

```
UpdateGraph (Batch) ;  
for (edge ∈ Batch) {  
    if (edge maps (u0, u1) ) M1 (u0, u1)  
    if (edge maps (u0, u2) ) M2 (u0, u2)  
    if (edge maps (u0, u3) ) M3 (u0, u3)  
    if (edge maps (u1, u3) ) M4 (u1, u3)  
    if (edge maps (u2, u3) ) M5 (u2, u3) }
```

// $\Delta M1 = \Delta R1 \bowtie R'2 \bowtie R'3 \bowtie R'4 \bowtie R'5$

void $\Delta M1$ (x0, x1) {

 // $\bowtie R'2$ (vertex u2)

 for (x2 \in $N'(x0)$) {

 // $\bowtie R'3 \bowtie R'4 \bowtie R'5$ (vertex u3)

 for (x3 \in $N'(x0) \cap N'(x1) \cap N'(x2)$) {

 output(x0, x1, x2, x3); } } }

```
//  $\Delta M2 = R1 \bowtie \Delta R2 \bowtie R'3 \bowtie R'4 \bowtie R'5$ 
```

```
void  $\Delta M2$  (x0, x2) {
```

```
    //  $\bowtie R1$  (vertex u1)
```

```
    for (x1  $\in$  N(x0)) {
```

```
        //  $\bowtie R'3 \bowtie R'4 \bowtie R'5$  (vertex u3)
```

```
        for (x3  $\in$  N'(x0)  $\cap$  N'(x1)  $\cap$  N'(x2)) {
```

```
            output(x0, x1, x2, x3); } } }
```

```
//  $\Delta M3 = R1 \bowtie R2 \bowtie \Delta R3 \bowtie R'4 \bowtie R'5$ 
```

```
void  $\Delta M3$  (x0, x3) {
```

```
//  $\bowtie R1 \bowtie R'4$  (vertex u1)
```

```
for (x1  $\in$  N(x0)  $\cap$  N'(x3)) {
```

```
//  $\bowtie R2 \bowtie R'5$  (vertex u2)
```

```
for (x2  $\in$  N(x0)  $\cap$  N'(x3)) {
```

```
    output(x0, x1, x2, x3); } } }
```

```
//  $\Delta M4 = R1 \bowtie R2 \bowtie R3 \bowtie \Delta R4 \bowtie R'5$ 
```

```
void  $\Delta M4$  (x1, x3) {
```

```
    //  $\bowtie R1 \bowtie R3$  (vertex u0)
```

```
    for (x0  $\in$  N(x1)  $\cap$  N(x3) ) {
```

```
        //  $\bowtie R2 \bowtie R'5$  (vertex u2)
```

```
        for (x2  $\in$  N(x0)  $\cap$  N'(x3) ) {
```

```
            output(x0, x1, x2, x3); } } }
```

```
//  $\Delta M5 = R1 \bowtie R2 \bowtie R3 \bowtie R4 \bowtie \Delta R5$ 
```

```
void  $\Delta M5$  (x2, x3) {
```

```
    //  $\bowtie R2 \bowtie R3$  (vertex u0)
```

```
    for (x0  $\in$  N(x2)  $\cap$  N(x3)) {
```

```
        //  $\bowtie R1 \bowtie R4$  (vertex u1)
```

```
        for (x1  $\in$  N(x0)  $\cap$  N(x3)) {
```

```
            output(x0, x1, x2, x3); } } }
```