

$$\begin{vmatrix} 11-x & -6 & 2 \\ -6 & 10-x & -4 \\ 2 & -4 & 6-x \end{vmatrix} = 0$$

is 6, and find the other two roots.

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17. If $n \in \mathbb{N}$, show that $(b-c)(c-a)(a-b)$ is a factor of

$$\begin{vmatrix} 1 & 1 & 1 \\ a & b & c \\ a^{n+2} & b^{n+2} & c^{n+2} \end{vmatrix}$$

18. If, $\alpha + \beta + \gamma = 2s$, prove

$$\begin{vmatrix} 1 & \cos \gamma & \cos \beta \\ \cos \gamma & 1 & \cos \alpha \\ \cos \beta & \cos \alpha & 1 \end{vmatrix} = 4 \sin s \sin (s - \alpha) \sin (s - \beta) \sin (s - \gamma)$$

19. Show that

$$\begin{vmatrix} 1 & \cos x - \sin x & \cos x + \sin x \\ 1 & \cos y - \sin y & \cos y + \sin y \\ 1 & \cos z - \sin z & \cos z + \sin z \end{vmatrix} = 2 \begin{vmatrix} 1 & \cos x & \sin x \\ 1 & \cos y & \sin y \\ 1 & \cos z & \sin z \end{vmatrix}$$

20. Evaluate the following determinants:

$$\text{a) } \begin{vmatrix} 0 & 0 & 1 & 2 & 3 \\ 0 & 0 & 4 & 5 & 6 \\ -1 & -4 & 0 & 7 & 8 \\ -2 & -5 & -7 & 0 & 9 \\ -3 & -6 & -8 & -9 & 0 \end{vmatrix}$$

$$\text{b) } \begin{vmatrix} 0 & 0 & a & b \\ 0 & 0 & c & d \\ -a & -c & 0 & 0 \\ -b & -d & 0 & 0 \end{vmatrix}$$

(See Example 7 and 8.)

ANSWERS TO EVEN NUMBERED EXERCISES

2. a) $adf + 2bce - ae^2 - dc^2 - fb$

b) -2

4. a) $(a^3 - 1)^2$, b) -575

8. 0

10. $(a - b)^2(2x - a - b)(a + b + 2x)$