

208. Find T, N, B, κ at the given point of the given curve:

- a) $r(t) = e^t \cos t i + e^t \sin t j + e^t k, A(1, 0, 1)$
- b) $r(t) = (1+t)i + (3-t)j + (2t+4)k, B(4, 0, 10)$
- c) $r(t) = 2Ch_{\frac{t}{2}}i + 2Sh_{\frac{t}{2}}j + 2tk, C(2, 0, 0)$

209. Find the equation of the FRENET planes of the curve

$$\vec{r} = \sin 3ti + \cos 3tj + 2t^{\frac{3}{2}}k \text{ at } (0, 1, 0)$$

210. Consider the space curve

$$r : x = \frac{(t-a)^3(t-b)}{t}, y = \frac{(t-a)(t-b)^3}{t}, z = t^3$$

show that if the osculating plane at a point P passes through Q on r , the osculating plane at Q passes through P .

211. Prove that

- a) $(T', T'', T''') = \kappa^3(\kappa\tau' - \kappa'\tau) = \kappa^5 \frac{d}{ds}(\frac{\tau}{\kappa})$
- b) $(B', B'', B''') = \tau^3(\kappa'\tau - \kappa\tau') = \tau^5 \frac{d}{ds}(\frac{\kappa}{\tau})$

212. Prove that

$$B = \dot{r}x\ddot{r}/K\dot{s}^3, N = (\dot{s}\ddot{r} - \ddot{s}\dot{r})/\kappa\dot{s}^2, \kappa^2 = (\ddot{r}^2 - \dot{s}^2)/\dot{s}^4. \text{ and } \tau = (\dot{r}\ddot{r}\ddot{\tau})/\kappa^2\dot{s}^6$$

213. Prove

- a) $r' \cdot r'' = 0, r'r''' = -\kappa^2, r' \cdot r''' = -3\kappa\kappa'$
- b) $r''' \cdot r''' = \kappa'\kappa'' + 2\kappa^3\kappa' + \kappa^2\tau\tau' + \kappa\kappa'\tau^2$
- c) $T' \cdot B' = -K\tau$

214. Squaring $r''' = -\kappa^2\tau + \kappa'N + K\tau B$ obtain

- a) $\tau^3 = \frac{1}{\kappa^2}r'''^2 - \kappa^2 - (\frac{\kappa'}{\kappa})^2$
- b) $r''' = -3\kappa\kappa'T + (\kappa'' - \kappa^3 - KT^2)N + (2K'T + KT')B$

215. Given $r^{(n)} = a_nT + b_nN + c_nB$ show that