

components, while x, y, z (coordinates of P) are scalar components of \vec{OP} .
Let

$$\vec{OP}_1 = x_1i + y_1j + z_1k = [x_1 \quad y_1 \quad z_1]^T$$

$$\vec{OP}_2 = x_2i + y_2j + z_2k = [x_2 \quad y_2 \quad z_2]^T$$

Then we have

$$\vec{OP}_1 + \vec{OP}_2 = (x_1 + x_2)i + (y_1 + y_2)j + (z_1 + z_2)k = [x_1 + x_2 \quad y_1 + y_2 \quad z_1 + z_2]^T$$

by properties of projections.

Also

$$\vec{OP}_1 - \vec{OP}_2 = (x_1 - x_2)i + (y_1 - y_2)j + (z_1 - z_2)k = [x_1 - x_2 \quad y_1 - y_2 \quad z_1 - z_2]^T$$

Accordingly any free vector \vec{AB} extending from the point $A(a_1, a_2, a_3)$ to $B(b_1, b_2, b_3)$ can be written as the position vector

$$\vec{OB} - \vec{OA} = (b_1 - a_1, b_2 - a_2, b_3 - a_3)$$

since $\vec{OA} + \vec{AB} = \vec{OB}$ or $\vec{AB} = \vec{OB} - \vec{OA}$.

When a vector is multiplied by a scalar, its all components being multiplied by the same scalar, we have

$$\lambda\vec{P} = \lambda(x, y, z) = (\lambda x, \lambda y, \lambda z)$$

by the properties of projections.

Observe analogy between matrices and vectors in the operation of addition and multiplication by scalars:

$$[a_1 \quad a_2 \quad a_3] \pm [b_1 \quad b_2 \quad b_3] = [a_1 \pm b_1 \quad a_2 \pm b_2 \quad a_3 \pm b_3],$$

$$\lambda[a_1 \quad a_2 \quad a_3] = [\lambda a_1 \quad \lambda a_2 \quad \lambda a_3].$$