

$R(u_0, u_1)$

v1	v2
v5	v2
v5	v3
v5	v6
v5	v7
v8	v6
v8	v7

 $R(u_0, u_2)$

v1	v2
v5	v2
v5	v3
v5	v6
v5	v7
v8	v6
v8	v7

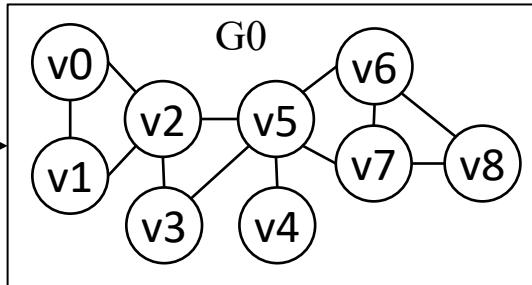
 $R(u_1, u_2)$

v2	v3
v3	v2
v6	v7
v7	v6

 \bowtie \bowtie $=$ $R(u_0, u_1, u_2)$

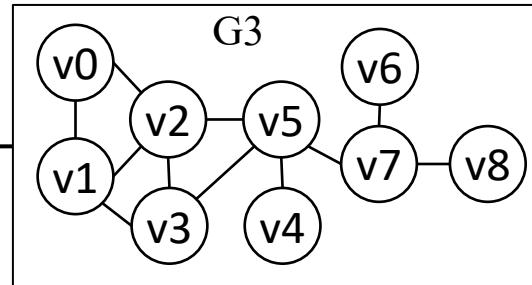
v5	v6	v7
v5	v7	v6
v5	v2	v3
v5	v3	v2
v8	v6	v7
v8	v7	v6

$$\Delta G_0 = (v_1 v_3, +)$$



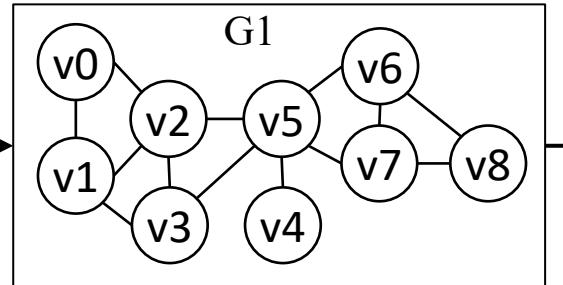
$$M_0 = \{v_5 v_6 v_7, v_8 v_6 v_7, v_5 v_2 v_3\}$$
$$\Delta M_0 = \{ +v_1 v_2 v_3 \}$$

$$\Delta G_3 = [\dots]$$



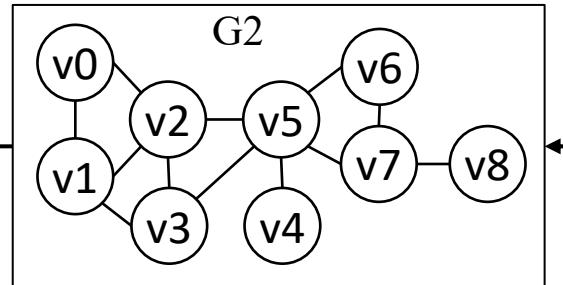
$$M_3 = \{v_5 v_2 v_3, v_1 v_2 v_3\}$$
$$\Delta M_2 = \{ \dots \}$$

$$\Delta G_1 = (v_6 v_8, -)$$



$$M_1 = \{v_5 v_6 v_7, v_8 v_6 v_7, v_5 v_2 v_3, v_1 v_2 v_3\}$$
$$\Delta M_1 = \{ -v_8 v_6 v_7 \}$$

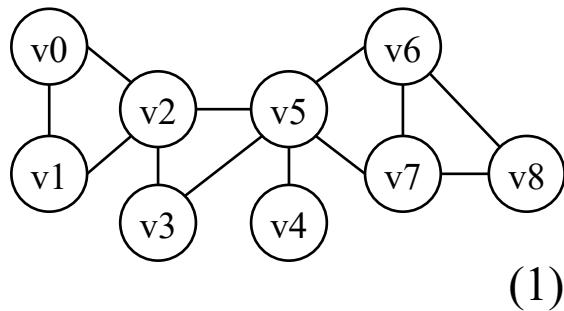
$$\Delta G_2 = (v_5 v_6, -)$$



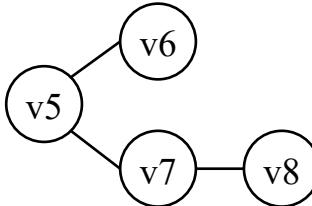
$$M_2 = \{v_5 v_6 v_7, v_5 v_2 v_3, v_1 v_2 v_3\}$$
$$\Delta M_2 = \{ -v_5 v_6 v_7 \}$$

...

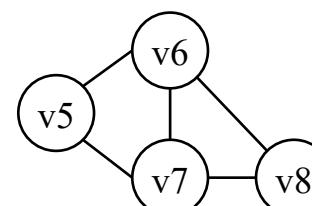
Data Graph G



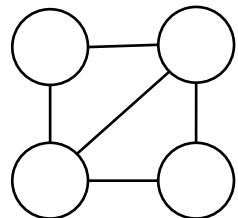
An edge-induced
subgraph of G



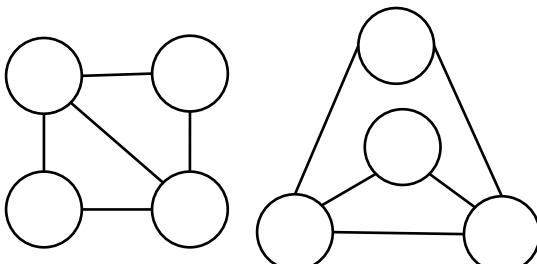
A vertex-induced
subgraph of G



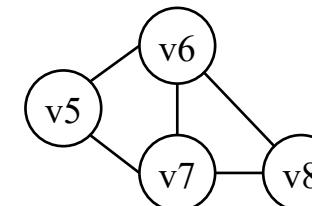
Query Graph Q

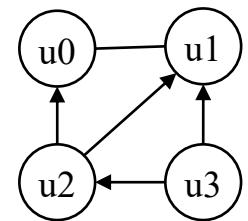


Two isomorphisms of Q

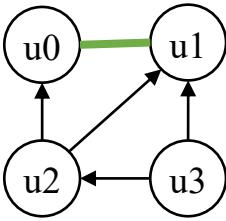


Subgraph in G that
is isomorphic to Q

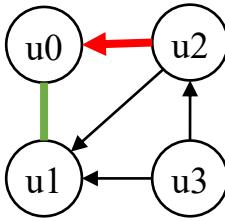




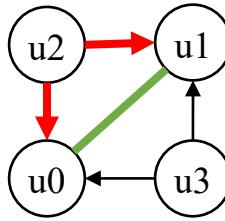
Schedule (0)



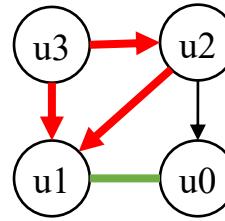
Schedule (1)



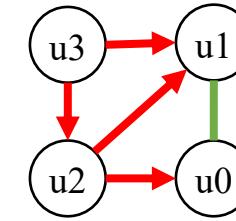
Schedule (2)



Schedule (3)



Schedule (4)



Schedule (5)

atching Order: {u0, u1, u2, u3}
r(v0, v1 ∈ All Edges in Graph){
for(v2 ∈ N(v0) ∩ N(v1)){
for(v3 ∈ N(v1) ∩ N(v2)) {
output (v0, v1, v2, v3) }}}}

(0)

$\Delta R1 \bowtie R2 \bowtie R3 \bowtie R4 \bowtie R5$

(1)

Matching Order: {u0, u1, u2, u3}

for(v0, v1 ∈ New Edge Set){
for(v2 ∈ N(v0) ∩ N(v1)){
for(v3 ∈ N(v1) ∩ N(v2)) {
output (v0, v1, v2, v3) }}}}

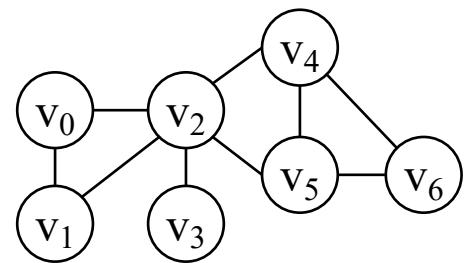
Matching Order: {u0, u2, u1, u3} (2)
for(v0, v1 ∈ New Edge Set){
for(v2 ∈ NN(v0) ∩ N(v1)){
for(v3 ∈ N(v1) ∩ N(v2)) {
output (v0, v1, v2, v3) }}} (4)

Matching Order: {u3, u2, u1, u0}
for(v0, v1 ∈ New Edge Set){
for(v2 ∈ N(v0) ∩ NN(v1)){
for(v3 ∈ NN(v1) ∩ NN(v2)) {
output (v0, v1, v2, v3) }}}}

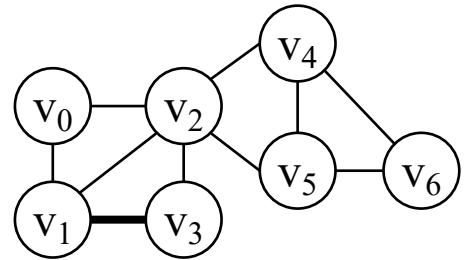
Matching Order: {u2, u1, u0, u3} (3)
for(v0, v1 ∈ New Edge Set){
for(v2 ∈ NN(v0) ∩ NN(v1)){
for(v3 ∈ N(v0) ∩ N(v1)) {
output (v0, v1, v2, v3) }}} (5)

Matching Order: {u3, u1, u2, u0}
for(v0, v1 ∈ New Edge Set){
for(v2 ∈ NN(v0) ∩ NN(v1)){
for(v3 ∈ NN(v1) ∩ NN(v2)) {
output (v0, v1, v2, v3) }}}}

Initial: $\{v_2, v_4, v_5, v_6\}$



$+ \{v_0, v_1, v_2, v_3\}$



- $\{v_2, v_4, v_5, v_6\}$

