I-Rex: An Interactive Debugger for SQL

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ABSTRACT

SQL is declarative in nature and rich in its features. Writing semantically correct SQL queries and finding logical bugs in SQL are not easy, even for experienced programmers, who are often used to the mindset of working with general-purpose programming languages (GPLs). While there are many GPL debuggers, SQL debugging has received much less attention. In this paper, we present I-Rex, a SQL debugger that enables users to inspect the logical execution of SQL queries visually and interactively to identify and potentially fix logical bugs in the queries. I-Rex draws analogies to the debugging paradigm of GPLs (e.g., stepping, watchpoints, etc.), making it easier for programmers to adopt. However, unlike debugging GPLs, which involves executing the underlying program in full to the point of interest, I-Rex allows users to jump to arbitrary points of interest by leveraging the power of the database systems, through selective materialization and query rewrites. To simplify deployment, I-Rex acts as a lightweight middleware on top of the database system; it imposes no overhead to prepare a database for debugging and maintains no state in the database systems during debugging sessions. We demonstrate the effectiveness of I-Rex through performance experiments as well as a user study in an educational setting.

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INTRODUCTION

Relational databases form the backbone of many data-intensive applications and scalable data analytics. Despite its age, SQL continues to retain its prevalence and importance due to its highly declarative nature (i.e., specifying what the answer should be rather than how to compute it) and its extensive set of features that have only grown over time. However, SQL is difficult to understand and debug. In debugging GPLs (e.g. C++ or Python) that are typically

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procedural (i.e. explicitly describing the steps required to compute the answer), it is natural to trace the execution of programs to debug them. However, this method becomes much trickier for SQL.

As a first attempt, one may consider "tracing" a query's logical or physical plan, a tree whose leaves represent base tables and internal nodes represent relational operators. Through this approach, the user can examine the intermediate results produced by each of the plan nodes. Unfortunately, there are several problems with this approach. Firstly, the database optimizer often compiles a SQL query into a plan that bears no resemblance to the original query, making plan tracing unhelpful in finding and fixing logical bugs in the original query. Secondly, debugging is usually an iterative process: the user may examine execution multiple times, sometimes with minor modifications to the query. However, even small changes can lead to the optimizer choosing a very different plan; for example, the addition or removal of even a simple condition in WHERE can enable or disable an index scan opportunity. Even if the physical plan remains the same, there is no guarantee that the execution and result order are reproducible. For example, the size of the buffer memory, the choice of the hash function, and variations in the speed of parallel threads at run-time can change the ordering of intermediate result rows. Such non-repeatable and seemingly inconsistent behaviors significantly complicate debugging.

Perhaps, one possible workaround would be to restrict the database optimizer to avoid optimization across syntactic blocks of a query, such that each subquery corresponds to some subtree in the plan, and the user can at least inspect the result of each subquery. However, this may result in inefficient handling of complex queries. Furthermore, correlated subqueries, a frequently used SQL construct, render this workaround ineffective for many queries. In Section 2, we give concrete examples that illustrate this challenge and demonstrate how I-Rex helps debug these types of queries.

In this work with I-Rex, we focus on finding logical errors instead of fixing performance issues, and we aim to build an interactive SQL debugger with the following desiderata:

- (1) The debugger should conceptually execute a SQL query in a completely reproducible manner that is faithful to how it is written and must be easy for programmers to understand.
- (2) The debugger should offer features analogous to those in GPL debuggers so that they are easy to learn and adopt.
- Unlike GPL debuggers, which must execute underlying programs in full to reach points of interest, this debugger should

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- support efficient implementation of powerful features that allow the user to jump directly to points of interest.
- (4) The debugger must scale to large databases and gracefully handle prohibitively large intermediate results.
- (5) The debugger should be simple to run (e.g., from a remote browser) and easy to deploy on top of a database, without modifying database system internals or requiring extensive preparation of the database for debugging.

At first glance, (1) necessitates executing the SQL query "literally" using a completely unoptimized plan, which runs counter to (4). Our key insight is that, at any given point in time, the user can examine only a small "window" of the entire execution. It suffices to support fast access to any given "window" without incurring the full cost of the unoptimized plan. Supporting such accesses, along with (2) and (3) while respecting (5), requires novel optimization — SQL's built-in OFFSET and LIMIT constructs fail to deliver acceptable performance for interactive debugging.

Addressing the above challenges through the development of I-Rex, we make the following contributions:

- I-Rex introduces a novel debugging paradigm for SQL that draws many parallels to GPL debugging. Each query block is viewed as a function, and correlated subqueries are considered functions with arguments. We define the *canonical execution* of a SQL query, which is reproducible and faithful to query syntax.
- I-Rex supports various debugging features analogous to GPL debugging, including stepping through execution, pausing to examine a particular point during execution (breakpoints), pausing automatically at points of interest (watchpoints), drilling down into subqueries (stepping "into" a function), and row-level tracing (information flow analysis) in both forward (from input to output) and backward (from output to input) directions.
- While performing the canonical execution would have been extremely inefficient and impractical, I-Rex supports fast "teleporting" from one point of execution to another without paying the cost of execution in between. We do so by constructing queries that directly compute, for a given window, information needed for debugging, and by applying selective materialization and rewrite optimizations to ensure efficiency on large databases.
- I-Rex has a web-based frontend and a middleware backend that runs on top of a database system. It imposes no overhead to prepare a database for debugging and maintains no state in the database during active debugging sessions. This architecture makes I-Rex easy to adopt and deploy.
- Our performance evaluation using the TPC-H benchmark shows the scalability of I-Rex on large databases. More specifically, it also demonstrates the advantage of our optimization techniques over standard database (PostgreSQL) support for retrieving windows of query result rows.
- We evaluate the efficacy of I-Rex with a large-scale user study of over 100 students in an introductory-level database course. Its findings indicate that I-Rex significantly improves students' efficiency in debugging SQL queries.

2 EXAMPLE USE OF I-REX FOR DEBUGGING

Since I-Rex conceptually executes SQL queries as they are written, it is particularly suitable for novices who are learning how SQL

bar	beer	price
Apex	Corona	1
Apex	Dixie	2
Edge	Amstel	4
Edge	Corona	1.5
Tavern	Amstel	3
Tavern	Erdinger	1

(a) Serves

drinker	bar	times			
Amy	Apex	1			
Ben	Edge	4			
Coy	Tavern	2			
Dan	3				
(b) Frequents					

drinker	beer			
Amy	Erdinger			
Ben	Budweiser			
Ben	Dixie			
Coy	Amstel			
Dan	Amstel			
Dan	Corona			
(c) Likes				

Figure 1: A toy database about beers, bars, and drinkers.

queries work on the logical level. Furthermore, it serves as a powerful tool for novices and data professionals alike to find and fix logical bugs. This section provides a walk-through of how to use I-Rex to debug an incorrect query; we introduce the interface, concepts, and features of I-Rex. More formal and detailed discussions will be presented in later sections.

Example 2.1. Consider the toy database in Figure 1, which stores information about beers, bars serving them, and drinkers who like beers and frequent bars. We want to write a query for the following task: every time a drinker frequents a bar, they buy one bottle of every beer they like or any beer priced \$2 or lower; find the expected weekly revenue of each bar and rank them by revenue from high to low. A user may come up with the following (incorrect) query:

```
SELECT s.bar, SUM(f.times_a_week * s.price) AS revenue -- Q
FROM Serves s, Frequents f
WHERE f.bar = s.bar
AND (s.price <= 2 OR
EXISTS (
SELECT * FROM Likes 1 WHERE f.drinker = 1.drinker -- Qimner
))
GROUP BY s.bar;</pre>
```

The above query intends to first find drinkers and beers available for purchase using a join between Serves and Frequents. It additionally applies the two (alternative) conditions for purchase: 1) the price is lower than \$2, and 2) the beer is liked by the drinker. Then, the query groups the intermediate results by bar and calculates the sum of revenue. There is a bug in the EXISTS subquery Q_{inner} , but the question for now is: how would a user examine the result of Q_{inner} ?

Note that Q_{inner} is correlated, with the value for f.drinker coming from the outer (i.e. enclosing) block. As a result, there is no way to inspect this result independently. This situation cannot be handled by a query plan with relational operators, where the result of each subtree depends on this subtree alone.

Indeed, most database optimizers will rewrite the above query for execution such that the subquery is decorrelated. The decorrelated subquery would be a join involving both Likes and Frequents to compute the original subquery for all possible drinker values in a single effort. Then, the result will be combined with the rest of the outer query. The new plan now consists of only relational operators and can be computed/debugged in a bottom-up fashion, but unfortunately, it is vastly different from the original query. Users without in-depth knowledge of query optimization will likely be confused.

Example 2.2. This incorrect query described above returns the following result for the database in Figure 1:

bar	revenue
Apex	3
Edge	38.5
Tavern	8

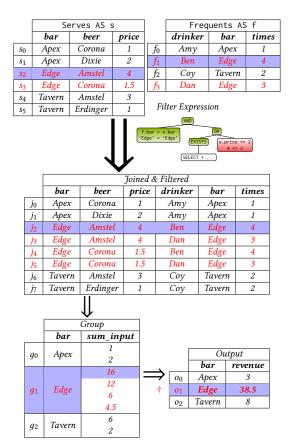


Figure 2: Debugging context for outer query block, Example 2.2.

Bindings from enclosing queries: f.drinker = 'Ben'

	Like	s AS l				
	drinker	beer				
l_0	Amy	Erdinger	Filter Expression		Filterea	! / Output
l	Ben	Budweiser	f.drinker = 1.drinker		drinker	beer
l:	Ben	Dixie	'Ben' = 'Amy'	00	Ben	Budweiser
l	Coy	Amstel		o_1	Ben	Dixie
l.	Dan	Amstel				
1	Dan	Corona]			

Figure 3: Debugging context for inner query block, Example 2.1.

Based on the user's knowledge of the database instance, the revenue of bar Edge seems to be higher than expected. We now walk through how to use I-Rex to debug the query, starting with this observation.

I-Rex presents a panel of UI debugging elements for each block of the query. Figure 2 illustrates the UI for the outer query block Q (for simplicity, we do not show the actual interface here as it contains other details that may be distracting for this discussion). I-Rex shows the execution of this block in stages, from top to bottom. At the very top, I-Rex shows all input tables in FROM. Note that one row from each input table is highlighted; this input combination ("combo") intuitively defines the current point of execution being examined. Then, I-Rex presents the "joined & filtered" result, which is the intermediate output after the WHERE clause is applied. The intermediate result row produced by the current input combo is automatically highlighted. Between this result table and the input tables, a "filter expression" tree shows how the WHERE condition evaluates over the current input combo.

The user can examine the value of each subexpression therein and see how the truth values (color-coded here) are combined by logical connectives. Following the joined & filtered result, I-Rex shows the GROUP BY result. For each group, in addition to the GROUP BY value, each group member's contribution to the final SUM aggregate is also shown. Again, the group and the member that the current input combo contributes to are automatically highlighted. Finally, the output table shows the final result of the query block.

For the convenience of subsequent discussion, we show a symbolic identifier (e.g., s_0 , f_2 , j_6 ...) for each row. We do assign internal row identifiers, whose purposes will be explained later in Section 3, but they are not explicitly displayed by the UI.

Given the unexpectedly high revenue of Edge, the user naturally wants to examine how that output row was computed. I-Rex supports tracing backward from output to input using a more general mechanism called pinning, denoted here by the red \dagger next to $o_1: \langle \text{Edge}, 38.5 \rangle$. A pinned output row intuitively narrows the execution down to only parts that are "relevant" to it (which we define formally later in Section 3). As shown in Figure 2, relevant rows in upstream tables are automatically colored red. Specifically, input rows s_2 and s_3 join with f_1 and f_3 in a nested-loop fashion to produce rows f_2 through f_3 in the joined & filtered table; they are further grouped into f_3 in the group table before finally producing f_3 .

As soon as the user pins o_1 , I-Rex identifies the relevant input combos and "positions" execution at the first input combo in lexicographical order — this is how the input combo $\langle s_2, f_1 \rangle$ was activated in the first place in Figure 2. Starting with this input combo, the user can step through other input combos relevant to o_1 , or manually choose any combo to investigate. Throughout the process, I-Rex automatically updates highlighting in downstream tables as well as the state of any expression evaluation trees, in effect supporting forward tracing.

When examining the execution for $\langle s_2, f_1 \rangle$ as shown in Example 2.2, the user notices that $\langle s_2, f_1 \rangle$ contributes a value of 16 to the final sum. According to the filter expression tree, the price of Amstel is higher than \$2, but EXISTS (Q_{inner}) returns true, meaning that Ben should like Amstel per query intention. I-Rex allows the user to "drill down" into the execution of Q_{inner} in this context. Recall that Q_{inner} is a correlated subquery. To a programmer, the analogy of evaluating Q_{inner} is a function call with a parameter setting for f.drinker, which takes its value from the current input combo. Hence, "drilling down" naturally corresponds to "stepping into" a function call in GPL debugging.

Once the user drills down to Q_{inner} , I-REX creates a new panel for debugging this subquery block, illustrated in Figure 3. The UI makes it clear that we are executing

| SELECT * FROM Likes 1 WHERE f.drinker = 1.drinker;

with parameter f.drinker set to Ben. In this case, a quick glance at the output table or the filter expression tree for this block should reveal the problem — nothing supports that Ben likes Amstel. In fact, this subquery does not even look for Amstel. Therefore, to fix the query, we should let the outer query "call" Q_{inner} with an additional parameter s.beer, and let Q_{inner} additionally test whether s.beer = 1.beer.

The user can modify the original query accordingly and restart the debugging session to verify that it fixes the problem. Because the new query is syntactically similar to the old, I-Rex will produce a very consistent experience for the user: the execution of the new query will

Bar	Beer	Price	Drinker	Bar	Times
Edge	Amstel	4	Ben	Edge	4
Edge	Amstel	4	Dan	Edge	3
Edge	Corona	1.5	Ben	Edge	4
Edge	Corona	1.5	Dan	Edge	3

Figure 4: A paginated table in I-Rex.

be nearly identical to the old, with the exact same stages and exact same ordering of input combos and intermediate result rows.

A Note on Scalability. While Example 2.2 simplifies our discussion by assuming a small database instance, realistic databases are much larger. Even with moderately sized databases, joins can easily produce large intermediate results. As we will see in Section 5, for some TPC-H benchmark queries, even with a moderate scaling factor of 1, a single intermediate result table can easily take an hour to print out entirely on the database server console. Hence, it is impractical to cache entire results at any location (database server, middleware, or user browser) or send them over the network.

Meanwhile, users generally cannot examine many rows simultaneously. Therefore, I-Rex UI supports a pagination mechanism to display each table (input, intermediate result, or final output); Figure 4 shows a screenshot. The user only sees a page's worth of data at once in each table. Data outside the visible page can be computed and fetched on demand (and subsequently cached or evicted). As the user interacts with the UI, I-Rex adjusts the visible portions of all displayed tables accordingly, so that each reflects the execution point defined by the current input combo. Similarly, the user can visit any pages of input tables to select a new input combo for tracing; I-Rex would automatically adjust downstream table displays to show corresponding intermediate result rows.

Hence, efficient pagination is key to scalable SQL debugging. With efficient pagination, I-Rex effectively allows the user to "teleport" across points of interest without incurring the execution cost in between, making I-Rex much more powerful than GPL debugging. Pagination also provides a more manageable and less overwhelming experience for users. While most database systems support efficient pagination of input tables, it is challenging to paginate intermediate results and associated debugging information. Furthermore, I-Rex's requirement of making execution reproducible imposes specific ordering of intermediate results that complicates optimization. We discuss our solution in Section 4.

3 DEBUGGING PARADIGM

This section describes the debugging paradigm of I-Rex. I-Rex supports a rich set of SQL query features, such as SELECT queries with inner cross joins, set/bag operations (e.g., UNION, INTERSECT, EXCEPT), subqueries (including correlated ones), outer joins and joins expressed in general JOIN syntax (except LATERAL), and WITH. However, it currently does not support recursive WITH, LATERAL joins, WINDOW functions, and any built-in functions whose results cannot be reliably reproduced (e.g., RAND).

3.1 Data and Execution Model

3.1.1 Table Model and IIDs. I-Rex allows users to interact with two types of tables: base tables and derived tables. Base tables are those that exist in the database, while derived tables are computed from the base tables during execution. To support reproducible execution (including ordering of intermediate result rows), we depart from the default unordered multiset semantics of SQL and instead model each table as an ordered list of rows, each associated with an internal row id (IID). A table's IIDs must be drawn from a totally ordered domain and uniquely identify the rows within the table. The IIDs do not influence the semantics of SQL query operators and should not be considered as extra columns by these operators. For example, if two rows have identical values for all columns (ignoring IID), they are still considered duplicates by SQL though their IIDs differ.

For a base table with a primary key declaration, we simply define IID to be its primary key value. Otherwise, we choose a compact UNIQUE key if one is available. In case that the table has no key, we use the database's internal row id (e.g., PostgreSQL's ctid); such ids are unique among duplicate rows.

For a derived table, we define its IID according to how the table is computed. For each SQL query operator, we define a *canonical execution procedure* and a *result IID synthesis function* (more details will be provided shortly). The IID synthesis function can compute the IID for each result row on the fly during canonical execution, such that the result rows are always produced in the IID order.

In addition to maintaining a reproducible order, I-Rex uses IIDs in supporting a variety of debugging features. Therefore, good IID designs positively impact performance, as we will see later in Section 4. While it is technically possible to simply make the IID of a row its sequence number in the result set, such numbers by themselves do not provide any information useful for tracing or possible query rewrite optimizations. As we will see below, most of the IIDs in I-Rex are "logical" instead of physical.

3.1.2 Query Blocks and Debugging Contexts. Given a query, I-Rex defines a canonical execution procedure that is always followed when debugging. A complex query can be viewed as a collection of syntactic blocks with dependencies among them. I-Rex models the canonical execution of such queries in terms of function calls:

- The outermost query block defines a function that computes the query result when executed.
- A subquery block defines a function that can be called by the function corresponding to its enclosing query block. A correlated subquery is analogous to a helper function with parameters, while a non-correlated subquery is comparable to a helper function without parameters. For instance, for Q_{inner} in Example 2.1, the caller is responsible for passing the values of external column references (e.g., f.drinker = 'Ben' in Figure 3) as parameters.
- Each table defined by WITH is a function that computes the table contents when the table is referenced.

Overall, the canonical execution starts by executing the function defined by the outermost query block, which then calls functions corresponding to its subqueries or tables defined by WITH, which may further call functions for their subqueries, etc.

As a function may be called multiple times, for each *invocation* of a function (i.e., an execution of a query block), I-Rex creates a

debugging context as needed, analogous to an "activation frame" in GPLs. As an example, Q in Example 2.1 calls Q_{inner} multiple times, with potentially different f.drinker values as arguments, resulting in different executions. This debugging context holds information specific to the particular execution of the query block, such as the values of external column references (i.e., parameter values).

3.1.3 Canonical Execution for Each Query Block. Having discussed the overall canonical execution procedure, we now zoom in on the canonical execution of each query block. For a complex construct such as SELECT, we further decompose its execution into *stages*, where each stage can be seen as an operator with its own canonical execution procedure and result IID synthesis function. We only discuss SELECT with inner cross joins below; Appendix A.1 discusses SQL set and block operations; Appendix A.2 discusses general join expressions including outerjoins.

The first stage in a SELECT block is *join & filter*. Its canonical execution is nested for-loops iterating through rows, one for each input table in FROM, in order. In the innermost loop, we test the WHERE condition (which may involve calling subqueries with parameter values obtained from the loop variables). The result row IID is synthesized as a vector whose components are the IIDs of the joining input rows. Note that the lexicographic order of these vector IIDs is consistent with the row production order. Considering Example 2.2 and Figure 2, the IID for Serves is its primary key (bar, beer), and the IID for Frequents is its primary key (drinker, bar). Therefore, the IID for the derived joined & filtered table has the format ((s.bar, s.beer), (f.drinker, f.bar)). In particular, j_2 's IID would be (s_2, f_1) , where we abuse notation slightly and use s_2 and f_1 to denote their IIDs (Edge, Amstel) and (Ben, Edge) respectively.

If the block contains grouping or aggregation, a *grouping* stage will be next. Its canonical execution is a stable sort of input rows according to the list of GROUP BY expressions² in order. Each result row starts with the GROUP BY expression values as columns, followed by additional columns needed to evaluate the remainder of the query (e.g. HAVING or SELECT expressions). The result row IID is synthesized as a vector whose components are the GROUP BY expressions in order, followed by the input row IID. This order puts member rows of a group together, allowing the UI to detect and display group boundaries (Figure 2). The *stable* sort ensures that the IID ordering is consistent with the row production order. For instance, in Figure 2, the IID of the first member row of g_1 is (Edge, j_2), where Edge also identifies the g_1 group.

The final stage of the SELECT block produces the *final output* for the entire block. The canonical execution processes the input rows in order. If HAVING is present, input rows whose group does not pass the HAVING condition are filtered out. Then, if the previous stage is a grouping stage, we produce one result row for each group of input rows, using the leading portion of the IID corresponding to GROUP BY expressions as the result IID. For instance, o_1 in Figure 2 would be Edge, same as g_1 's. Otherwise, no aggregation is involved,

and we simply produce one result row for each input row, using the same IID for the result. In either case, the IID order is consistent with the result row production order.

Several special cases associated with the final stage are worth noting. If any HAVING or SELECT expression contains subqueries, they would be handled the same way as in the join & filter stage. If SELECT is followed by DISTINCT, the canonical execution will further perform a sort of all result rows using all columns in some order (optimized to be maximally consistent with the input IID order) and output only distinct rows; the result IID will be synthesized as a vector whose components are all the columns in the order chosen. If ORDER BY is present, the canonical execution will further perform a stable sort of all result rows according to the ORDER BY expressions, and the result IID will be synthesized as a vector whose components start with the ORDER BY expressions and end with the input IID.

3.2 Debugging Operations

We now describe what operations a user can perform in a debugging context with I-Rex, focusing on those requiring formalization and more in-depth discussion; others mentioned in earlier sections with straightforward semantics (e.g., visualization of expression tree evaluation) are omitted. Again, we describe the operations mostly in the context of SELECT blocks with inner cross joins, although we have generalized them to other SOL constructs.

3.2.1 Input Combo Space and Execution Positioning. Recall that a debugging context refers to a specific execution of a query block. To represent the entire execution of a debugging context, we define its input combo space as an ordered set of input combos (combinations), each representing a particular point in execution. The (conceptual) current point of execution is called the active input combo for the debugging context. For a SELECT debugging context with n input tables, the active input combo is the n input rows being examined inside the innermost loop by the canonical execution of the join & filter stage, and it is represented by an n-dimensional vector whose components are the IIDs of these input rows. For instance, the active input combo of the SELECT debugging context shown in Figure 2 is $\langle s_2, f_1 \rangle$, drawn from the input combo space $\{s_0, \ldots, s_5\} \times \{f_0, \ldots, f_3\}$.

The user can position the execution of a debugging context at a particular point using either *stepping* or *teleporting*. With *stepping*, I-Rex automatically advances the active input combo to its successor (or predecessor if stepping in reverse order) in the input combo space. For example, (ignore the pin and) suppose the active input combo in Figure 2 were $\langle s_0, f_3 \rangle$; stepping would advance it to $\langle s_1, f_0 \rangle$, followed by $\langle s_1, f_1 \rangle$, consistent with the processing order of the canonical execution. With *teleporting*, given any input table, through the paginated display illustrated in Figure 4, the user can jump or scroll to any page and select a particular row as active; I-Rex will then update the active input combo accordingly. Even more advanced execution positioning can be achieved by pinning, which will be described shortly.

¹In implementation, I-Rex performs straightforward optimizations to compact the IID by removing known redundancies. For example, since all result rows have f.bar = s.bar, we can simplify the IID as (s.bar, s.beer, f.drinker) without affecting uniqueness or ordering. For brevity, in subsequent discussions, please assume that such optimizations will be applied implicitly at the implementation level.

 $^{^2\}mathrm{An}$ aggregate query without GROUP BY can be regarded as having an empty list of GROUP BY expressions.

³Per SQL standard, every ORDER BY expression must correspond to an output column. For SQL dialects that do not have this restriction, complex ORDER BY may necessitate a separate stage to help debugging. We will not elaborate here.

Finally, to handle outer joins and the special case of empty input tables, we extend our definition of the input combo space with a special value \perp ; see Appendix A.2 for details.

3.2.2 Forward Tracing. An active input combo in the debugging context can produce *derivative* rows in the downstream result tables produced by the stages. Intuitively, the input combo contributes to the computation of derivative rows; formally, the input combo participates in the how-provenance [38] of the derivative row. As discussed in Section 2, once the active input combo is set, I-Rex automatically refreshes all visualizations of expression trees, such that they reflect evaluation over the active input combo or its derivative rows. I-Rex also automatically refreshes all result table displays. such that they show the pages containing and highlighting the derivative rows. This forward tracing feature allows the user to examine the effect of input rows on subsequent processing and potentially understand why a desired effect is not achieved. Note that for a SELECT block, a given input combo can contribute to at most one result row per stage, so there is no ambiguity in which derivative rows to show downstream.

For example, in Figure 2, the active input combo $\langle s_2, f_1 \rangle$ has one derivative row per result table, namely j_2 , the first row in g_1 , and o_1 . In Figure 3, there is no derivative row for the active input combo $\langle l_0 \rangle$. By design, I-Rex ensures this rule of at most one derivative per stage for other blocks (such as set/bag operations) as well.

3.2.3 Pinning: Tracing and Watchpointing. We first describe the semantics of pinning and then discuss its use for tracing and watchpointing. Consider all tables displayed for a debugging context. I-Rex allows the user to pin up to one row from each of these tables. Formally, each pinned row defines a subset of the input combo space, called the row's pinned (input combo) space. Overall, the pinned space for the debugging context is its input combo space intersected with each of the pinned spaces defined by the pinned rows. Intuitively, the pinned space allows the user to narrow the execution down to the points of interest while debugging.

Consider a SELECT block joining n tables in FROM with input combo space $\mathbf{R} = \prod_{i=1}^n R_i$, where each R_i denotes the ordered list of IIDs for the i-th input table. A pinned row in the j-th input table with IID x defines a pinned space of $\prod_{i=1}^{j-1} R_i \times \{x\} \times \prod_{j=i+1}^n R_i$; i.e., the user is interested only in input combos with x participating. A pinned row in a result (intermediate or final) table defines a pinned space of $\{v \mid v \in \mathbf{R} \land x \text{ is a derivative row of } v\}$; i.e., the user is interested only in input combos that contribute to x.

Considering Figure 2, the pinned space for the pinned o_1 is $\{\langle s_2, f_1 \rangle, \langle s_2, f_3 \rangle, \langle s_3, f_1 \rangle, \langle s_3, f_3 \rangle\}$ because all these input combos contribute to the total revenue calculation for o_1 . If the user additionally pins f_1 in Frequents; this pinned row will have a pinned space of $\{s_0, \ldots, s_5\} \times \{f_1\}$. Thus, the overall pinned space for the debugging context will be $\{\langle s_2, f_1 \rangle, \langle s_3, f_1 \rangle\}$, meaning the user only wants to investigate how Dan contributes to Edge's total revenue.

Pinning has multiple uses. First, it augments I-Rex's tracing capability: pinning effectively allows *backward tracing* from a pinned result row produced by any stage to the pinned space of input combos, and then from there, forward tracing to result rows further downstream. Second, combined with stepping, pinning provides a form of *watchpointing*. With a pinned space in effect, I-Rex restricts stepping to the pinned space, effectively setting a watchpoint

that pauses execution only at points relevant to the pinned rows. In Figure 2, with o_1 pinned, execution automatically stops at the 4 relevant input combos $\langle s_2, f_1 \rangle$, $\langle s_2, f_3 \rangle$, $\langle s_3, f_1 \rangle$, $\langle s_3, f_3 \rangle$, skipping irrelevant portions of execution before, after, and in between.

3.2.4 Drilling Down and Pulling Up. As illustrated in Example 2.2, I-Rex allows the user to drill down into a subquery, analogous to "stepping into" a function call. Besides drilling down into subqueries in WHERE, HAVING, and SELECT expressions, I-Rex also allows drilling down into subqueries in FROM, which can be either directly nested therein or via a reference to some WITH definition. In these cases, the user can drill down directly through a particular row in a derived input table; I-Rex will open the debugging context for the subquery responsible for producing that table and automatically pin that row in the subquery's final output table.

When debugging a complex query with many nested blocks, I-Rex essentially maintains a "call stack" of debugging contexts. To let the user *pull up* from a subquery debugging context, I-Rex simply returns the user to the previous debugging context on the stack, which belongs to the enclosing query block. The state of the subquery debugging context is still preserved until the user changes the active input combo in the enclosing block's debugging context, which forces "stepping out" from the last subquery function call.

4 SYSTEM AND OPTIMIZATIONS

In this section, we describe the implementation and optimizations of the I-Rex system. Given a query Q being debugged, a straightforward approach would be to carry out the canonical execution of Q and collect all debugging information in one go, but this approach is not scalable, as the following example shows.

Example 4.1. Consider a TPC-H [10] database instance generated with a scale factor of 1 (i.e., total size of all tables is 1GB), and the following subquery in the FROM clause of benchmark query Q8:

If we were to compute and display the ten entire tables (eight input, one joined & filtered, and one output) for the debugging context, their contents alone would take 1,825MB. Lineage data needed to relate input combos and derivative rows would take another 88MB, not to mention information for the filter expression tree. Shipping close to 2GB of data (or more) from the database server to the I-Rex client introduces unacceptable overhead. Furthermore, this level of memory usage is demanding, as most browser tabs only use less than 1GB of memory. The situation becomes more unattainable when debugging on bigger databases and/or complex queries with multiple blocks.

To address this challenge, I-Rex uses three high-level ideas. 1) Rather than showing the entire canonical execution of a query Q being debugged, let the user examine one small, relevant window of this execution at a time. 2) To obtain all debugging information needed for a particular execution window, instead of performing the canonical execution and instrumenting it, we can formulate SQL queries based on Q to compute such information directly and

declaratively. 3) We can judiciously compute some summary data and then use them to further rewrite these queries to be more efficient, without requiring special support from the database.

As described in Section 2, I-Rex realizes idea (1) above using a paginated display for each table (based or derived). For each debugging context, the active input combo, introduced in Section 3.2, marks the current point of execution and controls which pages to display by default: pages containing the input combo for input tables, and the page containing the derivative row for each subsequent stage. Together, these pages define the "window" of execution as seen by the user. In the following, we first show in Section 4.1 how I-Rex optimizes pagination using ideas (2) and (3) above. Then, Section 4.2 discusses how I-Rex optimizes tracing and pinning. Section 4.3 describes the overall system and other details.

4.1 Optimizing Pagination

Given a base or derived table to display, the potential savings of pagination are easy to see: by focusing on one page at a time, we only need to compute, transmit, and render content on this page alone. The baseline solution to pagination supported by SQL uses its OFFSET and LIMIT features. However, OFFSET and LIMIT alone often do not lead to faster queries (which we will experimentally verify in Section 5). The optimizer typically has insufficient knowledge to skip directly to the OFFSET-th result row, so the query often executes from the very beginning to OFFSET+LIMIT, creating enormous waste. Furthermore, for queries that enforce a specific result order (which is the norm in I-REX as it aims to provide consistent and reproducible orderings for all results), simply determining the order would often involve computing and sorting all result rows, which ends up saving no computation cost.

To overcome this limitation, we observe that if we know which input rows contribute to the particular result page, we can use such information to prefilter the input rows and reduce execution cost. For example, in the joined & filtered table of Figure 2, suppose a user only needs to retrieve the page containing rows j_2 through j_5 . It turns out that we only need $\{s_1, s_2\}$ from Serves and $\{f_1, f_3\}$ from Frequents to compute this page. In general, explicitly enumerating a set of such input rows is not scalable, but we can instead compute a compact summary of this set, at the expense of potentially introducing some false positives (but never any false negatives).

I-Rex has three types of summary-based filters, described further below, to cover the range of design trade-offs: 1) IID-based filters, 2) "sargable" [62] filters, and 3) Bloom filters [12]. All three filters require precomputing a summary of what input rows contribute to the content of each page. We will show later in Section 4.3 how I-Rex does so as part of the initialization step of the debugging context. That step produces a *milestone table* for each input table of the debugging context and for the result table of each stage. For each page of table contents, a milestone row contains the summaries of input rows that contribute to the page. The milestone tables are cached by the I-Rex client. Subsequently, when the user requests a particular page of a table, I-Rex consults the corresponding milestone table to generate a *page-fetch query* that incorporates filtering using the summaries pertaining to the page requested.

	min_iid		s.bar	s.beer	f.drinker	f.bar
0	((Apex, Corona),		[Apex, Edge]	[Amstel, Dixie]	[Amy, Ben]	[Apex, Edge]
	(Amy, Apex))					
1	((Edge,	Amstel),	[Edge, Edge]	[Amstel, Corona]	[Ben, Dan]	[Edge, Edge]
	(Dan, Edge))					
2	((Tavern, Amstel),		[Tavern, Tavern]	[Amstel, Erdinger]	[Coy, Coy]	[Tavern, Tavern]
	(Coy, Tavern))					

Table 1: Milestone table for the joined & filtered table in Figure 2, with 3 pages and page size of 3 (rows). The IIDs have the format ((s.bar, s.beer), (f.drinker, f.bar)), and three minimum IIDs are those of the rows j_0 , j_3 , and j_6 respectively. The Bloom filter column is omitted

4.1.1 IID-Based Filtering. Recall that I-Rex sorts every table by its IID to ensure consistency and reproducibility. Hence, pages of a table partition its rows into consecutive, non-overlapping IID ranges. To enable IID-based filtering, we precompute, in the milestone table, the minimum IID among rows on each page. For example, Table 1 shows the milestone table for the joined & filtered table in Figure 2, with the minimum IID for each page captured by the min_iid column. Using this information, I-Rex can add a tight range condition on IID to the WHERE clause of a page-fetch query.

Continuing with the same example, the following query fetches the contents of the second page of the joined & filtered table, while also synthesizing the IID for each result row:

Note that the lower IID bound is the minimum IID of the second page as recorded in Table 1, and the (open) upper IID bound is the minimum IID of the next page.

IID-based filtering serves two purposes. First, it rejects any result row not on the requested page. This feature is indispensable because the other types of filtering implemented may introduce false positives and admit result rows outside the requested page; therefore, I-Rex always activates IID-based filtering to ensure correctness. Second, IID-based filtering can enable more efficient execution. However, its potential is limited: from a range bound on a multi-component IID, we can safely infer a range bound only on the leading component, but not on subsequent components. For example, in the page-fetch query above, the query optimizer may infer that s.bar (and hence f.bar by transitivity) falls within [Edge, Tavern] and use an index on s.bar (or f.bar), but nothing is known about s.beer or f.drinker. This limitation motivates other types of filtering below.

4.1.2 Sargable Filtering. To enable efficient page-fetch queries, we aggressively look for opportunities to inject safe, sargable [62] predicates that enable index plans. To this end, for each column A in an input table, where an index already exists on A, I-Rex computes a concise summary of the A values, in the form of a single range [min, max], over all input rows that contribute to each page of the result table. For example, Table 1 shows the milestone table for the joined & filtered table in Figure 2, assuming that s.bar, s.beer, f.drinker, f.bar are the four indexed columns in Serves and Frequents. With this information, I-Rex injects a range condition for each of these columns in the WHERE clause of a page-fetch query.

Using the same example, the page-fetch query for the second page of the joined & filtered table can now be augmented as follows:

```
| SELECT ... FROM Serves s, Frequents f
| WHERE (...) -- original WHERE conditions
| -- sargable filtering:
| AND s.bar BETWEEN 'Edge' AND 'Edge'
| AND s.beer BETWEEN 'Amstel' AND 'Corona'
| AND f.drinker BETWEEN 'Ben' AND 'Dan'
| AND f.bar BETWEEN 'Edge' AND 'Edge'
| AND ... -- IID-based filtering
| ORDER BY 1; -- order by IID
```

Since the sargable filters are always on indexed columns, they enable the optimizer to consider index plans that access only the relevant parts of the input tables. Even when index plans are not the most optimal, the inexpensive filter conditions still reduce the number of rows involved in downstream processing (e.g., join) and hence overall execution cost.

Remarks. Note that an intelligent optimizer might be able to infer the same bounds on s.bar and f.bar from the IID-based filtering condition; however, sargable filtering makes them explicit and more easily recognizable by the optimizer. Furthermore, the bounds on s.beer and f.drinker cannot be inferred.

On the other hand, pushing down filters too aggressively may have a negative effect when the filters are not selective, which can happen if the page size is not small and the result row ordering does not correlate with the filter column value. The optimizer may underestimate the output cardinality of the filter and choose a secondary index scan that is less efficient than a table scan. Therefore, we only inject a sargable filter for column *A* if its range on the requested page covers a small percentage of the entire domain of *A*. I-Rex uses 30% as a cutoff, which works well empirically.

Finally, instead of using one range to summarize input column values for a page, we can use multiple ranges to reduce false positives, at the expense of higher precomputation and storage costs for milestones. This trade-off is worth investigating as future work. However, even if individual input column values are free of false positives, we must still keep the IID-based filtering condition, because duplicate column values and joins can still admit result rows outside the requested page.

4.1.3 Bloom Filtering. Correlated subqueries in WHERE can still bottleneck query execution, especially if the external columns they reference are not indexed and therefore not covered by sargable filtering. One approach to avoid evaluating expensive correlated subqueries is memoization: regarding each correlated subquery q as a function, we can cache all value settings of the external columns that q is invoked with, along with the corresponding results returned by q. However, this approach is not scalable as the number of possible value settings can be high (even with sophisticated decorrelation techniques [63] to restrict such settings) and results can be large, requiring large cache spaces. Furthermore, if this cache is deployed on the client, the client must embed the cache contents explicitly into the page-fetch query, which makes resulting SQL complicated and harder to optimize.

To balance space efficiency and performance, we take an approximate approach at a coarser grain: instead of capturing the behavior of each subquery precisely, we consider the entire WHERE condition (including any constituent subqueries), and use a Bloom filter [12]

to track, for each page, the set of "relevant" input column values for which the entire WHERE evaluates to true. We choose relevant columns to be all input table column externally referenced by any subquery, plus any input table column involved in an atomic condition together with some subquery. For instance, in our running example (Q from Example 2.1), the only relevant input column is f.drinker. As another example, if the WHERE condition is A IN (q(B)), where q is a correlated subquery with external column reference B, the set of relevant input columns would be {A, B}. As shown in Section 4.3, a single SQL query can precompute such Bloom filters conveniently using a user-defined aggregate function, together with the rest of the milestone table.

Continuing with our running example, the page-fetch query for the second page of the joined & filtered table is now updated to:

```
|| SELECT ... FROM Serves s, Frequents f

|| WHERE (...) -- original WHERE conditions

|| AND ... -- sargable filtering

|| AND ... -- IID-based filtering

|--- Bloom filtering:

|| AND BLOOM_CHECK('10101010', f.drinker)

|| ORDER BY 1; -- order by IID
```

Here, BLOOM_CHECK(F,e) is a user-defined function that checks whether an entry e is in the Bloom filter F. Given the probabilistic design of Bloom filters, BLOOM_CHECK may return false positives but not false negatives. '10101010' is the Bloom filter computed for the second page, encoding all f.drinker values over input combos that contribute to this page. Failing BLOOM_CHECK allows query execution to save time by bypassing the evaluation of the expensive subquery. In this example, row f_2 , with f.drinker of Coy, fails the subquery condition, so the computed Bloom filter will not have the contribution of Coy. Hence, when evaluating the above page-fetch query, even though Coy still passes the sargable filter, it will likely fail BLOOM_CHECK, allowing the rest of WHERE including the subquery to be skipped. On the other hand, because of false positives, passing BLOOM_CHECK does not mean WHERE must evaluate to true; the original WHERE condition still must be included.

Remarks. The proposition below (proof in Appendix B) implies that there is considerable freedom in choosing the set of relevant input columns to track for a Bloom filter. To one extreme, we can simply feed the IIDs of the input rows into the Bloom filter, such that it tracks which input combos contribute to the requested page. However, the number of distinct entries can be huge, especially if the query involves aggregation, raising the false positive rate. Instead, we have decided to track input column values that influence the outcome of evaluating conditions involving subqueries, because there may be far fewer distinct values that need to be tracked. This heuristic has worked well in practice for I-Rex.

PROPOSITION 4.2. Suppose functions $BLOOM_GEN : \mathcal{P}(tuples) \rightarrow bitstrings \ and \ BLOOM_CHECK : bitstrings \times tuples \rightarrow \{true, false\} \ satisfy \ e \in \mathcal{V} \Rightarrow BLOOM_CHECK(BLOOM_GEN(\mathcal{V}), e) \ for \ any \ tuple \ e \ and \ any \ set \ \mathcal{V} \ of \ tuples \ of \ the \ same \ sort. \ Let \ \{R_i\} \ denote \ a \ list \ of \ (potentially \ aliased) \ input \ tables \ and \ \Theta \ a \ condition \ over \ \{R_i\}. \ For \ any \ subset \ \mathcal{A} \ of \ columns \ in \ \{R_i\}, \ the \ following \ two \ queries \ are \ equivalent:$

```
\begin{array}{l} \mid\mid Q_1\colon \mathsf{SELECT} \star \mathsf{FROM} \ \dots, R_i, \dots \ \mathsf{WHERE} \ \Theta; \\ \mid\mid Q_2\colon \mathsf{SELECT} \star \mathsf{FROM} \ \dots, R_i, \dots \ \mathsf{WHERE} \ \Theta \ \mathsf{AND} \ \mathsf{BLOOM\_CHECK}(F, \ \langle \mathcal{A} \rangle); \\ \mid\mid \ \mathsf{where} \ F = \ \mathsf{BLOOM\_GEN}(\mathsf{SELECT} \ \langle \mathcal{A} \rangle \ \mathsf{FROM} \ \dots, R_i, \dots \ \mathsf{WHERE} \ \Theta). \end{array}
```

Finally, note that Bloom filter conditions are not sargable and cannot be used to avoid full table scans. Evaluating them introduces overhead too. Therefore, I-Rex uses Bloom filtering only for "short-circuiting" evaluation of expensive WHERE clauses with subqueries. Also, if a Bloom filter returns too many false positives, the overhead of BLOOM_CHECK may outweigh the savings achieved by skipping subquery evaluation. Hence, we estimate the false positive rate of each constructed Bloom filter using its size (bits), number of hash functions, and the number of insertions. We inject the BLOOM_CHECK condition only if this rate is less than 50%.

4.2 Optimizing Tracing and Pinning

With optimized page fetches, users can freely move around a table with a paginated display. However, a debugging context displays multiple tables, and I-REX must coordinate the pages displayed across tables to show the end-to-end derivation from the current input combo to output, so that users can forward- or backward-trace (using pinning). We now discuss how to optimize these operations.

4.2.1 Forward Tracing. For forward tracing, we already have access to the input combo as well as their IIDs and row contents. Conceptually, to forward-trace through a particular stage, it suffices to determine the IID (say t) of the derivative row produced by this stage, if one exists. Then, given the target IID t, I-Rex searches the milestone table of the stage's result table for the page whose IID range contains t, and fetches this page. If the fetched page indeed contains t, we have successfully forward-traced through the stage; otherwise, we know that the input combo yields no result rows.

Determining the target IID in the first place is usually straightforward, thanks to the logical nature of our IIDs. For example, given the input combo $\langle s_2, f_1 \rangle$ in Figure 2, the target IID for the join & filter stage is simply the concatenation of the IIDs of s_2 and f_1 . In cases where we cannot easily determine the target IID, I-Rex can compute it using a query. For example, to forward-trace through the group stage, we need to compute the GROUP BY expression value, the leading component of the result row IID. In this running example, the GROUP BY expression is simply s.bar, so we could have read its value Edge directly from row s_2 . Otherwise, in general cases where the GROUP BY expression is complex (e.g., involving subqueries), I-Rex would generate a query to compute its value, e.g.:

```
|| SELECT s.bar -- arbitrary GROUP BY expression
|| FROM Serves s, Frequents f -- same as the original query block
|| WHERE (s.bar, s.beer) = ('Edge', 'Amstel') AND (f.bar, f.beer) = ('Ben', 'Edge'); -- use IID values to specify input combo
```

The cost of such queries is negligible because of the highly specific WHERE condition.

4.2.2 Pinning for Backward Tracing and Watchpointing. Without loss of generality, assume that a single derivative row is pinned.⁴ Our goal is to determine the first (lexicographically) input combo in the pinned subspace. If only one input combo contributes to the pinned derivative row, we can simply infer the former from the pinned row's IID (the same applies when backward-tracing from a stage to its preceding stage). For example, in Figure 2, if a user pins the first member row of g_1 in the group table, the IID of this row, (Edge, (s_2, f_1)), will reveal the input combo (s_2, f_1) .

If multiple input combos contribute to one pinned derivative row, the situation is more complicated. Such cases arise when backward-tracing from a pinned row in a post-grouping stage, e.g., the final stage of Figure 2. Here, we first infer the group, identified by its GROUP BY expression value (say g), from the IID of the pinned row. There are two cases. First, if there are no additional pins on the input rows, we simply need to determine the first input combo contributing to group g. To this end, I-Rex searches the milestone table of the group table for the last page whose min_iid is less than $(g, -\infty)$, and fetches that page. If the fetched page contains any member row of g, the IID of the first such row will reveal the desired input combo. Otherwise, it can be shown that the next page's min_iid must give the desired input combo. Hence, the cost of recovering the input combo is only one page fetch in the worst case.

Example 4.3. Considering Figure 2 again. Assuming a page size of 3 (rows) for all tables and o_1 is pinned, I-Rex can quickly determine that the first page in the group table (which contains all tuples from g_0 and one tuple from g_1) is the last page whose min_iid is smaller than $\langle Edge, -\infty \rangle$. It thus generates the following query to fetch the first page of the group table:

```
| SELECT (s.bar) -- group IID

| ((s.bar, s.beer), (f.drinker, f.bar)) -- input combo IID

| s.price * f.times -- sum_input

| FROM Serves s, Frequents f

| WHERE (...) -- original WHERE

| AND ... -- sargable filtering

| -- group IID and input combo IID filtering

| AND ((s.bar), ((s.bar, s.beer), (f.drinker, f.bar))) >= (('Apex'), (('Apex', 'Corona'), ('Amy', 'Apex')))

| AND ((s.bar), ((s.bar, s.beer), (f.drinker, f.bar))) < (('Edge'), (('Edge', 'Amstel'), ('Dan', 'Edge')))

| ORDER BY 1, 2; -- first order by group, then by input combo
```

After obtaining the following result, it can be easily identified that the last tuple in the page carries the first input combo IIDs that contribute to o_1 :

group IID	input combo IID	sum_input
(Apex)	((Apex, Corona), (Amy, Apex)))	1
(Apex)	((Apex, Dixie), (Amy, Apex)))	2
(Edge)	((Edge, Amstel), (Ben, Edge)))	16

Second, when there are additional pins on the input rows, I-Rex instead generates a query to determine the first input combo in the subspace further constrained by the additional pins. This query inherits the FROM and WHERE clauses from the original query, but further includes in WHERE conditions to restrict input rows by the pins and ensure that GROUP BY expression evaluates to g; it then computes the minimum input combo in SELECT.

Example 4.4. Continuing from Example 4.3. When s_2 is further pinned in addition to o_1 , to compute the first input combo in the subspace of the group table, I-Rex generates the following query:

```
| SELECT (s.bar) -- group IID
| ((s.bar, s.beer), (f.drinker, f.bar)) -- input combo IID
| FROM Serves s, Frequents f
| WHERE (...) -- original WHERE
| AND (s.bar, s.beer) = ('Edge', 'Amstel')
| ORDER BY 1, 2 -- first order by group, then by input combo
| LIMIT 1; -- only need first input combo
```

The above query locates $\langle s_2, f_1 \rangle$ as the first input combo, and I-Rex can now decide the page to fetch in the group table by a simple binary search using the group IID and input combo IID.

 $^{^4\}mathrm{Since}$ I-Rex enforces that there is only one derivative row per stage, it suffices to consider the derivative row in the earliest stage.

Recall that to support watchpointing, I-Rex automatically colors rows in each table relevant to the pinned subspace. The case where the pinned subspace contains only one input combo is straightforward: relevant rows are simply those in the input combo and those that are its derivatives. Otherwise, I-Rex extends the page-fetch query to return an additional column that indicates whether each row is relevant to the pinned subspace. The SELECT expression for this column is a Boolean expression testing whether the input rows conform to the pins and the GROUP BY expression evaluates to the same value as the pinned group.

4.3 System Implementation Details

Architecture. I-Rex has a client-server setup, with a Web frontend as the client and a middleware server between the client and the database server. In a common use case in education, many student users may run debugging sessions against one large, shared, readonly database. To ensure scalability and easy deployment, we adhere to a strictly stateless design, where neither the middleware nor the database server stores any session-specific information:

- When a user starts a debugging session, I-Rex middleware analyzes the query and decomposes it into a graph of query blocks in an internal representation. This representation specifies how each block is further broken down into stages, and contains metadata such as how to resolve external column references for correlated subqueries. The client caches this representation.
- When the user enters a debugging context (i.e., "calling" a query block), the client sends the cached representation of this block back to the middleware along with any parameter settings for the call. The middleware's debugging context initializer computes the milestone tables for all input tables of the debugging context and all result tables of its constituent stages, by querying the database (discussed below). The debugging context initializer also generates SQL query templates needed to support various debugging operations discussed earlier in this section. The client caches these milestone tables and SQL templates.
- When user carries out various operations in the debugging context, the client consults the cached milestone tables to instantiate required SQL queries according to the cached templates. It also caches the results of page-fetch queries, so repeated accesses to the same page, which can happen frequently during debugging, do not need recomputation. Cached pages can be evicted to make space for new ones.

Overall, note that debugging sessions leave no state on the middleware or the database. The middleware handles all complex SQL query analysis and rewrites, and the client simply needs to fill in the values of certain query parameters. The only cached data whose size depends on the database are the milestone tables. However, since there is only one milestone row per display page, and all columns are compact summaries of constant size, the milestone tables are orders of magnitude smaller than the corresponding tables. To make them even more scalable, milestones could be made hierarchical and refined on demand, but as shown later in Section 5, the current single-level design already works well.

Additional Details on Query Rewriting. As discussed earlier, all information needed for debugging can be computed by rewriting the original SQL query in some fashion. I-Rex performs most

query rewriting in its debugging context initializer. We have already shown how to generate queries for fetching pages (Section 4.1) and supporting other debugging operations (Section 4.2). As for computing milestones for each table in the debugging context, a single SQL query suffices, as illustrated by the following, which computes Table 1 (including the Bloom filters) for our running example:

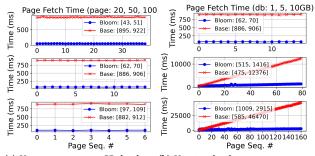
```
| WITH tmp(seq, iid, s_bar, s_beer, f_drinker, f_bar) AS (
| SELECT ROW_NUMBER() OVER (ORDER BY s.bar, s.beer, f.drinker, f.bar) - 1, --
| result row sequence number when sorted by IID ((s.bar, s.beer), (f.drinker, f.bar)), -- IID |
| s.bar, s.beer, f.drinker, f.bar -- relevant for sargable & Bloom filtering |
| FROM Serves s, Frequents f WHERE (...) -- same as original query |
| ) |
| SELECT MIN_IID(iid), -- per-page minimum IID |
| -- per-page range bounds for sargable fitering: |
| ARRAY[MIN(s_bar), MAX(s_bar)], ARRAY[MIN(s_beer), MAX(s_beer)], |
| ARRAY[MIN(f_drinker), MAX(f_drinker)], ARRAY[MIN(f_bar), MAX(f_bar)], |
| -- per-page Bloom filter: |
| BLOOM_GEN(p_partkey) |
| FROM tmp GROUP BY seq / page_size ORDER BY seq / page_size; |
| -- page_size is the number of rows per page
```

After generating the SQL queries as discussed above and earlier, I-Rex further applies several rewrite optimizations. First, if a scalar subquery contains no external column references, the debugging context initializer will simply precompute its result and replace the uses of this subqueries by its result. Second, for any sargable condition injected into a query, we consider pushing it down further into a subquery. Such cases often arise when, for example, we identify a range bound on some indexed column, and this column (or another column equated to it by WHERE) is referenced by a subquery as an external column; here, we inject the range bound into the subquery as well. Third, if the query's FROM contains a subquery or table defined by WITH, we check whether the injected conditions imply an equality or range condition the IID of the input table. If yes, we consult the milestones of the input table to construct sargable filters to further inject into the subquery defining the input table. We call this last optimization recursive pushdown. Finally, pushdown through outer joins, which is especially tricky, is discussed in Appendix B.

5 PERFORMANCE EXPERIMENTS

We conduct experiments to evaluate the performance and scalability of I-Rex. We focus on evaluating page-fetch queries (Section 4.1) and milestone computation (Section 4.3), as they are the most expensive queries that I-Rex uses; other operations (Section 4.2) either use page-fetch queries or relatively cheap queries with highly selective conditions. The baseline for fetching pages is to use SQL OFFSET and LIMIT. We enable various pagination optimizations in I-Rex to evaluate their respective benefits. IID-based filtering is always enabled (for correctness). Section 5.1 enables Bloom filtering but not other optimizations, while Section 5.2 enables sargable filtering but not others. Finally, Section 5.3 enables all optimizations, and also evaluates the overhead of milestone computation.

We use the TPC-H benchmark [10] and generate three database instances of sizes 1GB (benchmark default), 5GB, and 10GB. In addition to the default indexes on the primary keys, we also create a reasonable set of secondary indexes (details in Appendix C) that simulate typical usage. For Sections 5.1 and 5.2, we show one query for each, where the respective optimization is applicable and can be



(a) Varying page size; 1GB database. (b) Varying database size; 50-row pages. Figure 5: Bloom filtering vs. baseline: time to fetch each page. $[\cdot, \cdot]$ in legend shows min/max page fetch times.

best evaluated; for the general evaluation in Section 5.3, we show results for all 22 benchmark queries.

All experiments were done locally on a 64-bit Ubuntu 22.04 LTS server with Intel(R) Xeon(R) Gold 6138 CPU @ 2.00GHz, 64GB RAM, and 256GB disk space. We used PostgreSQL [59] (version 16) and only changed the following configurations: we turned off parallelism for simplier and fair interpretability of results; we set work_mem to 128MB and shared_buffers to 8GB.

5.1 Effectiveness of Bloom Filtering

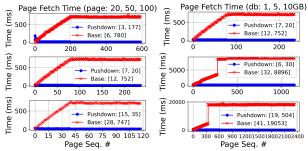
This experimental setup uses a variant of TPC-H Q2:

As discussed in Section 4.1, I-Rex precomputes a Bloom filter for the p_partkey values for input rows that contribute to each result page, and when fetching a page, uses the Bloom filter to short-circuit the evaluation of the rest of WHERE containing an expensive correlated subquery. However, the bloom filter is only used for membership checking if the false positive rate is less than 50%.

By default, we set the number of Bloom filter bits to m=1024; we conservatively estimate the number of unique p_partkey in each page (denoted by n) as the page size; accordingly, we set the number of Bloom filter hash functions to $\frac{m}{n} \times \ln 2$.

We conduct two sets of experiments. First, we fix the database size to 1GB and vary the page size. Second, we fix the page size to 50 and vary the database size. We compare page-fetch queries with Bloom filtering with the baseline using OFFSET and LIMIT. We collect the execution times reported by the EXPLAIN ANALYZE command for all queries and show them in Figure 5.

Overall, the results show that Bloom filtering is very effective for Q2. When the database size is relatively small (Figure 5a), the baseline consistently takes around 900ms to reproduce a page, because its execution cost is dominated by the computation of the entire result and sorting them first; in contrast, Bloom filtering takes 43 to 109ms, with larger pages requiring more time. Under larger database sizes (Figure 5b), baseline switches to a different plan whose cost grows linearly with the starting position of the page fetch, eventually matching the cost of executing the entire query when



(a) Varying page size; 1GB database. (b) Varying database size; 50-row pages. Figure 6: Sargable filtering vs. baseline: time to fetch each page. [·,·] in legend shows min/max page fetch times.

fetching pages near the tail; Bloom filtering performance remains scalable and depends much less on the fetch position, saving as much as 11s ($8.7\times$ speedup) and 43s ($15.9\times$ speedup) for 5GB and 10GB databases, respectively.

5.2 Effectiveness of Sargable Filtering

This setup uses the joined & filtered table for benchmark Q7:

We create sargable range filters for all index columns in the input tables based on the precomputed milestones, but only if the ranges cover no more than 30% of the domain, as discussed in Section 4.1. We run two sets of experiments similar to those for Bloom filtering, with results shown in Figure 6. Overall, we observe that the baseline using OFFSET and LIMIT performs progressively worse when it fetches pages later in the result table, until its running time plateaus when the plans switch to essentially computing and sorting the entire result; in contrast, sargable filtering performs well across all pages regardless of their position, and its advantage over the baseline widens dramatically toward later pages. With a 1GB database (Figure 6a), baseline can take up to 780ms to fetch a page, while sargable filtering takes no more than 180ms (4.3× speedup). Fixing the page size at 50 and using larger databases (Figure 6b), sargable filtering's benefit is even greater. For the 10GB database, the baseline takes about 19s to fetch a page positioned at 1/6-th of the entire result or later, while sargable filtering takes about 0.5s (38× speedup) in the worst case.

5.3 General Evaluation

For general evaluation, we apply all I-Rex optimizations to all TPC-H queries, and compare the execution times of the resulting page-fetch queries with those of the baseline approach. IID-based and sargable filtering can be applied to all queries, while Bloom filtering is only applicable to Q4, Q16, Q18, and Q20–22. Because of limited space, we only show in Table 2 the results for the joined & filtered table of Q18, which is the most expensive query in our experiments; remaining results are presented in Appendix C. The results generally echo the findings from the experiments on Bloom/sargable filtering, and confirm the benefit of combining optimizations. Specifically in Table 2, I-Rex performs no worse (and sometimes

	1GB (ms)		1GB (ms) 5GB (ms)			10GB	(ms)
Page	I-Rex	Baseline	I-Rex	Baseline	I-Rex	Baseline	
head	3,919.89	8,801.75	21,717.035	75,903.361	52,355.55	158,664.23	
middle	3,919.76	12,270.41	24,999.351	91,594.34	47,736.515	181,742.56	
tail	4,423.78	15,739.07	21,717.478	107,285.319	49,884.912	204,820.89	

Table 2: I-Rex vs. baseline: time to fetch a page in the joined & filtered table of Q18; 50-row pages and varying database size. Here, head refers to the first query while tail refers to the second to the last (as the last page sometimes is not full).

	Milestone	Query	Original	Query		
Q18	Exec. time (ms) Output (MB)		Q18 Exec. time (ms)		Exec. time (ms)	Output (MB)
joined & filtered	22,619.063	52	16,847.586	1272		
group	18,208.509	9	18,368.903	70		
output	19,340.111	9	20,751.758	75		

Table 3: Milestone vs. original queries: execution time and output size; 50-row pages and 1GB database.

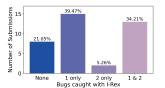
better) than the baseline for pages at the beginning of the results, and significantly better for later pages, with $3 \times$ to $5 \times$ speedup.

Finally, we evaluate the overhead of debugging context initialization, which is dominated by the cost of running milestone queries (such as the one in Section 4.3). We compare their costs with those of simply computing the entire results of the corresponding original query blocks. Because of limited space, we only show in Table 3 the results for the three most expensive milestone/original query pairs, with a 1GB database and 50-row pages; the remaining results are in Appendix C. All three pairs come from Q18's stages. Since milestone queries conceptually summarize the output of the original queries, we do not expect them to run faster than the latter. As Table 3 shows, their performance is in fact comparable to the original queries. Recall from earlier experiments that baseline pagefetch queries often cost as much as the original queries, so this observation implies that I-Rex can benefit from milestone-enabled optimizations for many page-fetch queries by paying only a onetime overhead equivalent to a single baseline page-fetch query. Finally, we note that the execution times reported are taken from EXPLAIN ANALYZE, which only measures the time spent in executing the query but not transmitting its result. We intentionally chose to exclude the latter time, because the outputs from the original queries can be too overwhelmingly large to transmit. For example, printing the entirety of Q18's joined & filtered table took more than an hour for a psql client running on the database server console. In contrast, as Table 3 shows, milestone queries return much smaller results, which are feasible to transmit to and handle by the client. The full results in Appendix C lead to the same conclusions.

6 USER STUDY

We conducted a user study in an undergraduate database course to evaluate the overall effectiveness of I-Rex on two aspects: 1) whether I-Rex helps users catch more logical bugs in SQL queries, and 2) whether I-Rex reduces the time to find such bugs.

Participants. We recruited 237 students from the course, who had just become familiar with SQL at the time of the user study. The participation was voluntary except for the incentive of an extra exercise to practice debugging skills. We considered the possibility of recruiting participants from other sources (e.g., Amazon Mechanical Turk), but decided against doing so because it was hard to quantify and control participants' SQL familiarity to a similar level. Since SQL familiarity has a significant impact on debugging time,



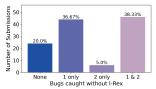


Figure 7: Bugs caught (out of two) for P1, using I-Rex vs. not.

the lack of control would make results difficult to interpret. The demanding nature of the tasks (as evidenced by the long debugging times measured, to be reported later) also makes quality control difficult for asynchronous and remote completion.

Preparation and Setup. The study was conducted during two 75minute discussion sessions in consecutive weeks. In the first session, students were given a tutorial on I-Rex and informed about the format of the survey-style quiz, which contained two SQL debugging problems P1 and P2. After the first discussion, I-Rex is made public for students to get familiar with. In the second session, students completed the quiz synchronously in a proctored environment, where they were asked not to discuss with classmates. For each problem in the quiz, students were provided a problem statement, an incorrect query, its incorrect output, and what the correct output should be; the details are in Appendix D. The database instance in the user study, on which both the incorrect and expected outputs were based, had been installed and worked on by students on their laptops early in the course. We also prepared a public pgAdmin Web interface for students to use during the study in case any had trouble accessing their own instances, thereby mitigating potential impact of setup issues on the measured debugging times.

To create treatment and control groups, students received the two problems in a random order. For the first problem they received, they were free to use any tool of their choice (e.g., Gradescope autograder, psql console, pgAdmin Web interface) except I-Rex. For the second problem, I-Rex was made available along with other tools; students had the option to use or not use I-Rex, and were asked to indicate it in the survey. For each problem, students were to describe the bugs they found in a free-response text box. P1 had two bugs and Q2 had three, though the students were not told how many. While students self-paced, they were recommended to spend 15-20 minutes on each problem. They were not allowed to move on to the second problem until they finished the first.

Results and Analysis. We collected the time it took students to solve each problem, whether they chose to use I-Rex, and the bugs they found. Of 237 students, 140 completed both problems and provided legitimate answers. Therefore, we based our analysis on these 140 responses. For the first problem, which must be completed without I-Rex, 73 students received P1, and 67 received P2. For the second problem, where using I-Rex was an option, 73 students received P2, and 36 of them chose not to use I-Rex; 67 students received P1, and 29 of them chose not to use I-Rex. Therefore, for P1, we have 38 submissions using I-Rex, and 102 not using I-Rex; for P2, we have 37 submissions using I-Rex, and 103 not.

We manually reviewed each response and checked whether the student identified the bugs correctly. Figure 7 shows the fraction of the submissions that correctly identified each possible subset of the bugs for P1, with (left) or without (right) help from I-Rex; Figure 8 does the same for P2. While the total submission numbers differ

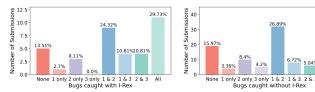


Figure 8: Bugs caught (out of three) for P2, using I-Rex vs. not.

Problem	# responses	Avg. time (s)	Avg. bugs found
P1 w/ I-Rex	38	771.52	1.13 / 2
P1 w/o I-Rex	102	1,235.66	1.18 / 2
P2 w/ I-Rex	37	1,147.04	1.91 / 3
P2 w/o I-Rex	103	1,657.53	1.85 / 3

Table 4: Average debugging time and bugs caught per problem.

between using/not using I-Rex, the distributions (fractions for possible subsets) are similar. Indeed, use of I-Rex had no discernable impact on the average number of bugs identified, as shown later in the last column of Table 4. While I-Rex did not seem to help students find more bugs, the comparison of debugging times, summarized in Table 4, reveals a major advantage of I-Rex. For P1, use of I-Rex reduces the average debugging time from 21 minutes to 13, a 38% reduction; for P2, I-Rex reduces the time from 28 minutes to 19, again by more than 30%. Combined with the earlier observation that the distributions of bugs correctly found are similar, we conclude that the I-Rex significantly improves students' efficiency in finding bugs without compromising accuracy. Had time been more constrained, use of I-Rex would result in more bugs found.

Remark. A counterargument to our conclusion might be that students might rush to get out of class or have just "warmed up" their debugging skills, so they generally spent less time on the second problem received. However, even if we restrict the scope of time comparison to the second problem received only, we can still see that I-Rex offers improvements. Of the 102 submissions of "Q1 w/o I-Rex", 29 of them had I-Rex as an option but did not use it, and their average debugging time was 1,029 seconds, compared with 771.52 seconds with I-Rex. Of the 103 submissions of "Q2 w/o I-Rex", 36 of them had I-Rex as an option but did not use it, and their average was 1,310 seconds, compared with 1,147.04 seconds with I-Rex.

7 RELATED WORK

Earlier versions of I-Rex, previously demonstrated [43, 53], precomputed and stored all debugging information in the client, which did not scale. The version described in this paper has refined existing debugging features and introduced new ones, and most importantly, added support for scalability, which requires a redesign of the system and development of new optimization techniques.

Finding Logical Errors in Queries. Work toward finding logical errors in queries can be classified into two categories. The first category [23, 24, 26–28, 33, 36, 42, 54, 60, 68] assumes knowledge of a correct reference query and uses it to help identify errors in an incorrect query. XData [24] checks the correctness of a query by running the query on self-generated testing datasets. Cosette [26–28], SQL-Solver [33], and QED [68] test query equivalence using constraint solvers and theorem provers. RATest [54] and c-instances [36] aim at constructing small and illustrative database instances to show

the differences between two queries. [23] develops a grading system that canonicalizes queries with rewrite rules and then decides query similarity using edit distance between the resulting logical plans. SQLRepair [60] and QR-Hint [42] focus on fixing the wrong query by proposing syntactical edits. I-Rex differs from this line of work in that it assumes no knowledge of the reference query. Dropping this assumption fundamentally changes the problem and makes the solution applicable in more settings.

The second category of work, including I-Rex, helps users debug a query without a given reference query, using a myriad of approaches. Qex [67] generates input relations and parameter values for unit-testing parameterized SQL queries. SQLLint [13-15] looks for patterns in the query indicative of common semantic errors and alerts users to them. Interactive query builders and query visualizers [1-5, 22, 40, 47, 52, 55] use diagrams to gain more intuitive understanding of query logic, hence helping with debugging. Frameworks for data exploration [5, 7, 32, 50] use signals such as query history and user feedback on query results to suggest queries, which may serve as an approach to debugging. A line of work known as algorithmic debugging [18, 19] guides users through a series of questions on whether intermediate query steps produce intended results, to locate buggy steps. Also useful to debugging is explaining to users what queries do in natural language, which has been researched over the years [16, 35, 46, 49, 64, 69]. While the systems discussed above provide complementary approaches to debugging, none supports debugging by tracing through query execution, as I-Rex and most GPL debuggers do.

Two systems in this second category, DESQL [41] and Habitat [31, 39], are the closest to I-Rex in terms of approach, as they also recognize the need to debug queries according to how they are written. DESQL [41] is a debugger for SQL in Spark, which decomposes the query into subqueries and helps users examine subqueries' output. While DESQL focuses on scalability like I-Rex, its optimizations primarily concern Spark instead of traditional database systems. Also, unlike I-Rex, DESQL does not support correlated subqueries or row-level tracing, and debugging commences only after the query fully executes. Habitat [31, 39] allows users to mark SQL subexpressions and inspect intermediate results side by side, connecting related result rows. It also lets users filter these results in order to focus on a subset of interest. However, Habitat differs from I-Rex in important ways. First, focusing on scalability, I-Rex avoids computing or showing full results of queries and subqueries, while Habitat executes its queries in full and shows their results in bulk. Although Habitat's focus filters can restrict these queries, they need to be defined manually and explicitly; in contrast, I-Rex's pinning and automatic pagination are intuitive and demand less user effort and expertise, and I-Rex has a suite of rewrite optimizations designed to improve query efficiency. Second, I-Rex and Habitat have different conceptual designs: I-Rex defines its canonical query execution to be row-oriented and reproducible (including row ordering), while Habitat presents a set-oriented view of SQL execution and allows more free-form exploration among query subexpressions. For example, consider debugging a correlated subquery. I-Rex lets the user "step into" its execution with specific settings of its external column references supplied by the "caller" (its enclosing query block), which is intuitive for GPL users. On the other hand, Habitat shows an intermediate table showing

the binding values and the corresponding subquery evaluation results side by side, analogous to the result of a decorrelated subquery. Users with different background and SQL expertise levels may prefer one design over the other; we believe I-Rex offers an attractive alternative.

Other Areas of Related Work. Several areas of research are related to some of the ideas and techniques used by I-Rex. First, data provenance [11, 17, 25, 38, 44] provides a natural way to trace query execution, explaining why and how a particular output is or is not produced. Many previous works [6, 8, 9, 29, 30, 37, 45, 48, 51, 61] have focused on making provenance capture a built-in feature in database systems. In particular, [56] proposes techniques for capturing provenance by rewriting SQL queries, just as I-Rex uses query rewriting to help support tracing and other debugging operations. However, [56] captures full provenance information for all query results; in contrast, for scalability and interactivity, I-Rex avoids materializing all provenance expressions, or even the entirety of one large provenance expression (e.g., for an aggregate result row), opting to compute pieces of provenance on demand instead.

Second, efficient pagination of query results has been studied in query processing and optimization literature. Recent advances have been made on direct access to query answers [20, 21, 34, 66], but their techniques require specialized indexes and apply only to conjunctive queries, less general than what I-Rex supports. Work on data skipping and predicate pushdown [57, 58, 65, 70] also requires significant changes to database system internals, but I-Rex chooses to leverage existing database systems for efficient pagination. The debugging use case and the stateless server design of I-Rex also motivate unique optimizations, such as client-cached milestones.

8 CONCLUSION AND FUTURE WORK

In this paper we have presented I-Rex, a novel interactive debugger for SQL that is easy to deploy on existing database systems and scales to massive databases. Conceptually, I-Rex executes the query being debugged in a canonical fashion that faithfully follows how the query is written, and lets users examine the execution using a rich set of features including but not limited to those found in GPL debuggers. I-Rex supports efficient exploration of any arbitrary point of execution without fully executing the underlying query. It does so by fully leverarging the database system: it formulates the selective computation of the debugging information around the point of interest as SQL queries, and employs materialization and query rewrite strategies to ensure their execution efficiency. Our performance experiments and user study demonstrate the efficiency and effectiveness of I-Rex.

There are multiple directions for future work. First, we can extend I-Rex to cover the SQL constructs that we do not already support, as mentioned at the beginning of Section 3. Second, it is worth investigating milestone designs beyond single ranges and Bloom filters used in Section 4.1. Third, there is no reason to restrict pins to input and derivative rows; we can support user-defined conditions as well. Finally, we plan to extend I-Rex so that it can isolate and help debug runtime SQL errors (such as division by zero), for which database systems usally provide uninformative feedback.

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A ADDITIONAL DETAILS ON DEBUGGING PARADIGM

A.1 Set/Bag Operation Blocks

A SQL set/bag operation block has the form

 $\mid\mid Q_R$ UNION|INTERSECT|EXCEPT [ALL] Q_S

where Q_R and Q_S are subqueries. Let R and S denote the tables returned by Q_R and Q_S , respectively. The canonical execution procedure of this block consists of two stages: a sort stage that sorts both R and S by their row contents and a final output stage that merges them to produce the result table. To determine the order for the sort stage, we pick a particular ordering of all columns, preferring to reuse *R*'s order (dictated by its IID) as much as possible. Further, to ensure a stable sort in the case of duplicates, we append each input table's IID to the column ordering as needed when sorting the table. The synthesized sort result IIDs have the same format. For instance, suppose that the IID for $R(A_1, A_2, A_3)$ is (A_3, A_1) , which implies that R is free of duplicates. In this case, R is already sorted by $(A_3, A_1, A_2, IID(R))$, and we would sort $S(B_1, B_2, B_3)$ accordingly by $(B_3, B_1, B_2, IID(S))$, assuming that S may contain duplicates. As another example, suppose that both input tables come from unsorted base tables with duplicates, and these tables' internal row ids serve as the IIDs. In this case, we would sort both tables by their columns, in order, followed by their respective IIDs.

The final output stage merges the two sorted tables. The output row IID always contains the value of columns in the same order as the sort stage IID, followed by a Boolean flag indicating the source input table (0 for R and 1 for S) and a sequence number (0-based) indicating its position among duplicates in the source input table. Depending on the set/bag operation involved, the stage's behavior and the last two components of the IID are defined differently. In the following, let t denote the content of a row in either R or S, and R[t] and S[r] the lists of duplicate rows in R and S (respectively) with this content.

- INTERSECT: We consider only the case when R[t] ≠ ∅, and output only the first row of R[t], with the last two components of the IID set to (0,0).
- EXCEPT: We consider only the case when R[t] ≠ Ø. Only if S[t] = Ø, we output the first row of R[t], with the last two components of the IID set to (0,0).
- UNION: If $R[t] \neq \emptyset$, we output the first row of R[t], with the last two components of the IID set to (0,0). otherwise, we output the

first row of S[t], with the last two components of the IID set to (1.0).

- INTERSECT ALL: Let m = min{|R[t]|, |S[t]|}. We output the first m rows of R[t], with the last two components of the IID set to (0, 0), ..., (0, m − 1).
- EXCEPT ALL: Let m = |R[t]| |S[t]|. Only if m > 0, we output the first m rows of R[t], with the last two components of the IID set to $(0,0), \ldots, (0,m-1)$.
- UNION ALL: Let m = |R[t]| + |S[t]|. We output all rows of R[t] followed by all rows of S[t], with the last two components of the IID set to $(0,0),\ldots,(0,|R[t]|-1)$ and then $(1,0),\ldots,(1,|S[t]-1|)$.

The input ("combo" would be somewhat a misnomer here) space for the debugging context is the concatenation of the rows of *R* followed by those of *S*. Hence, from the two input tables, only one row can be highlighted as currently active, and no input pinning is allowed because it is not useful in this context. Although the definitions above associate each output row with a particular input row, the I-Rex interface hides this detail, so users will still observe the SQL semantics. To be more specific, given an input row, we define its derivative "row" (if one exists) in the final output table as the group of all duplicate rows, which can only be pinned/unpinned together. The interface also provides an explanation for the number of duplicates or the absence of output rows for the given input row.

A.2 Join Expressions

I-Rex treats explicit JOIN expressions in FROM essentially as subqueries. Hence, each such expression gives rise to a separate debugging context with two input tables (base or derived). Inner joins can be handled in the same way as a more general SELECT block (Section 3.1). We focus on outer joins here. Let R and S denote the two input tables. We augment the input combo space by adding a special IID \bot to each input table whose side of the output can be padded with NULLs. Intuitively, \bot stands for "no row" from that input table, and behaves in the I-Rex interface as a special last row of the table. For example, for S in R LEFT JOIN S, we add \bot to indicate "no row from S." If a row $r \in R$ joins with no row from S, the left outerjoin result should contain a row for r padded with NULLs in S columns; its IID would be (r, \bot) .

When ordering by IIDs, \bot should be considered last in value. Internally, I-Rex represents \bot in SQL using an IID whose components are all NULLs, assuming input rows do not have NULLs for all their IID components. When generating queries involving comparison with IIDs possibly containing NULLs, however, we need to replace the ROW(...) comparisons with special code because SQL comparisons involving NULLs always yield the UNKNOWN truth value. For example, instead of generating ROW(A, B)>=ROW(1, 2) when B can be NULL, we would generate

```
| | A>1 OR (A=1 AND (B IS NULL OR B>=2))
```

Selection of the active input combo and stepping work the same way as in SELECT (Section 3.1), except when the input combo involves a \bot , I-Rex show an explanation of why a NULL-padded result row is or is not produced, instead of the filter expression tree.

B ADDITIONAL DETAILS ON DEBUGGING PARADIGM

B.1 Proof of Proposition 4.2

PROOF. First note that when $\Theta \Leftrightarrow \bot$ (i.e., Θ is equivalent to logical false), both queries are obviously equivalent as they return empty results on all possible database instances regardless of the evaluation of BLOOM_CHECK. Therefore, we now proceed to prove that both queries are equivalent when at least Q_1 returns a non-empty result (i.e., Θ is not equivalent to \bot).

Now assuming Q_1 and Q_2 are not equivalent, then there must exist input tables $\{R_i'\}$ where Q_1,Q_2 return results \mathcal{V}_1 and \mathcal{V}_2 respectively, and a tuple $e' \in \mathcal{V}_1$ but $e' \notin \mathcal{V}_2$ (it cannot happen vice versa as $\Theta \Leftarrow \Theta$ AND BLOOM_CHECK(F, $\langle \mathcal{A} \rangle$)), thus there must exist a subset \mathcal{A}' from e' such that BLOOM_CHECK(F, $\langle e'[\mathcal{A}'] \rangle$) is evaluated to false. Observing that F is obtained from BLOOM_CHECK($\mathcal{V}_1[\mathcal{A}']$) and $e' \in \mathcal{V}_1$, this implies BLOOM_CHECK(F, $\langle e'[\mathcal{A}'] \rangle$) must be true as Bloom filter returns no false negative. Therefore, e' must also be in \mathcal{V}_2 and $\{R_i'\}$ does not exist. As a result, Q_1 and Q_2 must be equivalent.

B.2 Pushdown through Outerjoins

Consider a page-fetch query that I-Rex generates for a full outer join debugging context, which has the form:

```
|| SELECT ROW(R.K, S.K) AS _iid
|| FROM R FULL JOIN S ON R.A = S.B
|| WHERE \Theta(R, S);
```

Here, Θ is condition based on the IID range of the requested page, which constrains R and S. Efficient execution of this query requires pushing down filters inferred from Θ to R and S. Unfortunately, such pushdowns are not always safe through outer joins. For example, suppose that the requested page is the last one, and its IID range implies the filter on R to be R.K IS NULL OR R.K>=100. Further suppose that some $s \in S$ joins with a single row $r \in R$ with R.K<100. The above page-fetch query should not return any output for s, since $\langle r,s \rangle$ does not belong to the requested page and hence fails the final WHERE. However, if we push the filter on R to below the outer join, the outer join will return a row containing s and R columns padded with NULLs, which passes the final WHERE.

To avoid the above issue and still enable pushdown, I-Rex first computes the inner join between R and S with pushdown. Then, only if the number of returned rows falls below the desired number on the requested page, which can be determined from the milestone table and should happen rarely, we issue additional queries to find rows in the outer join result but not in the inner.

C ADDITIONAL EXPERIMENTAL RESULTS

We present the remaining experiment results over TPC-H benchmark.

For each table in the TPC-H schema, we have the following indexes (all indexes are btree indexes in PostgreSQL):

- customer
 - primary index: c_custkey
 - secondary indexes: None
- lineitem
 - primary index: (l_orderkey, l_linenumber)
 - secondary indexes: l_partkey, l_suppkey, l_shipdate

 $^{^5\}mathrm{In}$ the extremely rare case when this assumption is violated, we choose an unused value from each domain instead.

- nation
 - primary index: n_nationkey
 - secondary indexes: n_name, n_regionkey
- orders
 - primary index: o_orderkey
 - secondary indexes: o custkey, o orderdate
- part
 - primary index: p_partkey
 - secondary indexes: None
- partsupp
 - primary index: (ps_partkey, ps_suppkey)
 - secondary indexes: ps_suppkey
- region
 - primary index: r_regionkey
 - secondary indexes: None
- supplier
 - primary index: s_suppkey
 - secondary indexes: s_name, s_phone

We ran experiments for three different page size: 50, 100 and 200 for all tables (stages) in all TPC-H queries. For each table, we prepared three queries: milestone query, page query and table query and thus collecting the following data over all testing instances (i.e., 1GB, 5GB and 10GB):

 The execution time and output size of the milstone query and the table query. The execution time of the page query and baseline query (by rewritting the table query with OFFSET and LIMIT) for retrieving the first page ("head"), middle page ("mid") and the second last ("tail") page.

Since each query potentially contains multiple query blocks and subsequently multiple tables, we present the statistics for the largest table (measured in MB) to compute for each query. For page size 50, 100 and 200, the experiment results are shown in Table 5, Table 6 and Table 7 respectively.

In summary, we make the following conclusions:

- The milestone queries usually run slower than the table queries, but with acceptable delays since they are run at the beginning of the debugging session without affecting debugging operations later. In some cases, the milestone queries run faster than the table queries. On the other hand, the output sizes of the milestone queries are always smaller than those of the table queires by a rough factor of the page size.
- The optimization for page query almost always outperforms the
 baseline, and differences between the execution time grows as
 the database size grows, especially for "mid" and "tail" pages.
 The optimizations are sensitive to page size but insensitive to the
 database size. There are only few cases where the optimizations
 "over-hint" the PosgreSQL optimizer and cause the execution
 time to be roughly the same as the baseline.

		10	BB	50	GB	100	GB
Query	Page	Opt.	Base	Opt.	Base	Opt.	Base
	head	0.153	0.057	0.169	0.143	0.065	0.085
Q1	mid	0.177	447.618	0.319	15298.829	0.107	30754.125
~	tail	0.146	895.18	0.17	30597.515	0.05	61508.166
	head	21.595	298.538	21.056	2438.586	22.218	5015.589
Q2	mid	23.268	330.474	20.483	2581.97	22.005	5333.441
22	tail	22.163	362.41	22.166	2725.353	21.301	5651.293
	head	1.473	4.414	10.946	72.055	11.53	77.334
Q3							
Q3	mid	1.04	368.188	13.097	6661.215	12.327	59183.467
	tail	0.881	731.962	12.418	13250.375	16.014	118243.911
	head	0.558	0.469	0.539	1.069	8.15	2.834
Q4	mid	0.604	123.425	0.527	637.045	4.283	10776.948
	tail	0.572	246.381	1.418	1265.02	2.525	21551.063
	head	15.559	10.106	13.385	18.279	211.732	146.347
Q5	mid	10.107	1629.932	7.337	13900.534	98.028	41247.203
	tail	6.284	3249.758	7.046	27782.79	104.97	81004.647
	head	0.507	0.252	0.845	0.661	1.347	0.659
Q6	mid	0.377	289.018	0.965	1650.336	2.917	39943.432
~	tail	0.279	576.43	1.685	3300.011	1.049	79886.205
	head	21.327	18.308	33.371	29.567	471.423	64.334
Q7	mid	16.771	362.32	28.868	4240.504	423.37	19761.341
	tail	19.863	704.532	20.394	8451.441	423.913	39458.348
	head	13.442	8.619	13.993	19.104	131.611	22.151
08	mid	10.776	1911.543	16.478	8284.359	98.392	25365.045
Q8	tail	13.79	3814.467	14.709	16549.614	131.145	50707.939
	head	1.416	381.569	15.264	6277.133	16.968	29119.466
Q9	mid	1.8	1675.868	22.93	13832.928	12.232	45990.497
	tail	1.119	2950.868	15.102	21388.724	10.875	62861.529
	head	1.219	1.874	4.67	4.74	7.683	2.989
Q10	mid	1.036	1061.645	5.087	11725.928	7.036	15279.263
	tail	1.04	2069.06	4.742	23447.117	4.76	30555.537
Q11	head	30.55	7.21	197.92	6.68	372.715	10.575
	mid	28.616	40.924	184.97	283.856	16.976	511.313
	tail	26.376	74.638	169.896	561.033	342.103	1012.051
	head	1.123	0.855	4.247	1.028	2.328	1.084
Q12	mid	2.353	492.485	2.906	8910.229	1.056	9485.278
~	tail	1.248	984.115	2.529	17819.43	0.82	18969,472
	head	0.231	0.168	0.222	0.186	0.2	0.192
Q13	mid	0.223	493.355	0.199	2686.416	0.24	5650.011
QIJ	tail	0.194	986.542	0.133	5372.647	0.207	11299.831
		6.304	1.99	40.092	2.22		
014	head					6.957	3.921
Q14	mid	5.755	139.76	40.416	849.248	4.337	1894.417
	tail	5.629	277.53	38.635	1696.275	3.477	3784.913
	head	1.138	0.297	0.405	0.814	1.956	0.267
Q15	mid	1.306	212.734	0.358	1314.475	3.711	2494.516
	tail	0.732	425.17	1.258	2628.135	2.244	4988.766
	head	2.615	2.438	13.866	10.562	26.847	21.011
Q16	mid	2.632	210.645	10.262	1230.19	23.322	2471.066
ļ	tail	2.395	418.852	9.427	2449.819	21.865	4921.12
	head	5.2	1.96	7.37	1.955	5.8	24.278
Q17	mid	2.414	1282.928	5.231	13873.386	5.965	31301.815
~	tail	2.559	2563.897	5.067	27744.817	5.836	62579.351
	head	3919.892	8801.745	21717.035	75903.361	52355.55	165931.984
Q18	mid	3919.762	12270.408	24999.351	91594.34	47736.515	188145.545
~-0	tail	4423.777	15739.07	21717.478	107285.319	49884.912	210359.105
	head	63.219	50.042	73.492	69.801	700.864	71.948
010	mid	60.963	97.058	73.492	422.959	102.82	680.822
Q19		66.037	144.074	75.354	771.506	85.536	1289.697
	tail						
000	head	0.141	0.059	0.154	0.053	0.264	0.498
Q20	mid	0.118	90.876	0.129	463.991	0.827	1136.924
	tail	0.124	181.692	0.792	927.93	0.844	2273.349
	head	21.59	833.851	53.231	21584.818	419.195	52731.23
Q21	mid	16.303	841.546	54.607	21390.896	357.162	52110.334
	tail	18.113	837.46	53.475	21254.656	518.892	51489.439
				4 680	000 461	0.014	641.022
	head	0.824	73.643	1.658	323.461	3.814	041.022
Q22	head mid	0.824 1.046	73.643 107.034	1.658	503.032	3.814	998.173 1355.323

Query DB size Milestone Table Milestone Table Q1 5 66757.254 34169.326 135.583 3809.747 Q1 5 66757.254 34169.326 1355.853 3809.747 Q2 5 1311.686 3561.809 0.031 0.647 Q3 5 7443.149 43601.631 1.056 45.735 Q4 5 7955.258 2601.872 2.145 92.932 Q4 5 1955.258 2601.872 1.899 31.649 Q5 5 7443.149 43601.631 1.056 45.735 Q4 5 1955.258 2601.872 1.899 31.649 Q5 1 2723.034 3953.535 0.366 30.979 Q5 5 13759.176 30937.301 4.675 154.836 Q6 5 5589.597 2505.285 8951 218.804 Q6 5 5589.597 2505.285 8951 <td< th=""><th></th><th></th><th colspan="2">Time (ms)</th><th colspan="3">Output Size (MB)</th></td<>			Time (ms)		Output Size (MB)		
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	O22						
1 10 1331.320 2012.412 0.436 4.009	2	10	1551.326	2012.412	0.458	4.069	

(a) Optimization vs. Baseline for Page Query Execution Time

(b) Milstone Query vs. Table Query

Table 5: Experiment results for Page Size 50. Shorter time and smaller sizes are highlighted.

		10	GB	5GB		10GB	
Query	Page	Opt.	Base	Opt.	Base	Opt.	Base
	head	0.092	0.157	0.095	0.106	0.258	0.089
Q1	mid	0.089	450.644	0.102	16320.778	0.405	30908.903
-	tail	0.102	901.132	0.081	32641.45	0.233	61817.717
	head	44.592	318.82	46.69	2580.597	45.526	5048.784
Q2	mid	46.063	341.12	42.468	2707.977	46.031	5350.129
~	tail	44.61	363.419	44.389	2835.357	43.822	5651.474
	head	2.298	8.315	14.022	50.756	23.466	154.061
Q3	mid	1.933	366.845	15.116	6688.845	20.304	59441.052
2.	tail	1.94	725.375	15.172	13326.933	20.182	118401.92
	head	1.004	0.842	2.822	0.862	15.327	4.289
Q4	mid	1.208	125.753	1.935	650.216	6.286	11112.106
χ.	tail	1.016	250.664	1.38	1299.571	4.286	22219.924
	head	18.294	16.98	35,305	22.441	367.671	230.179
Q5	mid	17.585	1678.536	16.627	14065.395	146.61	40401.774
23	tail	13.1	3285.056	17.244	28002.402	134.78	80573.369
	head	0.745	0.534	2.076	0.534	2.895	0.538
06							
Q6	mid	0.676	296.977	0.606	1693.265	4.688	41093.476
	tail	0.509	565.074	1.23	3385.997	1.766	81893.843
0-	head	41.808	28.7	61.38	52.018	946.975	55.532
Q7	mid	27.809	369.064	55.629	4353.019	649.816	19842.907
	tail	27.667	695.718	35.851	8654.019	593.511	39630.282
	head	28.152	12.265	28.002	22.943	247.418	24.732
Q8	mid	20.745	1927.807	31.936	8373.202	221.967	25327.403
	tail	22.398	3843.349	29.754	16723.462	206.956	50630.074
	head	2.227	389.589	25.745	6031.313	27.844	29081.397
Q9	mid	1.988	1698.267	35.081	13767.171	25.463	46311.933
	tail	1.949	3006.946	24.147	21503.029	24.073	63542.47
	head	3.528	1.349	8.099	8.962	12.316	3.35
Q10	mid	1.588	1048.416	7.454	11860.303	10.354	15360.343
	tail	1.879	2095.483	7.331	23711.644	8.291	30717.336
	head	52.714	5.543	296.591	12.83	615.864	21.86
Q11	mid	55.176	41.634	317.3	294.6	724.889	508.906
~	tail	58.274	77.724	295.98	576.369	559.893	995.951
	head	1.907	1.645	3.757	4.948	3.159	1.836
Q12	mid	3.929	499.537	2.384	9183.807	2.08	9426.057
2.5	tail	1.964	997.429	1.923	18362.666	1.69	18850.279
	head	0.379	0.257	0.37	0.642	0.82	0.656
Q13	mid	0.379	477.302	0.337	2855.172	0.798	5597.041
Q13	tail	0.324	954.347	0.304	5709.702	0.758	11193.425
		6.925	3.679	42.57	4.942		
014	head	6.068		41.569	855.593	121.01 126.782	11.66 1897.004
Q14	mid		145.425				
	tail	6.091	287.172	41.044	1706.244	117.149	3782.347
	head	0.662	0.51	2.037	0.479	4.343	0.478
Q15	mid	0.634	220.523	3.608	1313.553	3.689	2524.079
	tail	0.752	440.536	0.52	2626.628	1.913	5047.679
	head	3.164	7.008	17.155	10.224	24.908	20.641
Q16	mid	3.355	213.954	10.817	1248.899	20.854	2473.624
	tail	3.646	420.901	10.047	2487.575	20.262	4926.607
	head	5.152	3.786	12.614	3.626	13.25	3.637
Q17	mid	4.848	1306.111	9.252	12169.355	13.778	30319.048
	tail	4.816	2608.435	8.428	24335.084	28.102	60634.458
	head	3963.758	8643.507	24134.374	74575.1	48786.827	169499.561
Q18	mid	4061.897	12245.213	24618.811	90277.508	46661.664	190886.288
	tail	4091.53	15846.92	26659.445	105979.916	53063.774	212273.016
	head	80.62	95.444	275.504	516.311	425.97	836.663
Q19	mid	79.97	120.793	232.757	641.094	434.126	1076.905
	tail	78.181	143.358	271.998	765.877	433.759	1317.148
	head	0.692	0.083	0.751	0.078	1.054	0.891
Q20	mid	0.754	86.401	0.797	458.918	1.671	1013.644
	tail	0.642	172.72	0.536	917.758	1.112	2026.396
	head	41.894	830.955	85.693	20382.458	678.648	51923.664
Q21	mid	28.909	831.803	70.865	20134.344	1071.348	51429.637
~	tail	30.357	832.652	61.558	20231.722	1051.124	51092.808
	head	4.299	68.512	4.51	319.805	2.876	659.813
Q22	mid	1.589	107.028	2.004	499.389	2.336	1007.544
	tail	1.604	136.537	1.529	677.494	1.997	1355.275
		1.001	150.557	1.027	577.171	2.,,,,	1555.275

Query DB size Milestone Table Milestone Table Q1 1 13029.523 2457.667 15.579 761.653 Q1 5 66150.01 39046.702 77.927 3809.747 Q2 5 1438.351 3650.785 0.015 0.647 Q3 5 7609.511 2992.648 0.108 9358 Q3 5 7609.511 2992.648 0.528 45.735 Q4 1 393.68 602.307 0.191 6.367 Q4 5 1956.036 2871.491 0.95 31.649 Q5 5 19919.163 31427.944 3.662 30.799 Q5 5 19919.163 31427.944 2.337 154.836 Q5 5 19919.163 31427.944 3.662 30.363 Q5 5 19919.163 31427.944 3.462 38.842 Q6 5 5666.841 5449.991 4.476 1218.94			Time (ms)		Output Size (MB)		
Q1 5 66150.01 39046.702 15.579 761.653 Q1 5 66150.01 39046.702 155.834 7618.516 Q2 5 1438.351 3650.785 0.015 0.647 Q1 10 3197.387 7330.617 0.031 1.31 Q3 5 7609.511 2992.468 0.528 45.735 Q4 5 1956.036 2871.491 0.95 31.649 Q4 5 1956.036 2871.491 0.95 31.649 Q5 5 13919.163 31427.944 2.337 154.836 Q5 5 13919.163 31427.944 2.337 154.836 Q6 5 5606.841 5449.991 4.662 30.884 Q6 5 5606.841 5449.991 4.676 218.804 Q7 5 8949.756 11575.322 0.369 4.602 Q8 5 3050.543 3391.072 29.027 232.655	Query	DB size					
10		1		2457.667		761.653	
Q2 5 1438.351 3650.785 0.015 0.647 10 3197.387 7330.617 0.031 1.31 Q3 5 7609.511 29926.468 0.528 45.735 10 20829.922 119386.492 1.072 92.932 1 393.68 602.307 0.191 6.367 Q4 5 1956.036 2871.491 0.95 31.649 10 19492.825 37588.076 1.895 63.165 25 5 13919.163 31427.944 2.337 154.836 05 5 13919.163 31427.944 2.337 154.836 05 5 13919.163 31427.944 2.337 154.836 05 5 13919.163 31427.944 2.337 154.836 05 5 35919.163 31427.944 2.337 154.836 06 5 5606.841 5449.391 4.476 2.338.84 10 15937.52 <t< td=""><td>Q1</td><td>5</td><td>66150.01</td><td>39046.702</td><td>77.927</td><td>3809.747</td></t<>	Q1	5	66150.01	39046.702	77.927	3809.747	
Q2 5 1438.351 3650.785 0.015 0.647 1 1402.237 7390.617 0.031 1.31 Q3 5 7609.511 2992.6468 0.528 45.735 10 20829.922 11938.6492 1.072 92.932 1 393.68 602.307 0.191 6.367 10 19492.825 3758.076 1.895 63.165 1 2794.965 3934.344 0.468 30.979 05 5 13919.163 31427.944 2.337 154.836 06 5 10937.878.956 88961.208 4.662 308.884 06 5 5606.841 5449.91 4.476 218.804 07 5 8949.756 11575.322 0.369 4.602 07 5 8949.756 11575.322 0.369 4.602 08 5 30360.543 23391.072 29.027 326.55 08 5 30360.543 233		10	132810.372	66195.529	155.834	7618.516	
10 3197.387 7330.617 0.031 1.31		1	280.11	501.518	0.003	0.129	
Q3 1 1402.237 2391.46 0.108 9.358 Q3 5 7609.511 2992.6468 0.528 45.735 10 20829.922 11938.6492 1.072 92.932 1 393.68 602.307 0.191 6.367 10 19492.825 37588.076 1.895 63.165 1 109492.825 3734.344 0.468 30.979 10 35787.956 88961.208 4.662 308.884 10 35787.956 88961.208 4.662 308.884 1 1077.996 1028.798 0.989 43.884 1 1077.996 1028.798 0.989 43.884 1 15937.32 83693.457 8.962 438.125 1 750.001 1388.376 0.076 0.947 27 5 8949.756 11575.322 0.369 4.602 28 5 30360.543 23391.072 29.027 326.55 10	Q2	5	1438.351	3650.785	0.015	0.647	
Q3 5 7609.511 2992.6468 0.528 45.735 Q4 1 393.68 602.307 0.191 6.367 Q4 5 1956.036 2871.491 0.95 31.649 10 19492.825 37588.076 1.895 63.165 1 2794.955 3934.344 0.468 30.979 Q5 5 13919.163 31427.944 2.337 154.836 1 1077.996 1028.798 0.898 43.884 Q6 5 5606.841 5449.391 4.476 218.804 10 15937.32 83693.457 8.962 438.125 1 750.001 1388.376 0.076 0.947 27 5 8949.756 11575.322 0.369 4.602 28 5 30360.543 23391.072 29.027 326.55 Q8 5 30360.543 23391.072 29.027 326.55 Q8 5 20769.045 25856.		10	3197.387	7330.617	0.031	1.31	
10 20829.922 119386.492 1.072 92.932		1	1402.237	2391.46	0.108	9.358	
Q4 1 393.68 602.307 0.191 6.367 Q4 5 1956.036 2871.491 0.95 31.649 10 19492.825 37588.966 1.895 63.165 Q5 1 2794.965 3934.344 0.468 30.979 10 35787.956 88961.208 4.662 308.884 Q6 5 506.841 5449.391 4.476 218.804 Q6 10 15937.32 83693.457 8.962 438.125 Q7 5 8949.756 11575.322 0.369 4.602 Q7 5 8949.756 11575.322 0.369 4.602 Q8 5 30360.543 23391.072 29.027 326.55 Q8 5 30360.543 23391.072 29.027 326.55 Q8 5 3056.543 23391.072 29.027 326.55 Q8 5 20769.045 25856.049 10.495 118.061 Q9 <td>Q3</td> <td>5</td> <td>7609.511</td> <td>29926.468</td> <td>0.528</td> <td>45.735</td>	Q3	5	7609.511	29926.468	0.528	45.735	
Q4 5 19492.825 37588.076 1.895 63.165 1 12794.965 3934.344 0.468 30.979 Q5 5 13919.163 31427.944 2.337 154.836 10 35787.956 88961.208 4.662 308.884 1 1077.996 1028.798 0.898 43.884 Q6 5 5606.841 5449.391 4.476 218.804 10 15937.32 83693.457 8.962 438.125 1 750.001 1388.376 0.076 0.947 27 5 8949.756 11575.322 0.369 4.602 10 18841.027 40373.876 0.745 9.306 Q8 5 30360.543 23391.072 29.027 326.55 10 61229.624 93859.353 58.6439 Q8 5 20769.045 25856.049 10.495 118.061 Q9 5 20769.045 25856.049 10.495 118		10	20829.922	119386.492	1.072	92.932	
10		1	393.68	602.307	0.191	6.367	
Q5 1 2794.965 3934.344 0.468 30.979 Q5 5 13919.163 31427.944 2.337 154.836 Q6 1 1077.996 1028.798 0.898 43.884 Q6 5 5606.841 5449.391 4.476 218.804 Q7 5 8949.756 11575.322 0.369 4.602 Q7 5 8949.756 11575.322 0.369 4.602 Q8 1 6068.222 4796.095 5.835 65.639 Q8 5 30360.543 23391.072 29.027 326.55 Q8 5 30360.543 23391.072 29.027 326.55 Q9 5 20769.045 25856.049 10.495 118.061 Q9 5 20769.045 25856.049 10.495 118.061 Q10 5 11587.553 14053.989 7.269 390.698 Q10 5 1587.553 14053.989 7.269 3	Q4	5		2871.491	0.95	31.649	
Q5 5 13919.163 31427.944 2.337 154.836 Q6 1 1077.996 88961.208 4.662 308.884 Q6 5 5606.841 5449.391 4.476 218.804 Q6 5 5606.841 5449.391 4.476 218.804 Q7 5 8949.756 11575.322 0.369 4.602 Q7 5 8949.756 11575.322 0.369 4.602 Q8 5 30360.543 23391.072 29.027 326.55 Q8 5 30360.543 23391.072 29.027 326.55 Q8 5 30360.543 23391.072 29.027 326.55 Q8 5 20769.045 2385.049 10.495 118.061 Q9 5 20769.045 25856.049 10.495 118.061 Q10 5 11587.533 14053.989 7.269 390.698 Q10 5 11587.533 14053.989 7.269		10	19492.825	37588.076	1.895	63.165	
10 35787.956 88961.208 4.662 308.884 1		1	2794.965	3934.344	0.468	30.979	
Q6 1 1077.996 1028.798 0.898 43.884 Q6 5 5606.841 5449.391 4.476 218.804 10 15937.32 83693.457 8.962 438.125 Q7 5 8949.756 11575.322 0.369 4.602 Q8 1 6068.222 4796.095 5.835 65.639 Q8 5 30360.543 23391.072 29.027 326.55 Q8 5 30360.543 23391.072 29.027 326.55 Q9 5 20769.045 28856.049 10.495 118.061 Q9 5 20769.045 25856.049 10.495 118.061 Q10 41547.519 64925.319 21.006 236.312 Q10 5 11587.553 14053.989 7.269 390.698 10 24067.6 38715.702 14.524 780.631 Q11 5 689.607 617.165 0.576 28146 Q1	Q5	5	13919.163	31427.944	2.337	154.836	
Q6 5 5606.841 5449.391 4.476 218.804 1 15937.32 83693.457 8.962 438.125 1 750.001 1388.376 0.076 0.947 2 10 18841.027 40373.876 0.745 9.306 1 6068.222 4796.095 5.835 65.639 Q8 5 30360.543 23391.072 29.027 326.55 10 61229.624 93859.353 58.142 654.091 10 41547.519 64925.319 21.006 236.312 29 5 20769.045 25856.049 10.495 118.061 10 41547.519 64925.319 21.006 236.312 11 137.414 125.681 0.121 59.28 Q10 5 11587.533 14053.989 7.269 390.698 1 137.414 125.681 0.121 59.28 Q11 5 689.607 617.165 0.576 28.146		10	35787.956	88961.208	4.662	308.884	
1		1	1077.996	1028.798	0.898	43.884	
Q7 5 8949.756 11575.322 0.369 4.602 Q8 1 6068.222 4796.095 5.835 65.639 Q8 5 30360.543 23391.072 29.027 326.55 Q8 5 30360.543 23391.072 29.027 326.55 Q9 1 2824.782 3857.867 2.134 23.998 10 61229.624 93859.353 58.142 654.091 Q9 5 20769.045 25856.049 10.495 118.061 10 41547.519 64925.319 21.006 236.312 21 1 2235.767 2775.5 1.449 77.861 Q10 5 11587.553 14053.989 7.269 390.698 Q11 5 689.607 617.165 0.576 28.146 Q11 5 689.607 617.165 0.576 28.146 Q12 5 6617.319 22186.895 1.974 52.627	Q6	5		5449.391	4.476		
Q7 5 8949.756 11575.322 0.369 4.602 10 18841.027 40373.876 0.745 9.306 1 6068.222 4796.095 5.835 65.639 Q8 5 30360.543 23391.072 29.027 326.55 10 61229.624 93859.353 58.142 654.091 Q9 5 20769.045 25856.049 10.495 118.061 10 41547.519 64925.319 21.006 236.312 Q10 5 11587.553 14053.989 7.269 390.698 10 24067.6 38715.702 14.524 780.631 Q11 5 689.607 617.165 0.576 28.146 Q11 5 689.607 617.165 0.576 28.146 Q12 5 6617.319 22186.895 1.974 52.627 1 1737.807 2334.203 0.394 105.07 Q12 5 6617.319 22186.895<		10	15937.32	83693.457	8.962	438.125	
10		1	750.001	1388.376	0.076	0.947	
Q8 1 6068.222 4796.095 5.835 65.639 Q8 5 30360.543 23391.072 29.027 326.55 10 61229.624 93859.353 58.142 654.091 Q9 5 20769.045 25856.049 10.495 118.061 10 41547.519 64925.319 21.006 236.312 210 5 11587.553 14053.989 7.269 390.698 10 24067.6 38715.702 14.524 780.631 21 137.414 125.681 0.121 5.928 Q11 5 689.607 617.165 0.576 28.146 Q11 5 689.607 617.165 0.576 28.146 Q12 5 6617.319 22186.895 1.974 52.627 Q12 5 6617.319 22186.895 1.974 52.627 Q13 5 28939.75 12261.105 17.98 372.001 Q13 5	Q7	5	8949.756	11575.322	0.369	4.602	
Q8 5 30360.543 23391.072 29.027 326.55 1 61229.624 93859.353 88.142 654.091 1 2824.782 3857.867 2.134 23.998 Q9 5 20769.045 25856.049 10.495 118.061 10 41547.519 64925.319 21.006 236.312 Q10 5 11587.553 14053.989 7.269 390.698 10 24067.6 38715.702 14.524 780.631 Q11 5 689.607 617.165 0.576 28.146 10 1311.196 15862.307 1.149 56.193 Q12 5 6617.319 22186.895 1.974 52.627 10 14404.903 25798.262 3.94 105.057 213 5 28939.75 12261.105 17.98 372.001 213 5 28939.75 12261.105 17.98 372.001 213 5 28939.75 1		10	18841.027	40373.876	0.745	9.306	
1		1	6068.222	4796.095	5.835	65.639	
Q9 1 2824.782 3857.867 2.134 23.998 Q9 5 20769.045 28585.049 10.495 118.061 10 41547.519 64925.319 21.006 236.312 Q10 5 11587.553 14053.989 7.269 390.698 Q10 5 11587.553 14053.989 7.269 390.698 Q11 5 689.607 617.165 0.576 28.146 Q11 5 689.607 617.165 0.576 28.146 Q12 5 6617.319 22186.895 1.974 52.627 Q12 5 6617.319 22186.895 1.974 52.627 Q13 5 2893.75 12261.105 17.98 372.001 Q13 5 2893.75 12261.105 17.98 372.001 Q14 5 2001.128 7033.305 1.347 22.79 18.571 Q14 5 201.128 7033.305 1.348 <t< td=""><td>Q8</td><td>5</td><td></td><td></td><td></td><td>326.55</td></t<>	Q8	5				326.55	
Q9 5 20769.045 25856.049 10.495 118.061 10 41547.519 64925.319 21.006 236.312 21 1 2235.767 2775.5 1.449 77.861 Q10 5 11587.553 14053.989 7.269 390.698 10 24067.6 38715.702 14.524 780.631 Q11 5 689.607 617.165 0.576 28.146 10 1311.196 15862.307 1.149 56.193 Q12 5 6617.319 22186.895 1.974 52.627 10 14404.903 25798.262 3.94 105.057 213 5 28939.75 12261.105 17.98 372.001 213 5 28939.75 12261.105 17.98 372.001 214 5 2001.128 7033.305 1.347 92.793 214 5 2001.128 7033.305 1.347 92.793 215 5		10	61229.624	93859.353	58.142	654.091	
10		1	2824.782	3857.867	2.134	23.998	
1 2235.767 2775.5 1.449 77.861 210 5 11587.553 14053.989 7.269 390.698 24067.6 38715.702 14.524 780.631 1 137.414 125.681 0.121 5.928 211 5 689.607 617.165 0.576 28.146 211 5 689.607 617.165 0.576 28.146 212 1 1737.807 2334.203 0.394 10.507 213 1 10 1311.196 15862.307 1.149 56.193 214 5 6617.319 22186.895 1.974 52.627 215 6617.319 22186.895 1.974 52.627 216 10 14404.903 25798.262 3.94 105.057 21 5899.366 2138.399 3.596 74.4 21 5 28939.75 12261.105 17.98 372.001 21 330.802 476.924 0.27 18.571 21 330.802 476.924 0.27 18.571 21 330.802 476.924 0.27 18.571 21 330.802 476.924 0.27 18.571 21 1014.581 707.173 1.083 52.914 21 2011.128 7033.305 1.347 92.793 21 1014.581 707.173 1.083 52.914 21 21 21 21 21 21 21 21	Q9	5	20769.045	25856.049	10.495	118.061	
Q10 5 11587.553 14053.989 7.269 390.698 10 24067.6 38715.702 14.524 780.631 Q11 1 137.414 125.681 0.121 5.928 Q10 5 689.607 617.165 0.576 28.146 10 1311.196 1862.307 1.149 56.193 Q12 5 6617.319 22348.03 0.394 10.507 Q12 5 6617.319 2218.895 1.974 52.627 10 14404.903 25798.262 3.94 105.057 Q13 5 28939.75 12261.105 17.98 372.001 Q14 5 28939.75 12261.105 17.98 372.001 Q14 5 2001.128 7033.305 1.347 92.793 Q14 5 2001.128 7033.305 1.347 92.793 Q15 5 5256.718 11050.796 5.423 265.099 Q15		10	41547.519	64925.319	21.006	236.312	
10		1	2235.767	2775.5	1.449	77.861	
Q11 1 137,414 125,681 0.121 5.928 Q11 5 689,607 617,165 0.576 28.146 0 1311,196 15862,307 1.149 56,193 1 1737,807 2334,203 0.394 10.507 10 14404,903 25798,262 3.94 105,057 1 5899,366 2138,399 3.596 74,4 Q13 5 28939,75 12261,105 17.98 372,001 1 058316,145 24704,791 35.96 744,001 1 380,802 476,924 0.27 18,571 Q14 5 2001,128 7033,305 1,347 92,793 Q15 5 5256,718 1050,796 5,423 265,099 10 1044,881 707,173 1,083 52,914 Q15 5 5256,718 1050,796 5,423 265,099 10 10870,044 40518,84 10.848 530,346	Q10	5	11587.553	14053.989	7.269	390.698	
Q11 5 689.607 617.165 0.576 28.146 10 1311.196 15862.307 1.149 56.193 Q12 5 6617.319 22186.895 1.974 52.627 10 14404.903 25798.262 3.94 105.057 Q13 5 28939.75 12261.05 17.98 372.001 Q14 5 28939.75 12261.105 17.98 372.001 Q14 5 2001.128 703.3305 1.347 92.793 10 3954.975 35885.574 2.696 185.705 1 1014.581 707.173 1.083 52.914 Q15 5 5256.718 1105.0796 5.423 265.099 10 10870.044 40151.84 10.848 530.346 Q16 5 2798.609 4488.92 1.839 81.74 Q17 5 2593.944 34723.602 3.6 5.6.0 Q1 5 2793.944 <t< td=""><td></td><td>10</td><td>24067.6</td><td>38715.702</td><td>14.524</td><td>780.631</td></t<>		10	24067.6	38715.702	14.524	780.631	
10		1	137.414	125.681	0.121	5.928	
Q12 1 1737.807 2334.203 0.394 10.507 Q12 5 6617.319 22186.895 1.974 52.627 10 14404.903 25798.262 3.94 105.057 213 5 2899.75 12261.105 17.98 372.001 10 58316.145 24704.791 35.96 744.001 1 380.802 476.924 0.27 18.571 Q14 5 2001.128 7033.305 1.347 92.793 10 3954.975 35885.574 2.696 185.705 1 1014.581 707.173 1.083 52.914 Q15 5 5256.718 11050.796 5.423 265.099 10 10870.044 40151.84 10.848 530.346 Q16 5 2798.609 4488.929 1.839 81.74 Q16 5 2793.944 34723.602 3.6 56.0 Q17 5 27933.944 34723.602	Q11	5	689.607	617.165	0.576	28.146	
Q12 5 6617.319 22186.895 1.974 52.627 10 14404.903 25798.262 3.94 105.057 Q13 5 28993.75 12261.105 17.98 372.001 10 58316.145 24704.791 35.96 744.001 Q14 5 2001.128 7033.305 1.347 92.793 10 3954.975 35885.574 2.696 185.705 1 1014.581 707.173 1.083 52.914 Q15 5 5256.718 11050.796 5.423 265.099 10 10870.044 40151.84 10.848 530.346 Q16 5 2798.609 4488.929 1.839 81.74 Q16 5 2798.609 4488.929 1.839 81.74 Q17 5 2593.944 34723.602 3.6 56.0 Q17 5 2793.944 34723.602 3.6 56.0 Q18 5 119339.262		10	1311.196	15862.307	1.149	56.193	
10		1	1737.807	2334.203	0.394	10.507	
Q13 1 5899.366 2138.399 3.596 74.4 Q13 5 28939.75 12261.105 17.98 372.001 10 58316.145 24704.791 35.96 744.001 1 380.802 476.924 0.27 18.571 201 10 3954.975 35885.574 2.696 185.705 1 1014.581 707.173 1.083 52.914 Q15 5 5256.718 11050.796 5.423 265.099 10 10870.044 40151.84 10.848 530.346 1 518.68 523.076 0.37 16.455 Q16 5 2798.609 4488.929 1.839 81.74 1 6134.681 6181.627 0.72 11.2 Q17 5 27933.944 34723.602 3.6 56.0 1 21986.933 16799.919 26.108 1272.737 Q18 5 119339.262 131820.25 130.43	Q12	5	6617.319	22186.895	1.974	52.627	
Q13 5 28939.75 12261.105 17.98 372.001 10 58316.145 24704.791 35.96 744.001 1 380.802 476.924 0.27 18.571 Q14 5 2001.128 7033.305 1.347 92.793 10 3954.975 35885.574 2.696 185.705 Q15 5 5256.718 11050.796 5.423 265.099 10 10870.044 40151.84 10.848 530.346 Q16 5 2798.609 4488.929 1.839 81.74 10 5636.501 6598.465 3.689 163.946 Q16 5 27933.944 34723.602 3.6 56.0 Q17 5 27933.944 34723.602 3.6 56.0 Q18 1 21986.933 16799.919 26.108 1272.737 Q18 5 119339.262 131820.25 130.43 6358.46 Q19 5 995.482		10	14404.903	25798.262	3.94	105.057	
10		1	5899.366	2138.399	3.596	74.4	
Q14 5 2001.128 7033.305 1.347 92.793 Q14 5 2001.128 7033.305 1.347 92.793 Q15 1 1014.581 707.173 1.083 52.914 Q15 5 5256.718 11050.796 5.423 265.099 Q16 5 2798.609 4488.929 1.839 81.74 Q16 5 2798.609 4488.929 1.839 81.74 Q17 5 27933.944 34723.602 3.6 56.0 Q17 5 27933.944 34723.602 3.6 56.0 Q18 5 119339.262 131820.25 130.43 6358.46 Q18 5 119339.262 131820.25 130.43 6358.46 Q19 5 905.482 6894.219 0.02 1.501 Q19 5 905.482 6894.219 0.109 7.47 Q20 5 15414.311 45633.142 3.289 1056.214 <td>Q13</td> <td>5</td> <td>28939.75</td> <td>12261.105</td> <td>17.98</td> <td>372.001</td>	Q13	5	28939.75	12261.105	17.98	372.001	
Q14 5 2001.128 7033.305 1.347 92.793 10 3954.975 35885.574 2.696 185.705 Q15 5 5256.718 11050.796 5.423 265.099 10 10870.044 40151.84 10.848 530.346 Q16 5 2798.609 4488.929 1.839 81.74 10 5636.501 6598.465 3.689 163.946 11 6134.681 6181.627 0.72 112.0 Q17 5 27933.944 34723.602 3.6 56.0 10 57508.86 64700.14 7.2 112.0 Q18 5 119339.262 131820.25 130.43 6358.46 10 252651.048 27391.1052 260.7 12709.096 Q19 5 995.482 6894.219 0.109 7.47 Q19 5 995.482 6894.219 0.109 7.47 Q20 5 15414.311 45633.142		10	58316.145	24704.791	35.96	744.001	
10 3954.975 35885.574 2.696 185.705 1		1	380.802	476.924	0.27	18.571	
Q15 1 1014.581 707.173 1.083 52.914 Q15 5 5256.718 11050.796 5.423 265.099 10 1087.044 40151.84 10.848 530.346 1 551.868 523.076 0.37 16.455 Q16 5 2798.609 4488.929 1.839 81.74 10 5636.501 6598.465 3.689 163.946 21 6134.681 6181.627 0.72 11.2 Q17 5 27933.944 34723.602 3.6 56.0 10 57508.86 64700.14 7.2 112.0 Q18 5 119339.262 131820.25 130.43 6358.46 10 252651.048 273911.052 260.7 12709.09 Q19 5 905.482 6894.219 0.109 7.47 10 1505.552 60837.304 0.211 14.506 Q20 5 15414.311 45633.142 16.443	Q14	5	2001.128	7033.305	1.347	92.793	
Q15 5 5256.718 11050.796 5.423 265.099 10 10870.044 40151.84 10.848 530.346 Q16 5 2798.609 4488.929 1.839 81.74 Q16 5 2798.609 4488.929 1.839 81.74 10 5636.501 6598.465 3.689 163.946 Q17 5 27933.944 34723.602 3.6 56.0 10 57508.86 64700.14 7.2 112.0 Q18 5 119339.262 131820.25 130.43 6358.46 10 252651.048 273911.052 260.7 12709.096 Q19 5 905.482 6894.219 0.109 7.47 Q19 5 905.482 6894.219 0.109 7.47 Q20 5 15414.311 45633.142 16.443 5279.964 Q20 5 15414.311 45633.142 16.443 5279.964 Q21 5		10	3954.975	35885.574	2.696	185.705	
10 10870.044 40151.84 10.848 530.346 1 551.868 523.076 0.37 16.455 Q16 5 2798.609 4488.929 1.839 81.74 10 5636.501 6598.465 3.689 163.946 2017 5 2793.944 34723.602 3.6 56.0 10 57508.86 64700.14 7.2 112.0 21 21986.933 16799.919 26.108 1272.737 Q18 5 119339.262 131820.25 130.43 6358.46 10 252651.048 273911.052 260.7 12709.096 Q19 5 995.482 6894.219 0.092 1.501 Q19 5 995.482 6894.219 0.109 7.47 Q20 5 15414.311 45633.142 16.443 5279.964 Q20 5 15414.311 45633.142 16.443 5279.964 Q21 5 13742.687 25023.		1		707.173	1.083	52.914	
10	Q15	5	5256.718	11050.796	5.423	265.099	
Q16 5 2798.609 4488.929 1.839 81.74 10 5636.501 6598.465 3.689 163.946 1 6134.681 6181.627 0.72 11.2 Q17 5 27933.944 34723.602 3.6 56.0 10 57508.86 64700.14 7.2 112.0 Q18 5 119339.262 131820.25 130.43 6358.46 10 252651.048 273911.052 260.7 12709.096 Q19 5 905.482 6894.219 0.109 7.47 10 1505.552 66837.304 0.211 14.506 Q20 5 15414.311 45633.142 16.443 5279.964 Q20 5 15414.311 45633.142 16.443 5279.964 Q21 5 13742.687 25023.161 0.125 6.538 Q21 5 13742.687 25023.161 0.125 6.538 Q22 5 765.807		10	10870.044	40151.84	10.848	530.346	
10 5636.501 6598.465 3.689 163.946 1		1		523.076		16.455	
Q17 5 27933.944 34723.602 3.6 5.0 Port of the control of	Q16	5	2798.609		1.839		
Q17 5 27933.944 34723.602 3.6 5.0 Port of the control of		10	5636.501	6598.465	3.689	163.946	
10 57508.86 64700.14 7.2 112.0		1		6181.627	0.72	11.2	
10	Q17	5		34723.602		56.0	
Q18 5 119339.262 131820.25 130.43 6358.46 10 252651.048 273911.052 260.7 12790.96 Q19 5 905.482 6894.219 0.109 7.47 10 1505.552 68837.304 0.211 14.506 Q20 5 15414.311 45633.142 16.443 5279.964 10 35581.996 91427.229 32.845 10557.545 Q21 5 13742.687 25023.161 0.125 6.538 Q21 5 13742.687 25023.161 0.125 6.538 Q21 5 162.503 165.083 0.023 0.045 Q22 5 765.807 886.335 0.114 2.035		10	57508.86	64700.14	7.2	112.0	
10 252651.048 273911.052 260.7 12709.096 1 162.155 404.626 0.022 1.501 1 1505.552 6894.219 0.109 7.47 10 1505.552 60837.304 0.211 14.506 1 3110.616 2668.742 3.289 1056.214 20 5 15414.311 45633.142 16.443 3279.964 10 35581.996 91427.229 32.845 10557.545 1 866.568 1455.808 0.026 1.332 21 5 13742.687 25023.161 0.125 6.538 10 34559.892 95153.337 0.256 13.417 20 21 5 765.807 886.335 0.114 2.035 30 22 5 765.807 886.335 0.114 2.035						1272.737	
Q19 1 162.155 404.626 0.022 1.501 Q19 5 905.482 6894.219 0.109 7.47 10 1505.552 60837.304 0.211 14.506 1 3110.616 2668.742 3.289 1056.214 Q20 5 15414.311 45633.142 16.443 3279.964 10 35581.996 91427.229 32.845 10557.545 Q21 5 13742.687 25023.161 0.125 6.538 Q21 5 13742.687 25023.161 0.125 6.538 10 34559.892 95153.337 0.236 13.417 Q22 5 765.807 886.335 0.014 2.035	Q18	5			130.43	6358.46	
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10 34559.892 95153.337 0.256 13.417 1 162.503 165.083 0.023 0.405 Q22 5 765.807 886.335 0.114 2.035							
Q22 1 162.503 165.083 0.023 0.405 Q35 765.807 886.335 0.114 2.035	Q21	!					
Q22 5 765.807 886.335 0.114 2.035							
10 1533.474 2025.742 0.229 4.069	Q22						
		10	1533.474	2025.742	0.229	4.069	

(a) Optimization vs. Baseline for Page Query Execution Time

(b) Milstone Query vs. Table Query

Table 6: Experiment results for Page Size 100. Shorter time and smaller sizes are highlighted.

		10	BB	5GB		10GB	
Query	Page	Opt.	Base	Opt.	Base	Opt.	Base
	head	0.146	0.389	0.433	0.387	0.49	0.163
Q1	mid	0.16	454.435	0.464	16284.424	0.461	30276.205
	tail	0.133	908.481	0.372	32568.462	0.405	60552.247
	head	55.255	321.231	91.769	2568.871	88.861	5104.092
Q2	mid	52.181	355.251	87.877	2711.985	92.542	5427.883
~	tail	53.35	389.271	91.139	2855.098	92.844	5751.674
	head	3.94	14.391	35.196	132.234	39.181	226.782
Q3	mid	3.909	365.739	26.025	6675.944	47.164	59440.776
25	tail	3.611	717.087	26.169	13181.499	43.333	118022.429
	head	2.242	1.713	2.14	1.733	13.369	7.061
Q4	mid	2.269	123,996	3.002	650.459	11.325	11214.848
21	tail	2.127	246.279	2.19	1299.185	8.845	22341.941
	head	28.833	37.402	51.504	71.031	577.779	413.569
Q5	mid	26.29	1746.625	36.167	14325.169	265.56	40522.6
QJ	tail	22.047	3369.844	35.608	28095.786	237.461	80631.631
	head	4.046	1.042	1.365	1.074	3.365	3.164
04				1.365		3.365 4.891	
Q6	mid	1.49	300.074		1670.156		40923.411
	tail	1.545	599.106	1.505	3339.238	1.842	81797.261
0=	head	65.141	53.139	102.474	81.208	1511.564	80.04
Q7	mid	52.02	390.365	73.626	4342.948	895.119	19402.032
	tail	49.058	722.125	65.171	8604.687	835.577	38724.024
	head	54.929	20.102	66.214	28.021	415.944	56.301
Q8	mid	44.767	1961.613	57.467	8389.363	312.842	25654.914
	tail	44.222	3903.124	51.861	16750.706	343.404	51253.527
	head	3.807	391.343	41.007	6039.289	43.95	29193.922
Q9	mid	3.982	1727.193	51.369	13735.98	41.83	46365.304
	tail	3.321	3056.58	47.51	21432.671	42.478	63536.687
	head	3.34	2.084	15.334	14.991	25.553	4.648
Q10	mid	3.258	1055.799	15.911	11791.208	18.078	15180.68
-	tail	3.534	2109.514	9.998	23567.424	20.76	30356.711
	head	107.842	10.874	562.752	18.136	1182.66	26.277
Q11	mid	102.869	42.147	571.399	291.854	1228.931	514.186
	tail	110.701	73.42	540.832	565.572	1083.823	1002.094
	head	4.596	3.41	4.939	7.39	5.62	3,739
Q12	mid	8.235	486.03	3.992	9115.702	4.735	9420.754
~	tail	3.682	968,651	3.468	18224.014	3.855	18837.768
	head	1.654	0.473	0.867	0.495	0.578	0.729
Q13	mid	1.587	456.661	0.765	2654.764	0.58	5625.206
215	tail	1.36	912.849	0.947	6597.823	0.625	11249.684
	head	7.708	9.054	45.371	15.041	122.05	15.072
Q14	mid	7.238	147.356	46.699	885.645	120.864	1911.871
Q14	tail	6.95	280.742	45.787	1734.791	123.123	3808.671
	head	3.735	0.85	3.158	2.645	9.409	1.126
015	mid	3.124	207.608	10.181	1307.789	5.79	2515.546
Q15	tail	1.263	414.366	3.237	2612.933	3.955	5029.967
01/	head	9.606	2.675	11.776	11.327	21.11	29.04
Q16	mid tail	11.049	208.386 412.058	12.759 11.599	1266.214	22.488 21.577	2464.479
		3.587			2521.1		4899.917
0:-	head	9.482	6.71	22.959	7.215	32.825	7.332
Q17	mid	9.251	1268.832	22.988	16872.764	41.268	28139.693
	tail	8.654	2530.953	22.979	33738.314	29.277	56272.054
04-	head	3903.961	8319.451	21528.099	81351.562	50643.69	171400.04
Q18	mid	4013.044	11809.205	19208.862	96954.308	51412.839	193322.243
	tail	3931.8	15298.959	23889.779	112557.054	53669.283	215244.446
	head	104.82	154.3	768.251	620.145	465.465	1135.042
Q19	mid	110.143	147.477	765.594	694.52	496.925	1232.457
	tail	113.428	141.114	778.368	768.895	462.613	1329.872
	head	0.461	0.33	1.302	0.12	0.74	1.838
Q20	mid	0.409	87.733	1.228	557.974	2.738	1064.696
	tail	0.399	175.135	1.128	1115.828	1.079	2127.553
	head	79.333	813.999	5911.734	20059.439	2018.207	51725.379
Q21	mid	53.285	819.563	4663.958	19896.141	1971.71	51234.28
			1	4640.000	10722 042	17/1 050	50743.181
	tail	55.42	813.999	4649.823	19732.842	1761.852	00/43.161
	tail head	55.42 2.861	813.999 66.346	3.595	334.122	9.744	680.439
Q22							

Query DB size 1 Q1 5 10 10 Q2 5 10 Q3 5	Time Milestone 12918.259 66166.286 132584.301 282.879 1423.001 3186.098	Table 2440.065 40957.384 65152.122 497.999	Output S Milestone 7.79 38.964 77.917	Table 761.653 3809.747
Q1 5 10 1 Q2 5 10 1 1	66166.286 132584.301 282.879 1423.001	40957.384 65152.122 497.999	38.964	3809.747
Q2 5 10 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	132584.301 282.879 1423.001	65152.122 497.999		
Q2 1 5 10 1	282.879 1423.001	497.999	77.917	
Q2 5 10	1423.001			7618.516
10			0.003	0.129
1	3186.098	3694.901	0.008	0.647
		7371.271	0.016	1.31
O3 5	1394.346	2403.439	0.054	9.358
	7529.177	37672.174	0.264	45.735
10	20757.397	119575.923	0.536	92.932
1	384.925	592.285	0.096	6.367
Q4 5	1941.103	3502.926	0.475	31.649
10	19626.549	37255.875	0.948	63.165
1	3029.376	3930.43	0.234	30.979
Q5 5	13764.754	30815.472	1.169	154.836
10	35644.992	88633.534	2.332	308.884
1 1	1165.378	1062.076	0.449	43.884
Q6 5	5583.563	5043.746	2.238	218.804
10	16028.371	83720.999	4.481	438.125
1 5	778.049	1504.937	0.038	0.947
Q7 5	8787.166	11226.01	0.184	4.602
10	18606.773	41071.627	0.372	9.306
00 5	6096.48	4880.251	2.918	65.639
Q8 5 10	30248.758 60868.096	22877.673 94180.357	14.514 29.071	326.55 654.091
O9 5	2867.998 20706.537	3785.434 25684.329	1.067 5.247	23.998 118.061
Q9 5 10	41036.521	65536.758	10.503	236.312
10	2298.852	2741.803	0.724	77.861
Q10 5	11682.06	13569.476	3.635	390.698
10	24156.397	39305.001	7.262	780.631
10	141.382	123.338	0.061	5.928
Q11 5	706.803	578.334	0.001	28.146
10	1325.331	15713.276	0.575	56.193
10	1691.273	2261.535	0.197	10.507
Q12 5	6628.787	22103.411	0.197	52.627
10	14411.088	26482.419	1.97	105.057
1	5904.443	2023.404	1.798	74.4
Q13 5	29358.318	12564.698	8.59	372.001
10	58269.683	24649.779	17.98	744.001
1	364.521	461.061	0.135	18.571
Q14 5	2023.895	18845.022	0.674	92.793
10	3965.741	35490.329	1.348	185.705
1	981.171	673.001	0.541	52.914
Q15 5	5233.873	20492.43	2.712	265.099
10	10794.957	40226.156	5.424	530.346
1	517.513	509.302	0.185	16.455
Q16 5	2663.285	3373.281	0.92	81.74
10	5422.138	6661.765	1.845	163.946
1	5814.768	5818.887	0.36	11.2
Q17 5	28270.684	34331.977	1.8	56.0
10	57033.56	64742.184	3.6	112.0
1	20843.893	16149.079	13.054	1272.737
Q18 5	117514.027	143138.813	65.215	6358.46
10	247356.887	269322.91	130.35	12709.096
1	159.498	387.317	0.011	1.501
Q19 5	937.639	10230.62	0.054	7.47
10	1524.313	63414.724	0.105	14.506
1	3002.178	2583.319	1.644	1056.214
Q20 5	15469.147	49269.443	8.221	5279.964
10	36276.083	93364.505	16.423	10557.545
1	811.625	1411.304	0.013	1.332
Q21 5	14187.38	25798.959	0.063	6.538
10	35656.018	96969.24	0.128	13.417
1	155.141	158.698	0.012	0.405
Q22 5	779.235	864.045	0.057	2.035
10	1561.38	1999.535	0.114	4.069

(a) Optimization vs. Baseline for Page Query Execution Time

(b) Milstone Query vs. Table Query

Table 7: Experiment results for Page Size 200. Shorter time and smaller sizes are highlighted.

D ADDITIONAL DETAILS ON USER STUDY

The user study is conducted with an instance of beer database with the following schema (keys are underlined):

- Drinker (name, address)
- Bar (name, address)
- Beer (name, brewery)
- Frequents (drinker, bar, times_a_week)
- Serves (bar, beer, price)
- Likes (drinker, beer)

D.1 Debugging Quesiton 1

Question Statement. For each bar Ben visits, find price of the most expensive and cheapest drink at that bar. Format the output as (bar, price), no duplicates.

The wrong query presented to the students are as follows:

```
WITH t1 AS (
 SELECT bar, price
 FROM serves
 WHERE price = (
     SELECT MAX(S1.price)
     FROM serves S1
     WHERE S1.bar = bar
 LINTON ALL
 SELECT bar, price
 FROM serves
 WHERE price = (
     SELECT MIN(S1.price)
     FROM serves S1
     WHERE S1.bar = bar
)
SELECT t1.bar, t1.price
FROM t1, frequents
WHERE t1.bar = frequents.bar
```

```
AND frequents.drinker = 'Ben';
```

The above query has two mistakes:

- UNION ALL creates duplicates when the most expensive and cheapest drink share the same price.
- The bar in both scalar subqueries are referencing the wrong column. Without correct aliasing, both bar refer to the bar in \$1, making the WHERE condition a tautology.

D.2 Debugging Quesiton 2

Question Statement. Suppose every time a drinker frequents a bar, he buys all his favorite beers at that bar. Find the expected weekly revenue of each bar and rank them by the revenue from high to low. The output should be in the format of (bar, revenue). If a bar is not frequented by any drinker, or it does not serve any beer, or none of its beer is liked by any drinker, output (bar, NULL).

The wrong query presented to the students are as follows:

```
SELECT S.bar,
SUM(F.times_a_week) * SUM(S.price) AS revenue
FROM serves S,
frequents F,
likes L
WHERE S.bar = F.bar
AND S.beer = L.beer
GROUP BY S.bar
ORDER BY revenue DESC;
```

The above query has three mistakes:

- The join predicate F. drinker = L. drinker is missing.
- The expression for sum is incorrect as it will blow up the result. The correct expression is SUM(F.times_a_week * S.price).
- There will be no "NULL" tuple produced by the query, i.e., bars which do not serve any beer / serve no liked by anyone will not be included in the result.