge base and the reasoning process. Concrete domain is used as a real model to represent abstract terminologies in image space. A hypothesis of an description might be generated from the observation or the axioms in the knowledge base. The relations between the hypothesis and reasoning are two directions, which allows validating the hypothesis with the help of standard reasoning and building a possible hypothesis within non-standard reasoning processes.

To summarize the ongoing and future work, we need to answer the following questions:

- *How to model knowledge and formalize an appropriate presentation in application domain? (Section 2)*

- *How to connect image level representation and symbolic level representation? (Section 3)*

- *How to overcome the semantic gap between numerical representation and qualitative representation of spatial relationships? (Section 3)*

- *How to generate hypotheses to explain the observed scene? (Section 4 and Section 5)*

- *How to define a criterion to choose a "best" explanation in our case? (Section 4 and Section 5)*

1.2   Related work

Recognition of perceptual objects and scene understanding, which translate low level signal information into meaningful semantic information, belong to one of the fundamental abilities of human beings. Semantics is important in image analysis, for various tasks such as image annotation, event detection and diagnostic problems. In some specific domains, like medical imaging and remote sensing, image interpretation combines image processing with artificial intelligence techniques to derive reasonable semantics. Prior knowledge is intensively used by experts who interpret visually an image. Evidently it should then also be used by machines to associate semantics with the image. However, image interpretation still faces some difficulties, one of which is how to accurately associate perceptual data with appropriate concepts. Without an expert knowledge, such a link cannot be established. This relation between visual perception and high-level linguistic expression is called *semantic gap*.

As a high level process of exploiting semantic in the scene, image interpretation involves two levels:

- relating low level features to semantics (from pixels to semantic information) [8, 24, 31, 17].

- inferring the description of the image content (from semantics to explanation) [3, 16].

Roughly speaking, the first level describes what is happening while the second one describes how it is happening [41]. The first level has been mainly studied in the field of multiple objects recognition. Image interpretation maps regions or groups of regions onto labels corresponding to semantic concepts (e.g. labels of anatomical structures for medical images). Various approaches employ Bayesian network with a combination of semantics and probabilistic inference mechanisms [29, 34, 38]. These techniques provide inference mechanisms by attempting to construct co-occurrence objects and contextual information with a probabilistic model for reasoning.

Further, a hierarchical representation of knowledge base is proposed and so-called image grammar [42, 46]. The grammar is a structured knowledge represented by an And-Or graph. In this graph, a global description of a scene is decomposed into parts, objects until primitive pixel patches from top to bottom. An And-node consists of a set of successive components and an Or-node is composed by alternative nodes. Meanwhile, a parsing method is proposed as inference within a probabilistic model in each node [22, 45].

The second level consists in reasoning at the language (knowledge) level. For the purpose of giving an adequate explanation, the second level is a logic-based reasoning to depict the image with a deep and abstract description from the point of view of an expert. There is not much work on image interpretation using logical knowledge representation and reasoning. However, formal language based on logic formalism has a strong associated semantics for knowledge representation as well as reasoning processes. An aggregation concept is proposed to represent a complex event or scene concerning occurrence objects, as well as spatial and temporal constraints configuration [16]. According to these defined aggregation and specific rules, a high-level interpretation is able to be inferred [32]. In addition, the results using Bayesian network and image grammar are limited to defined descriptions. A complex description can also be generated when non-explicitly presented in the knowledge base [3].

2 Preliminaries

2.1 Ontology

Experts' knowledge is expressed in terms of diverse vocabulary of special domain in natural language which is difficult to be interpreted by machines. In order to facilitate automated reasoning process with background knowledge base, a structural semantic based model is an effective means to represent the prior knowledge. The term ontology is derived from philosophy and then used for the purpose of expressing common sense knowledge in computer science [1]. Since then, ontologies was adopted for image interpretation tasks [6, 24, 40]. Ontologies are defined as *"a formal specification of a shared conceptualization"* [39], which deal with modeling a universal and reusable knowledge among different applications for a specific domain. Ontologies is also studied for reasoning service within its expressive formal description. An ontology mainly contains *individuals*, *concepts*, *properties* and *axiom rules*. These components enable the background knowledge to be understood and processable by machines.

2.2 Description Logics

As mentioned above, ontologies require a formal representation language and well-defined semantics for reasoning services. Description Logics (DLs) is a family of knowledge representation logical formalisms, which is seen as good candidates for ontologies [23]. The basic elements of Description logics are concepts (unary predicates), roles (binary predicates) and individuals. Besides the formal knowledge representation, the other reason of treating DLs as an important logical formalism is its ability of reasoning process. Implicit information can be inferred from explicit knowledge description, such as satisfiability checking [4]. In this part, we introduce syntax and semantics of a description logic language $\mathcal{ALC}$ as well as its reasoning services.

2.2.1 Syntax and semantics

We first recall the syntax and semantics of the basic language of Description Logics ($\mathcal{ALC}$).

Definition 1 (Signature)**.** *The syntax of a Description Logic is defined over a signature, which is defined as three disjoint sets $Sig = (N_C, N_R, N_I)$. N_C is a set of concept names that refers to a set of entities with the same characteristics. N_I is a set of individuals that contains instances of the concepts in N_C. N_R is a set of role names that refers to the binary relationships between two individuals or two concepts.*

Definition 2 (Concept expression)**.** *The set of concept expression is recursively built from the signature such that:*

- *all the concept names, as well as $\top$ (top concept) and $\bot$ (bottom concept) are concepts,*

- *if C and D are two concepts in N_C and r is a role in N_R then $\neg C$ (negation), $C \sqcap D$ (conjunction), $C \sqcup D$ (union), $\exists r.C$ (existential quantification), $\forall r.C$ (universal quantification) are also concepts.*

Let $\mathfrak{C}$ be the infinite set of all the concepts that can be defined using constructors and signature elements.

Definition 3 (Terminological box (TBox) and assertional box (ABox))**.** *A general concept inclusion axiom (GCI) is an expression of the form $C \sqsubseteq D$ for two concepts. An equality is an expression of the form $C \equiv D$. An equality can be written in terms of GCI: $C \sqsubseteq D$ and $D \sqsubseteq C$. A TBox is a finite set of GCIs (an equality is expressed by two GCIs), denoted by $\mathcal{T}$.*

An ABox is a set of individual assertions: $a : C$, $b : D$ and $(a, b) : r$, where $a \in N_I$ and $b \in N_I$ are two instances of concepts C and D, called concept assertions, and the binary relation between a and b is an assertion of role r, called role assertion. An ABox is denoted by $\mathcal{A}$.

A knowledge base is a pair of TBox and ABox: $\mathcal{K} = (\mathcal{T}, \mathcal{A})$.

Definition 4 (Model of $\mathcal{ALC}$)**.** *An interpretation $\mathcal{I} = (\Delta^\mathcal{I}, \cdot^\mathcal{I})$ provides the semantics of concepts and roles. $\Delta^\mathcal{I}$ is a non-empty set which indicates the entire "world" of the application domain. $\cdot^\mathcal{I}$ is an interpretation function which connects concept and individual symbols to $\Delta^\mathcal{I}$ and roles to $\Delta^\mathcal{I} \times \Delta^\mathcal{I}$.*

- *Every concept $C \in N_C$ is interpreted as a subset of $\Delta^\mathcal{I}$, represented by $C^\mathcal{I} \subseteq \Delta^\mathcal{I}$.*

- *Every role r is interpreted as a subset of $\Delta^\mathcal{I} \times \Delta^\mathcal{I}$, denoted as $r^\mathcal{I} \subseteq \Delta^\mathcal{I} \times \Delta^\mathcal{I}$.*

- *Every individual $a \in N_I$ is interpreted as an element in the set $\Delta^\mathcal{I}$, denoted as $a^\mathcal{I} \in \Delta^\mathcal{I}$.*

The interpretation for concept expressions and axioms in the knowledge base are shown in Table 1.

Constructor	Syntax	Semantics	Example
Atomic Concept	C	$C^\mathcal{I} \subseteq \Delta^\mathcal{I}$	*Human*
Negation	$\neg C$	$\Delta^\mathcal{I} \backslash C^\mathcal{I}$	*¬Human*
Top	$\top$	$\top^\mathcal{I} = \Delta^\mathcal{I}$	*All*
Bottom	$\bot$	$\bot^\mathcal{I} = \emptyset^\mathcal{I}$	*Nothing*
Conjunction	$(C \sqcap D)$	$C^\mathcal{I} \cap D^\mathcal{I}$	*Human $\sqcap$ Male*
Disjunction	$(C \sqcup D)$	$C^\mathcal{I} \cup D^\mathcal{I}$	*Female $\sqcup$ Male*
Universal Qualification	$\forall R.C$	$\{x \in \Delta^\mathcal{I} \mid \forall y \in \Delta^\mathcal{I} : \langle x, y \rangle \in R^\mathcal{I} \text{ implies } y \in C^\mathcal{I}\}$	*$\forall$hasChild.Human*
Existential Restriction	$\exists R.C$	$\{x \in \Delta^\mathcal{I} \mid \exists y \in \Delta^\mathcal{I} : \langle x, y \rangle \in R^\mathcal{I} \text{ and } y \in C^\mathcal{I}\}$	*$\exists$hasChild.Female*
Subsumption	$C \sqsubseteq D$	$C^\mathcal{I} \subseteq D^\mathcal{I}$	*Man $\sqsubseteq$ Human*
Concept definition	$C \equiv D$	$C^\mathcal{I} = D^\mathcal{I}$	*Father $\equiv$ Man $\sqcap$ $\exists$hasChild.Hum*
Concept Assertion	$a : C$	$a^\mathcal{I} \in C^\mathcal{I}$	*John : Man*
Role Assertion	$(a, b) : R$	$\langle a^\mathcal{I}, b^\mathcal{I} \rangle \in R^\mathcal{I}$	*(John, Lea) : hasChild*

Table 1: Syntax and interpretations of $\mathcal{ALC}$.

An example of the knowledge base referring brain anatomy is as follows[1]:

$$TBox = \{Hemisphere \sqsubseteq \exists isPartOf.Brain$$
$$BrainStructure \sqsubseteq \exists isPartOf.Brain$$
$$BrainDisease \sqsubseteq \exists isPartOf.Brain \sqcap \neg BrainStructure$$
$$Tumor \sqsubseteq BrainDisease$$
$$LVl \sqsubseteq BrainStructure \sqcap \exists (rightOf \sqcap closeTo).CNl$$
$$LVr \sqsubseteq BrainStructure \sqcap \exists (leftOf \sqcap closeTo).CNr$$
$$CNl \sqsubseteq BrainStructure$$
$$CNr \sqsubseteq BrainStructure$$

$$ABox = \{a : CNl$$
$$b : unknownobject$$
$$c : Brain$$
$$\langle a,b \rangle : leftOf, closeTo$$
$$\langle b,c \rangle : isPartOf\}$$

This knowledge base example demonstrates a practical way to represent brain anatomy. For instance, $LVl \sqsubseteq BrainStructure \sqcap \exists (rightOf \sqcap closeTo).CNl$ expresses that the left lateral ventricle belongs to the brain structure which is on the right of and close to the left caudate nucleus. In the ABox, a, b, c are individuals of observed objects in the image. $a : CNl$ is a concept assertion and $\langle b, c \rangle : isPartOf$ is a role assertion, expressing that b is a part of c.

2.2.2 Reasoning services

Implicit information which is not explicitly defined in the knowledge base needs to be inferred with reasoning services. Reasoning services in Description Logic are decision procedures based on a knowledge base model. The basic reasoning on concept in Description Logics is subsumption checking (written as $\mathcal{T} \vDash C \sqsubseteq D$) and concept satisfiability checking (written as $\mathcal{T} \nvDash C \equiv \bot$). Subsumption checking is a decision procedure to check whether a concept D is more general than another concept C. Checking satisfiability of a concept C is a decision procedure to determine whether C has a model with respect to the TBox. Complex reasoning services are built based on the basic ones. For example, classification is a decision procedure to find subconcept and superconcept relationships between concepts in a given terminology. This allows us to find a position in terminological hierarchy. Therefore, classification can be reduced to subsumption checking of each pair of concepts in the given terminology. The definitions of subsumption and satisfiability of a concept are introduced as follows [4]:

- subsumption checking: $\mathcal{T} \vDash C \sqsubseteq D$ if $C^{\mathcal{I}} \subseteq D^{\mathcal{I}}$ for every model of $\mathcal{I}$ of $\mathcal{T}$.

- concept satisfiability: C is satisfiable with respect to $\mathcal{T}$ if there exists a model $\mathcal{I}$ of $\mathcal{T}$ such that $C^{\mathcal{I}} \neq \emptyset$.

All the reasoning problems like subsumption, classification, consistency checking, can be reduced as a concept satisfiability problem [4].

2.3 Tableau method reasoning

The tableau algorithm is an efficient decision procedure for this problem [5, 33, 20]. This method tries to construct a model of a concept C with respect to the given terminological knowledge. All the concepts are required to be expressed in negation normal form (NNF).

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[1]Due to the limited space, left and right lateral ventricles are abbreviated to LVl and LVr. Similarly, left and right caudate nuclei are denoted by CNl and CNr

Definition 5. *(Negation normal form) Negation normal form is a form of concept expression such that the negation constructor appears only before atomic concepts. The rules of transformation are described as follows:*

- $\neg(\neg C) \equiv C,$

- $\neg(C \sqcup D) \equiv \neg C \sqcap \neg D,$

- $\neg(C \sqcap D) \equiv \neg C \sqcup \neg D,$

- $\neg(\exists r.C) \equiv \forall r.\neg C,$

- $\neg(\forall r.C) \equiv \exists r.\neg C$

Definition 6 (A tableau for $\mathcal{ALC}$). *Let D be an $\mathcal{ALC}$ concept in NNF and let R_D be the set of roles in $\mathcal{ALC}$, a tableau T for D is defined as a triple $(\mathbf{S}, \mathcal{L}, \mathcal{E})$, where $\mathbf{S}$ is a set of interpretation elements; $\mathcal{L}$ relates each interpretation element to a set of concepts occurring in D (from $\mathbf{S}$ to $\mathcal{P}(\mathfrak{C})$); $\mathcal{E}$ relates each pair of interpretation elements to a set of roles in R_D (from $\mathbf{S} \times \mathbf{S}$ to $\mathcal{P}(R_D)$).*

The decision procedure to check the satisfiability of a given concept D is based on constructing a model using the tableau method. Let x and y be two interpretation elements in $\mathbf{S}$ ($x, y \in \mathbf{S}$), C, E be two concepts occurring in D and $r \in R_D$. The model is constructed as a tree structure where each node corresponds to an element of interpretation $x \in \Delta^{\mathcal{I}}$. The node is labeled with a set of concepts $\mathcal{L}(x)$. The edge between the nodes x and y is labeled with corresponding roles $r \in \mathcal{E}(\langle x, y \rangle)$. The following properties hold:

- *if $C \in \mathcal{L}(x)$, then $\neg C \notin \mathcal{L}(x)$.*

- *if $C \sqcap E \in \mathcal{L}(x)$, then $C \in \mathcal{L}(x)$ and $E \in \mathcal{L}(x)$.*

- *if $C \sqcup E \in \mathcal{L}(x)$, then $C \in \mathcal{L}(x)$ or $E \in \mathcal{L}(x)$.*

- *if $\exists r.C \in \mathcal{L}(x)$, then there exists some $y \in \mathbf{S}$ such that $r \in \mathcal{E}(\langle x, y \rangle)$ and $C \in \mathcal{L}(y)$.*

- *if $\forall r.C \in \mathcal{L}(x)$, then for all existing $y \in \mathbf{S}$ such that $r \in \mathcal{E}(\langle x, y \rangle)$, $C \in \mathcal{L}(y)$.*

To check the satisfiability of a concept D, the tableau method is initialized by a root node associated with an interpretation element x and $D \in \mathcal{L}(x)$. The tableau is expanded with new nodes for $\exists r.C$. The edge linking two nodes is labeled with a role r. Each node is updated by adding or removing elements in $\mathcal{L}(x)$ and $\mathcal{E}(\langle x, y \rangle)$ according to following rules:

$\sqcap$-rule: if $C_1 \sqcap C_2 \in \mathcal{L}(x)$, x is not indirectly blocked and $\{C_1, C_2\} \not\subseteq \mathcal{L}(x)$, then $\mathcal{L}(x) \rightarrow \mathcal{L}(x) \cup \{C_1, C_2\}$.

$$\mathcal{L}(x) = \{C_1 \sqcap C_2\}$$
$$|$$
$$\mathcal{L}(x) = \{C_1 \sqcap C_2, \ C_1, \ C_2\}$$

$\sqcup$-rule: if $C_1 \sqcup C_2 \in \mathcal{L}(x)$, x is not indirectly blocked and $\{C_1, C_2\} \cap \mathcal{L}(x) \neq \emptyset$, then $\mathcal{L}(x) \rightarrow \mathcal{L}(x) \cup \{C\}$ *for some* $C \in \{C_1, C_2\}$.

$$\mathcal{L}(x) = \{C_1 \sqcup C_2\}$$
$$\mathcal{L}(x) = \{C_1 \sqcup C_2, \ C_1\} \qquad \mathcal{L}(x) = \{C_1 \sqcup C_2, \ C_2\}$$

$\exists$-rule: if $\exists r.C \in \mathcal{L}(x)$, x is not blocked and x has no r-neighbor y with $C \notin \mathcal{L}(y)$, then create a new node y with $\mathcal{E}(\langle x, y \rangle)$ and $\mathcal{L}(y) = \{C\}$.

$$\mathcal{L}(x) = \{\exists r.C\}$$
$$|$$
$$\mathcal{L}(x) = \{\exists r.C\}$$
$$\mathcal{L}(y) = \{C\}$$
$$\mathcal{E}(\langle x, y\rangle) = \{r\}$$

$\forall$-rule: if $\forall r.C \in \mathcal{L}(x)$, x is not indirectly blocked and there exists an r-neighbor y of x with $C \notin \mathcal{L}(y)$, then $\mathcal{L}(y) \rightarrow \mathcal{L}(y) \cup \{C\}$.

$$\mathcal{L}(x) = \{\forall r.C\}$$
$$\mathcal{L}(y) = \{D\}$$
$$\mathcal{E}(\langle x, y\rangle) = \{r\}$$
$$|$$
$$\mathcal{L}(x) = \{\forall r.C\}$$
$$\mathcal{L}(y) = \{C,\ D\}$$
$$\mathcal{E}(\langle x, y\rangle) = \{r\}$$

The tableau is said to be complete when there exists a clash in some node x or none of the rules mentioned above can be applied in the tableau. For a given concept D, D *is satisfiable* if the tableau is complete without a clash, otherwise D *is unsatisfiable*.

Definition 7. *(Clash) A tableau contains a clash if, for a node x and a concept C, $\{C, \neg C\} \subseteq \mathcal{L}(x)$.*

$$\mathcal{L}(x) = \{C,\ \neg C\}$$
$$|$$
$$\boxtimes$$

3 Qualitative spatial reasoning

Qualitative spatial relations such as "contains", "left of", "close to", "between" can be categorized into three types: topological relations [28], directional relative relations and distances [18]. These relations are frequently used at a linguistic level by humans when describing a scene [19]. Even though quantitative information is more precise, human cannot use it as accurate as machine. Hence through qualitative representation to describe the relation of spatial objects is crucial. The aim of our study is applying human knowledge to the description of qualitative relationships and the reasoning tasks with spatial objects in a complex scene. Qualitative spatial reasoning deals with the following questions, among others:

- Can we recognize an object from known objects and their spatial relations?

- Which relationships are satisfied between two objects when their relationships are not explicitly described in a given knowledge base?

- Is a recognized spatial arrangement of a scene consistent with the given knowledge of the scene?

The reasoning task can be summarized as follows:

1. Determining whether an object satisfies a spatial configuration, where an object is described by an observation of spatial arrangement and a spatial configuration is defined using expert knowledge. Then the task is considered as a consistency checking of the observed object with respect to spatial configuration in the knowledge base.

2. Determining the relationship between two objects from other spatial arrangement. The implicit relation between two objects can be inferred by other known spatial relations in a spatial arrangement.

3. Determining consistency of spatial arrangement in a given configuration of the scene with respect to a specific domain knowledge. This task verifies the consistency between the observation and the spatial configuration defined using expert knowledge.

In this sections, we discuss different representations of spatial relations and illustrate our formalism to perform spatial reasoning.

3.1 State of the art

Spatial relationship is an important factor for image interpretation in brain images due to the similar appearance among brain structures [8]. Chen *et al.* discussed a border range of spatial relation representations [9]. Different spatial calculi are summarized for various aspects of space (topology, direction, distance, object shape, etc.). Basic qualitative spatial relations are summarize in Table.2.

Topological relations	Directional relations	Distance relations
dc ("disconnected from")	left of	far from
eq ("equal with", "identical")	right of	close to
po ("intersect with", "partially overlaps")	above	
ec ("external connected with","touches", "adjacent")	below	
tpp ("tangential proper part of")	in front of	
tppi ("inversion of tpp")	behind	
ntpp ("not tangential proper part of")		
ntppi ("inversion of ntpp")		

Table 2: Basic spatial relations

3.1.1 Topology

Topology has been mostly investigated and the most popular representation is based on *Region Connection Calculus* (RCC) [10]. The collection {*dc, eq, po, ec, tpp, tppi, ntpp, ntppi*} is a set of disjoint exhaustive topological relations defined as RCC8 [35]. Between any two objects in topological space, only one of eight relations can be hold. Therefore, a useful reasoning mechanism of RCC8 based on a composition table is proposed in [14] (Table.3). Let A, B, C be three objects in topological space, both A, B and B, C are adjacent (*ec*). Then the possible relations between A, C can be found within the table. This reasoning mechanism allows answer the second and the third questions of qualitative spatial reasoning problems. However, the composition table only gives possible relations and many of composition rules give no information like $dc(A, B)$ and $dc(B, C)$ (All the relations are possibly hold between A and C from the composition table). Further, the RCC8 representation and composition table were constructed for determining a satisfaction problem in a specific arrangement [43, 44]. Unfortunately, the inference within this kind of representation is undecidable [43]. Afterwards, Lutz *et al.* exploited qualitative reasoning in concrete domains with constraint satisfaction problems [30]. In the context of brain anatomy, only the inclusion relations are interested [36]. The property of transitivity is emphasized in this context.

	dc (B,C)	**ec (B,C)**	eq (B,C)	ntpp (B,C)	tpp (B,C)	ntppi (B,C)	tppi (B,C)	op (B,C)
dc (A,B)	dc or ec or eq or ntpp or tpp or ntppi or tppi or op	dc or ec or ntpp or tpp or op	dc	dc or ec or ntpp or tpp or op	dc or ec or ntpp or tpp or op	dc	dc	dc or ec or ntpp or tpp or op
ec (A,B)	dc or ec or eq or ntpp or tpp or ntppi or tppi or op	**dc or ec or ntpp or tpp or op**	dc	dc or ec or ntpp or tpp or op	dc or ec or ntpp or tpp or op	dc	dc	dc or ec or ntpp or tpp or op
eq (A,B)	dc	ec	eq	ntpp	tpp	ntppi	tppi	op
ntpp (A,B)	dc	dc	ntpp	ntpp	ntpp	dc or ec or eq or ntpp or tpp or ntppi or tppi or op	dc or ec or ntpp or tpp or op	dc or ec or ntpp or tpp or op
tpp (A,B)	dc	dc or ec	tpp	ntpp	tpp or ntpp	dc or ec or ntppi or tppi or op	dc or ec or eq or tpp or tppi or op	dc or ec or ntpp or tpp or op
ntppi (A,B)	dc or ec or ntppi or tppi or op	ntppi or tppi or op	ntppi	eq or ntpp or tpp or tppi or ntppi or op	tppi or ntppi or op	ntppi	ntppi	tppi or ntppi or op
tppi (A,B)	dc or ec or ntppi or tppi or op	ec or ntppi or tppi or op	tppi	ntpp or tpp or op	eq or tpp or tppi or op	ntppi	ntppi or tppi	ntppi or tppi or op
op (A,B)	dc or ec or ntppi or tppi or op	dc or ec or ntppi or tppi or op	op	ntpp or tpp or op	ntpp or tpp or op	dc or ec or ntppi or tppi or op	dc or ec or ntppi or tppi or op	dc or ec or eq or ntpp or tpp or ntppi or tppi or op

Table 3: The 64 compositions of binary topological relations between objects A and C via the third object B. Extracted from [14].

3.1.2 Direction

Directional relations are seen as primarily important spatial relationships in brain anatomical images [8, 24, 31, 17]. As mentioned in [8], a direction is defined by a *target object*, a *reference object* and a *reference system*. In an 3D space, directional relations are represented by six basic terms (e.g.: right, above, behind, etc.). In order to compute directional relationships between two objects, many methods such as histograms

of angles and morphological approaches are summarized in [8]. Fuzzy representation is employed in these approaches. A fuzzy landscape of a certain direction is computed using morphological dilatation with respect to the reference object. The satisfaction degree of the direction between the target object and the reference object is evaluated by comparison between the target object and the fuzzy landscape. In crisp logic, many researches are based on two categories: point based and extend object based (bounding box) [9]. However, both of two representation ignore the influence of objects forms. The representation is not as accurate to human intuition as fuzzy representation.

3.2 Role Box

In this section, we give the logical formalism to represent qualitative spatial relationships as roles and corresponding properties in terms of role axioms within a role box.

3.2.1 Syntax and semantics of roles

Definition 8. *(Role syntax) Let N_R be a set of role names, the inverse roles and the negation of roles are represented by r^- and $\neg r$. Complex roles are characterized with $r_1 \sqcap r_2$ and $r_1 \sqcup r_2$. Role axioms are used for modeling properties of roles such as inclusion ($r_1 \sqsubseteq r_2$), role composition ($r_1 \circ r_2$).*

Table 4 describes a main syntax and semantics of roles for Description Logics.

Constructor	Syntax	Semantics
Atomic role	r	$r^{\mathcal{I}} \subseteq \Delta^{\mathcal{I}} \times \Delta^{\mathcal{I}}$
Inverse role	r^-	$\{\langle x,y\rangle,\ x \in \Delta^{\mathcal{I}},\ y \in \Delta^{\mathcal{I}}\mid (y,x) \in r^{\mathcal{I}}\}$
Role negation	$\neg r$	$\Delta^{\mathcal{I}} \times \Delta^{\mathcal{I}} \setminus r^{\mathcal{I}}$
Role composition	$r_1 \circ r_2$	$\{(x,z), x \in \Delta^{\mathcal{I}},\ z \in \Delta^{\mathcal{I}}\mid \exists y \in \Delta^{\mathcal{I}}, \langle x,y\rangle \in r_1^{\mathcal{I}}\ and\ (y,z) \in r_2^{\mathcal{I}}\}$
Role conjunction	$r_1 \sqcap r_2$	$r_1^{\mathcal{I}} \cap r_2^{\mathcal{I}}$
Role disjunction	$r_1 \sqcup r_2$	$r_1^{\mathcal{I}} \cup r_2^{\mathcal{I}}$
Role inclusion	$r_1 \sqsubseteq r_2$	$r_1^{\mathcal{I}} \subseteq r_2^{\mathcal{I}}$
Role equivalence	$r_1 \equiv r_2$	$r_1^{\mathcal{I}} = r_2^{\mathcal{I}}$

Table 4: Basic spatial relations

Definition 9. *(Role inclusion axiom) A role inclusion axiom is defined in the form:*

$$r \sqsubseteq s,$$

where r and s are basic roles in N_R or complex roles built with role constructors. A role equivalence $r \equiv s$ can be rewritten in the form $r \sqsubseteq s$ and $s \sqsubseteq r$.

Definition 10. *(RBox) A role box, denoted by RBox, is a finite set of axioms for N_R based on a set of roles $\mathbf{R} = N_R \cup \{r^-\mid r \in N_R\}$, where r^- represents the inversion of role r. Based on role inclusions and role equivalences, role axioms characterize role properties such that:*

- *role composition: $u \circ v \sqsubseteq r_1 \sqcup \cdots \sqcup r_n$ with $n \geqslant 1$, which is interpreted as $(u \circ v)^{\mathcal{I}} \subseteq r_1^{\mathcal{I}} \cup \cdots \cup r_n^{\mathcal{I}}$. If there exists three interpretation elements $x,y,z \in \Delta^{\mathcal{I}}$, $\langle x,y\rangle \in u^{\mathcal{I}}$ and $\langle y,z\rangle \in v^{\mathcal{I}}$ implies $\langle x,z\rangle \in r_1^{\mathcal{I}} \cup \cdots \cup r_n^{\mathcal{I}}$.*

- *transitive role: $r \circ r \sqsubseteq r$, which is interpreted as $(r \circ r)^{\mathcal{I}} \subseteq r^{\mathcal{I}}$. If there exists three interpretation elements $x,y,z \in \Delta^{\mathcal{I}}$, $\langle x,y\rangle \in r^{\mathcal{I}}$ and $\langle y,z\rangle \in r^{\mathcal{I}}$ implies $\langle x,z\rangle \in r^{\mathcal{I}}$.*

- *inverse roles: $u \equiv v^-$, which is interpreted as $u^{\mathcal{I}} = v^{-\mathcal{I}}$. There exists two interpretation elements $x,y \in \Delta^{\mathcal{I}}$, then $\langle x,y\rangle \in u^{\mathcal{I}}$ iff $\langle y,x\rangle \in v^{\mathcal{I}}$.*

- *symmetric role: $r \equiv r^-$, which is interpreted as $r^{\mathcal{I}} = r^{-\mathcal{I}}$. There exists two interpretation elements $x,y \in \Delta^{\mathcal{I}}$, then $\langle x,y\rangle \in r^{\mathcal{I}}$ iff $\langle y,x\rangle \in r^{\mathcal{I}}$.*

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- *disjoint roles: $u \sqsubseteq \neg v$. which is interpreted as $u^{\mathcal{I}} \subseteq \Delta^{\mathcal{I}} \setminus v^{\mathcal{I}}$ or $u^{\mathcal{I}} \cap v^{\mathcal{I}} = \emptyset$. There exists two interpretation elements $x, y \in \Delta^{\mathcal{I}}$, $\langle x, y \rangle \in u^{\mathcal{I}}$ implies $\langle x, y \rangle \notin v^{\mathcal{I}}$.*

The knowledge base used for spatial reasoning in our framework is built with three blocks: terminologies (TBox), role axioms (RBox) and assertions (ABox) ($\mathcal{K} = \{\mathcal{T}, \mathcal{R}, \mathcal{A}\}$).

To ensure the termination of tableau construction, a mechanism for detecting cyclic expansions called *blocking* is used. To define *blocking*, we first introduce the term *r-neighbor*.

Definition 11. *(r-neighbor) In the tableau, an edge $\langle x, y \rangle$ labeled with role r relates two nodes x and y, y is called a successor of x and x is called a predecessor of y. An ancestor is the transitive closure of predecessor, where the transitive closure refers to an indirect reachability relation constructed from a set of direct edges. A node y is a r-neighbor of a node x if*

- *x is a predecessor of y and $\mathcal{E}(\langle x, y \rangle) = \{r\}$.*

Definition 12. *(Blocking)*

- *A node x is directly blocked, which indicates that it has a unique ancestor y such that $\mathcal{L}(y) = \mathcal{L}(x)$.*

- *Otherwise, it is indirectly blocked if its predecessor y is blocked by another ancestor u.*

A node x is blocked if for some ancestor y, y is blocked or $\mathcal{L}(y) = \mathcal{L}(x)$.

3.3 From image to symbolic representation

The transformation of representation from low-level numerical data to symbolic level is first phase of the framework. Concretely, objects and contextual information are extracted and represented within terminologies using an ABox.

3.4 Spatial reasoning using tableaux method

4 Abductive reasoning

Abductive reasoning is a backward-chaining inference, concerned generating hypotheses and finding the "best" explanation on the basis of surprising observation. Unlike the inference operation of standard reasoning presented in Section.2, abductive reasoning is a non-monotonic reasoning. New knowledge should be added in order to positively entail the observation. Image interpretation for a diagnostic problem fits abductive reasoning mechanism. When facing an pathological brain imaging, an expert has to resort to his knowledge of pathological anatomy, in order to give an explanation for observed image. In this section, we will introduce how abductive is applied in image interpretation task from two aspects (generation and selection).

4.1 State of the art of abductive reasoning

Abductive reasoning is first proposed by Charles S. Peirce in philosophy. Afterwards, abductive is developed in artificial intelligence and cognitive science. Aliseda [2] gave a general overview of abduction in propositional logic and proposed tableaux methods for abduction. Further, in the context of Description Logics, four types of abduction problems are described by Elisenbroich [15]. Let $\mathcal{L}$ be a DL, $\mathcal{K} = \{\mathcal{T}, \mathcal{A}\}$ be a knowledge base in $\mathcal{L}$, C, D two concepts in $\mathcal{L}$ and suppose that they are satisfiable with respect to $\mathcal{K}$. The logical formalisms of abduction in DLs are represented as follows:

- Concept abduction: given an observation concept O, a hypothesis is a concept H such that $\mathcal{K} \vDash H \sqsubseteq O$.

- TBox abduction:

- ABox abduction: let S_a be a set of assertions as observation, a hypothesis is a set of S_b of ABox assertion such that $\mathcal{K} \cup S_b \vDash \phi(a)$.

- Knowledge base abduction:

[32] use DL-safe rules(expressive but preserve decidability). [37] multimedia interpretation as abduction. [11, 12] adapted tableaux methods in Description Logics formalisms. [7] discussed a set of basic minimality criteria for abductive reasoning. [2, 15, 11, 12, 27, 26, 21, 13, 25, 7]

4.2 Abductive reasoning for image interpretation

In the context of image interpretation,

4.3 Minimality criteria

Abduction as Inference to the Best Explanation. filter inconsistent and redundant ones

5 Perspectives

Several directions will be presented in this section:

- concrete domain with fuzzy logic.

- how to generate potential hypotheses.

- how to select the "best" explication with an appropriate minimality criterion.

- perspective of publications.

6 Activities

- project LOGIMA

- seminars

- doctoral formation

References

[1] James H Alexander, Michael J Freiling, Sheryl Shulman, Jeffery Staley, Steven Rehfuss, and Steven Messick. Knowledge level engineering ontological analysis. In *Proceedings of the 5th National Conference on Artificial Intelligence (AAAI)*, pages 963–968, 1986.

[2] Atocha Aliseda-Llera. *Seeking explanations: abduction in logic, philosophy of science and artificial intelligence*. PhD thesis, University of Amsterdam, 1997.

[3] Jamal Atif, Céline Hudelot, and Isabelle Bloch. Explanatory reasoning for image understanding using formal concept analysis and description logics. *IEEE Transactions on Systems, Man, and Cybernetics: Systems*, 44(5):552–570, 2014.

[4] Franz Baader. *The Description Logic handbook: theory, implementation, and applications*. Cambridge university press, 2003.

[5] Franz. Baader and Ulrike Sattler. An overview of tableau algorithms for description logics. *Studia Logica*, 69(1):5–40, 2001.

[6] Hichem Bannour and Céline Hudelot. Towards ontologies for image interpretation and annotation. In *Procedding of 9th International Workshop on Content-Based Multimedia Indexing (CBMI)*, pages 211–216. IEEE, 2011.

[7] Meghyn Bienvenu. Complexity of abduction in the $\mathcal{EL}$ family of lightweight description logics. In *Proceedings of the Eleventh International Conference on Principles of Knowledge Representation and Reasoning (KR08)*, pages 220–230, 2008.

[8] Isabelle Bloch. Fuzzy spatial relationships for image processing and interpretation: a review. *Image and Vision Computing*, 23(2):89 – 110, 2005.

[9] Juan Chen, Anthony G. Cohn, Dayou Liu, Shengsheng Wang, Jihong Ouyang, and Qiangyuan Yu. A survey of qualitative spatial representations. *The Knowledge Engineering Review*, FirstView:1–31, 10 2013.

[10] Anthony G Cohn, Brandon Bennett, John Gooday, and Nicholas Mark Gotts. Qualitative spatial representation and reasoning with the region connection calculus. *GeoInformatica*, 1(3):275–316, 1997.

[11] Simona Colucci, Tommaso Di Noia, Eugenio Di Sciascio, Francesco M. Donini, and Marina Mongiello. A uniform tableaux-based approach to concept abduction and contraction in $\mathcal{ALN}$. In *Proceedings of the 17th International Workshop on Description Logics (DL)*, volume 104, pages 158–167, 2004.

[12] Tommaso Di Noia, Eugenio Di Sciascio, and Francesco M. Donini. A tableaux-based calculus for abduction in expressive description logics: Preliminary results. In *Proceedings of 22nd International Workshop on Description Logics (DL)*, 2009.

[13] Jianfeng Du, Guilin Qi, Yi-Dong Shen, and Jeff Z. Pan. Towards practical abox abduction in large OWL DL ontologies. In *Proceedings of the 25th AAAI Conference on Artificial Intelligence (AAAI-11)*, pages 1160–1165, 2011.

[14] Max J Egenhofer. Reasoning about binary topological relations. In *Advances in Spatial Databases*, pages 141–160. Springer, 1991.

[15] Corinna Elsenbroich, Oliver Kutz, and Ulrike Sattler. A case for abductive reasoning over ontologies. In *OWL: Experiences and Directions*, volume 216, pages 10–20, 2006.

[16] Sofia Espinosa Peraldi, Atila Kaya, Sylvia Melzer, Ralf Möller, and Michael Wessel. Multimedia interpretation as abduction. In *Proceedings of the 20th International Workshop on Description Logics (DL)*, pages 323–330, 2007.

[17] Geffroy Fouquier, Jamal Atif, and Isabelle Bloch. Sequential model-based segmentation and recognition of image structures driven by visual features and spatial relations. *Computer Vision and Image Understanding*, 116(1):146 – 165, 2012.

[18] John Freeman. The modelling of spatial relations. *Computer Graphics and Image Processing*, 4(2):156–171, 1975.

[19] Christian Freksa. Qualitative spatial reasoning. *Cognitive and Linguistic Aspects of Geographic Space*, (63):361–372, 1991.

[20] Rajeev Goré and Linh Anh Nguyen. Exptime tableaux with global caching for description logics with transitive roles, inverse roles and role hierarchies. In *Automated Reasoning with Analytic Tableaux and Related Methods*, pages 133–148. Springer, 2007.

[21] Oliver Gries, Ralf Möller, Anahita Nafissi, Maurice Rosenfeld, Kamil Sokolski, and Michael Wessel. A probabilistic abduction engine for media interpretation based on ontologies. In *Web Reasoning and Rule Systems*, pages 182–194. Springer, 2010.

[22] Feng Han and Song-Chun Zhu. Bottom-up/top-down image parsing with attribute grammar. *IEEE Transactions on Pattern Analysis and Machine Intelligence*, 31(1):59–73, 2009.

[23] Ian Horrocks and Ulrike Sattler. A description logic with transitive and inverse roles and role hierarchies. *Journal of logic and computation*, 9(3):385–410, 1999.

[24] Céline Hudelot, Jamal Atif, and Isabelle Bloch. Fuzzy spatial relation ontology for image interpretation. *Fuzzy Sets and Systems*, 159(15):1929–1951, 2008.

[25] Kewen Wang Jianfeng Du and Yi-Dong Shen. A tractable approach to abox abduction over description logic ontologies. In *28th AAAI Conference on Artificial Intelligence (AAAI-14)*, pages 1034–1040. Springer, 2014.

[26] Szymon Klarman Ken Halland, Arina Britz. Tbox abduction in $\mathcal{ALC}$ using a dl tableau. In *Proceedings of the 27th International Workshop on Description Logics (DL)*, pages 556–566, 2014.

[27] Szymon Klarman, Ulle Endriss, and Stefan Schlobach. Abox abduction in the description logic $\mathcal{ALC}$. *Journal of Automated Reasoning*, 46(1):43–80, 2011.

[28] Benjamin Kuipers. Modeling spatial knowledge. *Cognitive Science*, 2(2):129–153, 1978.

[29] Jiebo Luo, Andreas E. Savakis, and Amit Singhal. A bayesian network-based framework for semantic image understanding. *Pattern Recognition*, 38:919–934, 2005.

[30] Carsten Lutz and Maja Miličić. A tableau algorithm for description logics with concrete domains and general tboxes. *Journal of Automated Reasoning*, 38(1-3):227–259, 2007.

[31] Olivier Nempont, Jamal Atif, and Isabelle Bloch. A constraint propagation approach to structural model based image segmentation and recognition. *Information Sciences*, 246:1–27.

[32] Bernd Neumann and Ralf Möller. On scene interpretation with description logics. *Image and Vision Computing*, 26(1):82–101, 2008.

[33] Linh Anh Nguyen. An efficient tableau prover using global caching for the description logic $\mathcal{ALC}$. *Fundamenta Informaticae*, 93(1):273–288, 2009.

[34] Spiros Nikolopoulos, Georgios Th. Papadopoulos, Ioannis Kompatsiaris, and Ioannis Patras. An evidence-driven probabilistic inference framework for semantic image understanding. In *Machine Learning and Data Mining in Pattern Recognition*, Lecture Notes in Computer Science, pages 525–539. Springer Berlin Heidelberg, 2009.

[35] David A Randell, Zhan Cui, and Anthony G Cohn. A spatial logic based on regions and connection. In *Proceedings of the Third International Conference on Principles of Knowledge Representation and Reasoning (KR)*, pages 165–176, 1992.

[36] Paulo Santos, Rodolpho Freire, Danilo N. dos Santos, Carlos Thomaz, Paulo Sallet, Mario Louza, and Anthony G. Cohn. *A region-based ontology of the brain ventricular system and its relation to schizophrenia*, chapter 7, pages 256–273. IGI Global, 2012.

[37] Murray Shanahan. Perception as abduction: Turning sensor data into meaningful representation. *Cognitive Science*, 29(1):103–134, 2005.

[38] Amit Singhal, Jiebo Luo, and Weiyu Zhu. Probabilistic spatial context models for scene content understanding. In *IEEE Computer Society Conference on Computer Vision and Pattern Recognition*, volume 1, pages 235–241, 2003.

[39] Rudi Studer, V Richard Benjamins, and Dieter Fensel. Knowledge engineering: principles and methods. *Data & knowledge engineering*, 25(1):161–197, 1998.

[40] Christopher Town. Ontological inference for image and video analysis. *Machine Vision and Applications*, 17(2):94–115, 2006.

[41] John K. Tsotsos. Image understanding. In *Encyclopedia of Artificial Intelligence. John Wiley*, pages 641–663. John Wiley & Sons, 1992.

[42] Kewei Tu, Meng Meng, Mun Wai Lee, Tae Eun Choe, and Song-Chun Zhu. Joint video and text parsing for understanding events and answering queries. *MultiMedia, IEEE*, 21(2):42–70, 2014.

[43] Michael Wessel. Obstacles on the way to spatial reasoning with description logics: Undecidability of $\mathcal{ALC}_{\mathcal{RA}\ominus}$. Technical report, University of Hamburg, Informatics Department (FBI-HH-M-297/00), 2000.

[44] Michael Wessel, Volker Haarslev, and Ralf Möller. $\mathcal{ALC}_{\mathcal{RA}} - \mathcal{ALC}$ with role axioms. In *Proceedings of the 13th International Workshop on Description Logics (DL)*, pages 21–30, 2000.

[45] Tianfu Wu and Song-Chun Zhu. A numerical study of the bottom-up and top-down inference processes in and-or graphs. *International journal of computer vision*, 93(2):226–252, 2011.

[46] Song-Chun Zhu and David Mumford. A stochastic grammar of images. *Foundations and Trends in Computer Graphics and Vision*, 2(4):259–362, 2006.