#### Chapter 13, Solution 5.

(a) If the coils are connected in series,

$$L = L_1 + L_2 + 2M = 50 + 120 + 2(0.5)\sqrt{50x120} = 247.4 \text{ mH}$$

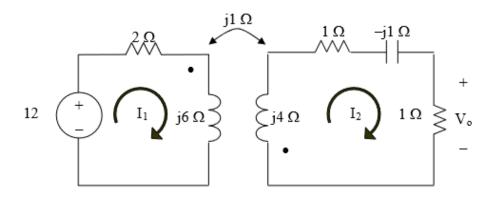
(b) If they are connected in parallel,

$$L = \frac{L_1 L_2 - M^2}{L_1 + L_2 - 2M} = \frac{50x120 - 38.72^2}{50 + 120 - 2x38.72} \text{ mH} = 48.62 \text{ mH}$$

(a) 247.4 mH, (b) 48.62 mH

## Chapter 13, Solution 7.

We apply mesh analysis to the circuit as shown below.



For mesh 1,  

$$(2+i6)I_1 + iI_2 = 24$$

For mesh 2,  $jI_1 + (2-j+j4)I_2 = jI_1 + (2+j3)I_2 = 0$  or  $I_1 = (-3+j2)I_2$ 

Substituting into the first equation results in  $I_2 = (-0.8762 + j0.6328)$  A.

$$V_o = I_2x1 = 1.081 \angle 144.16^{\circ} V$$
.

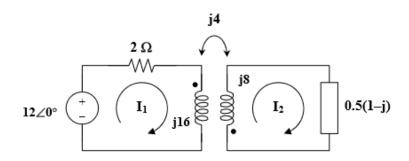
## Chapter 13, Solution 24.

(a) 
$$k = M/\sqrt{L_1L_2} = 1/\sqrt{4x^2} = 0.3535$$

(b) 
$$\omega = 4$$
 
$$1/4 \ F \ leads to \ 1/(j\omega C) = -j/(4x0.25) = -j$$
 
$$1||(-j) = -j/(1-j) = 0.5(1-j)$$
 
$$1 \ H \ produces \ j\omega M = j4$$

4 H produces j16

2 H becomes j8



$$12 = (2 + j16)I_1 + j4I_2$$

or 
$$6 = (1+j8)I_1 + j2I_2$$
 (1)

$$0 = (j8 + 0.5 - j0.5)I_2 + j4I_1 \text{ or } I_1 = (0.5 + j7.5)I_2/(-j4)$$
 (2)

Substituting (2) into (1),

$$24 = (-11.5 - j51.5)I_2 \text{ or } I_2 = -24/(11.5 + j51.5) = -0.455 \angle -77.41^\circ$$
 
$$V_o = I_2(0.5)(1 - j) = 0.3217 \angle 57.59^\circ$$
 
$$v_o = 321.7cos(4t + 57.6^\circ) \text{ mV}$$

(c) From (2), 
$$I_1 = (0.5 + j7.5)I_2/(-j4) = 0.855 \angle -81.21^\circ$$
  
 $i_1 = 0.885\cos(4t - 81.21^\circ) \text{ A}, \ i_2 = -0.455\cos(4t - 77.41^\circ) \text{ A}$   
At  $t = 2s$ ,  
 $4t = 8 \text{ rad} = 98.37^\circ$ 

$$i_1 = 0.885\cos(98.37^{\circ} - 81.21^{\circ}) = 0.8169$$

$$i_2 = -0.455\cos(98.37^{\circ} - 77.41^{\circ}) = -0.4249$$

$$w = 0.5L_1i_1^2 + 0.5L_2i_2^2 + Mi_1i_2$$

$$= 0.5(4)(0.8169)^2 + 0.5(2)(-.4249)^2 + (1)(0.1869)(-0.4249) = 1.168 J$$

#### Chapter 13, Solution 41.

We reflect the 2-ohm resistor to the primary side.

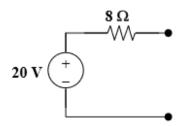
$$Z_{in} = 10 + 2/n^2$$
,  $n = -1/3$ 

Since both  $I_1$  and  $I_2$  enter the dotted terminals,  $Z_{in} = 10 + 18 = 28$  ohms

$$I_1 = 14\angle 0^{\circ}/28 = 500 \text{ mA} \text{ and } I_2 = I_1/n = 0.5/(-1/3) = -1.5 \text{ A}$$

## Chapter 13, Solution 53.

(a) The Thevenin equivalent to the left of the transformer is shown below.



The reflected load impedance is  $Z_L$ ' =  $Z_L/n^2$  =  $200/n^2$ .

For maximum power transfer,  $8 = 200/n^2$  produces n = 5.

(b) If 
$$n = 10$$
,  $Z_L' = 200/10 = 2$  and  $I = 20/(8+2) = 2$   
 $p = I^2 Z_L' = (2)^2 (2) = 8$  watts.

#### Chapter 13, Solution 71.

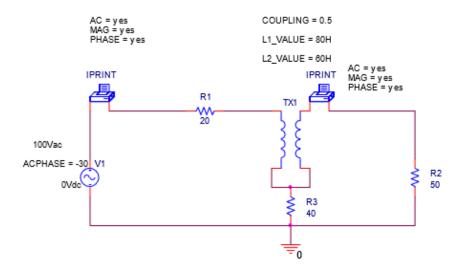
$$\begin{split} Z_{in} &= V_1/I_1 \\ But & V_1I_1 = V_2I_2, \text{ or } V_2 = I_2Z_L \text{ and } I_1/I_2 = N_2/(N_1+N_2) \\ Hence & V_1 = V_2I_2/I_1 = Z_L(I_2/I_1)I_2 = Z_L(I_2/I_1)^2I_1 \\ & V_1/I_1 = Z_L[(N_1+N_2)/N_2]^2 \\ & Z_{in} = \left[1+(N_1/N_2)\right]^2Z_L \end{split}$$

## Chapter 13, Solution 78.

We convert the reactances to their inductive values.

$$X = \omega L$$
  $\longrightarrow$   $L = \frac{X}{\omega}$ 

The schematic is as shown below.



FREQ IM(V\_PRINT1)IP(V\_PRINT1)

1.592E-01 1.347E+00 -8.489E+01

FREQ IM(V\_PRINT2)IP(V\_PRINT2)

1.592E-01 6.588E-01 -7.769E+01

Thus,

 $I_1 = 1.347 \angle -84.89^{\circ}$  amps and  $I_2 = 658.8 \angle -77.69^{\circ}$  mA

# Chapter 13, Solution 90.

(a) 
$$n = V_2/V_1 = 240/2400 = 0.1$$

(b) 
$$n = N_2/N_1 \text{ or } N_2 = nN_1 = 0.1(250) = 25 \text{ turns}$$

(c) 
$$S = I_1V_1 \text{ or } I_1 = S/V_1 = 4x10^3/2400 = 1.6667 \text{ A}$$

$$S = I_2V_2 \text{ or } I_2 = S/V_2 = 4x10^4/240 = 16.667 A$$