

# $\gamma K_S K_{\pi^0}$ , $\gamma K K_{\pi^0}$

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$$\psi' \rightarrow \gamma \eta'_c, \eta'_c \rightarrow KK\pi^0$$

# Initial Event Selection

Charged Tracks:  $n_{\text{Good}}=2, n_{\text{Charge}}=0$

- $R_{vz} < 10\text{cm}$
- $R_{vxy} < 1\text{cm}$
- $\cos\theta < 0.93$

Good Photons:  $n_{\text{Gam}} \geq 3$

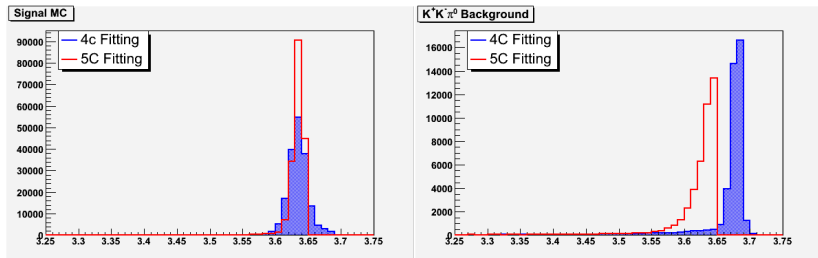
- $\text{energy} > 40 \text{ MeV}$
- $\text{time in } [0,14] \text{ (*50 ns)}$
- At 20 degree from the extrapolation of a MDC track.

PID: 1  $K^+$ , 1  $K^-$

- TOF,  $dE/dx$
- $p(K) > p(\pi), p(K) > 0.001$

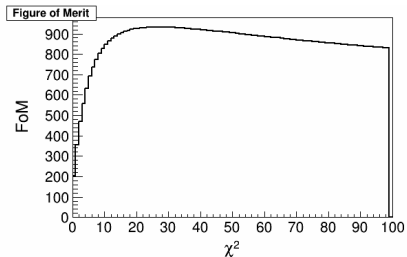
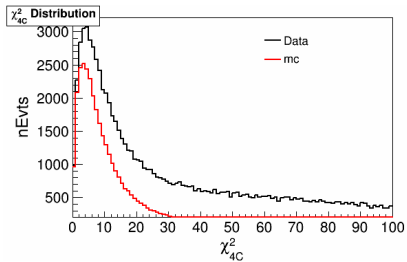
# Kinematic Fit

- 5c kinematic fit( $p_4, m_{\pi^0}$ ) to decide the choice of  $\gamma$
- 4c kinematic fit( $5C + \text{unfix } m(\gamma_{rad})$ ) for mass representation



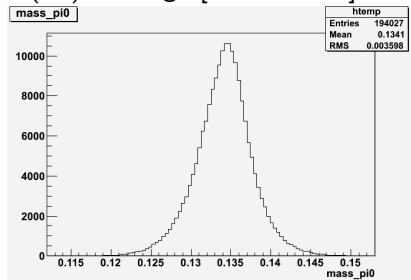
# Kinematic Fit

•  $\chi^2_{4c} < 30$



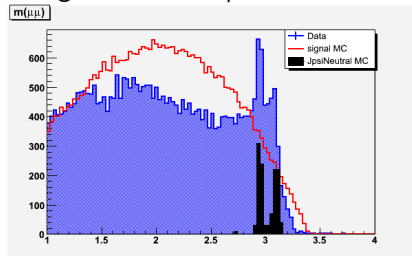
# $\pi^0$ mass requirement

$m(\pi^0)$  in range  $[0.127, 0.141]$ .



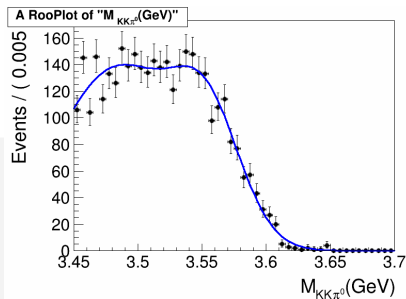
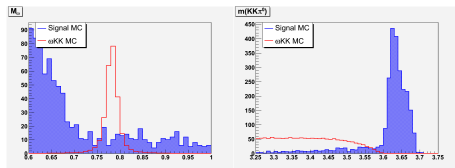
$\psi' \rightarrow \text{Neutral} + J/\psi, J/\psi \rightarrow \mu\mu/KK$  background

Require  $M(\mu\mu) < 2.9$ , where  $M(\mu\mu)$  is calculated by assuming the two charged tracks as  $\mu$ .



# $\psi' \rightarrow \omega KK$ background

Require  $M(3\gamma)$  outside of  $[0.74, 0.82]$ . The remaining spectrum is fit to double gaussian.



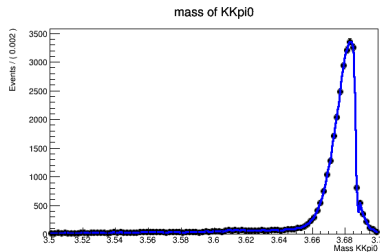
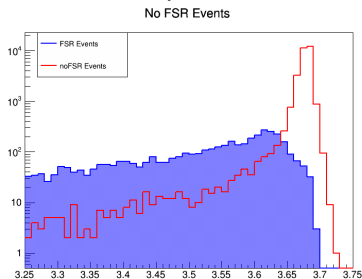


# $\pi^0 KK$ background shape

$f_{FSR}$  describe the difference of FSR ratio in data/MC. Calculating from existing result:

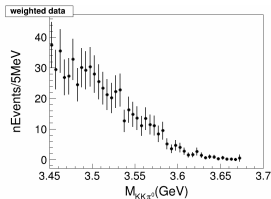
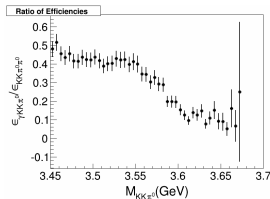
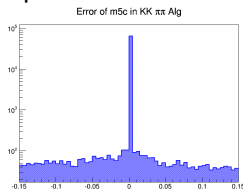
$$f_{\gamma KK\pi^0} = 2 * f_{\gamma KK\pi\pi} - f_{\pi\pi\pi\pi} = 1.08 \pm 0.15 \quad (1)$$

Get the lineshape from the reweighted sum of the FSR and no-FSR events.



# $\pi^0\pi^0 KK$ background (fake 5c mass)

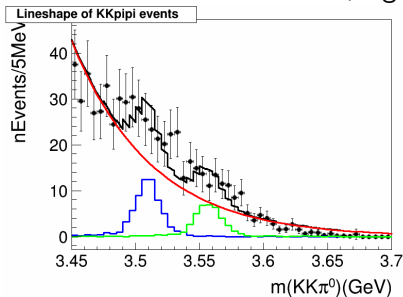
Run  $KK\pi\pi$  algorithm on data, re-weight the mass spectrum with the ratio of efficiency when  $KK\pi^0\pi^0$  MC events try to pass the  $\gamma KK\pi^0$  and  $KK\pi\pi$  algorithms, to get the  $KK\pi^0\pi^0$  contribution in  $\gamma KK\pi$  Alg's result. The mass in  $KK\pi\pi$  algorithm is calculated from a 5C kinematic fit (the best fit when missing 1 photon in  $KK\pi^0\pi^0$  candidates) without chisquare requirement.



## $\pi^0\pi^0 KK$ background shape (fake 5c mass)

The  $KK\pi\pi$  background is described with a Gaussian Function. To get its parameters, the  $\chi_{cj}$  background are considered by using MC shape.

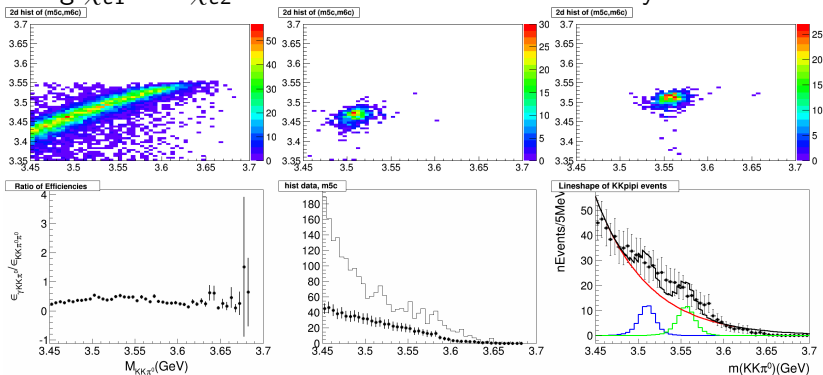
Fit Result: mean= $0.0 \pm 8.8$ , sigma= $0.464 \pm 0.000$



# $\pi^0\pi^0KK$ background (mass transforming matrix)

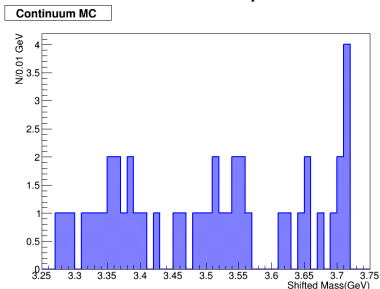
Alternatively, get the matrix of (5c mass, 6c mass) from 10 mil.  $\pi^0\pi^0KK$  MC events, and transform the histograms accordingly.

Assuming  $\chi_{c1}$  and  $\chi_{c2}$  masses distribute in the same way.



# Continuum Background

Estimated from  $42.6 pb^{-1}$  data @ 3650 MeV.



# Lineshape Description

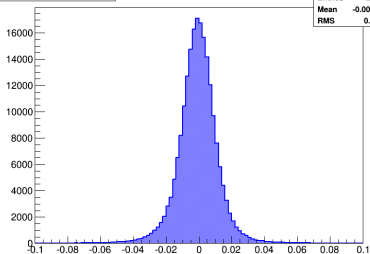
- $\chi_{cj}$ : MC shape convolved with a gaussian
- $\eta_c(2S)$ :  $(BW(m) \times E_\gamma^3 \times \text{dampingFunc}) \otimes \text{Gaussian}$
- Damping Function:  $\frac{E_0^2}{E_\gamma E_0 + (E_\gamma - E_0)^2}$  (KEDR) or  $\exp(-E_\gamma^2/8\beta^2)$  (CLEO)
- Background Shapes:  $\omega KK$  as double Gaussian,  $KK\pi\pi$  as Gaussian,  $KK\pi^0$  as re-weighted MC shape
- Continuum background not considered in fit.

# Resolution of Gauss

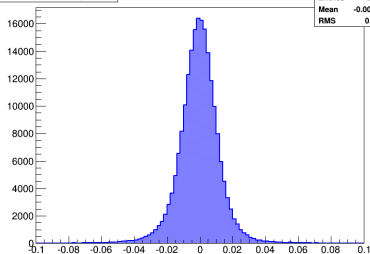
$\chi_{c1}$ : width=13.08 MeV,  $\chi_{c2}$ : width=13.32 MeV;  
with linear extrapolation, for  $\eta_c$  width=13.76 MeV

 $\Delta(KK\pi)$  in  $\chi_{c1}$  MC

hmassdif2	
Entries	249104
Mean	-0.0006138
RMS	0.01308

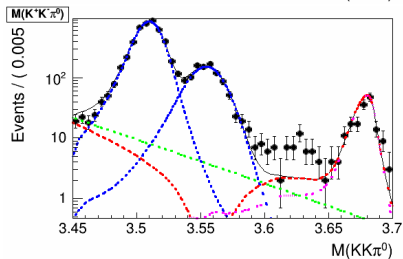
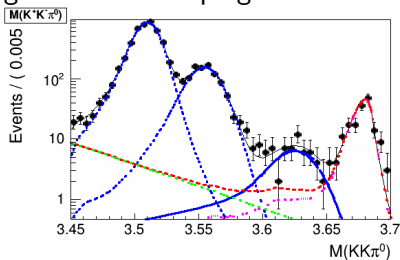
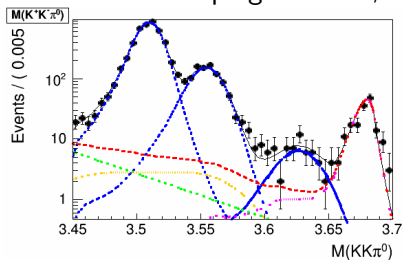
 $\Delta(KK\pi)$  in  $\chi_{c2}$  MC

hmassdif3	
Entries	246897
Mean	-0.0005362
RMS	0.01332



# Fit Result

Left: KEDR damping function; Right: CLEO damping function.





Things that needs further checking:

- $\pi^0\pi^0 KK$  lineshape parameters
- Continuum Background
- CLEO damping function

$$\psi' \rightarrow \gamma \eta'_c, \eta'_c \rightarrow K_s K \pi$$

# Event Selection

Charged Tracks:  $n_{\text{Good}}=4$ ,  $n_{\text{Charge}}=0$

- $R_{VZ} < 10\text{cm}$
- $R_{VXY} < 1\text{cm}$
- $\cos\theta < 0.93$

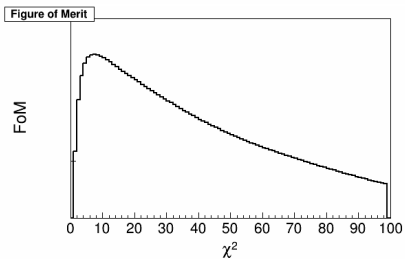
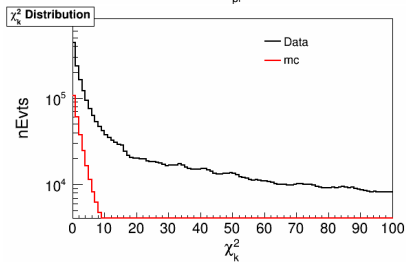
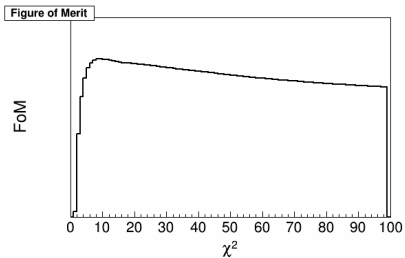
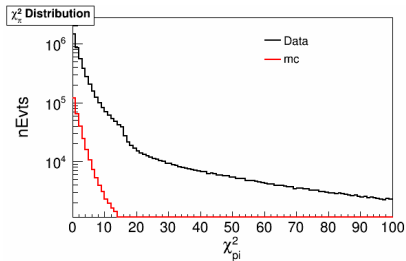
Good Photons:  $n_{\text{Gam}} \geq 1$

- energy  $> 40\text{ MeV}$
- time in  $[0,14]$  (\*50 ns)
- At 20 degree from the extrapolation of a MDC track.

PID:

- TOF,  $dE/dx$
- $\chi_K^2$ ,  $\chi_\pi^2$  of each track saved for later cuts

# $\chi^2$ of PID



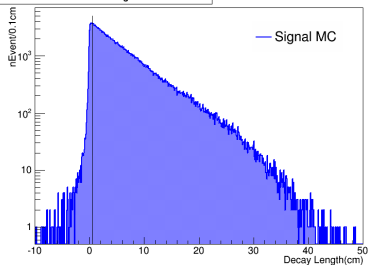
# Secondary Vertex Fit

## Secondary Vertex Fit for $K_s$

- decay length at least 0.5 cm
- mass within  $[-7 \text{ MeV}, +7 \text{ MeV}]$  around  $m(K_s)$
- candidate with minimal  $(\chi^2_{vtx} + \chi^2_{svtx})$  is chosen

# Secondary Vertex Fit - $K_S$ decay length

Decay Length of  $K_S^0$  Candidates



# Secondary Vertex Fit - $K_S$ Mass Window

Decay Length of  $K_S^0$  Candidates

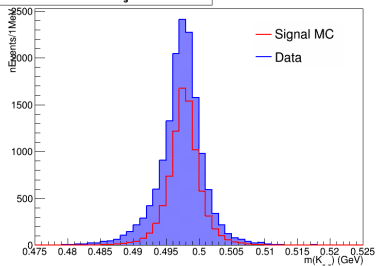
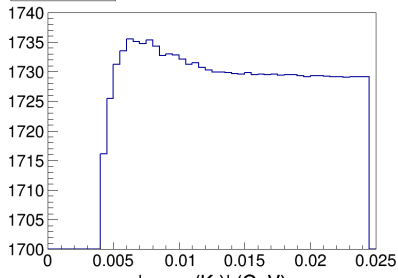
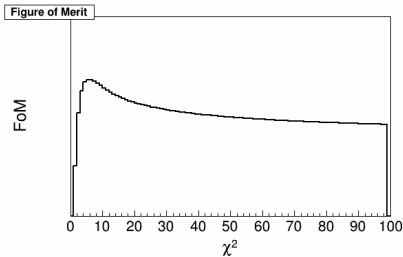
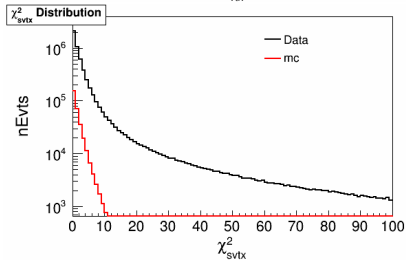
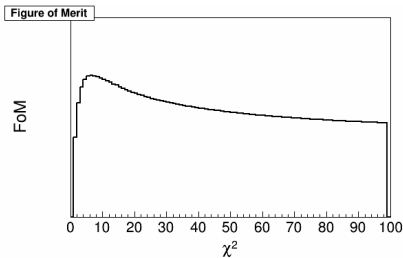
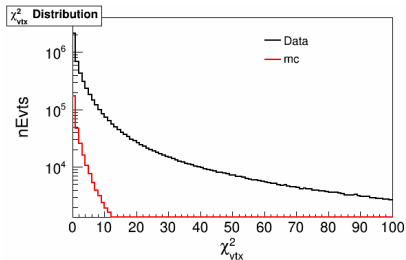


Figure of Merit



# $\chi^2$ of vertex fit and secondary vertex fit

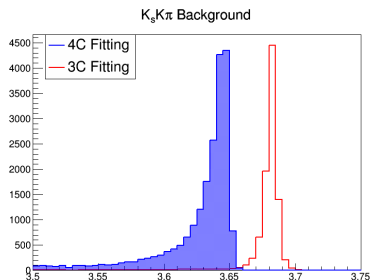
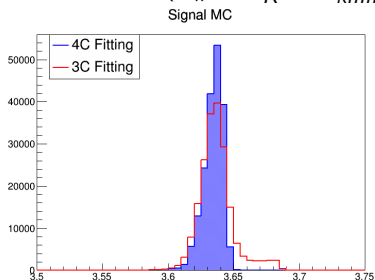




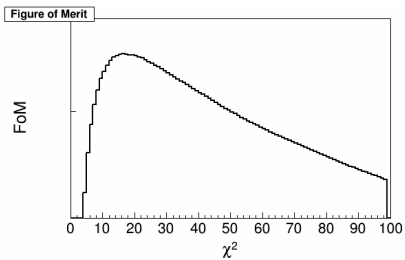
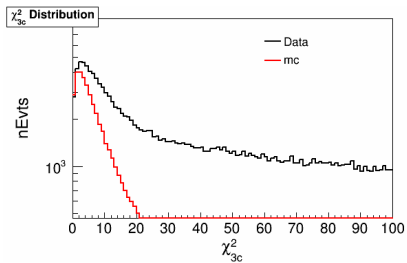
# Kinematic Fit

3C: 4 momentum, loosen  $\gamma$  mass.

Iterating over either track being K, and over  $\gamma$  candidates. Combination with minimal  $(\chi^2_\pi + \chi^2_K + \chi^2_{kmfit})$  is chosen.

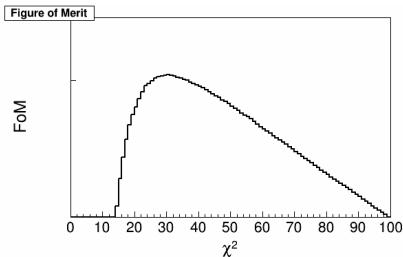
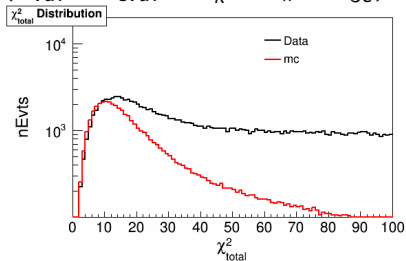


# $\chi^2$ of 3C



$\chi^2$  total

$$(\chi_{vtx}^2 + \chi_{svtx}^2 + \chi_k^2 + \chi_\pi^2 + \chi_{3c}^2) < 30 \text{ required}$$



# Background Composition

No.	decay chain	final states	iTopology	nEvt	nTot
0	$\psi' \rightarrow \gamma \chi_{c1}, \chi_{c1} \rightarrow K^- \pi^+ \bar{K}^0, K_S \rightarrow \pi^+ \pi^-$	$\pi^- K^- \pi^+ \pi^+ \gamma$	3	1938	1938
1	$\psi' \rightarrow \gamma \chi_{c1}, \chi_{c1} \rightarrow K^+ \pi^- \bar{K}^0, K_S \rightarrow \pi^+ \pi^-$	$\pi^- \pi^- \pi^+ \gamma K^+$	1	1932	3870
2	$\psi' \rightarrow J/\psi \pi^+ \pi^-, J/\psi \rightarrow \mu^+ \mu^-$	$\mu^+ \pi^- \mu^- \pi^+$	0	1772	5642
3	$\psi' \rightarrow J/\psi \pi^+ \pi^-, J/\psi \rightarrow e^+ e^-$	$e^+ \pi^- e^- \pi^+$	5	1209	6851
4	$\psi' \rightarrow \gamma \chi_{c2}, \chi_{c2} \rightarrow \bar{K}^0 K^+ \pi^-, K_S \rightarrow \pi^+ \pi^-$	$\pi^- \pi^- \pi^+ \gamma K^+$	17	534	7385
5	$\psi' \rightarrow \gamma \chi_{c2}, \chi_{c2} \rightarrow K^0 K^- \pi^+, K_S \rightarrow \pi^+ \pi^-$	$\pi^- K^- \pi^+ \pi^+ \gamma$	11	482	7867
6	$\psi' \rightarrow \gamma \chi_{c0}, \chi_{c0} \rightarrow K_S K_S, K_S \rightarrow \pi^+ \pi^-, K_S \rightarrow \pi^+ \pi^-$	$\pi^- \pi^- \pi^+ \pi^+ \gamma$	9	382	8249
7	$\psi' \rightarrow \gamma \chi_{c1}, \chi_{c1} \rightarrow K^{*+} K^-, K^{*+} \rightarrow K^0 \pi^+, K_S \rightarrow \pi^+ \pi^-$	$\pi^- K^- \pi^+ \pi^+ \gamma$	10	279	8528
8	$\psi' \rightarrow \gamma \chi_{c1}, \chi_{c1} \rightarrow K^{*-} K^+, K^{*-} \rightarrow \bar{K}^0 \pi^-, K_S \rightarrow \pi^+ \pi^-$	$\pi^- \pi^- \pi^+ \gamma K^+$	14	257	8785
9	$\psi' \rightarrow \gamma \chi_{c1}, \chi_{c1} \rightarrow K^* \bar{K}^0, K^* \rightarrow K^+ \pi^-, K_S \rightarrow \pi^+ \pi^-$	$\pi^- \pi^- \pi^+ \gamma K^+$	12	256	9041
10	$\psi' \rightarrow \gamma \chi_{c1}, \chi_{c1} \rightarrow \bar{K}^* K^0, \bar{K}^* \rightarrow K^- \pi^+, K_S \rightarrow \pi^+ \pi^-$	$\pi^- K^- \pi^+ \pi^+ \gamma$	2	209	9250
11	$\psi' \rightarrow \gamma K_S K^+ \pi^-, K_S \rightarrow \pi^+ \pi^-$	$\pi^- \pi^- \pi^+ \gamma K^+$	6	153	9403
12	$\psi' \rightarrow \gamma \chi_{c2}, \chi_{c2} \rightarrow K_S K_S, K_S \rightarrow \pi^+ \pi^-, K_S \rightarrow \pi^+ \pi^-$	$\pi^- \pi^- \pi^+ \pi^+ \gamma$	8	136	9539
13	$\psi' \rightarrow K_1^+ K^-, K_1^+ \rightarrow \rho^+ K^0, \rho^+ \rightarrow \pi^+ \pi^0, K_S \rightarrow \pi^+ \pi^-$	$\pi^- K^- \pi^0 \pi^+ \pi^+$	19	129	9668
14	$\psi' \rightarrow K_1^- K^+, K_1^- \rightarrow \rho^- \bar{K}^0, \rho^- \rightarrow \pi^- \pi^0, K_S \rightarrow \pi^+ \pi^-$	$\pi^- \pi^- \pi^0 \pi^+ K^+$	15	128	9796
15	$\psi' \rightarrow \gamma K_S K^- \pi^+, K_S \rightarrow \pi^+ \pi^-$	$\pi^- K^- \pi^+ \pi^+ \gamma$	35	117	9913
16	$\psi' \rightarrow \bar{K}^* K^0, \bar{K}^* \rightarrow K^- \pi^+, K_S \rightarrow \pi^+ \pi^-$	$\pi^- K^- \pi^+ \pi^+$	28	105	10018
17	$\psi' \rightarrow K^* \bar{K}^0, K^* \rightarrow K^+ \pi^-, K_S \rightarrow \pi^+ \pi^-$	$\pi^- \pi^- \pi^+ K^+$	25	98	10116
18	$\psi' \rightarrow \gamma \chi_{c1}, \chi_{c1} \rightarrow a_0^- \pi^+, a_0^- \rightarrow K^0 K^-, K_S \rightarrow \pi^+ \pi^-$	$\pi^- K^- \pi^+ \pi^+ \gamma$	38	77	10193
19	$\psi' \rightarrow K^+ \bar{K}^* \pi^-, \bar{K}^* \rightarrow \bar{K}^0 \pi^0, K_S \rightarrow \pi^+ \pi^-$	$\pi^- \pi^- \pi^0 \pi^+ K^+$	20	54	10247
20	$\psi' \rightarrow \gamma \chi_{c1}, \chi_{c1} \rightarrow a_0^+ \pi^-, a_0^+ \rightarrow \bar{K}^0 K^+, K_S \rightarrow \pi^+ \pi^-$	$\pi^- \pi^- \pi^+ \gamma K^+$	23	52	10299
21	$\psi' \rightarrow K^- K^* \pi^+, K^* \rightarrow K^0 \pi^0, K_S \rightarrow \pi^+ \pi^-$	$\pi^- K^- \pi^0 \pi^+ \pi^+$	61	49	10348
22	$\psi' \rightarrow K_1^+ K^-, K_1^+ \rightarrow K_0^+ \pi^0, K_0^+ \rightarrow K^0 \pi^+, K_S \rightarrow \pi^+ \pi^-$	$\pi^- K^- \pi^0 \pi^+ \pi^+$	7	42	10390
23	$\psi' \rightarrow K_1^- K^+, K_1^- \rightarrow K_0^- \pi^0, K_0^- \rightarrow \bar{K}^0 \pi^-, K_S \rightarrow \pi^+ \pi^-$	$\pi^- \pi^- \pi^0 \pi^+ K^+$	53	39	10429
24	$\psi' \rightarrow \gamma \eta_c(2S), \eta_c(2S) \rightarrow K^- K^0 \pi^+, K_S \rightarrow \pi^+ \pi^-$	$\pi^- K^- \pi^+ \pi^+ \gamma$	66	30	10459
25	$\psi' \rightarrow \gamma \eta_c(2S), \eta_c(2S) \rightarrow K^+ \bar{K}^0 \pi^-, K_S \rightarrow \pi^+ \pi^-$	$\pi^- \pi^- \pi^+ \gamma K^+$	108	28	10487
26	$\psi' \rightarrow K_1^- K^+, K_1^- \rightarrow \bar{K}_0^* \pi^-, \bar{K}_0^* \rightarrow \bar{K}^0 \pi^0, K_S \rightarrow \pi^+ \pi^-$	$\pi^- \pi^- \pi^0 \pi^+ K^+$	13	203	10510
27	$\psi' \rightarrow K_1^+ K^-, K_1^+ \rightarrow K^{*+} \pi^0, K^{*+} \rightarrow K^0 \pi^+, K_S \rightarrow \pi^+ \pi^-$	$\pi^- K^- \pi^0 \pi^+ \pi^+$	65	21	10531
28	$\psi' \rightarrow \gamma \chi_{c2}, \chi_{c2} \rightarrow K^{*+} K^{*-}, K^{*+} \rightarrow K^0 \pi^+, K^{*-} \rightarrow K^- \pi^0, K_S \rightarrow \pi^+ \pi^-$	$\pi^- K^- \pi^0 \pi^+ \pi^+ \gamma$	52	21	10552
29	$\psi' \rightarrow K_1^+ K^-, K_1^+ \rightarrow K^* \pi^+, K^* \rightarrow K^0 \pi^0, K_S \rightarrow \pi^+ \pi^-$	$\pi^- K^- \pi^0 \pi^+ \pi^+$	64	21	10573

Table 1:

## $\gamma K_S K_S$ Background

Require that the two tracks outside the best  $K_S$  candidate can't be a  $K_S$  candidate.

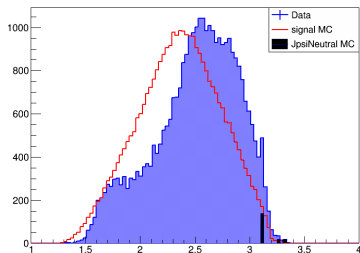
It's regarded as a  $K_S$  candidate if the other two tracks can pass a vertex fit and the invariant mass is in the range of  $[-10 \text{ MeV}, +10 \text{ MeV}]$  around  $m(K_S)$ .

The efficiency for  $\gamma K_S K_S$  *component* without and with such a cut is 1.53% and 0.86%, while it's 18.1% and 18.0% for signal.

# $J/\psi$ + Neutral Background

Require the largest recoil mass of  $m(\pi\pi)$  of all  $\pi$  pairs to be smaller than 3.05 GeV.

Largest  $\pi\pi$  Recoil Mass



# $K_s K\pi$ Background

Study the process of  $\psi' \rightarrow \gamma\chi_{c1}, \chi_{c1} \rightarrow K_s K\pi(\gamma_{FSR})$ . To get the  $R_{data}/R_{mc}$ , where  $R = \frac{N_{FSR}}{N_{noFSR}}$ .

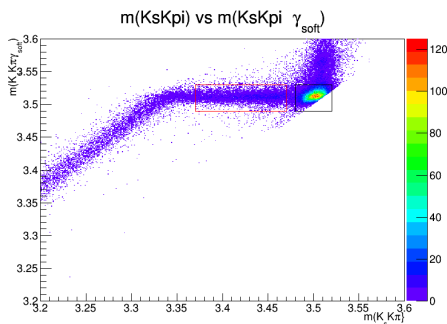
## $\gamma\gamma K_s K\pi$ Algorithm

- $n_{good}=4, n_{charge}=0, n_{Gam}\geq 2$
- PID (dE/dx, TOF)(p, k,  $\pi$ ) to get chisquare
- secondary vertex fit:  $m(K_s)$  in  $[-15 \text{ MeV}, +15 \text{ MeV}]$ ; the other two tracks shouldn't make  $K_s$
- kinematic fit: (4C for combination; 3c for mass,  $\gamma_{soft}$  with flexible mass)

# $K_S K \pi$ Background - estimate $R_{data}/R_{mc}$

$$\chi_{4c}^2 < 50, \chi_{vtx}^2 < 30, \chi_{svtx}^2 < 30, len > 0.5, \text{ veto } m(\gamma\gamma) \text{ in } [0.1, 0.155]$$

noFSR Events and **FSR Events** in boxes. Background events in data identified by truth info in Inclusive MC.



	FSR	noFSR
<b>12mc</b>	147	296
<b>12mc bkg</b>	66	12
<b>09mc</b>	43	68
<b>09mc bkg</b>	18	3
<b>12data</b>	168	206
<b>09data</b>	53	54
<b><math>\chi_{cl}</math> MC(09)</b>	9697	29127

$$R_{mc,09} = 25/65, R_{mc,12} = 81/284$$

$$R_{data,09} = 35/51, R_{data,12} = 102/194$$

$$R_{sig} = 9697/29127$$



# $K_S K \pi$ Background - estimate $R_{data}/R_{mc}$

alternative cuts

$$\chi_{3c}^2 + \chi_{vtz}^2 + \chi_{svtz}^2 + \chi_{\pi}^2 + \chi_k^2 < 50, len > 0.5, \text{ veto } m(\gamma\gamma) \text{ in } [0.1, 0.155] \quad \chi_{4c}^2 + \chi_{vtz}^2 + \chi_{svtz}^2 + \chi_{\pi}^2 + \chi_k^2 < 50, len > 0.5, \text{ veto } m(\gamma\gamma) \text{ in } [0.1, 0.155]$$

	FSR	noFSR
12mc	150	1615
12mc bkg	74	43
09mc	47	446
09mc bkg	23	14
12data	175	1205
09data	57	347
$\chi_{c1}$ MC(09)	9932	199018

$$R_{mc,09} = 24/432, R_{mc,12} = 76/1575$$

$$R_{data,09} = 34/333 = 0.102, R_{data,12} = 101/1162 = 0.0869$$

$$R_{sig} = 9932/199018 = 0.0499$$

	FSR	noFSR
12mc	99	184
12mc bkg	38	4
09mc	33	40
09mc bkg	12	2
12data	124	116
09data	42	26
$\chi_{c1}$ MC(09)	8793	16848

$$R_{mc,09} = 21/38, R_{mc,12} = 61/180$$

$$R_{data,09} = 30/24 = 1.25, R_{data,12} = 86/112 = 0.768$$

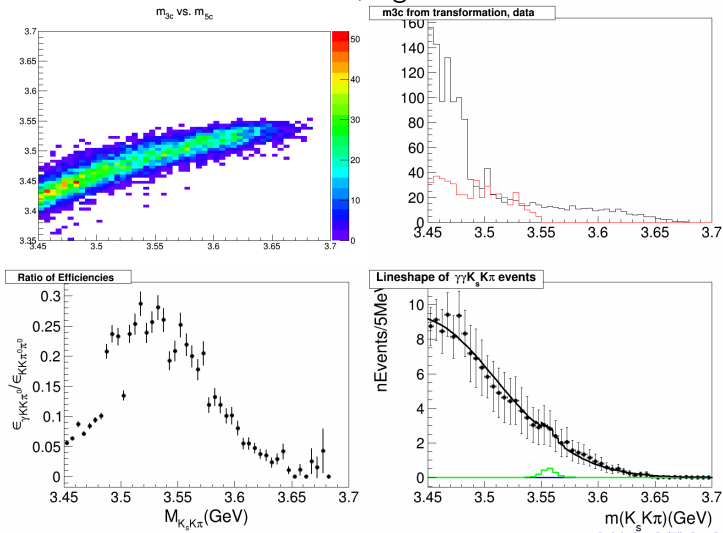
$$R_{sig} = 8793/16848 = 0.522$$

The ratio is decided to be stable; uncertainty around 40%.

$n(\text{FSR})/n(\text{noFSR})=7221/82298$ ; taking  $R_{data}/R_{mc} = 1.5$ .

# $\pi^0 K_s K \pi$ Background

Gaussian. mean= $3.44 \pm 0.03$ , sigma= $0.071 \pm 0.013$



# Fit Result

Around 160 events in 2012 data.

