

72. Test for convergence: $\sum_1 \frac{1^3+2^3+\dots+n^3}{(n+1)!}$

73. Discuss convergence:

a) $\sum_1 \left[\frac{1 \cdots (2n-1)}{2 \cdots (2n)} \right]^p$ b) $\sum_1 \left| \frac{1 \cdots (2n-1)}{2 \cdots (2n)} \frac{4n+3}{2n+2} \right|^2$

74. Test for convergence:

a) $\sum_1 \frac{1}{(2n-1)(2n+1)}$ b) $\sum_1 \frac{1}{1+e^{1/n}}$

75. Test for convergence by comparison:

a) $\sum_2 \frac{1}{n^3-1}$ b) $\sum_1 \frac{\sin n}{n^3}$ c) $\sum_0 \frac{n+5}{n^2-3n-5}$ d) $\sum_2 \frac{1}{\sqrt{n} \ln n}$

76. Show convergence of

a) $\sum_0 e^{-a_n}$ b) $\sum_0 \ln(1 - \frac{1}{a_n})$

where $a_n > 0$ and $a_n \rightarrow \infty$.

77. Find the sums:

a) $\sum_{(1)} \frac{1}{(2n+1)(2p+2n+1)}$ b) $\sum_1 \frac{n(n+1)}{(n+2)(n+3)(n+4)(n+5)}$
 $, (p \in \mathbb{N})$

78. Test for convergence:

a) $\sum_0 (\frac{n+1}{n+2}) n^2$ b) $\sum_1 (\frac{(n-1)(n-2)}{n^2}) n^2$

79. If $\sum u_n, \sum v_n$ are series of positive terms, show that

a) $\sum G_n$ b) $\sum H_n$

are convergent, where H_n, G_n are geometric and harmonic means of u_n, v_n respectively.

80. Test for convergence:

a) $\sum_1 \frac{1}{a^n + n^{1/a}}$ b) $\sum_1 a \sin \frac{1}{n}, (a \neq 0)$

81. Test for convergence: