

CHAPTER 1

SEQUENCES AND SERIES

1. SEQUENCES OF NUMBERS

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1.1. DEFINITIONS. if $f : D \rightarrow R$ is a function whose domain D admits the set I_p of consecutive integers $p, p+1, p+2, \dots, n, \dots$ as a subset, then the infinitely many numbers

$$(1.1) \quad f(p), f(p+1), \dots, f(n), \dots$$

written in this order, is called an infinite sequence or simply a sequence, where $f(p), f(p+1), \dots, f(n), \dots$ are called the first term, the second term, \dots , the general term respectively.

¹ For brevity one denotes $f(n)$ usually by a letter with the subscript n , say a_n , and the sequence (1) by

$$(f(n))_p^\infty \text{ or } (a_n)_p^\infty$$

or more simply by

$$(f(n))_p \text{ or } (a_n)_p$$

Examples

$$(n)_1 : 1, 2, 3, \dots, n, \dots$$

$$\left(\frac{n}{n-2}\right)_3 : 3, \frac{4}{2}, \frac{5}{3}, \dots, \frac{n}{n-2}, \dots$$

¹In the book it writes brevity, but it think, it should be brevity