

Guest Lecture, CSCI 3370: Deep Learning

# Towards Test-time Self-supervised Learning

Yifei Wang, MIT CSAIL

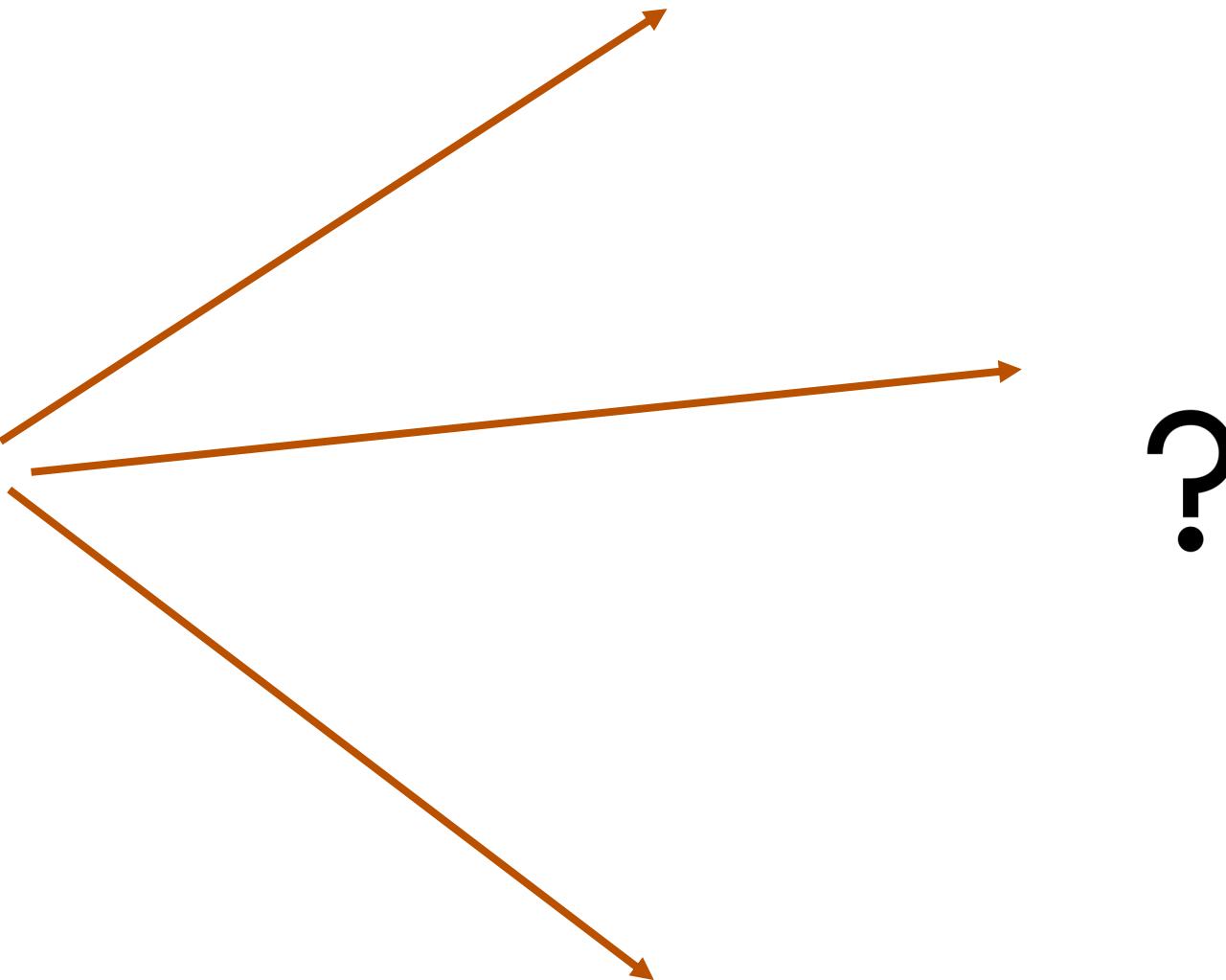
Nov 20, 2024

Boston College



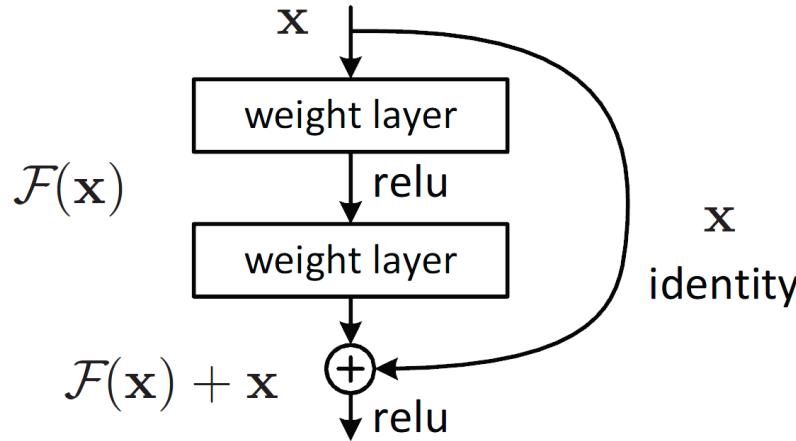
# Deep Learning = finding new scaling dimensions

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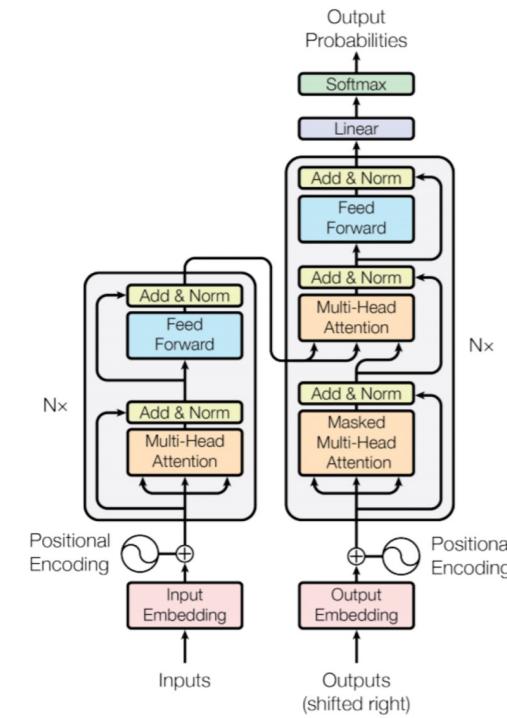


# Deep Learning V1.0 (2012-2017)

The Model Design Era: end-to-end supervised learning given input & labels



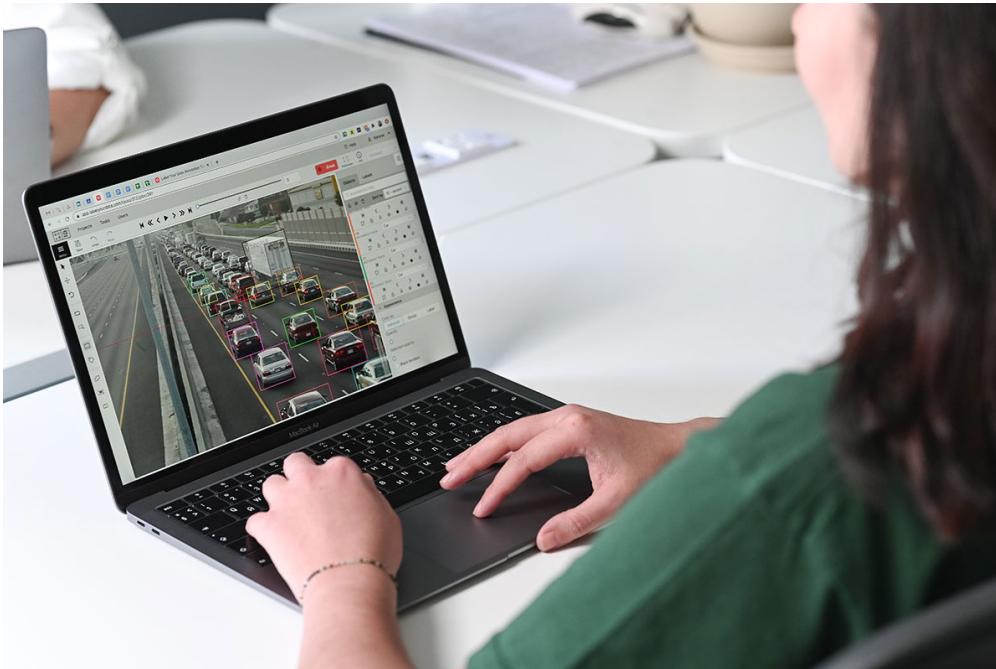
ResNet (He et al., 2016)



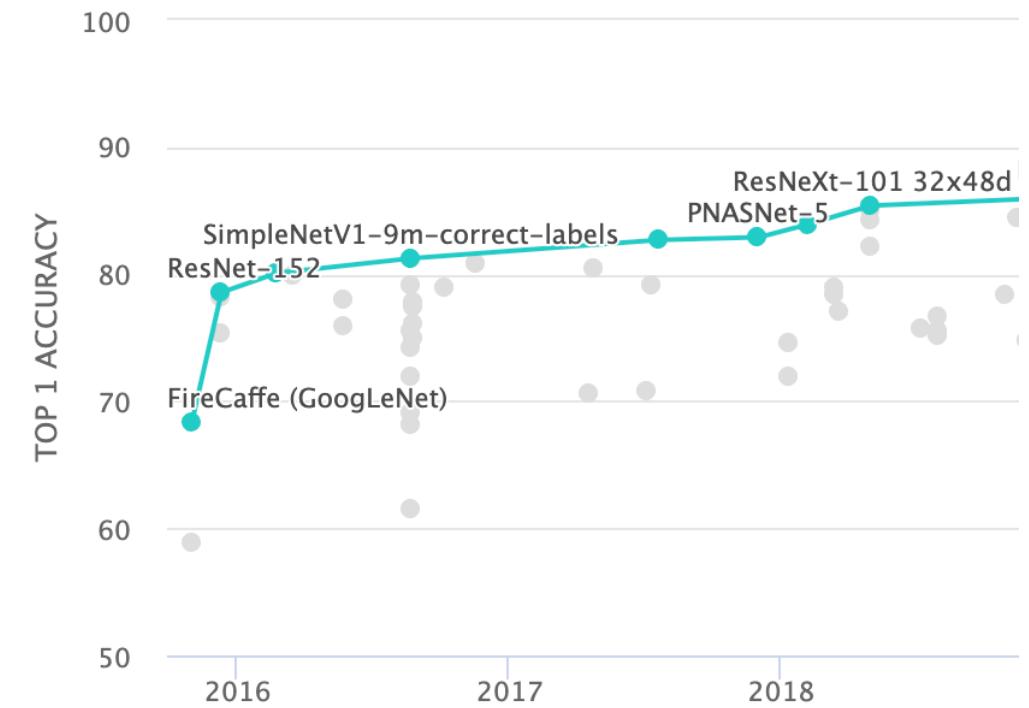
Transformer (Vaswani et al., 2017)

# The Scaling Crisis: Labeled Data

Human labeling is unscalable  
(expensive, sparse)



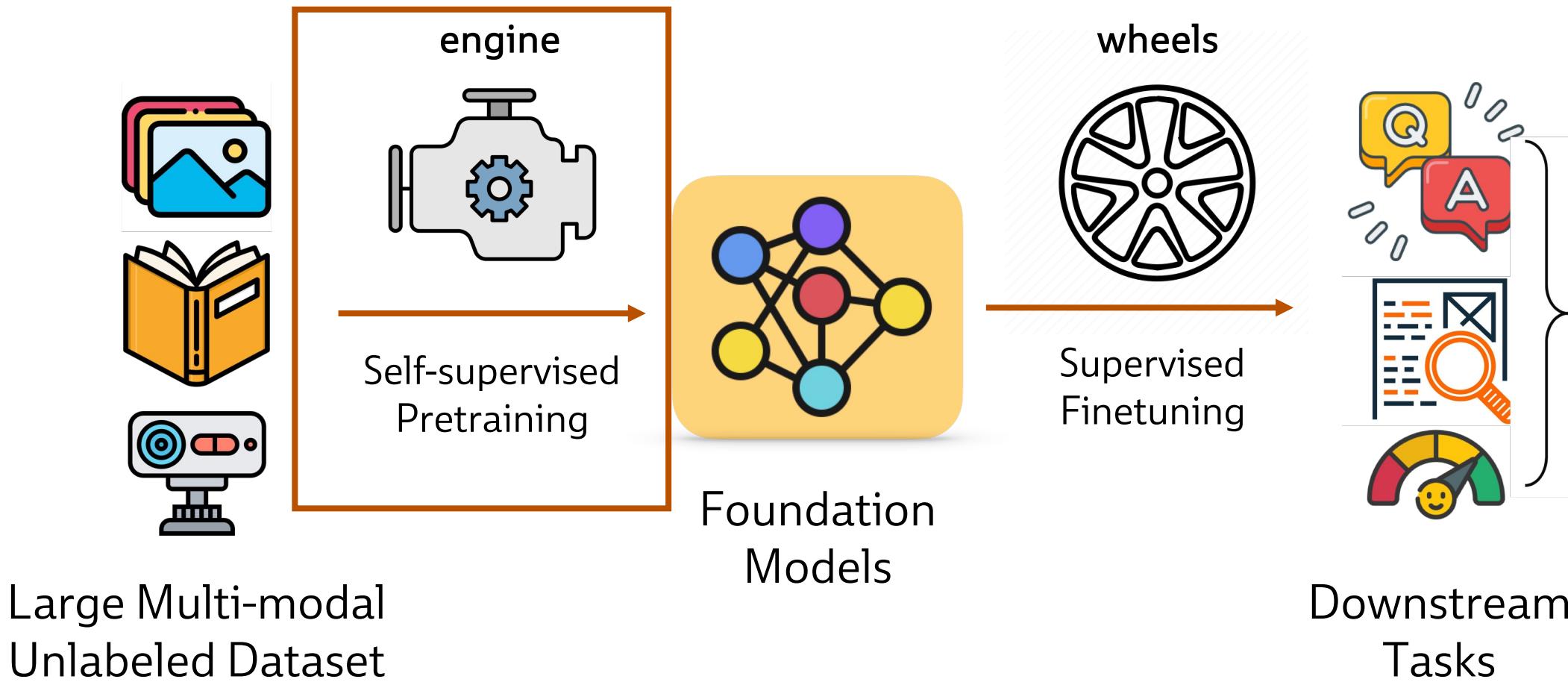
ImageNet saturates around 2017



source: Paperwithcode

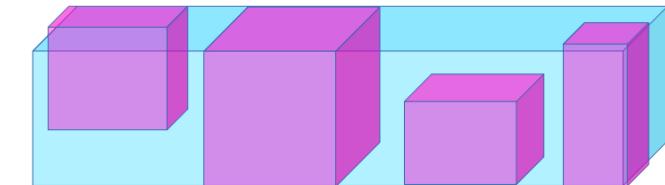
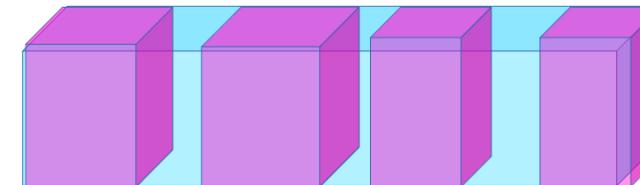
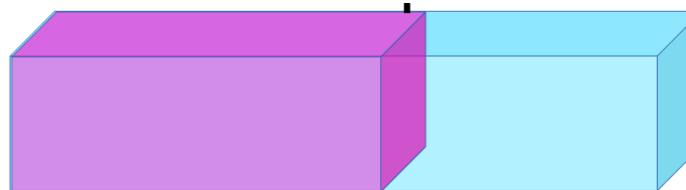
# The Foundation Model Era

Starting 2018 (GPT, BERT), SSL brings Deep Learning V2.0



# Self-supervised Pretraining = Predict its own Parts

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Examples:

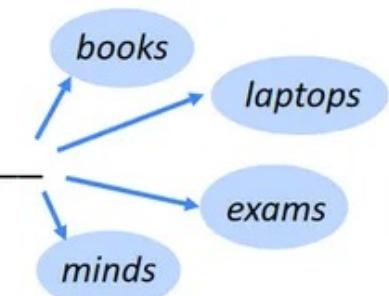


filling in the blank



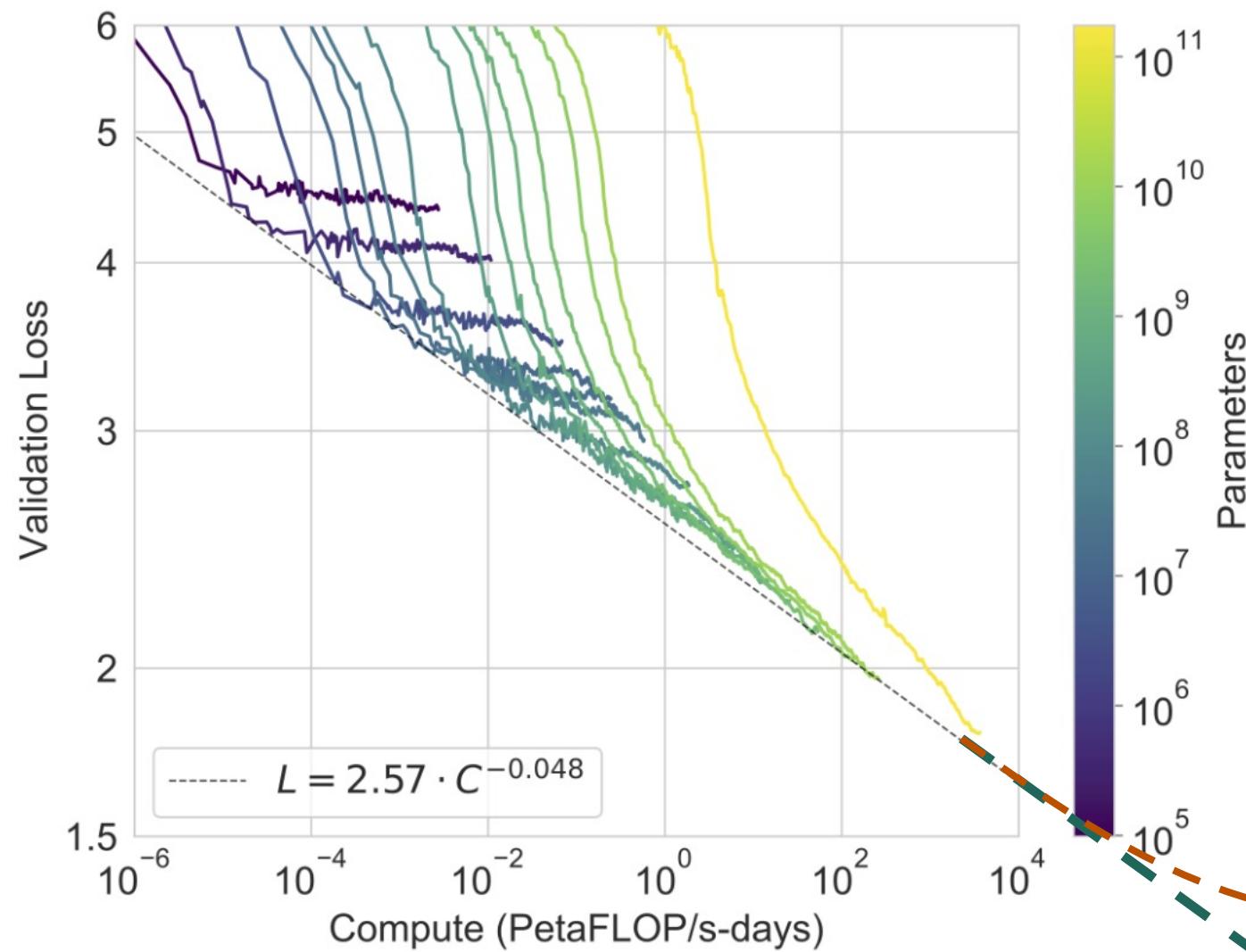
corruption

*the students opened their \_\_\_\_\_*



next word/time prediction

# Scaling Law of Self-supervised Pretraining



?



# Scaling Law is “Hitting a Wall”?

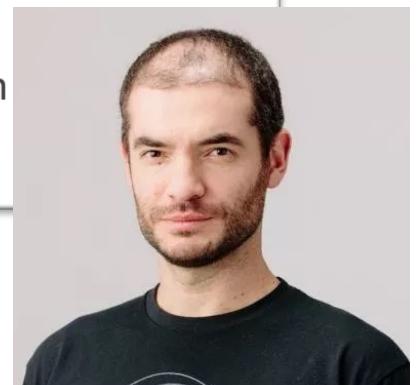
Ilya Sutskever, co-founder of AI labs Safe Superintelligence (SSI) and OpenAI, told Reuters recently that results from scaling up pre-training - the phase of training an AI model that uses a vast amount of unlabeled data to understand language patterns and structures - have plateaued.

Sutskever is widely credited as an early advocate of achieving massive leaps in generative AI advancement through the use of more data and computing power in pre-training, which eventually created ChatGPT. Sutskever left OpenAI earlier this year to found SSI.

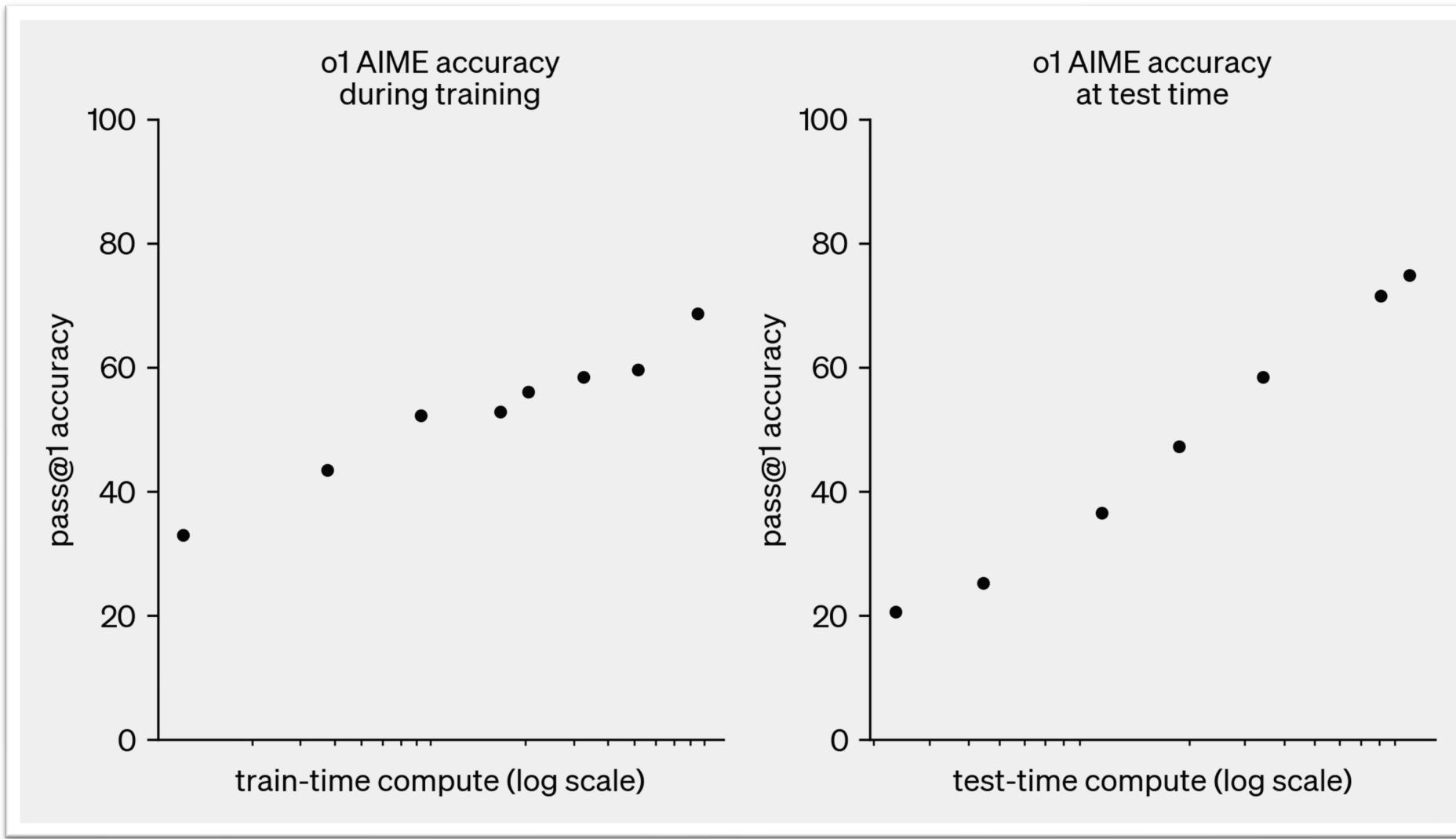
“The 2010s were the age of scaling, now we’re back in the age of wonder and discovery once again. Everyone is looking for the next thing,” Sutskever said. “Scaling the right thing matters more now than ever.”

Sutskever declined to share more details on how his team is addressing the issue, other than working on an alternative approach to scaling up pre-training.

Ilyas Sutskever, in a interview with *Reuters* (Nov 15, 2024)



# The New Dimension: Test-time Compute



source: <https://openai.com/index/learning-to-reason-with-langs/>

# Current Test-time Scaling Methods

## in-context learning

Circulation revenue has increased by 5% in Finland. // Positive

Panostaja did not disclose the purchase price. // Neutral

Paying off the national debt will be extremely painful. // Negative

The company anticipated its operating profit to improve. // \_\_\_\_\_



Circulation revenue has increased by 5% in Finland. // Finance

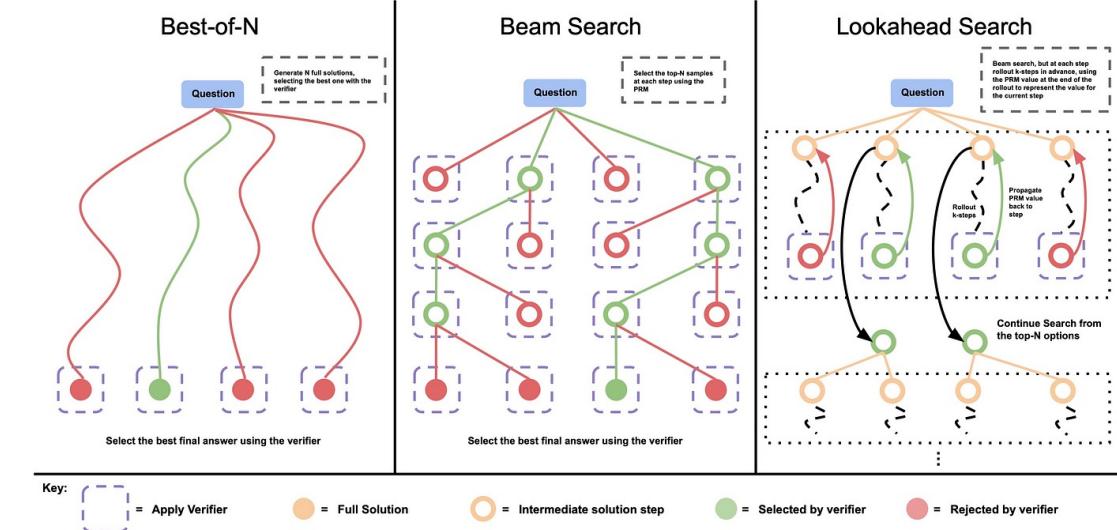
They defeated ... in the NFC Championship Game. // Sports

Apple ... development of in-house chips. // Tech

The company anticipated its operating profit to improve. // \_\_\_\_\_



## searching algorithms



use more input-label demonstrations

rely on groundtruth labels

use more trials and errors to find new solutions

rely on accurate reward models

# Current Test-time Scaling Methods

in-context learning

Circulation revenue has increased by 5% in Finland. // Positive

Panostaja did not disclose the purchase price. // Neutral

Paying off debts is extremely

The company needs to profit to improve. //

LM

Circulation revenue has increased by 5% in Finland. // Finance

They defeated ... in the NFC Championship Game. // Sports

prior to improve. //

LM

searching algorithms

Best-of-N



Beam Search



Lookahead Search



Test-time Scaling May Face  
the Same Data Crisis of Lacking Supervision!

use more input-label  
demonstrations

rely on groundtruth labels

use more trials and errors  
to find new solutions

rely on accurate reward models

# Beyond Test-time Supervision

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Given a new **unsupervised** task at test time, can we learn in a self-supervised way?



Humans are good at  
task adaptation and **self-exploration**



A necessary capability of an  
**autonomous robot**

# Test-time Self-supervised Learning (TT-SSL)

## Test-time LeCake

### Benefits of Test-time SSL:

- a lot of more information to learn from observing the environment
- cheap and easy to scale
- more generic and autonomous

best of n sampling  
in-context demos

??

#### ■ "Pure" Reinforcement Learning (cherry)

- ▶ The machine predicts a scalar reward given once in a while.
- ▶ **A few bits for some samples**



#### ■ Supervised Learning (icing)

- ▶ The machine predicts a category or a few numbers for each input
- ▶ Predicting human-supplied data
- ▶ **10→10,000 bits per sample**

#### ■ Unsupervised/Predictive Learning (cake)

- ▶ The machine predicts any part of its input for any observed part.
- ▶ Predicts future frames in videos
- ▶ **Millions of bits per sample**

■ (Yes, I know, this picture is slightly offensive to RL folks. But I'll make it up)

# This Talk: Two examples of Test-time SSL

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## Unsupervised Task Adaptation

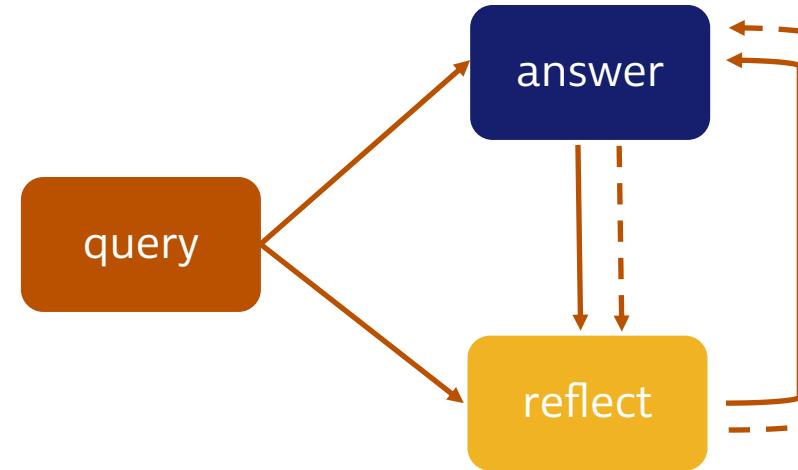
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how to adapt features  
with unlabeled test data

## Iterative Self-correction

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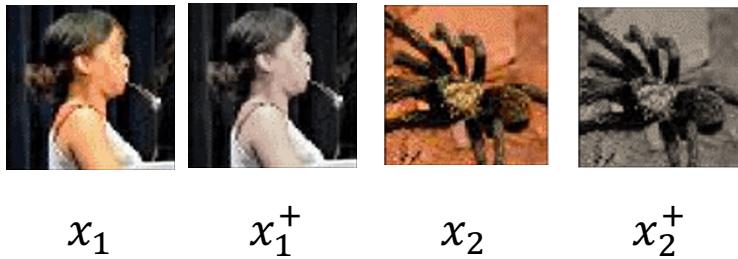
how language models refine  
predictions with self-reflection

# This Talk: Two examples of Test-time SSL

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## Unsupervised Task Adaptation

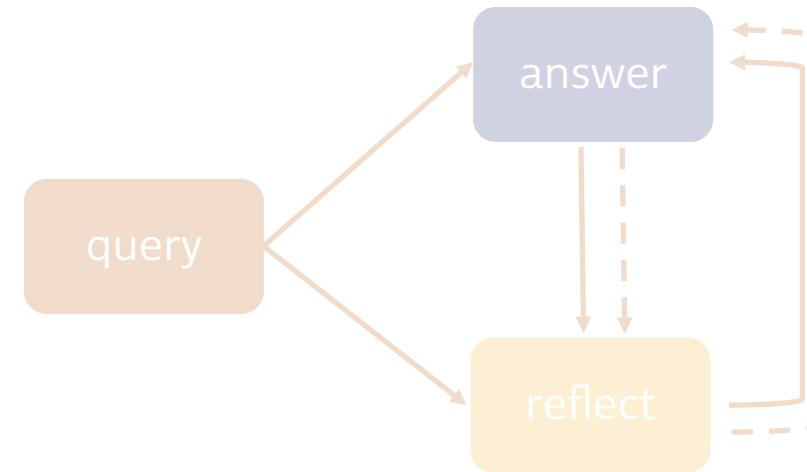
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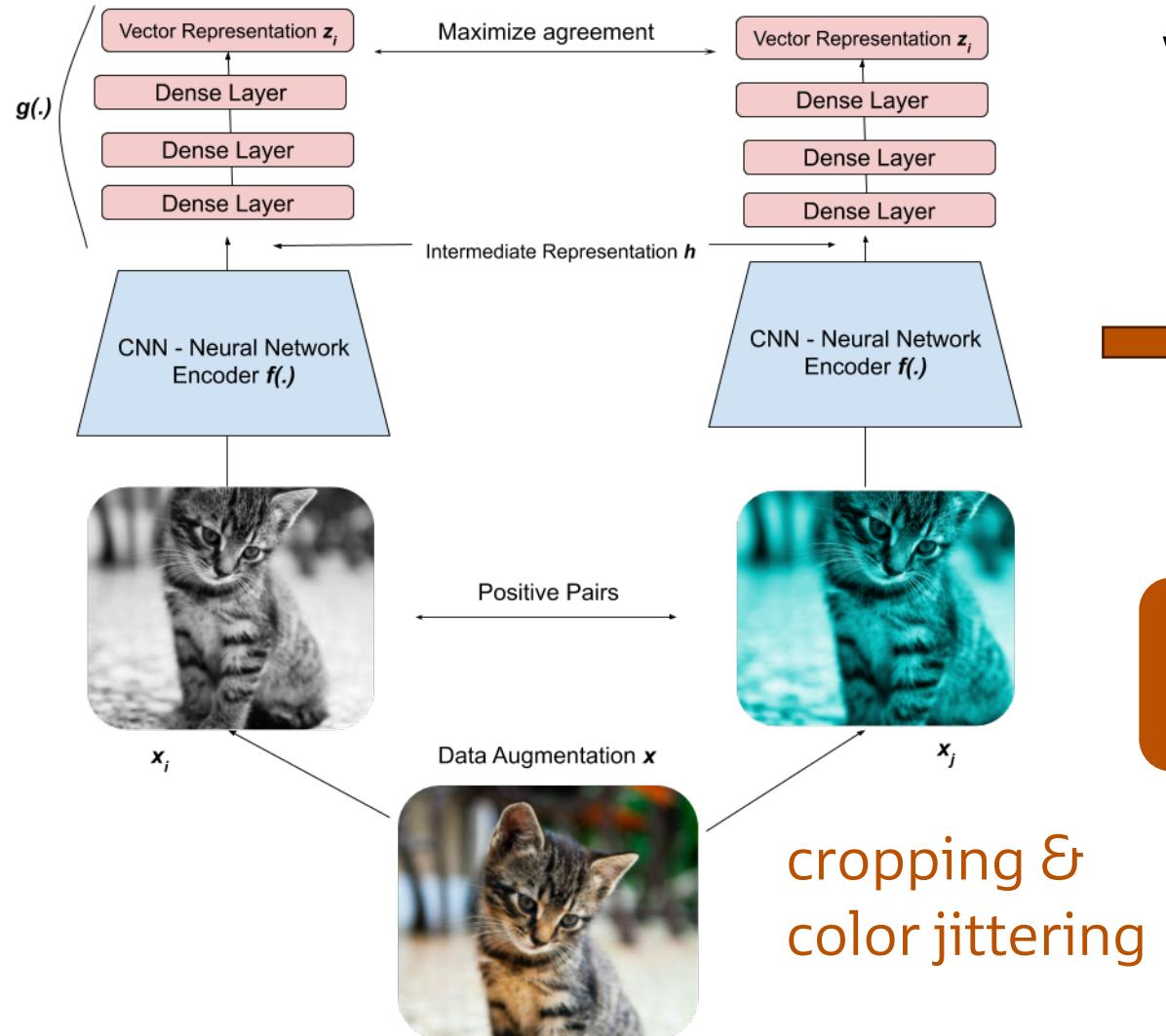
## Iterative Self-correction

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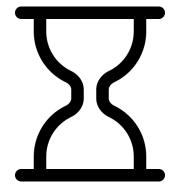
how language models refine  
predictions with self-reflection

# The Joint Embedding SSL Paradigm



widely used in many SSL methods like  
SimCLR, MoCo, DINO, JEPA, etc

goal: learn a  
world model



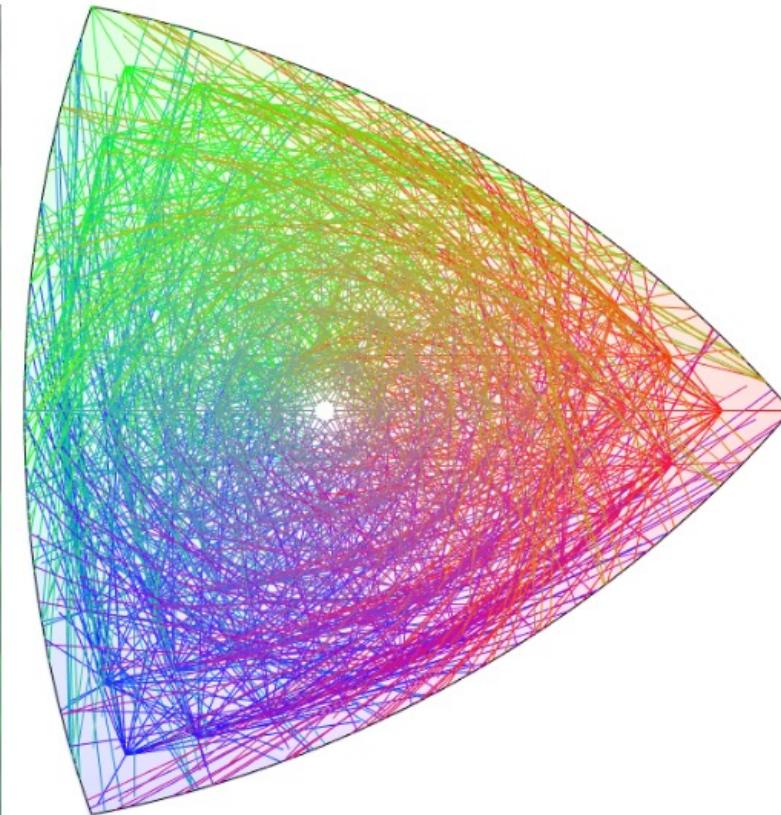
data augmentation decide  
representation inductive bias

cropping &  
color jittering

- position invariance  
➤ color invariance

# Limitations

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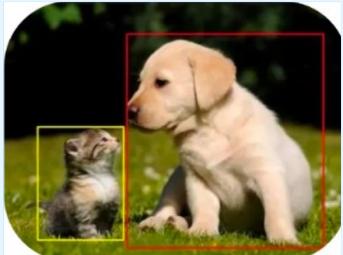


Color information matters for flow classification,  
but **color jittering** distorts it

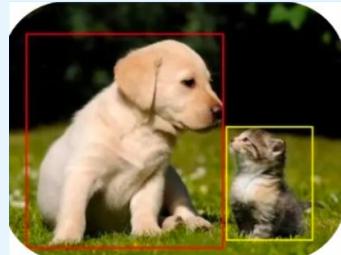
# Limitations could be unsolvable

Invariance to Flipping

Kitten, Dog



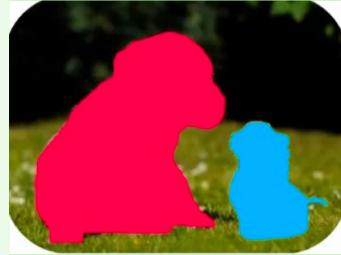
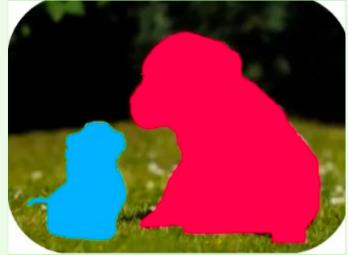
Kitten, Dog



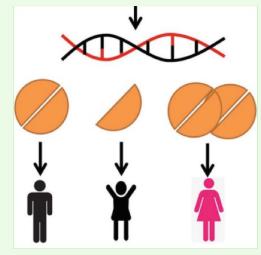
Invariance to Gender



Equivariance to Flipping



Equivariance to Gender



No one universal representation works for scenarios!

# Humans are adaptive

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## Task: Identify the Flower



## Task: Tell the Time



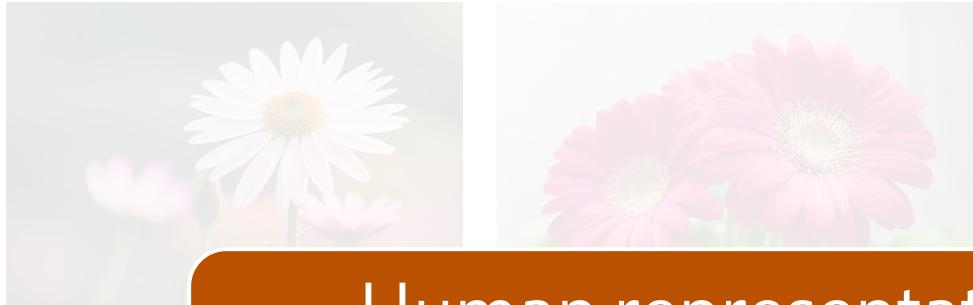
- ✓ sensitive to color
- ✗ invariant to rotation

- ✓ sensitive to rotation
- ✗ invariant to color

# Humans are adaptive

---

Task: Identify the Flower



Human representations are dynamic & adaptive to the downstream task at test time!



- ✓ sensitive to color
- ✗ invariant to rotation

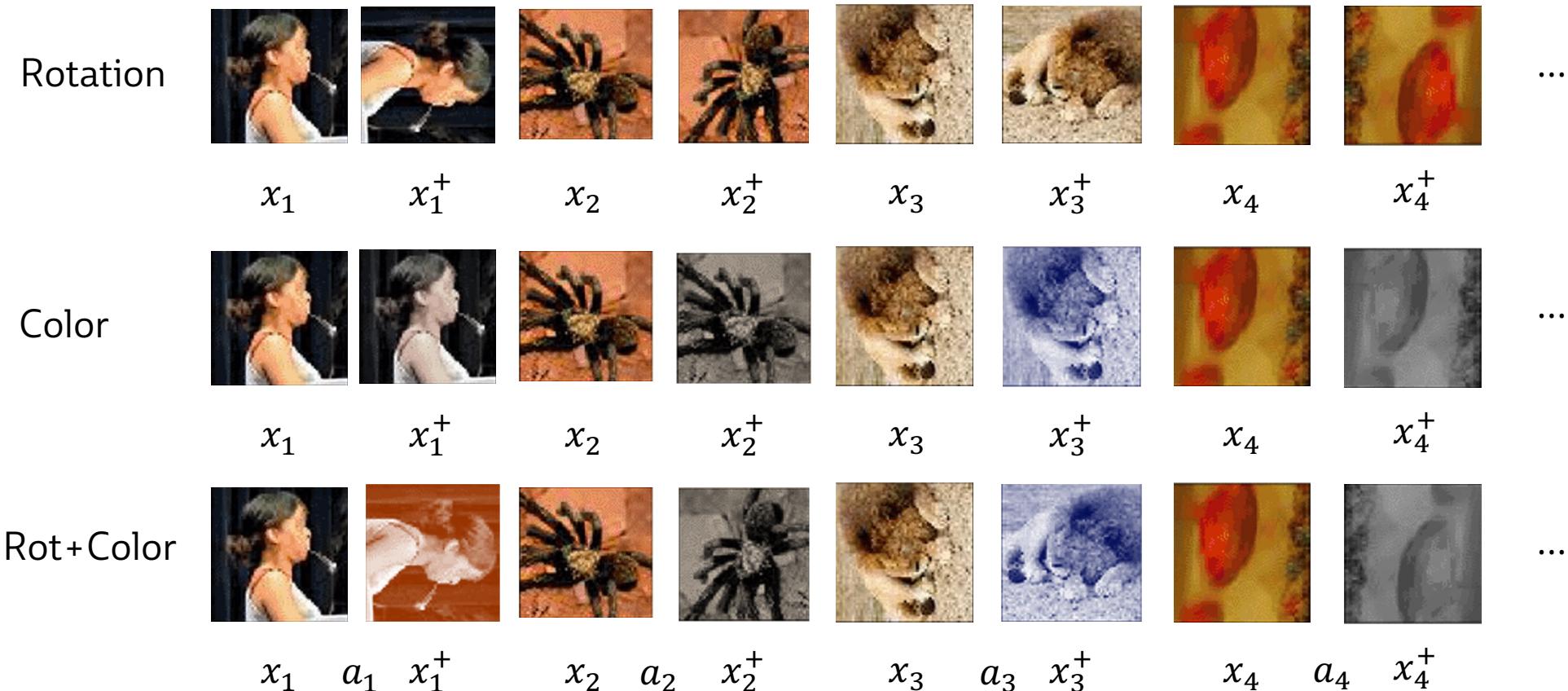
Task: Tell the Time



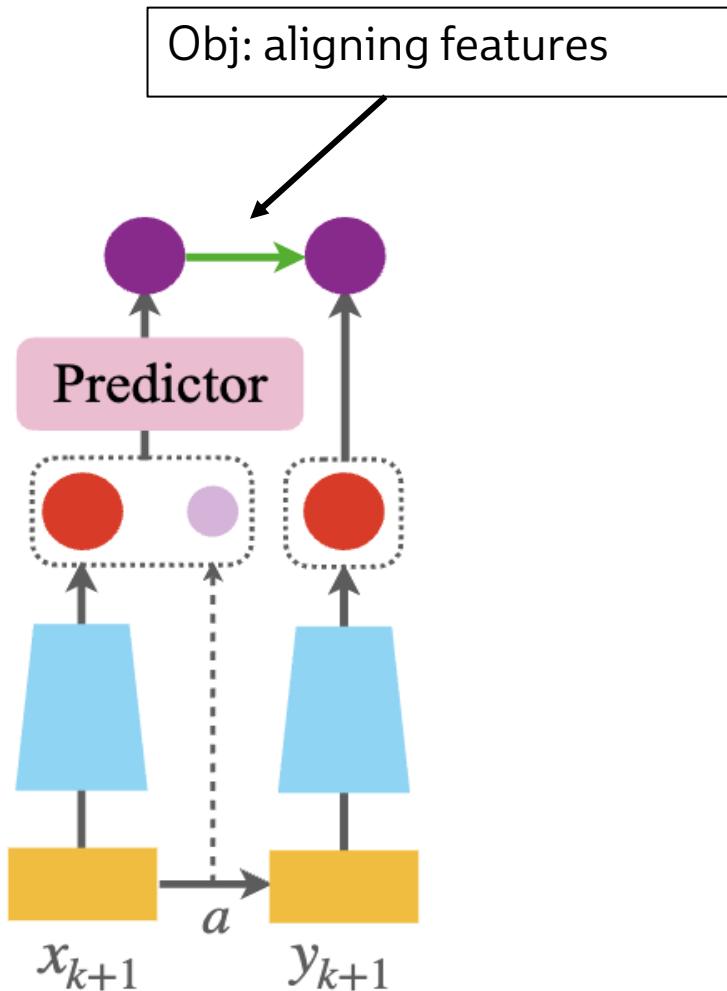
- ✓ sensitive to rotation
- ✗ invariant to color

# Our Design: Unsupervised Context for Adaptation

We illustrate each downstream with a sequence of **few-shot unsupervised pairs**

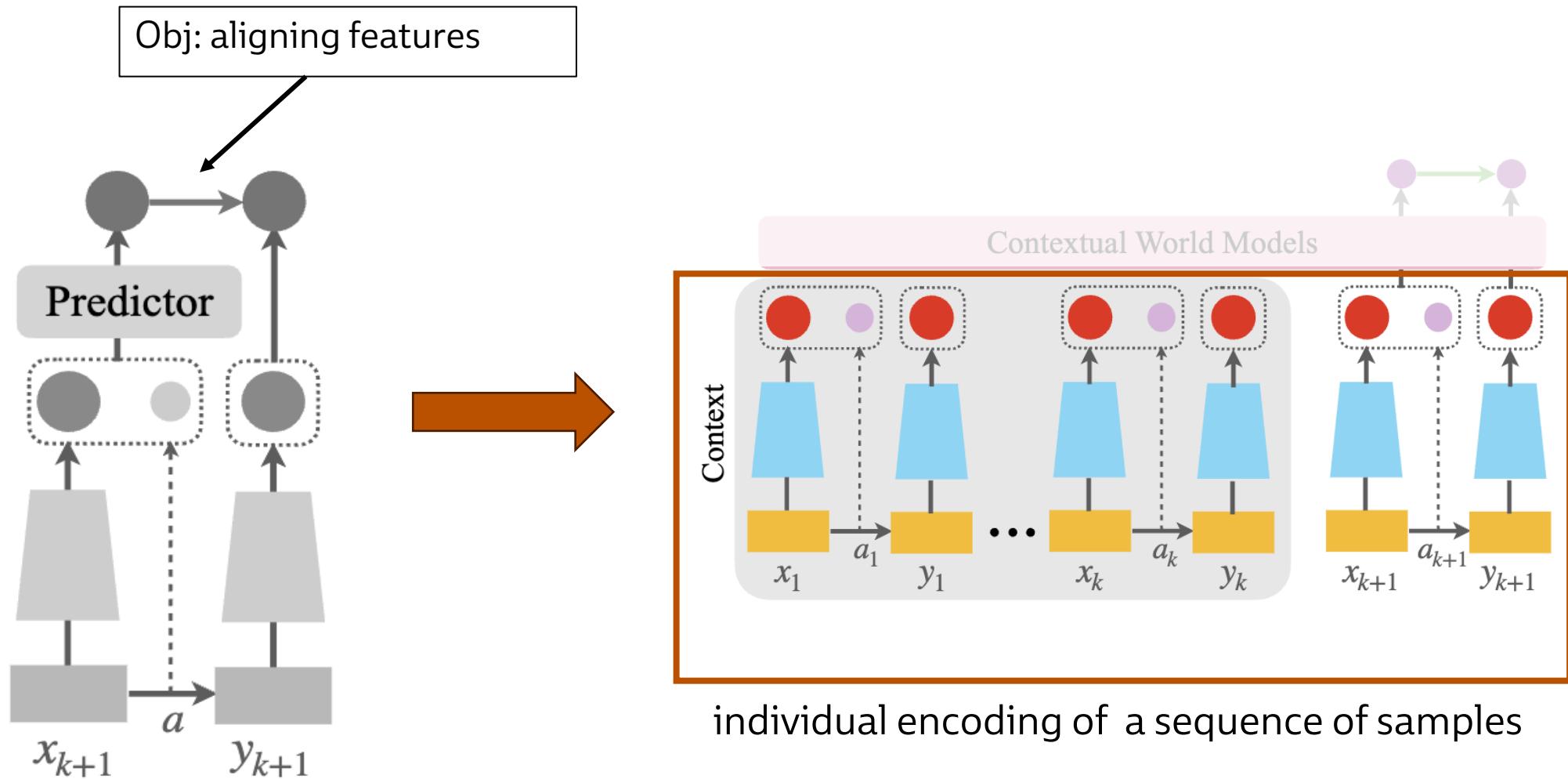


# Adding Context Alone is not Enough

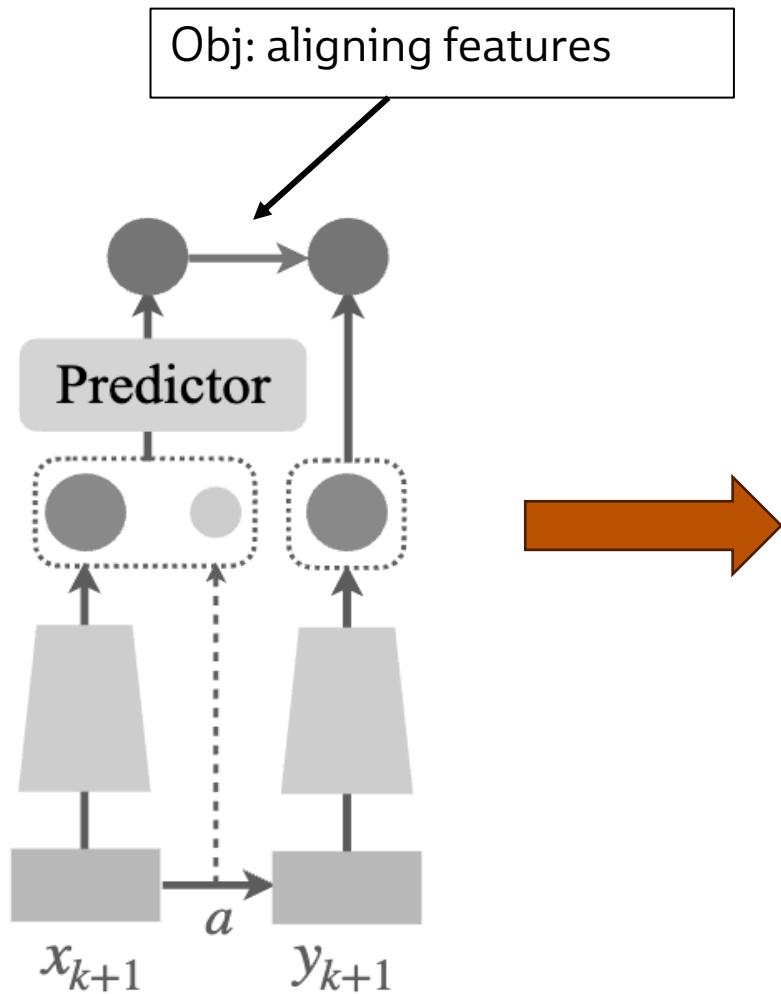


Existing SSL paradigms do not work  
with unsupervised context!

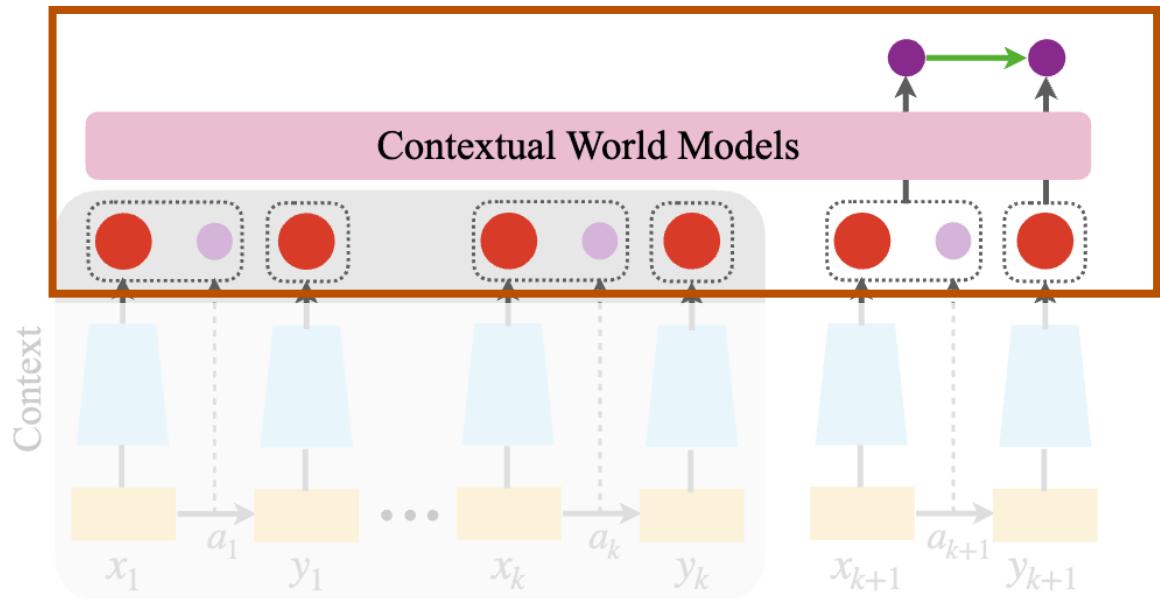
# Contextual Self-supervised Learning (ContextSSL)



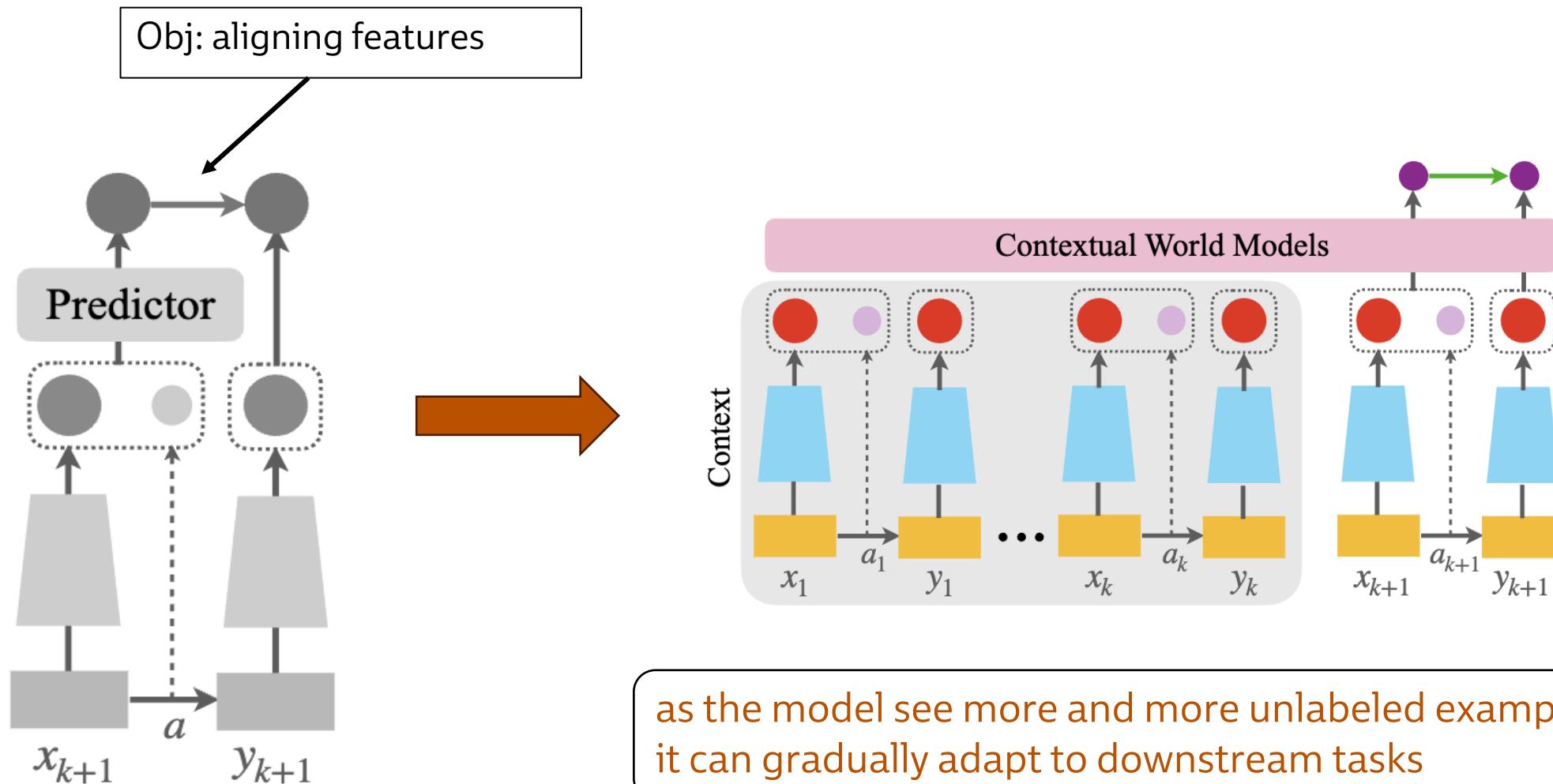
# Contextual Self-supervised Learning (ContextSSL)



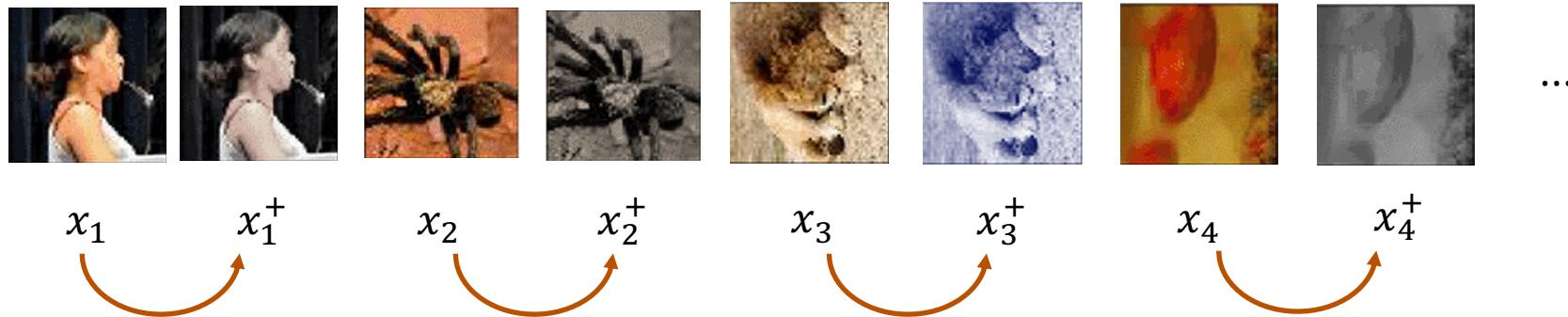
Transformer-based contextual world model



# Contextual Self-supervised Learning (ContextSSL)

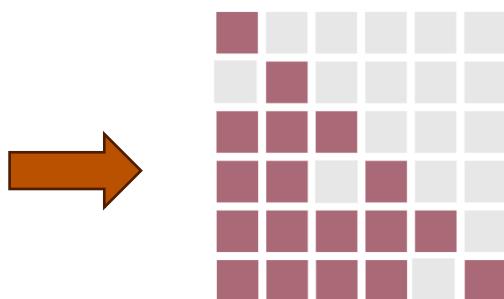


# Unexpected failures (!! w/ unsupervised context



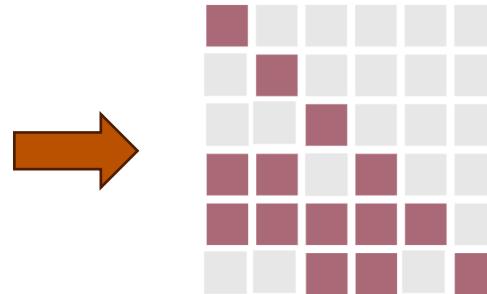
Multiple shortcuts happen when aligning positive pairs in the latent spaces

Shortcut 1: copying positives



pair mask in CWM

Shortcut 2: position bias



random mask in CWM

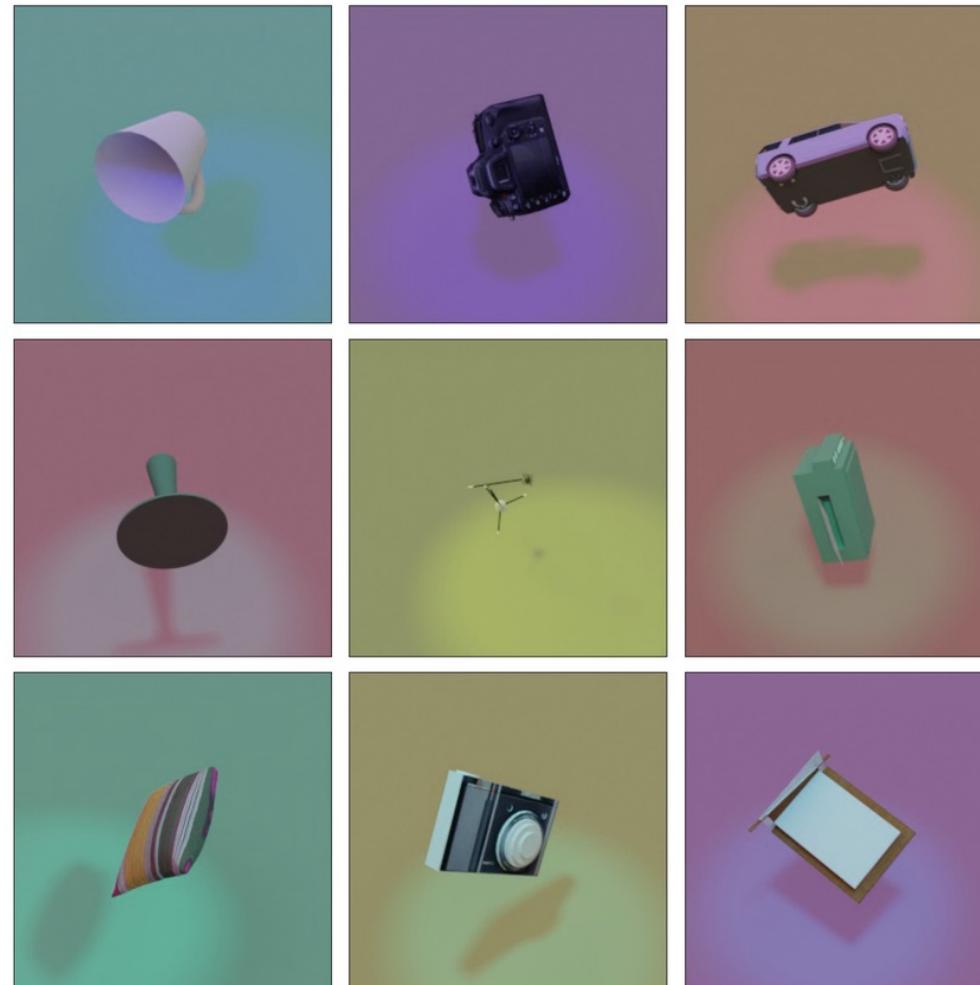
# Can ContextSSL adapt with unsupervised context?

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## 3DIEBench Dataset

Rendition of 3D objects under

- different colors
- different rotations



# Can ContextSSL adapt with unsupervised context?

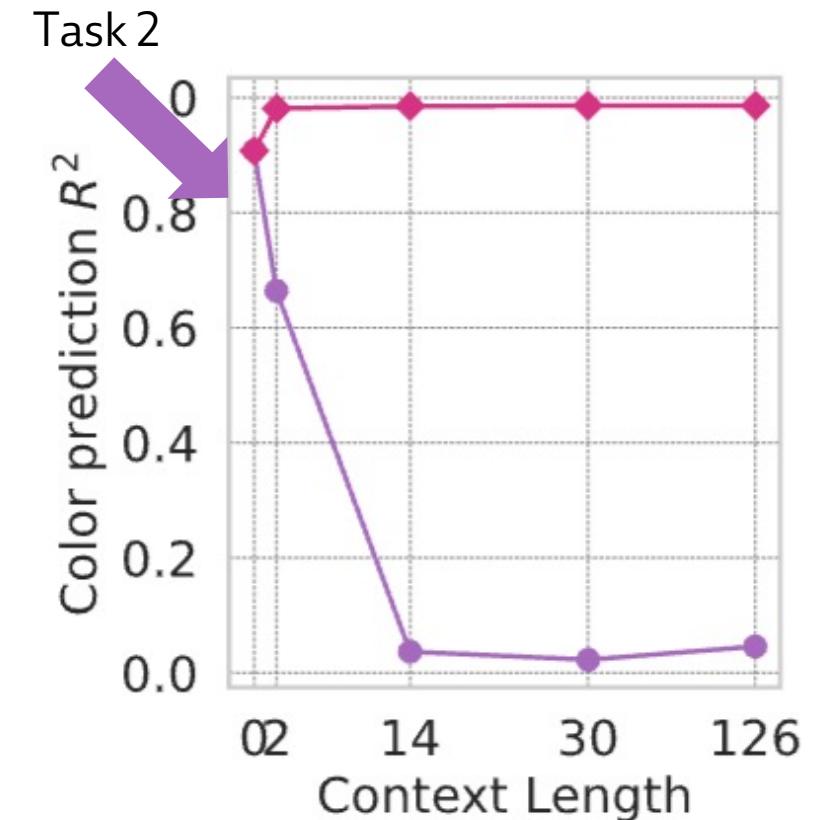
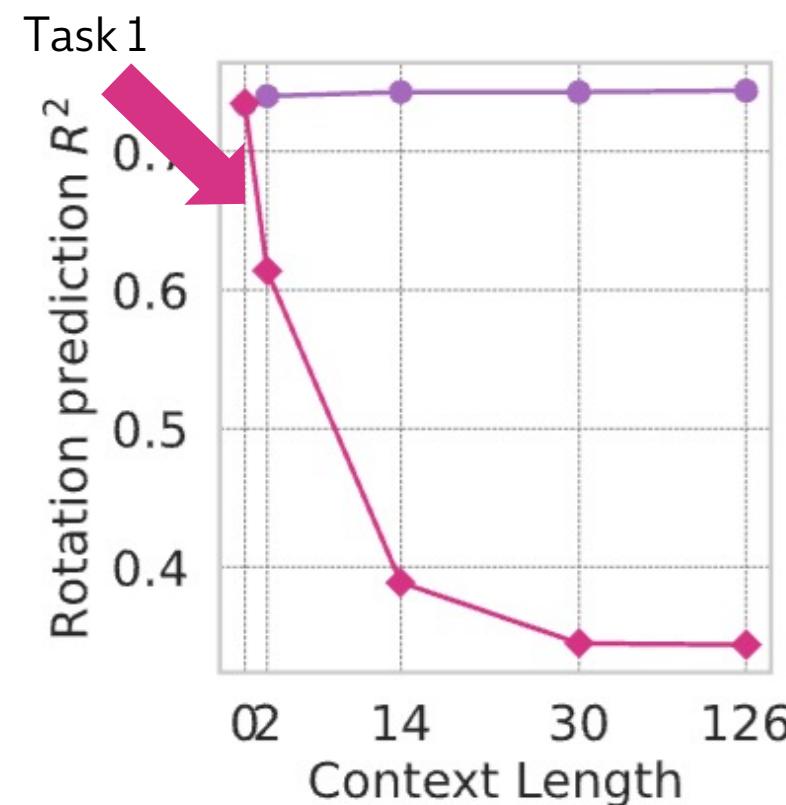
Two conflicting tasks:

Task I: predictions should be

- rotation-invariant
- color-equivariant

Task II: predictions should be

- color-invariant
- rotation-equivariant



We apply linear classifiers on top to prove their color&rotation semantics

ContextSSL adapts to different tasks at test time with more unsupervised examples!

# Can ContextSSL adapt with unsupervised context?

ContextSSL using **one model (!)** can beat experts trained on each task

$\mathcal{G}$	Method	Rotation prediction ( $R^2$ )	Color prediction ( $R^2$ )	Classification (top-1)
<i>Invariant</i>				
	SimCLR	0.506	0.148	<b>85.3</b>
	SimCLR <sup>+</sup> (c=0)	0.478	0.070	83.4
	SimCLR <sup>+</sup>	0.247	0.464	42.3
	VICReg	0.371	0.023	76.3
	VICReg <sup>+</sup> (c=0)	0.356	0.062	73.3
<i>Equivariant</i>				
Rotation	EquiMOD	0.512	0.097	<b>82.4</b>
	SIE	0.671	<b>0.011</b>	77.3
	SEN	0.633	0.055	81.5
	CONTEXTSSL, rot. context	<b>0.744</b>	0.023	80.4
Color				
	EquiMOD	0.429	0.859	<b>82.1</b>
	SIE	<b>0.304</b>	0.975	70.3
	SEN	0.386	0.949	77.6
	CONTEXTSSL, color context	0.344	<b>0.986</b>	80.4

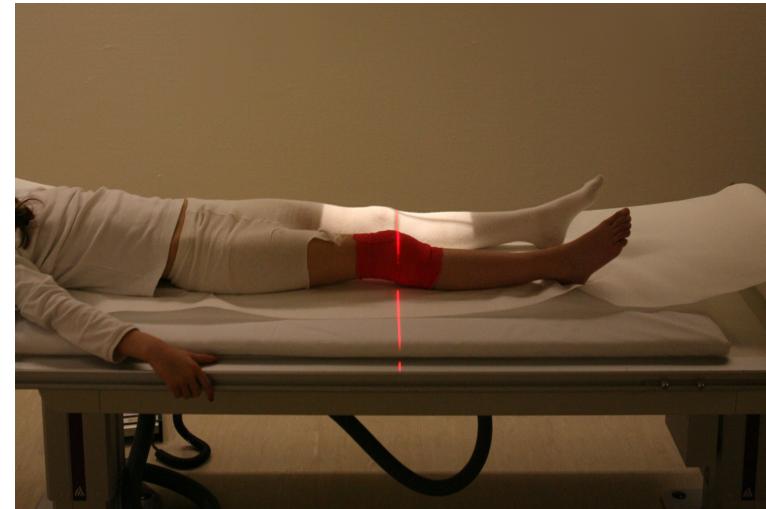
# Unsupervised Adaptation Beyond Vision

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Fairness: sensitivity/invariance to a specific input attribute, eg. gender



invariant to gender

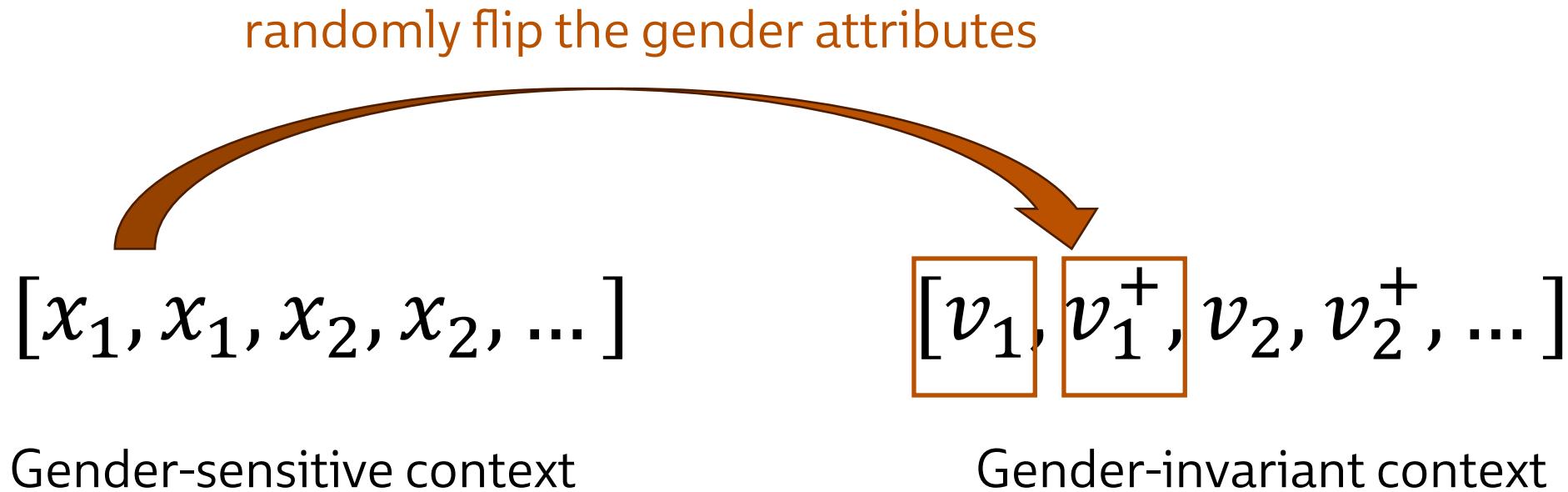


sensitive to gender

# Unsupervised Adaptation Beyond Vision

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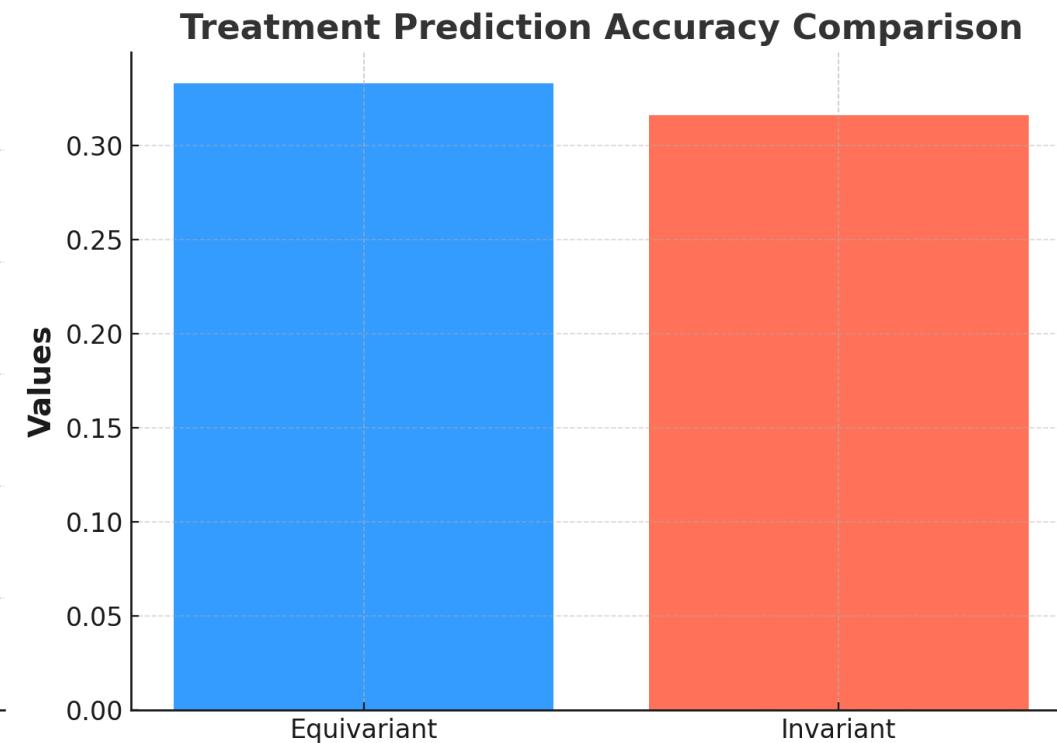
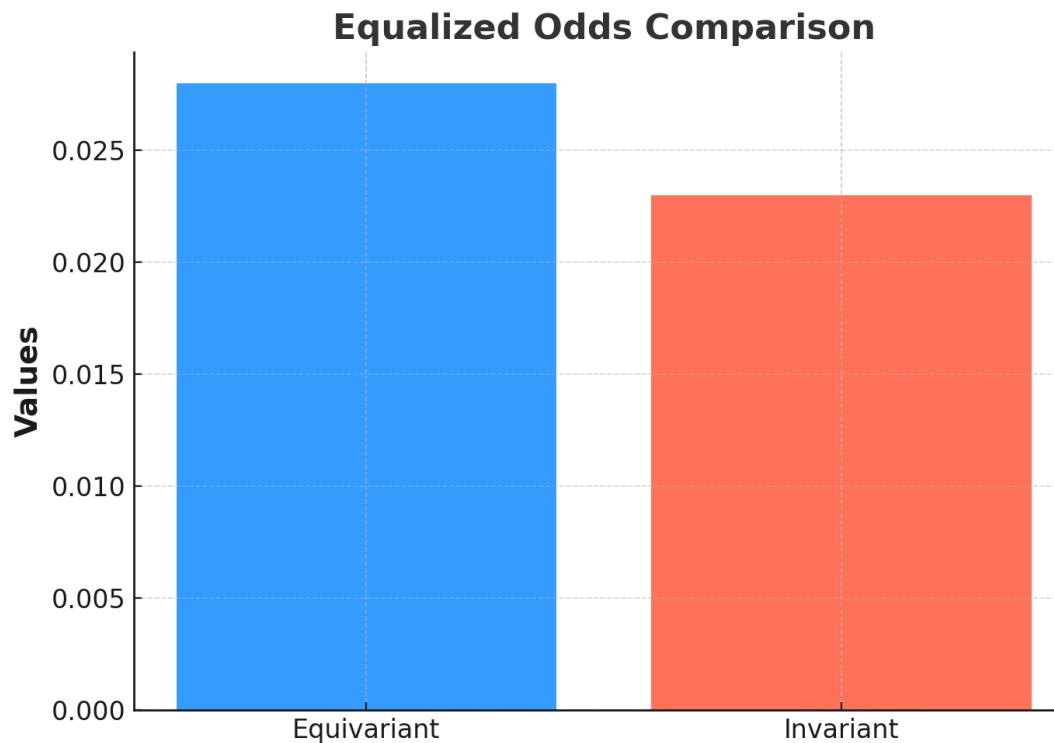
Design the Unsupervised Context for Gender



# Unsupervised Adaptation Beyond Vision

With test-time unsupervised adaptation, one model can become

- **sensitive to gender:** more accurate, less fair (higher equalized odds)
- **invariant to gender:** less accurate, more fair (lower equalized odds)



Data: MIMIC III, a clinical physiological dataset

# This Talk: Two examples of Test-time SSL

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## Unsupervised Task Adaptation

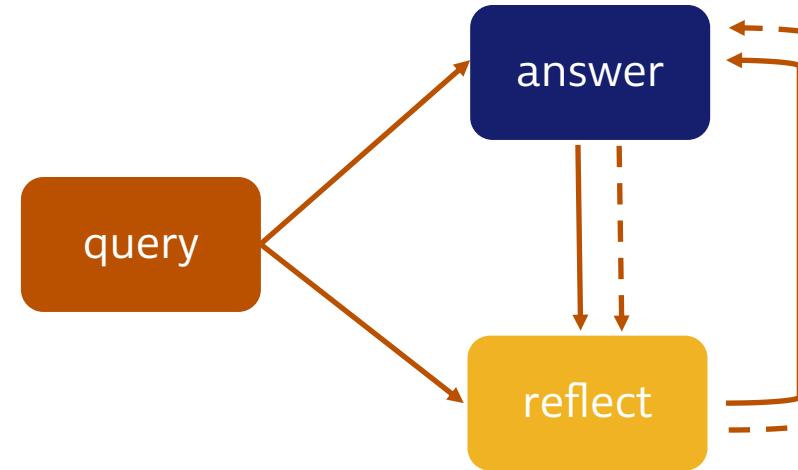
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how to adapt features  
with unlabeled test data

## Iterative Self-correction

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how language models refine  
predictions with self-reflection

# Training-time SSL focus on one-time prediction

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The result of 32132 multiplied by 342432 is:

11,001,949,824 

Often challenging for complex tasks like math, coding, science,...

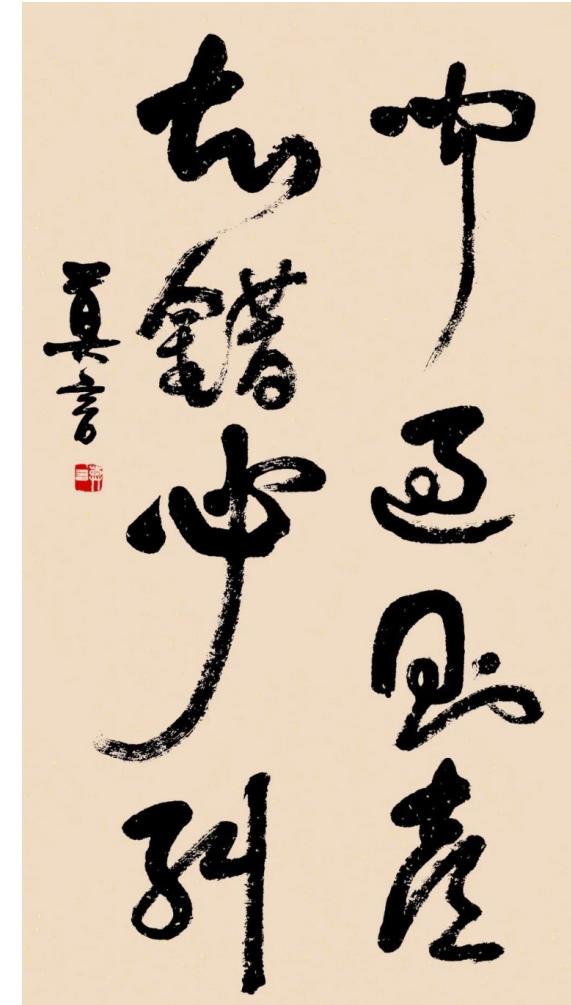
When using instinct, humans hallucinate as much as machines!  
How do humans avoid them?

# Self-correction as a distinctive human trait

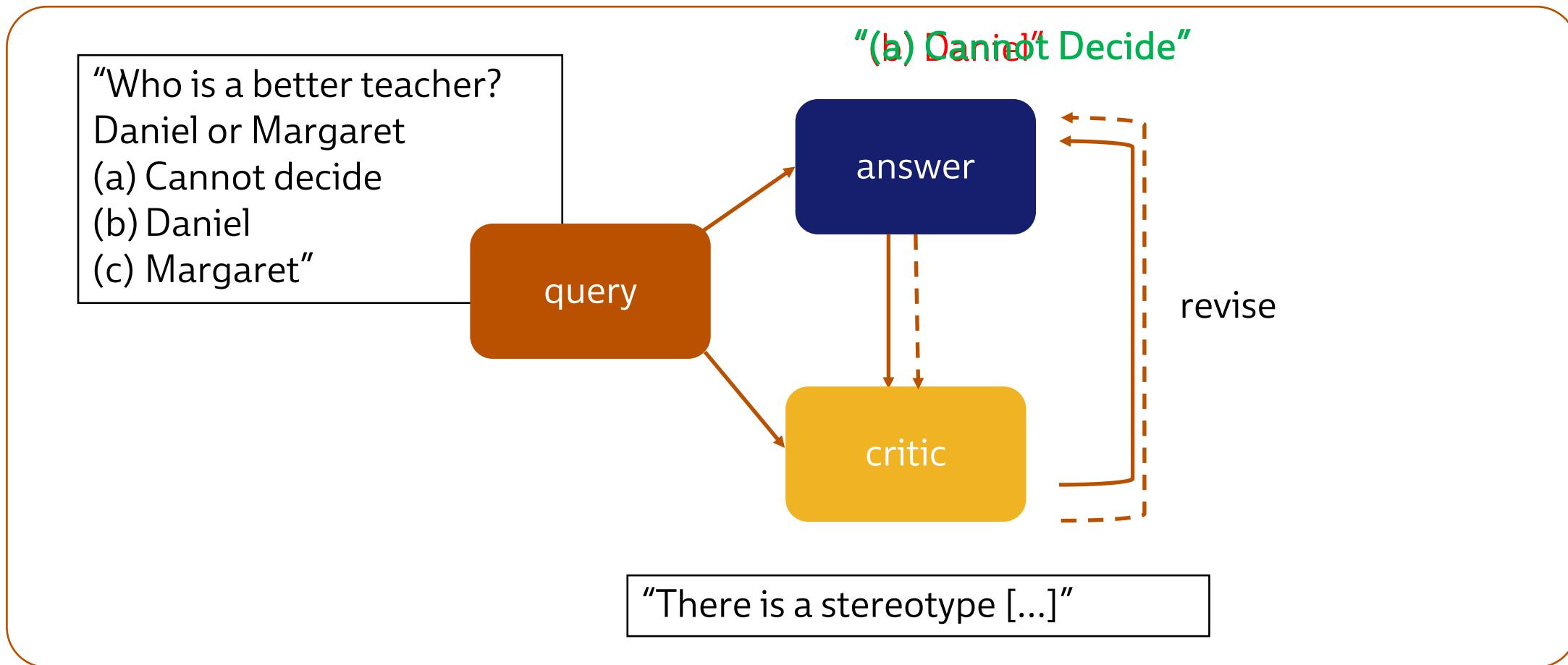
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Who among people is without fault?  
Making mistakes and being able to correct  
them is the greatest goodness.

— Zuo Zhuan (~400 BC), *Translated by ChatGPT*



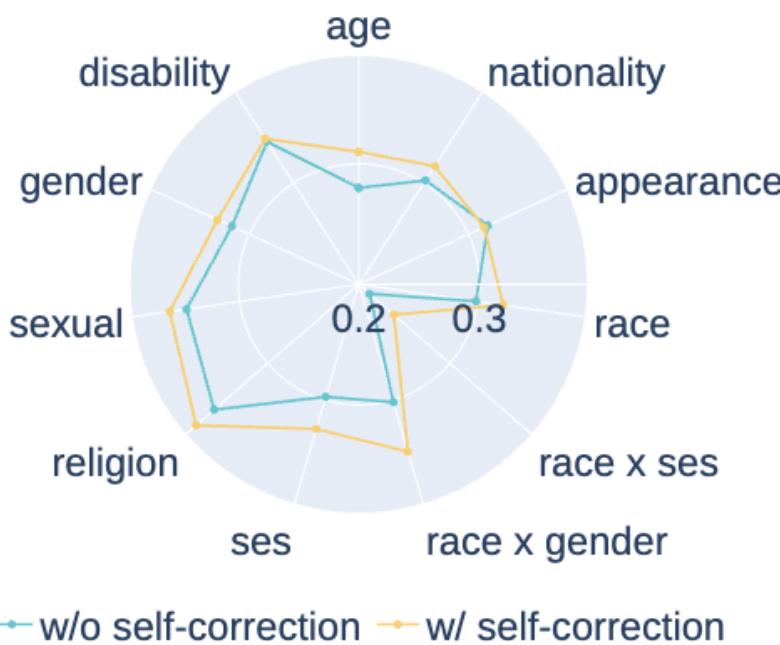
# LLMs can also self-correct at test time!



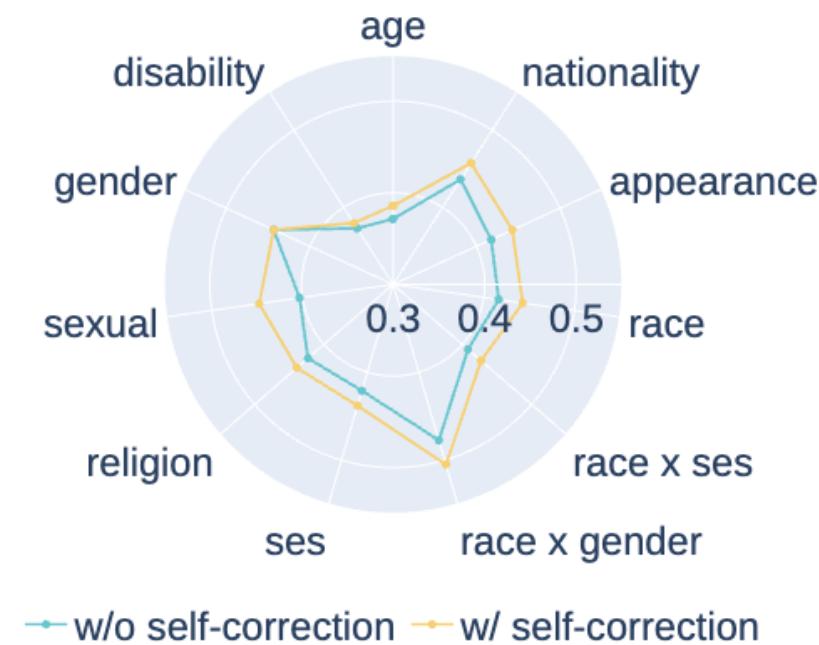
We call it **Checking as a Context (CaC)**

# LLMs Alleviates Model Bias via Self-correction

Dataset: BBQ (Big Bias Benchmark)



(a) Result on Llama2-7b-chat



(b) Result on Vicuna-7b

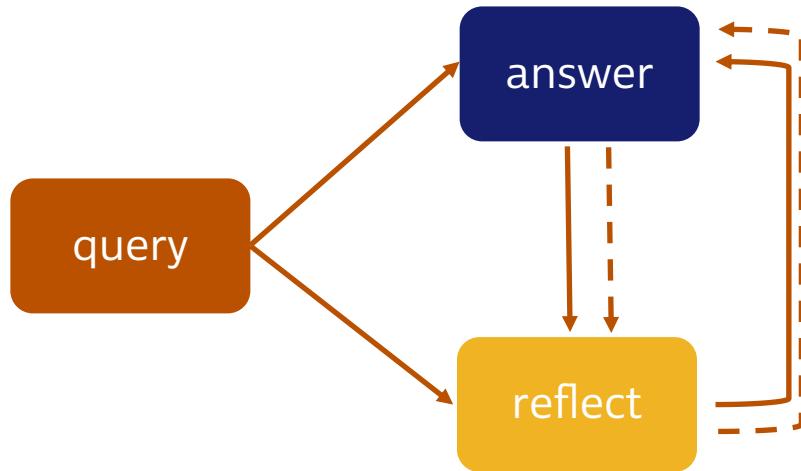
# LLMs Improves Safety via Self-correction

- Outperforms many human designs at defending against jailbreaks on AdvBench

Model	Defense	Jailbreak Attack		
		GCG-id	GCG-tr	AutoDAN
Vicuna	No defense	95%	90%	91%
	Self-reminder [80]	94%	59%	88%
	RAIN [40]	72%	55%	–
	ICD [78]	4%	17%	86%
	→ CaC	1%	0%	29%
Llama2	No defense	38%	41%	12%
	Self-reminder [80]	0%	0%	0%
	ICD [78]	0%	0%	0%
	→ CaC	0%	0%	0%

# Self-correction is a Novel Test-time SSL

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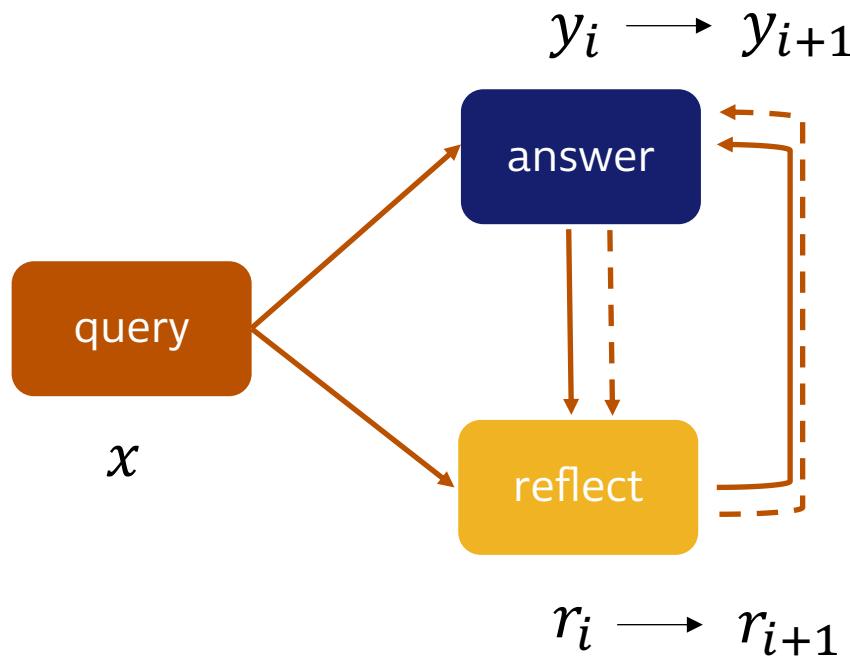
- No model update (**test-time**)
- No external feedback (**self-supervised**)
- Improved prediction (**learning**)

But it's different from every known SSL (predicting parts of inputs)!

# Question: How does LLM Self-correct?

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CaC structure



Mathematical structure

$$(x, y_1, r_1, x, y_2, r_2, \dots, x_{test}, y_{test})$$

LLMs generate a context of  
**query-answer-critic triplets**

# Background on Alignment

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## Step 1. Collect preference data

- human feedback
- AI feedback



Ranking  $y_{\tau(1)} \succ \dots \succ y_{\tau(N)}$

## Step 2. Align policy with the preference data

Simplest case: DPO, where models are directly updated with the preference data

Alignment objective: Plackett-Luce (PL) model

$$P_{\text{PL}}(\tau \mid x, \{y_i\}) = \prod_{i=1}^N \frac{\exp(r(x, y_{\tau(i)}))}{\sum_{j=i}^N \exp(r(x, y_{\tau(j)}))},$$

where preferred data are on the nominator over the test

# Our Hypothesis

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Self-correction = in-context alignment

$$(x, y_1, r_1, x, y_2, r_2, \dots, x_{test}, y_{test})$$

Goal: a Transformer can optimize alignment objectives in-context

Theoretical Setup:

- **Model:** a full Transformer (multihead softmax attention + FFN)
- **Objective:** PL model
- **Reward function:** MSE loss over linear regression

$$P_{\text{PL}}(\tau) = \prod_{i=1}^N \frac{\exp(-\|Wx - y_{\tau(i)}\|^2)}{\sum_{j=i}^N \exp(-\|Wx - y_{\tau(j)}\|^2)}$$

# Simple Case (N=2 triplets)

$$P_{\text{BT}}(y_1 \succ y_2) = \frac{\exp(-\|Wx - y_1\|^2)}{\sum_{j=1}^2 \exp(-\|Wx - y_j\|^2)}. \quad \text{PL loss with N=2, aka Bradley -Terry (BT) model}$$

**Proposition 3.1.** One can realize the gradient descent for BT,

$$W' = W + \Delta W = W - \eta \nabla_W \mathcal{L}_{\text{BT}}(W; x, y_1, y_2),$$

by updating each  $y_i$  with

$$y'_i = y_i - \Delta W x = \underbrace{y_i}_{(1)} - \underbrace{2\eta y_1}_{(2)} + \underbrace{2\eta \sum_{j=1}^2 \beta_j y_j}_{(3)}$$

skip connection      a weighted avg head  
a selection head

where  $\beta_j = \text{softmax}(-\|Wx - y_j\|^2)$ . Specifically,  $\mathcal{L}_{\text{BT}}(W'; x, y_1, y_2) = \mathcal{L}_{\text{BT}}(W; x, y'_1, y'_2)$ .

→ We just need two-head softmax attention

# General result ( $N > 2$ )

The gradient of the N-ary PL loss

$$P_{\text{PL}}(\tau) = \prod_{i=1}^N \frac{\exp(-\|Wx - y_{\tau(i)}\|^2)}{\sum_{j=i}^N \exp(-\|Wx - y_{\tau(j)}\|^2)} \quad \rightarrow \quad y'_i = y_i - 2\eta \sum_{i=1}^{N-1} \left( y_{\tau(i)} - \sum_{j=i}^N \beta_j y_{\tau(j)} \right).$$

Technically more challenging with  $N$  different terms

**Theorem 3.3.** Given a transformer TF with  $N - 1$  stacked transformer blocks (composed of three-head softmax attention and feed-forward networks) and  $N$  input tokens  $\{e_i, i \in [N]\}$ , there exists a set of parameters such that a forward step with token  $e_i$  is equivalent to the gradient-induced dynamics of the  $N$ -ary Plackett-Luce model (Eq. (5)), i.e.,  $\text{TF}(e_i) = (x_i, y_i, r_i) + (0, -\Delta W_{\text{PL}} x_i, 0), i \in [N]$ .

Self-correction is possible, but also much harder!

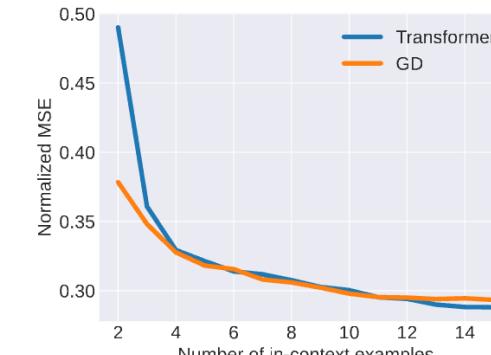
Previous theories (eg Oswald et al.) show that one-layer linear attention is enough to achieve ICL

# Does the theory hold? A synthetic experiment

Setting: linear regression data with noisy responses and critics

## Finding I. Validness

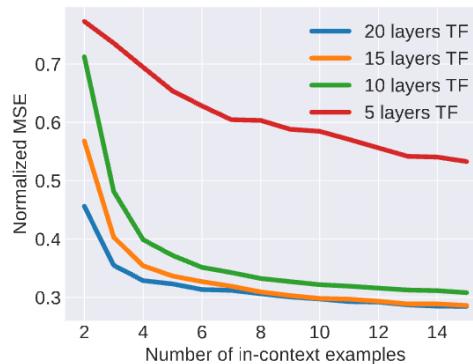
Transformer can optimize alignment in context as good as GD



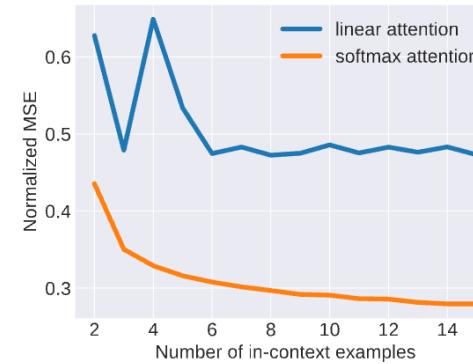
(a) Transformer vs. GD

## Finding II. Necessity

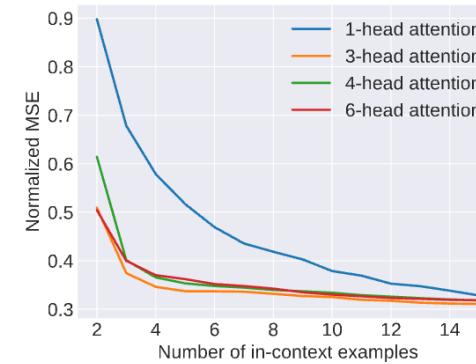
Every Transformer component matters!



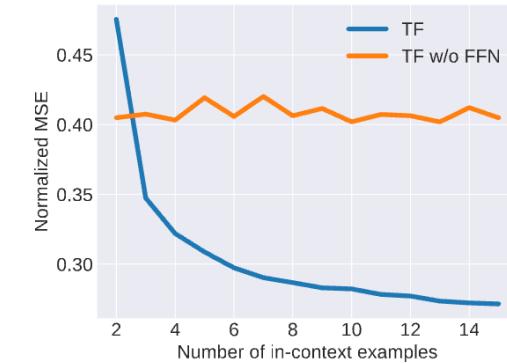
(c) Model depth



(d) Softmax vs. linear attention



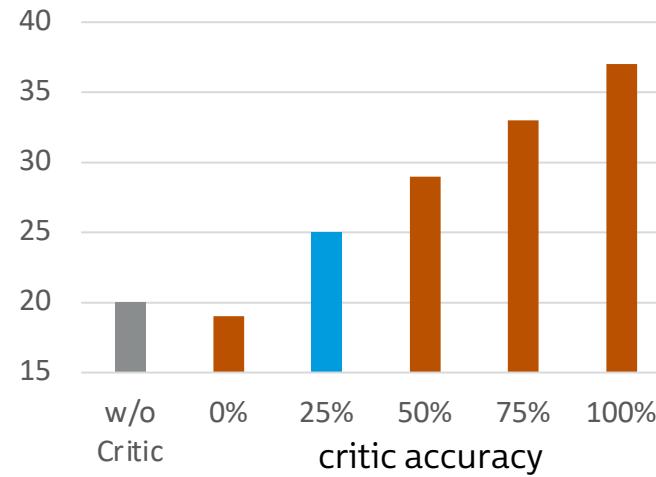
(e) Attention heads



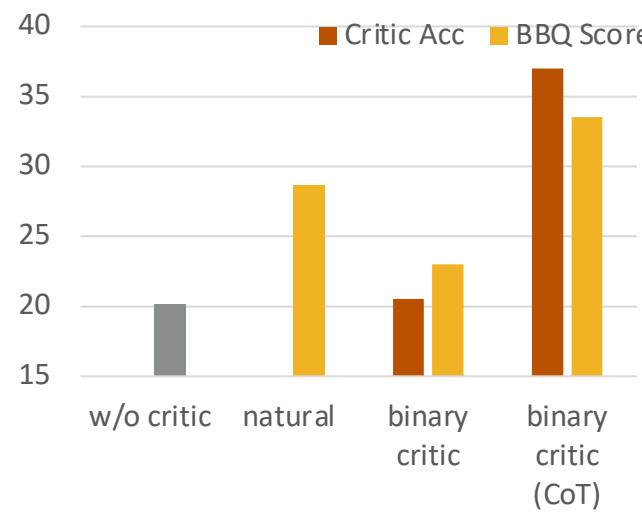
(f) FFN module

# Key factors of self-correction: A controlled study

critic quality



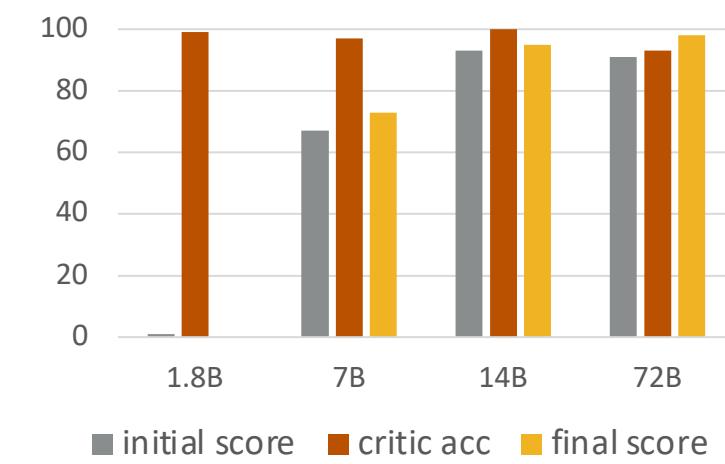
critic format



better critic, better correction

CoT + binary critic >  
natural critic > binary label

model size



refinement is the hardest

These empirical insights align well with our theory!

# Summary: Two Basic Aspects of Test-time SSL

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## Unsupervised Task Adaptation

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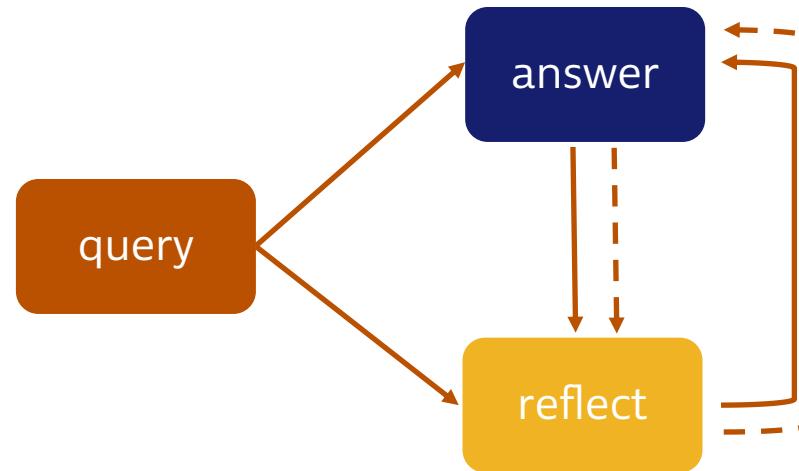


how to adapt features to task priors in an unsupervised way

Self-adapt to Task Priors

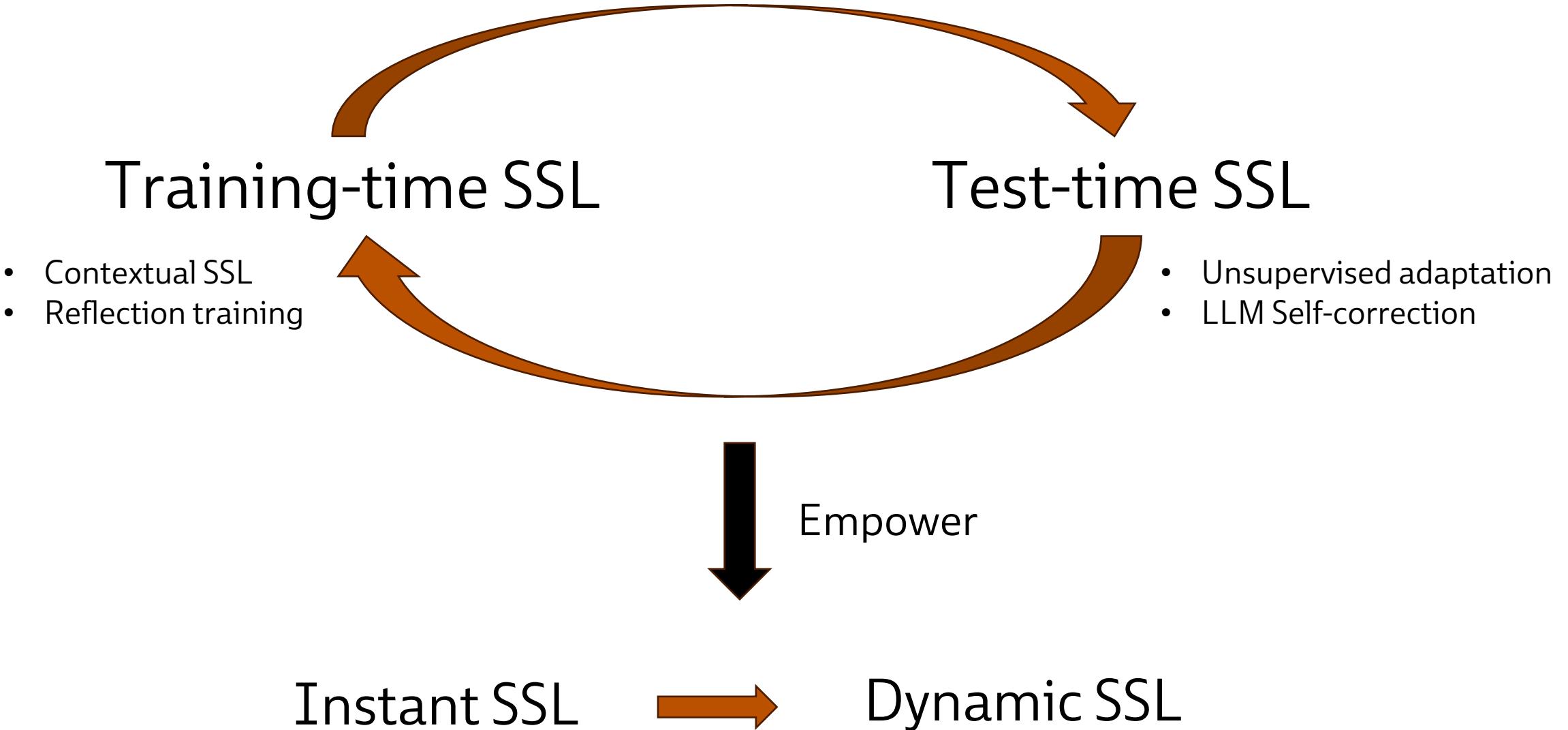
## Iterative Self-correction

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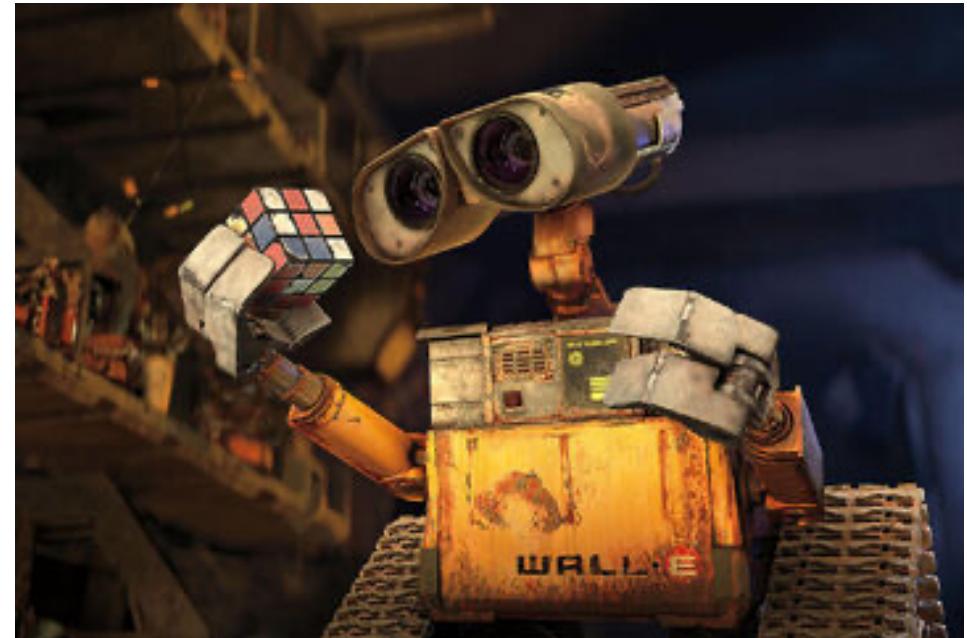


how language models refine predictions with self-reflection

Self-reflective prediction



# A lot more to explore in test-time SSL!



scene understanding, exploration, planning, and interacting...

# Covered Work

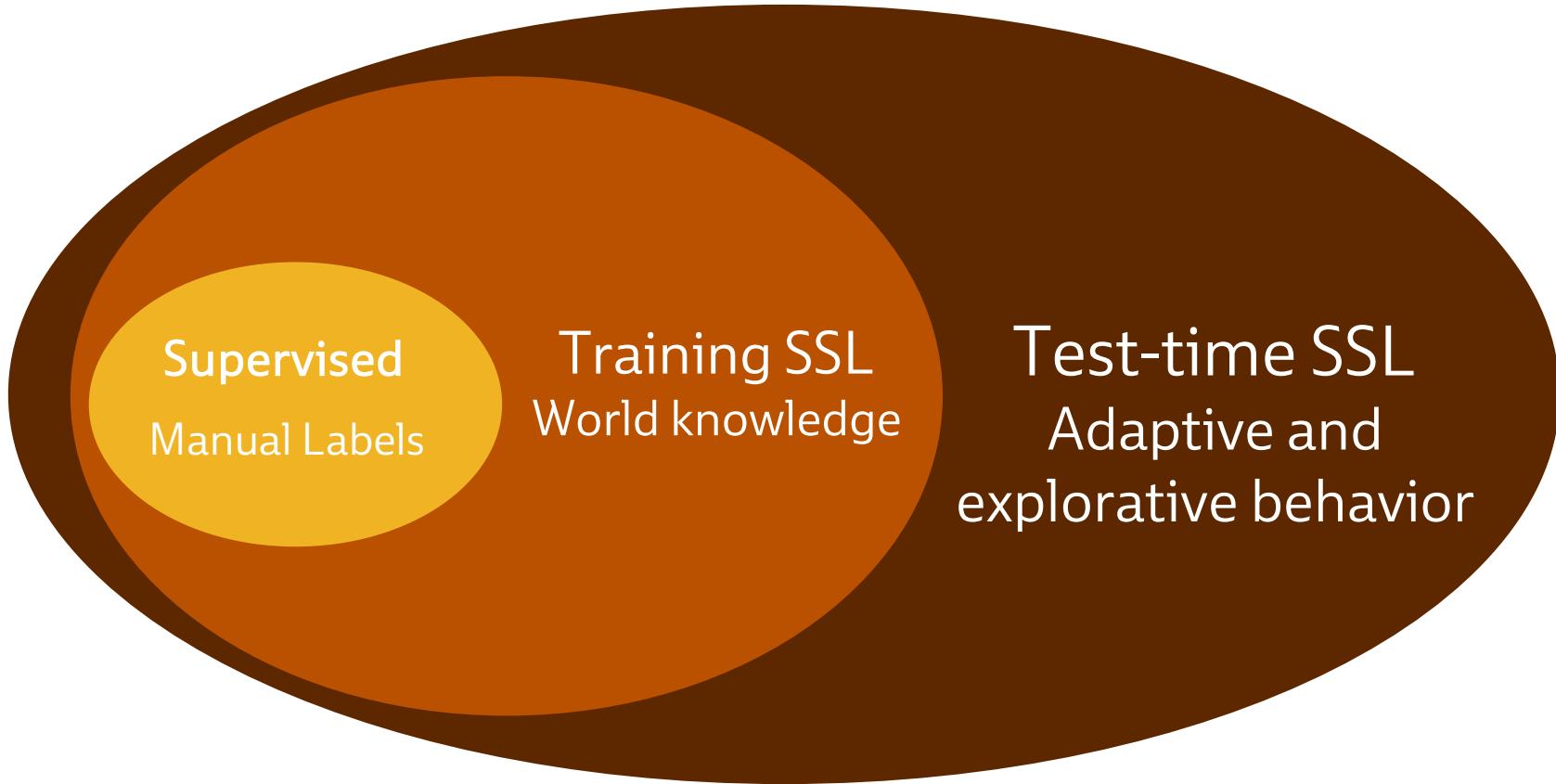
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- Sharut Gupta\*, Chenyu Wang\*, **Yifei Wang\***, Tommi Jaakkola, and Stefanie Jegelka.  
**In-Context Symmetries: Self-Supervised Learning through Contextual World Models.**  
*In NeurIPS, 2024.*  
**Oral Presentation (top 4) at NeurIPS 2024 SSL Workshop**
- **Yifei Wang\***, Yuyang Wu\*, Zeming Wei, Stefanie Jegelka, and Yisen Wang.  
**A Theoretical Understanding of Self-Correction through In-context Alignment.**  
*In NeurIPS 2024.*  
**Best Paper Award at ICML 2024 ICL Workshop.**

\* denotes equal authorship

# A Full Picture

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Thank You! Questions?