

1. Let  $q_1, \dots, q_n$  be  $n$  values of  $q = f(x)$  for  $n$  direct measurements of  $x_1, \dots, x_n$ , where  $f$  is known function. In this case  $q_i$ 's become *indirect* measurements of  $q$ .

It can be shown that the best value  $\bar{q}$  of  $q$  is  $\bar{q} = f(\bar{x})$  where  $\bar{x}$  and  $\bar{y}$  are the arithmetic means of  $x_i$ 's and  $q_i$ 's respectively.

EXAMPLE 0.1. The length  $l$  of a simple pendulum is measured as 24,8; 25,1; 25,0; 24,8; 25,0; 25,1; 24,7; 25,1 cm. Then

- a) find the best length  $\bar{l}$
- b) find the best period.

**Solution.**

- a)  $\bar{l} = (\sum l_i)/8 = 24,95$  cm,
- b)  $T = \pi\sqrt{l/g} = \pi\sqrt{24,95/g} = 4.99\pi/\sqrt{g}$ .

2. Let  $y$  be related to  $x$  by an unknown function  $f$ , and let  $y_1, \dots, y_n$  be the measured values of  $y$  corresponding to a set of selected values  $x_1, \dots, x_n$  of  $x$ .

When one plots the points  $P_i(x_i, y_i)$  on a rectangular coordinate system  $Oxy$ , we obtain a distribution of  $y$  against  $x$ .

Now the problem is to determine the best function giving this distribution.

The solution of the problem involves the following steps:

- i. from the distribution guess the type of the function as linear, quadratic, exponential,  $\dots$ ,
- ii. write the general form of the function,
- iii. by the use of the MLS, determine the unknown parameters.

