

- function given by the rule $y = |x - 1| - 2|x| + x$ to be
- a) a constant function,
 - b) an invertible function.

Solution.

The given function is the piecewisely defined function:

$$y = \begin{cases} 1 + 2x & \text{if } x \in (-\infty, 0] \\ 1 - 2x & \text{if } x \in (0, 1] \\ -1 & \text{if } x \in (1, \infty). \end{cases}$$

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- a) A domain of restriction is $(1, \infty)$,
- b) A domain of restriction is $(-\infty, 0]$ on which the function is increasing, or $(0, 1]$ on which it is decreasing.

0.1. Operation with functions. Let

$$f: I \rightarrow \mathbb{R}, \quad y = f(x)$$

be a function with domain I. If $c \in \mathbb{R}$, then the function

$$(0.1) \quad cf: I \rightarrow \mathbb{R}, \quad y = (cf)(x) = cf(x)$$

is called a *scalar multiple* of f.

Let now be given two functions

$$f: I \rightarrow \mathbb{R}, \quad y = f(x)$$

$$g: J \rightarrow \mathbb{R}, \quad y = g(x)$$

with non disjoint domain I and J, then f+g, f-g, fg,

¹Corrected: "0)" in the first case of the equation must be closed interval "0]"

²Corrected: Missing element of sign in the third case