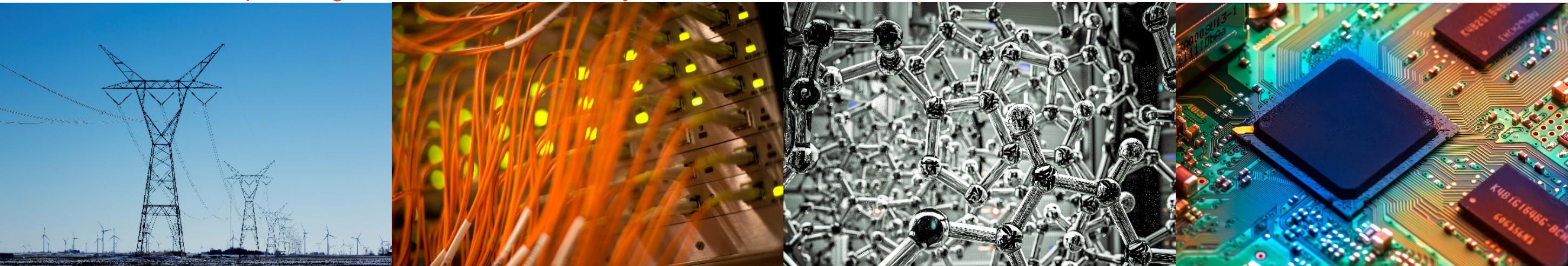


# The role of molecular ions in the overall ionic composition of polar wind outflow

<sup>1</sup>Mei-Yun Lin, <sup>1</sup>Raluca Ilie and <sup>2</sup>Alex Glocer

<sup>1</sup>Department of Electrical and Computer Engineering, University of Illinois at Urbana-Champaign

<sup>2</sup>NASA Goddard Space Flight Center, Greenbelt, Maryland

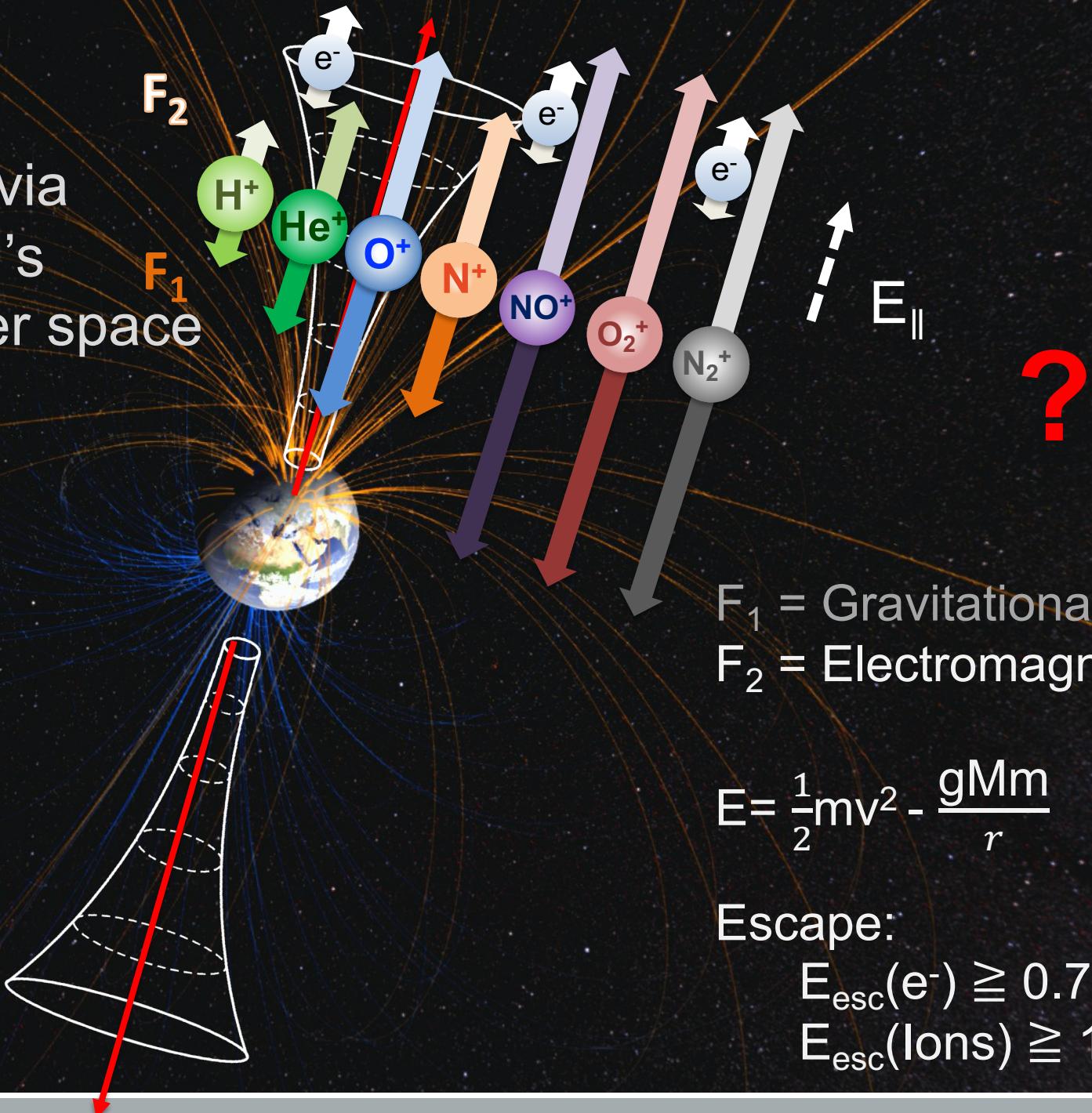


**I ILLINOIS**

Electrical & Computer Engineering

COLLEGE OF ENGINEERING

Ions and electrons escape via open field lines to the Earth's magnetosphere and to outer space



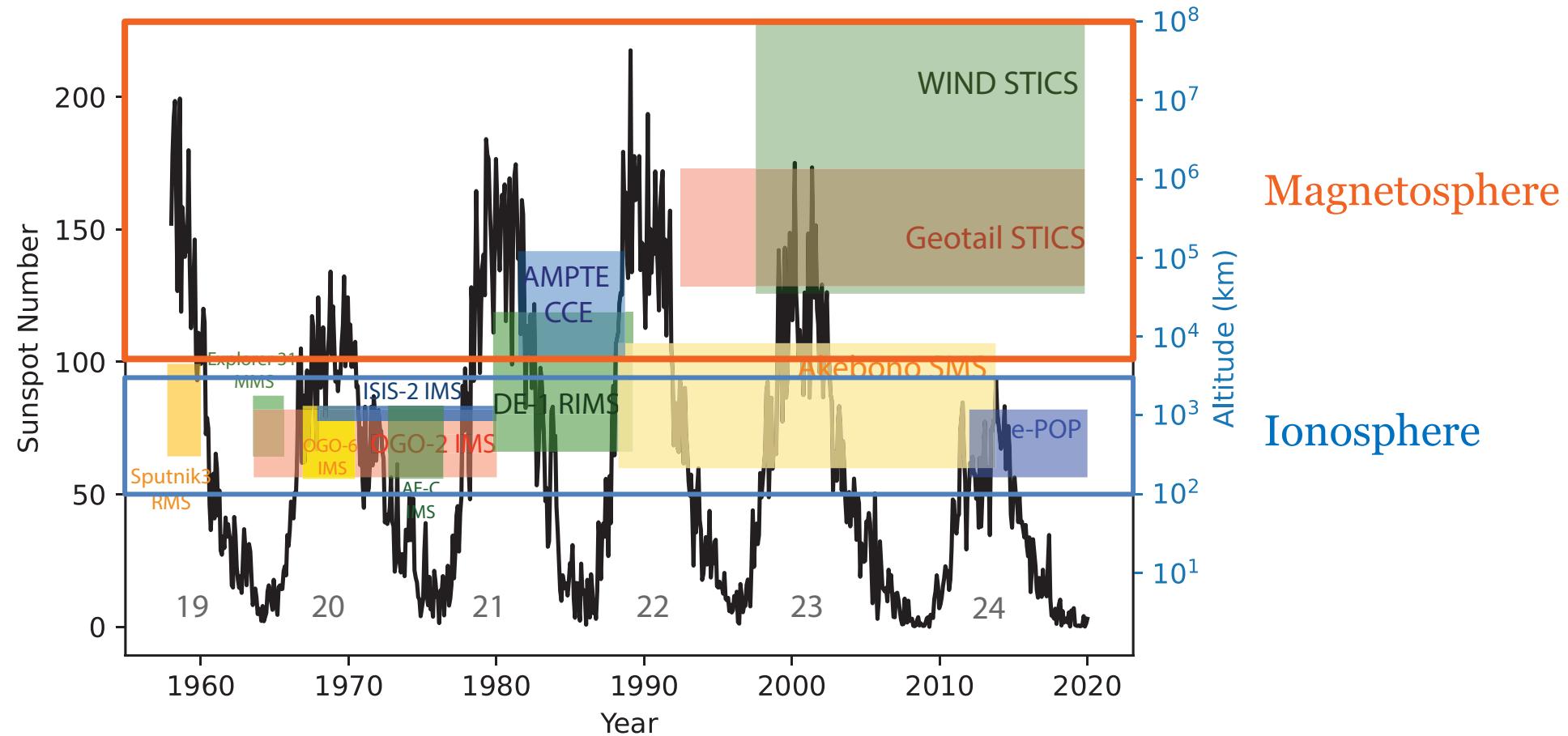
$$E = \frac{1}{2}mv^2 - \frac{gMm}{r}$$

# Escape:

$$E_{\text{esc}}(e^-) \geq 0.7 \text{ eV}$$

$$E_{\text{esc}}(\text{lons}) \geq 10 \text{ eV}$$

# 60 Years of N<sup>+</sup> observation



- The presence of N<sup>+</sup> ions could change plasma characteristics in the inner magnetosphere.

# Polar Wind Outflow Model (referred to as 3iPWOM)

- Chemical & Collisional Scheme
- Suprothermal Electron: GLOW
- Neutral Density: NRLMSISE-90

At each time step, solves for the n, T, v, and  $E_{\parallel}$

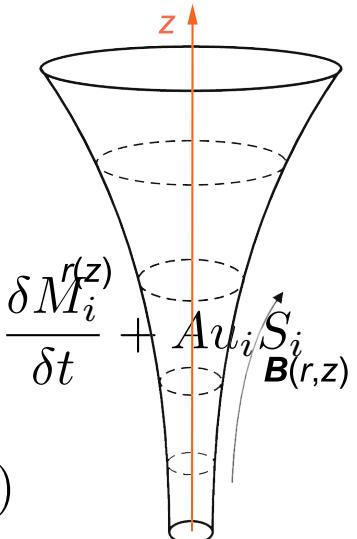
Solves for the **transport** and  $E_{\parallel}$  equations for  $H^+$ ,  $He^+$ ,  $O^+$

$$\frac{\partial}{\partial t}(A\rho_i) + \frac{\partial}{\partial r}(A\rho_i u_i) = AS_i$$

$$\frac{\partial}{\partial t}(A\rho_i u_i) + \frac{\partial}{\partial r}(A\rho_i u_i^2) + A \frac{\partial p_i}{\partial r} = A\rho_i \left( \frac{e}{m_i} E_{\parallel} - g \right) + A \frac{\delta M_i^{r(z)}}{\delta t} + Au_i S_i \mathbf{B}(r,z)$$

$$\begin{aligned} \frac{\partial}{\partial t} \left( \frac{1}{2} A\rho_i u_i^2 + \frac{1}{\gamma_i - 1} Ap_i \right) + \frac{\partial}{\partial r} \left( \frac{1}{2} A\rho_i u_i^3 + \frac{\gamma_i}{\gamma_i - 1} Au_i p_i \right) \\ = A\rho_i u_i \left( \frac{e}{m_i} E_{\parallel} - g \right) + \frac{\partial}{\partial r} \left( A\kappa_i \frac{\partial T_i}{\partial r} \right) + A \frac{\delta E_i}{\delta t} + Au_i \frac{\delta M_i}{\delta t} + \frac{1}{2} Au_i^2 S_i \end{aligned}$$

$$E_{\parallel} = -\frac{1}{en_e} \left[ \frac{\partial}{\partial r} (p_e + \rho_e u_e^2) + \frac{A'}{A} \rho_e u_e^2 \right] + \frac{1}{en_e} \frac{\partial}{\partial r} \left( \sum_i \frac{m_e}{m_i} \left[ (u_e - u_i) S_i - \frac{\delta M_i}{\delta t} \right] + \frac{\delta M_e}{\delta t} \right)$$



# Seven Ion Polar Wind Outflow Model :7iPWOM

- New **Chemical & Collisional Scheme**
- **Suprathermal Electron: GLOW**
- Neutral Density: NRLMSISE-00

At each time step, solves for the n, T, v, and  $E_{\parallel}$

Developed from PWOM (Glocer et al., 2018), 7iPWOM solves Transport Equations and  $E_{\parallel}$  equation for  $H^+$ ,  $He^+$ ,  $N^+$ ,  $O^+$ ,  $N_2^+$ ,  $NO^+$ ,  $O_2^+$

$$\frac{\partial}{\partial t}(A\rho_i) + \frac{\partial}{\partial r}(A\rho_i u_i) = A S_i \quad [1]$$

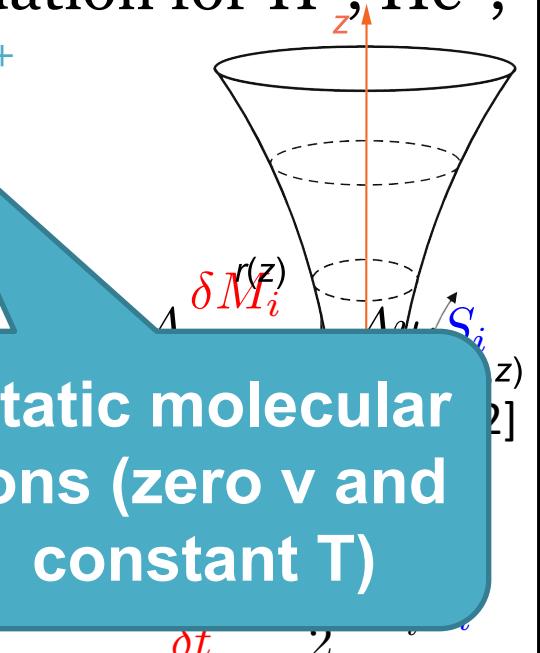
Source term

$$\frac{\partial}{\partial t}(A\rho_i u_i) + \frac{\partial}{\partial r}(A\rho_i u_i^2) + A \frac{\partial p_i}{\partial r} = A\rho_i \left( \frac{e}{m_i} E_{\parallel} - g \right)$$

$$\begin{aligned} \frac{\partial}{\partial t} \left( \frac{1}{2} A\rho_i u_i^2 + \frac{1}{\gamma_i - 1} A p_i \right) + \frac{\partial}{\partial r} \left( \frac{1}{2} A\rho_i u_i^3 + \frac{1}{\gamma_i - 1} A p_i u_i \right) \\ = A\rho_i u_i \left( \frac{e}{m_i} E_{\parallel} - g \right) + \frac{\partial}{\partial r} \left( A\kappa_i \frac{\partial T_i}{\partial r} \right) + A \frac{\partial}{\partial r} \left( \frac{1}{2} A\rho_i u_i^2 \right) \end{aligned}$$

$$E_{\parallel} = -\frac{1}{en_e} \left[ \frac{\partial}{\partial r} (p_e + \rho_e u_e^2) + \frac{A'}{A} \rho_e u_e^2 \right] + \frac{1}{en_e} \left( \sum_i \frac{m_e}{m_i} \left[ (u_e - u_i) S_i - \frac{\delta M_i}{\delta t} \right] + \frac{\delta M_e}{\delta t} \right) \quad [3]$$

Blue: Chemistry Related; Red: Collision Related



*Correct Equation*

# Chemistry and Collisions

3iPWOM  
 $\text{H}^+$ ,  $\text{He}^+$ ,  $\text{O}^+$

Chemistry process	Reaction rate( $\text{cm}^3 \text{s}^{-1}$ )	Reference
$\text{O} + h\nu \longrightarrow \text{O}^+ + e^-$	see text	
$\text{O}_2 + h\nu \longrightarrow \text{O}^+ + \text{O} + e^-$	see text	
$\text{He} + h\nu \longrightarrow \text{He}^+ + e^-$	see text	
$\text{H} + h\nu \longrightarrow \text{H}^+ + e^-$	see text	
$\text{O} + e^* \longrightarrow \text{O}^+ + 2e^-$	see text	
$\text{O}_2 + e^* \longrightarrow \text{O}^+ + \text{O} + 2e^-$	see text	
$\text{He} + e^* \longrightarrow \text{He}^+ + 2e^-$	see text	
$\text{H} + e^* \longrightarrow \text{H}^+ + 2e^-$	see text	
$\text{O}^+ + \text{N}_2 \longrightarrow \text{N} + \text{NO}^+$	$1.2 \times 10^{-12}$	[R. Schunk & Nagy, 2009]
$\text{O}^+ + \text{O}_2 \longrightarrow \text{O}_2^+ + \text{O}$	$2.1 \times 10^{-11}$	[R. Schunk & Nagy, 2009]
$\text{He}^+ + \text{O}_2 \longrightarrow \text{O}^+ + \text{O} + \text{He}$	$9.7 \times 10^{-10}$	[R. Schunk & Nagy, 2009]
$\text{He}^+ + \text{N}_2 \longrightarrow \text{N}_2^+ + \text{He}$	$5.2 \times 10^{-10}$	[R. Schunk & Nagy, 2009]
$\text{He}^+ + \text{N}_2 \longrightarrow \text{N}^+ + \text{N} + \text{He}$	$7.8 \times 10^{-10}$	[R. Schunk & Nagy, 2009]
$\text{H}^+ + \text{O} \longrightarrow \text{H} + \text{O}^+$	$2.2 \times 10^{-11} \times T_e^{0.5}$	[R. Schunk & Nagy, 2009]
$\text{H} + \text{O}^+ \longrightarrow \text{H}^+ + \text{O}$	$2.5 \times 10^{-11} \times T_e^{0.5}$	[R. Schunk & Nagy, 2009]

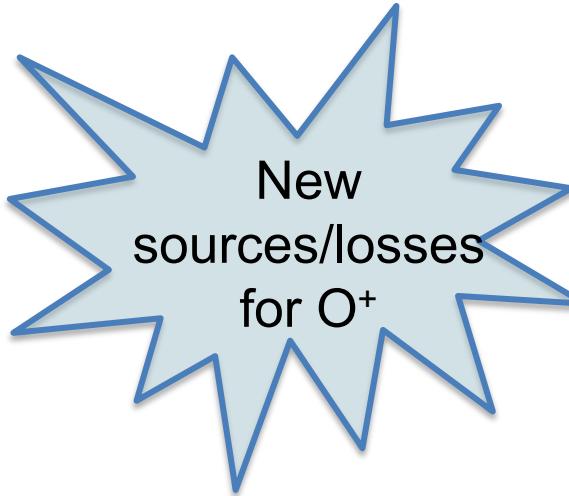
# Chemistry and Collisions

3iPWOM  
 $\text{H}^+$ ,  $\text{He}^+$ ,  $\text{O}^+$

7iPWOM  
 $\text{H}^+$ ,  $\text{He}^+$ ,  $\text{N}^+$ ,  $\text{O}^+$ ,  
 $\text{N}_2^+$ ,  $\text{NO}^+$ ,  $\text{O}_2^+$

Chemistry process	Reaction rate( $\text{cm}^3 \text{s}^{-1}$ )	Reference
$\text{O} + \text{h}\nu \longrightarrow \text{O}^+ + \text{e}^-$	see text	
$\text{O}_2 + \text{h}\nu \longrightarrow \text{O}^+ + \text{O} + \text{e}^-$	see text	
$\text{He} + \text{h}\nu \longrightarrow \text{He}^+ + \text{e}^-$	see text	
$\text{H} + \text{h}\nu \longrightarrow \text{H}^+ + \text{e}^-$	see text	
$\text{O} + \text{e}^* \longrightarrow \text{O}^+ + 2\text{e}^-$	see text	
$\text{O}_2 + \text{e}^* \longrightarrow \text{O}^+ + \text{O} + 2\text{e}^-$	see text	
$\text{He} + \text{e}^* \longrightarrow \text{He}^+ + 2\text{e}^-$	see text	
$\text{H} + \text{e}^* \longrightarrow \text{H}^+ + 2\text{e}^-$	see text	
$\text{O}^+ + \text{N}_2 \longrightarrow \text{N} + \text{NO}^+$	$1.2 \times 10^{-12}$	[R. Schunk & Nagy, 2009]
$\text{O}^+ + \text{O}_2 \longrightarrow \text{O}_2^+ + \text{O}$	$2.1 \times 10^{-11}$	[R. Schunk & Nagy, 2009]
$\text{He}^+ + \text{O}_2 \longrightarrow \text{O}^+ + \text{O} + \text{He}$	$9.7 \times 10^{-10}$	[R. Schunk & Nagy, 2009]
$\text{He}^+ + \text{N}_2 \longrightarrow \text{N}_2^+ + \text{He}$	$5.2 \times 10^{-10}$	[R. Schunk & Nagy, 2009]
$\text{He}^+ + \text{N}_2 \longrightarrow \text{N}^+ + \text{N} + \text{He}$	$7.8 \times 10^{-10}$	[R. Schunk & Nagy, 2009]
$\text{H}^+ + \text{O} \longrightarrow \text{H} + \text{O}^+$	$2.2 \times 10^{-11} \times T_e^{0.5}$	[R. Schunk & Nagy, 2009]
$\text{H} + \text{O}^+ \longrightarrow \text{H}^+ + \text{O}$	$2.5 \times 10^{-11} \times T_e^{0.5}$	[R. Schunk & Nagy, 2009]
$\text{N} + \text{h}\nu \longrightarrow \text{N}^+ + \text{e}^-$	see text	
$\text{N}_2 + \text{h}\nu \longrightarrow \text{N}^+ + \text{N} + \text{e}^-$	see text	
$\text{N}_2 + \text{h}\nu \longrightarrow \text{N}_2^+ + \text{e}^-$	see text	
$\text{O}_2 + \text{h}\nu \longrightarrow \text{O}_2^+ + \text{e}^-$	see text	
$\text{NO} + \text{h}\nu \longrightarrow \text{N}^+ + \text{O} + \text{e}^-$	see text	
$\text{NO} + \text{h}\nu \longrightarrow \text{NO}^+ + \text{e}^-$	see text	
$\text{NO} + \text{h}\nu \longrightarrow \text{O}^+ + \text{N} + \text{e}^-$	see text	
$\text{N}_2 + \text{e}^* \longrightarrow \text{N}_2^+ + 2\text{e}^-$	see text	
$\text{O}_2 + \text{e}^* \longrightarrow \text{O}_2^+ + 2\text{e}^-$	see text	
$\text{N}_2 + \text{e}^* \longrightarrow 2\text{N}^+ + 3\text{e}^-$	see text	
$\text{N}_2 + \text{e}^* \longrightarrow \text{N}^+ + \text{N} + 2\text{e}^-$	see text	
$\text{N}^+ + \text{O}_2 \longrightarrow \text{NO}^+ + \text{O}$	$3.07 \times 10^{-10}$	[R. Schunk & Nagy, 2009]
$\text{N}^+ + \text{O}_2 \longrightarrow \text{O}_2^+ + \text{N}$	$2.32 \times 10^{-10}$	[R. Schunk & Nagy, 2009]
$\text{N}^+ + \text{O}_2 \longrightarrow \text{O}^+ + \text{NO}$	$4.6 \times 10^{-11}$	[R. Schunk & Nagy, 2009]
$\text{N}^+ + \text{NO} \longrightarrow \text{NO}^+ + \text{N}$	$2 \times 10^{-11}$	[Lindinger et al., 1974]
$\text{N}^+ + \text{O} \longrightarrow \text{N} + \text{O}^+$	$2.2 \times 10^{-12}$	[Richards & Voglozin, 2011]
$\text{N}^+ + \text{H} \longrightarrow \text{N} + \text{H}^+$	$3.6 \times 10^{-12}$	[Harada et al., 2010]
$\text{N}_2^+ + \text{N} \longrightarrow \text{N}^+ + \text{N}_2$	$10^{-11}$	[Richards & Voglozin, 2011]
$\text{N}_2^+ + \text{NO} \longrightarrow \text{NO}^+ + \text{N}_2$	$4.1 \times 10^{-10}$	[R. Schunk & Nagy, 2009]
$\text{N}_2^+ + \text{O} \longrightarrow \text{NO}^+ + \text{N}$	$1.3 \times 10^{-10}$	[R. Schunk & Nagy, 2009]
$\text{N}_2^+ + \text{O} \longrightarrow \text{O}^+ + \text{N}_2$	$1.0 \times 10^{-11}$	[R. Schunk & Nagy, 2009]
$\text{N}_2^+ + \text{O}_2 \longrightarrow \text{O}_2^+ + \text{N}_2$	$5.0 \times 10^{-11}$	[R. Schunk & Nagy, 2009]
$\text{O}^+ + \text{NO} \longrightarrow \text{NO}^+ + \text{O}$	$8.0 \times 10^{-13}$	[R. Schunk & Nagy, 2009]
$\text{N}^+ + \text{e}^- \longrightarrow \text{N}$	$3.6 \times 10^{-12} \times (\frac{250}{T_e})^{0.7}$	[R. Schunk & Nagy, 2009]
$\text{N}_2^+ + \text{e}^- \longrightarrow \text{N} + \text{N}$	$2.2 \times 10^{-7} \times (\frac{300}{T_e})^{0.39}$	[R. Schunk & Nagy, 2009]
$\text{NO}^+ + \text{e}^- \longrightarrow \text{N} + \text{O}$	$4.0 \times 10^{-7} \times (\frac{300}{T_e})^{0.5}$	[R. Schunk & Nagy, 2009]
$\text{O}_2^+ + \text{e}^- \longrightarrow \text{O} + \text{O}$	$2.4 \times 10^{-7} \times (\frac{300}{T_e})^{0.7}$	[R. Schunk & Nagy, 2009]

# Chemistry and Collisions



3iPWOM  
 $H^+$ ,  $He^+$ ,  $O^+$

7iPWOM  
 $H^+$ ,  $He^+$ ,  $N^+$ ,  $O^+$ ,  
 $N_2^+$ ,  $NO^+$ ,  $O_2^+$

Chemistry process	Reaction rate( $cm^3 s^{-1}$ )	Reference
$O + h\nu \rightarrow O^+ + e^-$	see text	
$O_2 + h\nu \rightarrow O^+ + O + e^-$	see text	
$He + h\nu \rightarrow He^+ + e^-$	see text	
$H + h\nu \rightarrow H^+ + e^-$	see text	
$O + e^* \rightarrow O^+ + 2e^-$	see text	
$O_2 + e^* \rightarrow O^+ + O + 2e^-$	see text	
$He + e^* \rightarrow He^+ + 2e^-$	see text	
$H + e^* \rightarrow H^+ + 2e^-$	see text	
$O^+ + N_2 \rightarrow N + NO^+$	$1.2 \times 10^{-12}$	[R. Schunk & Nagy, 2009]
$O^+ + O_2 \rightarrow O_2^+ + O$	$2.1 \times 10^{-11}$	[R. Schunk & Nagy, 2009]
$He^+ + O_2 \rightarrow O^+ + O + He$	$9.7 \times 10^{-10}$	[R. Schunk & Nagy, 2009]
$He^+ + N_2 \rightarrow N_2^+ + He$	$5.2 \times 10^{-10}$	[R. Schunk & Nagy, 2009]
$He^+ + N_2 \rightarrow N^+ + N + He$	$7.8 \times 10^{-10}$	[R. Schunk & Nagy, 2009]
$H^+ + O \rightarrow H + O^+$	$2.2 \times 10^{-11} \times T_e^{0.5}$	[R. Schunk & Nagy, 2009]
$H + O^+ \rightarrow H^+ + O$	$2.5 \times 10^{-11} \times T_e^{0.5}$	[R. Schunk & Nagy, 2009]
$N + h\nu \rightarrow N^+ + e^-$	see text	
$N_2 + h\nu \rightarrow N^+ + N + e^-$	see text	
$N_2 + h\nu \rightarrow N_2^+ + e^-$	see text	
$O_2 + h\nu \rightarrow O_2^+ + e^-$	see text	
$NO + h\nu \rightarrow N^+ + O + e^-$	see text	
$NO + h\nu \rightarrow NO^+ + e^-$	see text	
$NO + h\nu \rightarrow O^+ + N + e^-$	see text	
$N_2 + e^* \rightarrow N_2^+ + 2e^-$	see text	
$O_2 + e^* \rightarrow O_2^+ + 2e^-$	see text	
$N_2 + e^* \rightarrow 2N^+ + 3e^-$	see text	
$N_2 + e^* \rightarrow N^+ + N + 2e^-$	see text	
$N^+ + O_2 \rightarrow NO^+ + O$	$3.07 \times 10^{-10}$	[R. Schunk & Nagy, 2009]
$N^+ + O_2 \rightarrow O_2^+ + N$	$2.32 \times 10^{-10}$	[R. Schunk & Nagy, 2009]
$N^+ + O_2 \rightarrow O^+ + NO$	$4.6 \times 10^{-11}$	[R. Schunk & Nagy, 2009]
$N^+ + NO \rightarrow NO^+ + N$	$2 \times 10^{-11}$	[Lindinger et al., 1974]
$N^+ + O \rightarrow N + O^+$	$2.2 \times 10^{-12}$	[Richards & Voglozin, 2011]
$N^+ + H \rightarrow N + H^+$	$3.6 \times 10^{-12}$	[Harada et al., 2010]
$N_2^+ + N \rightarrow N^+ + N_2$	$10^{-11}$	[Richards & Voglozin, 2011]
$N_2^+ + NO \rightarrow NO^+ + N_2$	$4.1 \times 10^{-10}$	[R. Schunk & Nagy, 2009]
$N_2^+ + O \rightarrow NO^+ + N$	$1.3 \times 10^{-10}$	[R. Schunk & Nagy, 2009]
$N_2^+ + O \rightarrow O^+ + N_2$	$1.0 \times 10^{-11}$	[R. Schunk & Nagy, 2009]
$N_2^+ + O_2 \rightarrow O_2^+ + N_2$	$5.0 \times 10^{-11}$	[R. Schunk & Nagy, 2009]
$O^+ + NO \rightarrow NO^+ + O$	$8.0 \times 10^{-13}$	[R. Schunk & Nagy, 2009]
$N^+ + e^- \rightarrow N$	$3.6 \times 10^{-12} \times (\frac{250}{T_e})^{0.7}$	[R. Schunk & Nagy, 2009]
$N_2^+ + e^- \rightarrow N + N$	$2.2 \times 10^{-7} \times (\frac{300}{T_e})^{0.39}$	[R. Schunk & Nagy, 2009]
$NO^+ + e^- \rightarrow N + O$	$4.0 \times 10^{-7} \times (\frac{300}{T_e})^{0.5}$	[R. Schunk & Nagy, 2009]
$O_2^+ + e^- \rightarrow O + O$	$2.4 \times 10^{-7} \times (\frac{300}{T_e})^{0.7}$	[R. Schunk & Nagy, 2009]

# Chemistry and Collisions

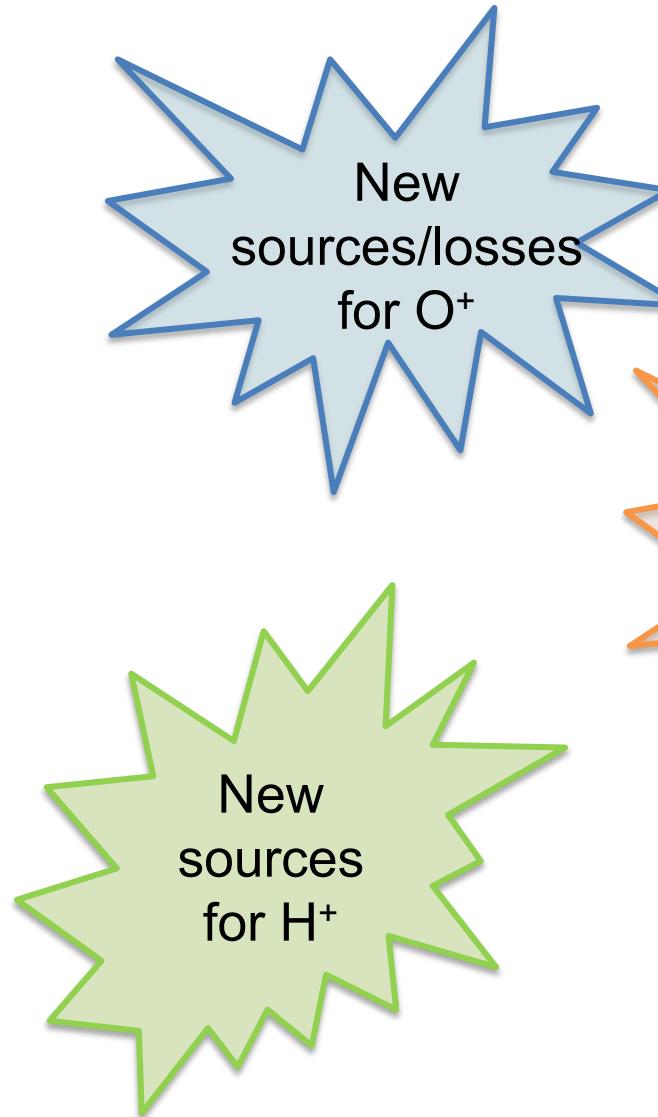


3iPWOM  
 $H^+, He^+, O^+$

7iPWOM  
 $H^+, He^+, N^+, O^+,$   
 $N_2^+, NO^+, O_2^+$

Chemistry process	Reaction rate( $cm^3 s^{-1}$ )	Reference
$O + h\nu \rightarrow O^+ + e^-$	see text	[R. Schunk & Nagy, 2009]
$O_2 + h\nu \rightarrow O^+ + O + e^-$	see text	[R. Schunk & Nagy, 2009]
$He + h\nu \rightarrow He^+ + e^-$	see text	[R. Schunk & Nagy, 2009]
$H + h\nu \rightarrow H^+ + e^-$	see text	[R. Schunk & Nagy, 2009]
$O + e^* \rightarrow O^+ + 2e^-$	see text	[R. Schunk & Nagy, 2009]
$O_2 + e^* \rightarrow O^+ + O + 2e^-$	see text	[R. Schunk & Nagy, 2009]
$He + e^* \rightarrow He^+ + 2e^-$	see text	[R. Schunk & Nagy, 2009]
$H + e^* \rightarrow H^+ + 2e^-$	see text	[R. Schunk & Nagy, 2009]
$O^+ + N_2 \rightarrow N + NO^+$	$1.2 \times 10^{-12}$	[R. Schunk & Nagy, 2009]
$O^+ + O_2 \rightarrow O_2^+ + O$	$2.1 \times 10^{-11}$	[R. Schunk & Nagy, 2009]
$He^+ + O_2 \rightarrow O^+ + O + He$	$9.7 \times 10^{-10}$	[R. Schunk & Nagy, 2009]
$He^+ + N_2 \rightarrow N_2^+ + He$	$5.2 \times 10^{-10}$	[R. Schunk & Nagy, 2009]
$He^+ + N_2 \rightarrow N^+ + N + He$	$7.8 \times 10^{-10}$	[R. Schunk & Nagy, 2009]
$H^+ + O \rightarrow H + O^+$	$2.2 \times 10^{-11} \times T_e^{0.5}$	[R. Schunk & Nagy, 2009]
$H + O^+ \rightarrow H^+ + O$	$2.5 \times 10^{-11} \times T_e^{0.5}$	[R. Schunk & Nagy, 2009]
$N + h\nu \rightarrow N^+ + e^-$	see text	[R. Schunk & Nagy, 2009]
$N_2 + h\nu \rightarrow N^+ + N + e^-$	see text	[R. Schunk & Nagy, 2009]
$N_2 + h\nu \rightarrow N_2^+ + e^-$	see text	[R. Schunk & Nagy, 2009]
$O_2 + h\nu \rightarrow O_2^+ + e^-$	see text	[R. Schunk & Nagy, 2009]
$NO + h\nu \rightarrow N^+ + O + e^-$	see text	[R. Schunk & Nagy, 2009]
$NO + h\nu \rightarrow NO^+ + e^-$	see text	[R. Schunk & Nagy, 2009]
$NO + h\nu \rightarrow O^+ + N + e^-$	see text	[R. Schunk & Nagy, 2009]
$N_2 + e^* \rightarrow N_2^+ + 2e^-$	see text	[R. Schunk & Nagy, 2009]
$O_2 + e^* \rightarrow O_2^+ + 2e^-$	see text	[R. Schunk & Nagy, 2009]
$N_2 + e^* \rightarrow 2N^+ + 3e^-$	see text	[R. Schunk & Nagy, 2009]
$N_2 + e^* \rightarrow N^+ + N + 2e^-$	see text	[R. Schunk & Nagy, 2009]
$N^+ + O_2 \rightarrow NO^+ + O$	$3.07 \times 10^{-10}$	[R. Schunk & Nagy, 2009]
$N^+ + O_2 \rightarrow O_2^+ + N$	$2.32 \times 10^{-10}$	[R. Schunk & Nagy, 2009]
$N^+ + O_2 \rightarrow O^+ + NO$	$4.6 \times 10^{-11}$	[R. Schunk & Nagy, 2009]
$N^+ + NO \rightarrow NO^+ + N$	$2 \times 10^{-11}$	[Lindinger et al., 1974]
$N^+ + O \rightarrow N + O^+$	$2.2 \times 10^{-12}$	[Richards & Voglozin, 2011]
$N^+ + H \rightarrow N + H^+$	$3.6 \times 10^{-12}$	[Harada et al., 2010]
$N_2^+ + N \rightarrow N^+ + N_2$	$10^{-11}$	[Richards & Voglozin, 2011]
$N_2^+ + NO \rightarrow NO^+ + N_2$	$4.1 \times 10^{-10}$	[R. Schunk & Nagy, 2009]
$N_2^+ + O \rightarrow NO^+ + N$	$1.3 \times 10^{-10}$	[R. Schunk & Nagy, 2009]
$N_2^+ + O \rightarrow O^+ + N_2$	$1.0 \times 10^{-11}$	[R. Schunk & Nagy, 2009]
$N_2^+ + O_2 \rightarrow O_2^+ + N_2$	$5.0 \times 10^{-11}$	[R. Schunk & Nagy, 2009]
$O^+ + NO \rightarrow NO^+ + O$	$8.0 \times 10^{-13}$	[R. Schunk & Nagy, 2009]
$N^+ + e^- \rightarrow N$	$3.6 \times 10^{-12} \times (\frac{250}{T_e})^{0.7}$	[R. Schunk & Nagy, 2009]
$N_2^+ + e^- \rightarrow N + N$	$2.2 \times 10^{-7} \times (\frac{300}{T_e})^{0.39}$	[R. Schunk & Nagy, 2009]
$NO^+ + e^- \rightarrow N + O$	$4.0 \times 10^{-7} \times (\frac{300}{T_e})^{0.5}$	[R. Schunk & Nagy, 2009]
$O_2^+ + e^- \rightarrow O + O$	$2.4 \times 10^{-7} \times (\frac{300}{T_e})^{0.7}$	[R. Schunk & Nagy, 2009]

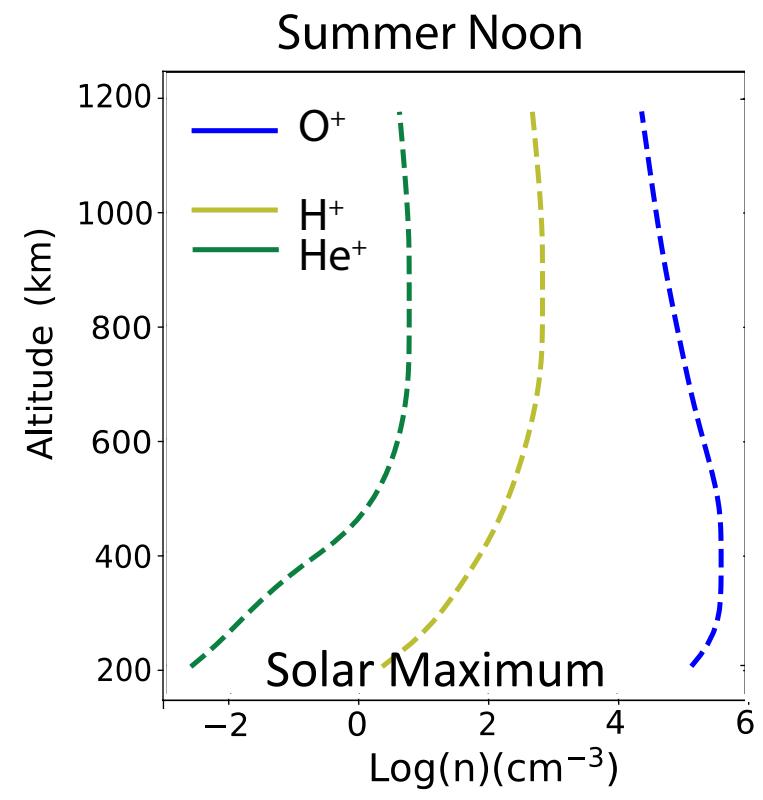
# Chemistry and Collisions



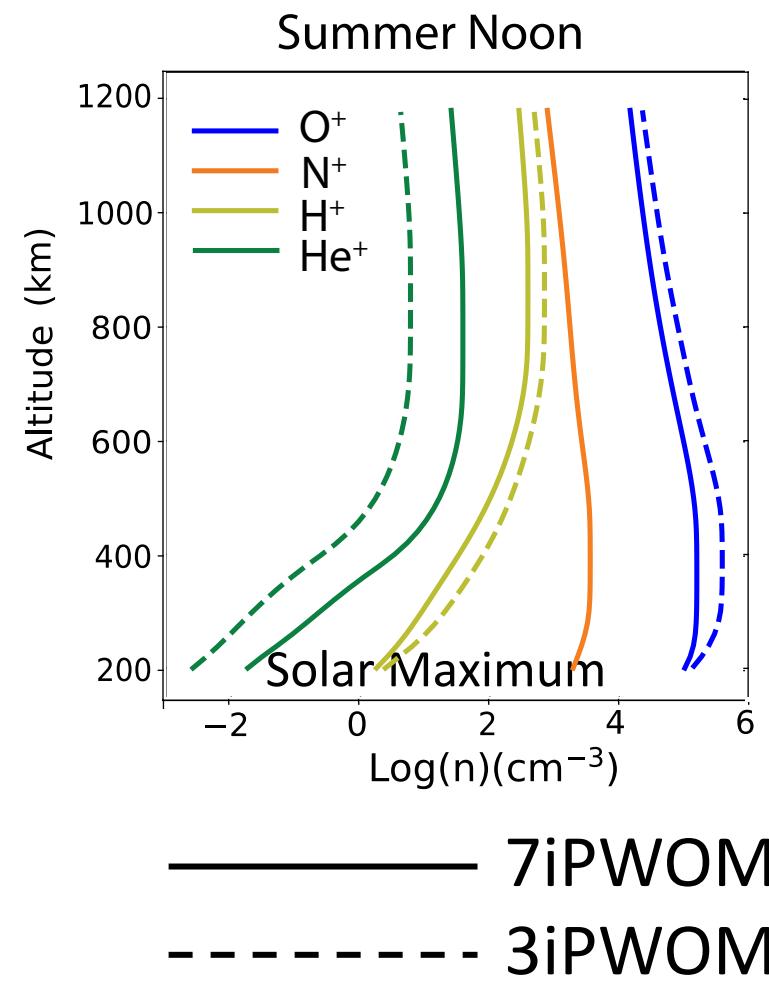
**3iPWOM**  
 $H^+, He^+, O^+$

**7iPWOM**  
 $H^+, He^+, N^+, O^+,$   
 $N_2^+, NO^+, O_2^+$

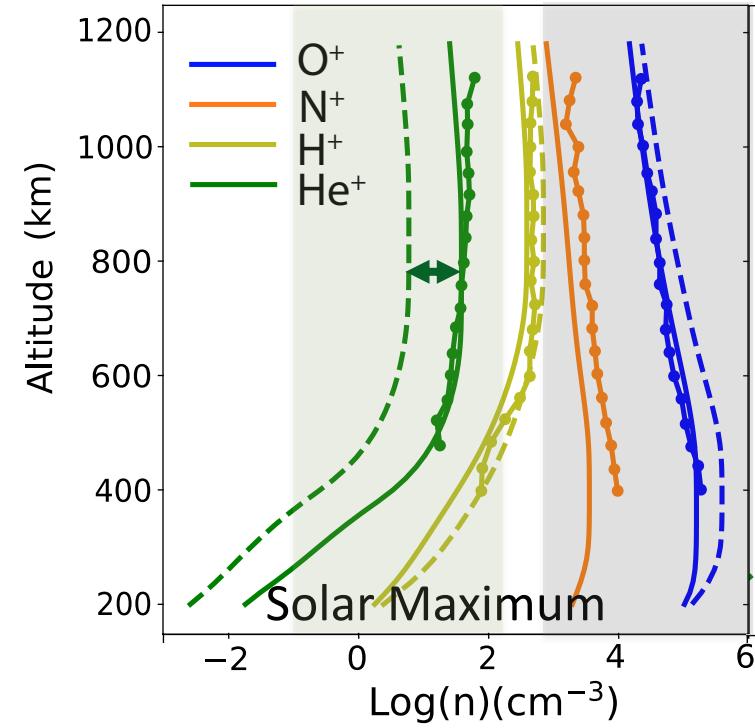
Chemistry process	Reaction rate( $cm^3 s^{-1}$ )	Reference
$O + h\nu \rightarrow O^+ + e^-$	see text	[R. Schunk & Nagy, 2009]
$O_2 + h\nu \rightarrow O^+ + O + e^-$	see text	[R. Schunk & Nagy, 2009]
$He + h\nu \rightarrow He^+ + e^-$	see text	[R. Schunk & Nagy, 2009]
$H + h\nu \rightarrow H^+ + e^-$	see text	[R. Schunk & Nagy, 2009]
$O + e^* \rightarrow O^+ + 2e^-$	see text	[R. Schunk & Nagy, 2009]
$O_2 + e^* \rightarrow O^+ + O + 2e^-$	see text	[R. Schunk & Nagy, 2009]
$He + e^* \rightarrow He^+ + 2e^-$	see text	[R. Schunk & Nagy, 2009]
$H + e^* \rightarrow H^+ + 2e^-$	see text	[R. Schunk & Nagy, 2009]
$O^+ + N_2 \rightarrow N + NO^+$	$1.2 \times 10^{-12}$	[R. Schunk & Nagy, 2009]
$O^+ + O_2 \rightarrow O_2^+ + O$	$2.1 \times 10^{-11}$	[R. Schunk & Nagy, 2009]
$He^+ + O_2 \rightarrow O^+ + O + He$	$9.7 \times 10^{-10}$	[R. Schunk & Nagy, 2009]
$He^+ + N_2 \rightarrow N_2^+ + He$	$5.2 \times 10^{-10}$	[R. Schunk & Nagy, 2009]
$He^+ + N_2 \rightarrow N^+ + N + He$	$7.8 \times 10^{-10}$	[R. Schunk & Nagy, 2009]
$H^+ + O \rightarrow H + O^+$	$2.2 \times 10^{-11} \times T_e^{0.5}$	[R. Schunk & Nagy, 2009]
$H + O^+ \rightarrow H^+ + O$	$2.5 \times 10^{-11} \times T_e^{0.5}$	[R. Schunk & Nagy, 2009]
$N + h\nu \rightarrow N^+ + e^-$	see text	[R. Schunk & Nagy, 2009]
$N_2 + h\nu \rightarrow N^+ + N + e^-$	see text	[R. Schunk & Nagy, 2009]
$N_2 + h\nu \rightarrow N_2^+ + e^-$	see text	[R. Schunk & Nagy, 2009]
$O_2 + h\nu \rightarrow O_2^+ + e^-$	see text	[R. Schunk & Nagy, 2009]
$NO + h\nu \rightarrow N^+ + O + e^-$	see text	[R. Schunk & Nagy, 2009]
$NO + h\nu \rightarrow NO^+ + e^-$	see text	[R. Schunk & Nagy, 2009]
$NO + h\nu \rightarrow O^+ + N + e^-$	see text	[R. Schunk & Nagy, 2009]
$N_2 + e^* \rightarrow N_2^+ + 2e^-$	see text	[R. Schunk & Nagy, 2009]
$O_2 + e^* \rightarrow O_2^+ + 2e^-$	see text	[R. Schunk & Nagy, 2009]
$N_2 + e^* \rightarrow 2N^+ + 3e^-$	see text	[R. Schunk & Nagy, 2009]
$N_2 + e^* \rightarrow N^+ + N + 2e^-$	see text	[R. Schunk & Nagy, 2009]
$N^+ + O_2 \rightarrow NO^+ + O$	$3.07 \times 10^{-10}$	[R. Schunk & Nagy, 2009]
$N^+ + O_2 \rightarrow O_2^+ + N$	$2.32 \times 10^{-10}$	[R. Schunk & Nagy, 2009]
$N^+ + O_2 \rightarrow O^+ + NO$	$4.6 \times 10^{-11}$	[R. Schunk & Nagy, 2009]
$N^+ + NO \rightarrow NO^+ + N$	$2 \times 10^{-11}$	[Lindinger et al., 1974]
$N^+ + O \rightarrow N + O^+$	$2.2 \times 10^{-12}$	[Richards & Voglozin, 2011]
$N^+ + H \rightarrow N + H^+$	$3.6 \times 10^{-12}$	[Harada et al., 2010]
$N_2^+ + N \rightarrow N^+ + N_2$	$10^{-11}$	[Richards & Voglozin, 2011]
$N_2^+ + NO \rightarrow NO^+ + N_2$	$4.1 \times 10^{-10}$	[R. Schunk & Nagy, 2009]
$N_2^+ + O \rightarrow NO^+ + N$	$1.3 \times 10^{-10}$	[R. Schunk & Nagy, 2009]
$N_2^+ + O \rightarrow O^+ + N_2$	$1.0 \times 10^{-11}$	[R. Schunk & Nagy, 2009]
$N_2^+ + O_2 \rightarrow O_2^+ + N_2$	$5.0 \times 10^{-11}$	[R. Schunk & Nagy, 2009]
$O^+ + NO \rightarrow NO^+ + O$	$8.0 \times 10^{-13}$	[R. Schunk & Nagy, 2009]
$N^+ + e^- \rightarrow N$	$3.6 \times 10^{-12} \times (\frac{250}{T_e})^{0.7}$	[R. Schunk & Nagy, 2009]
$N_2^+ + e^- \rightarrow N + N$	$2.2 \times 10^{-7} \times (\frac{300}{T_e})^{0.39}$	[R. Schunk & Nagy, 2009]
$NO^+ + e^- \rightarrow N + O$	$4.0 \times 10^{-7} \times (\frac{300}{T_e})^{0.5}$	[R. Schunk & Nagy, 2009]
$O_2^+ + e^- \rightarrow O + O$	$2.4 \times 10^{-7} \times (\frac{300}{T_e})^{0.7}$	[R. Schunk & Nagy, 2009]



----- 3iPWOM



## Summer Noon

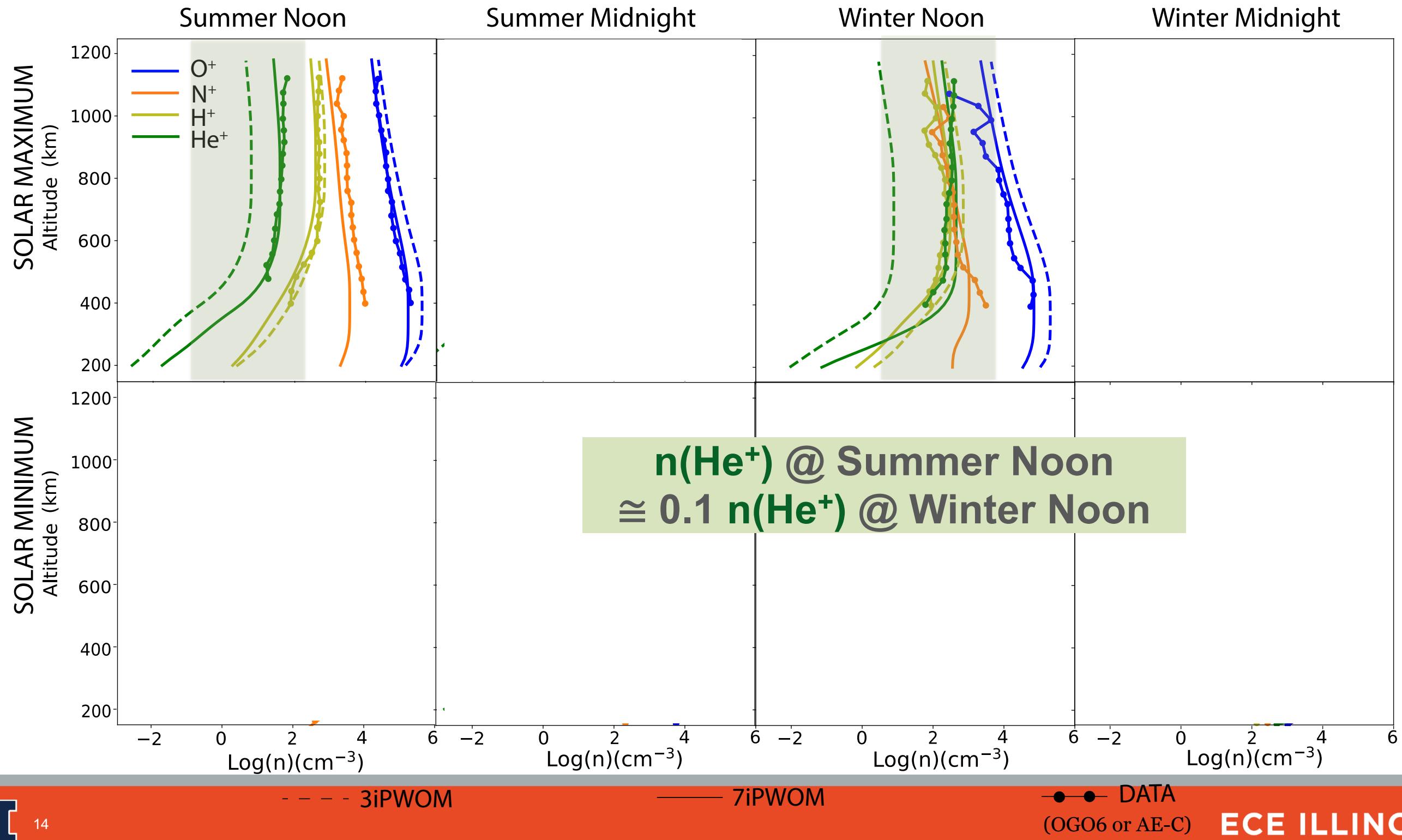


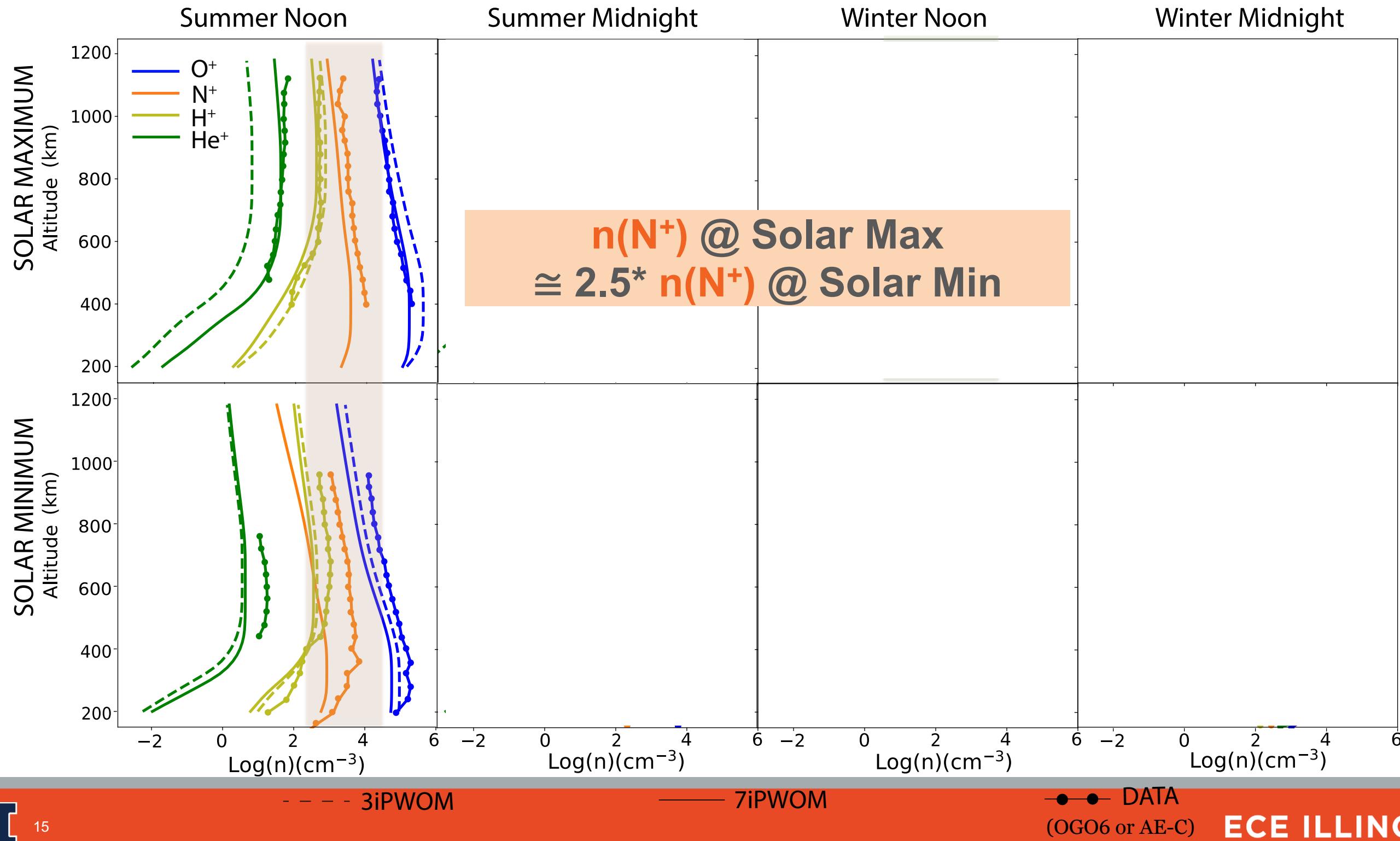
● OGO-6 Data  
— 7iPWOM  
- - - 3iPWOM

- Comparison with observations shows that the presence of  $\text{N}^+$  improves the outflow solution for *all species*.

- $\text{He}^+$  solution shows the biggest improvement, as 7iPWOM predicts a density **one order of magnitude higher than 3iPWOM**, aligned with observations.

$$n(\text{N}^+) \approx 10\% \text{ of } n(\text{O}^+)$$



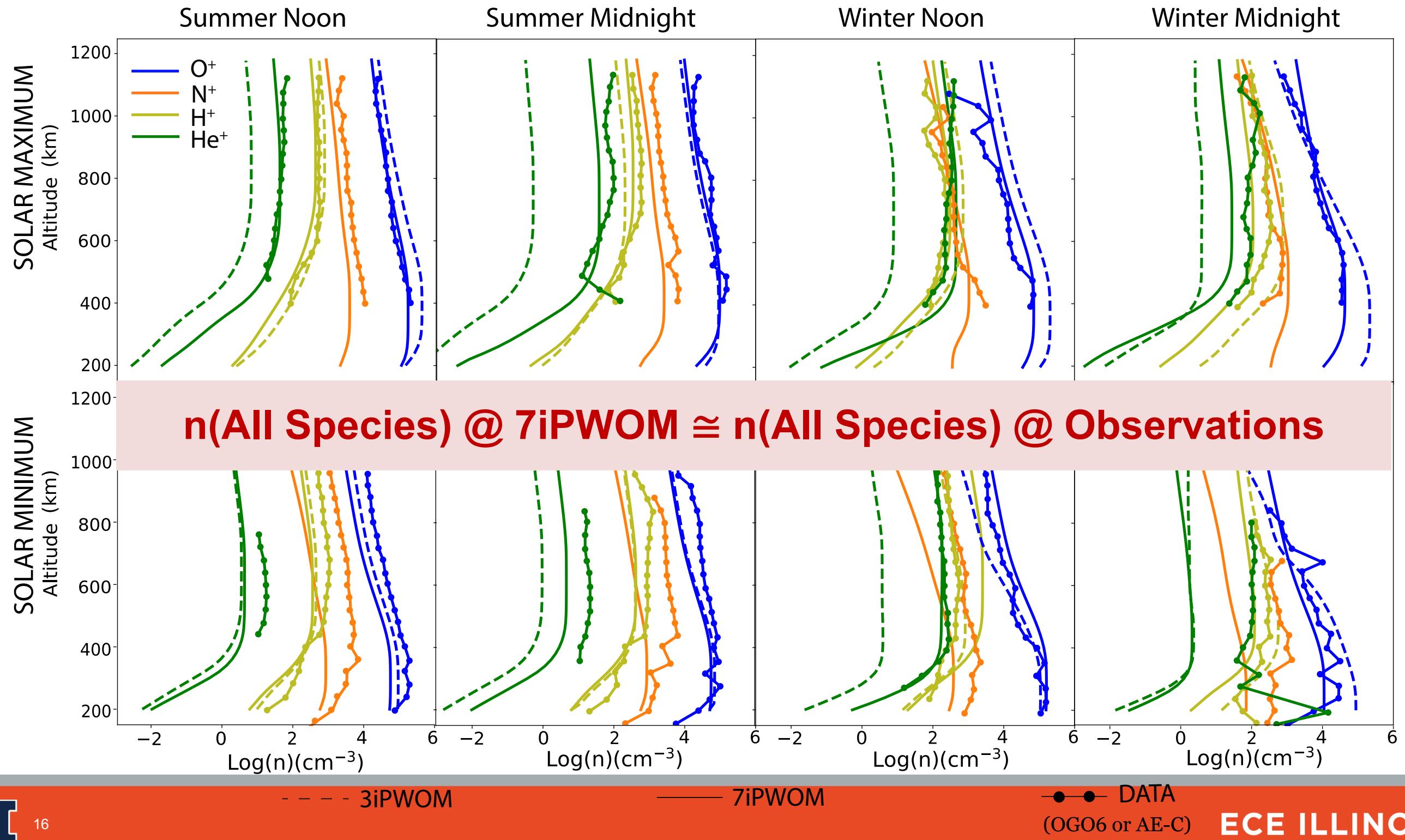


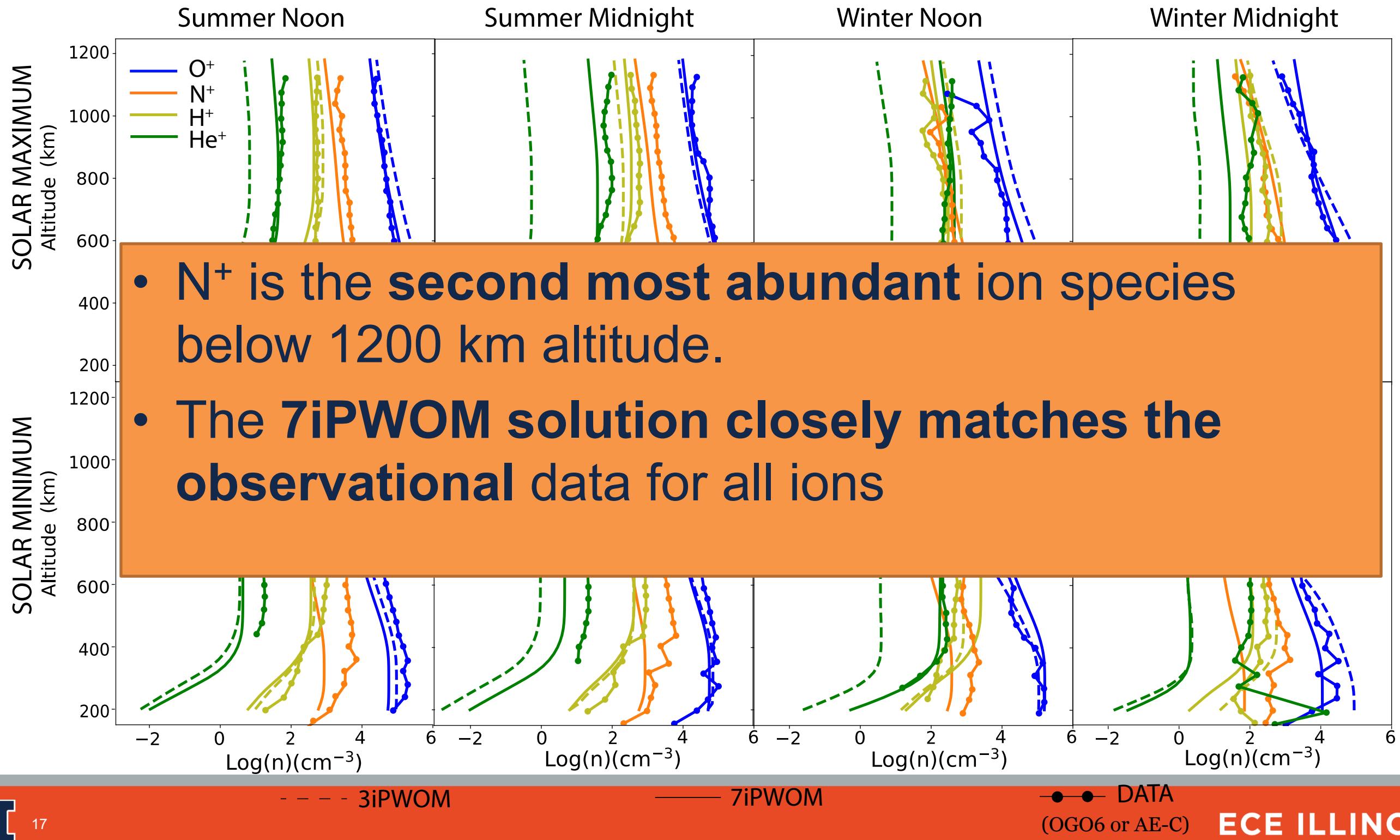
3iPWOM

7iPWOM

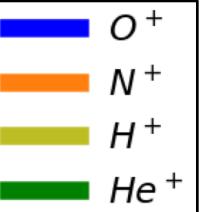
● DATA  
(OGO6 or AE-C)

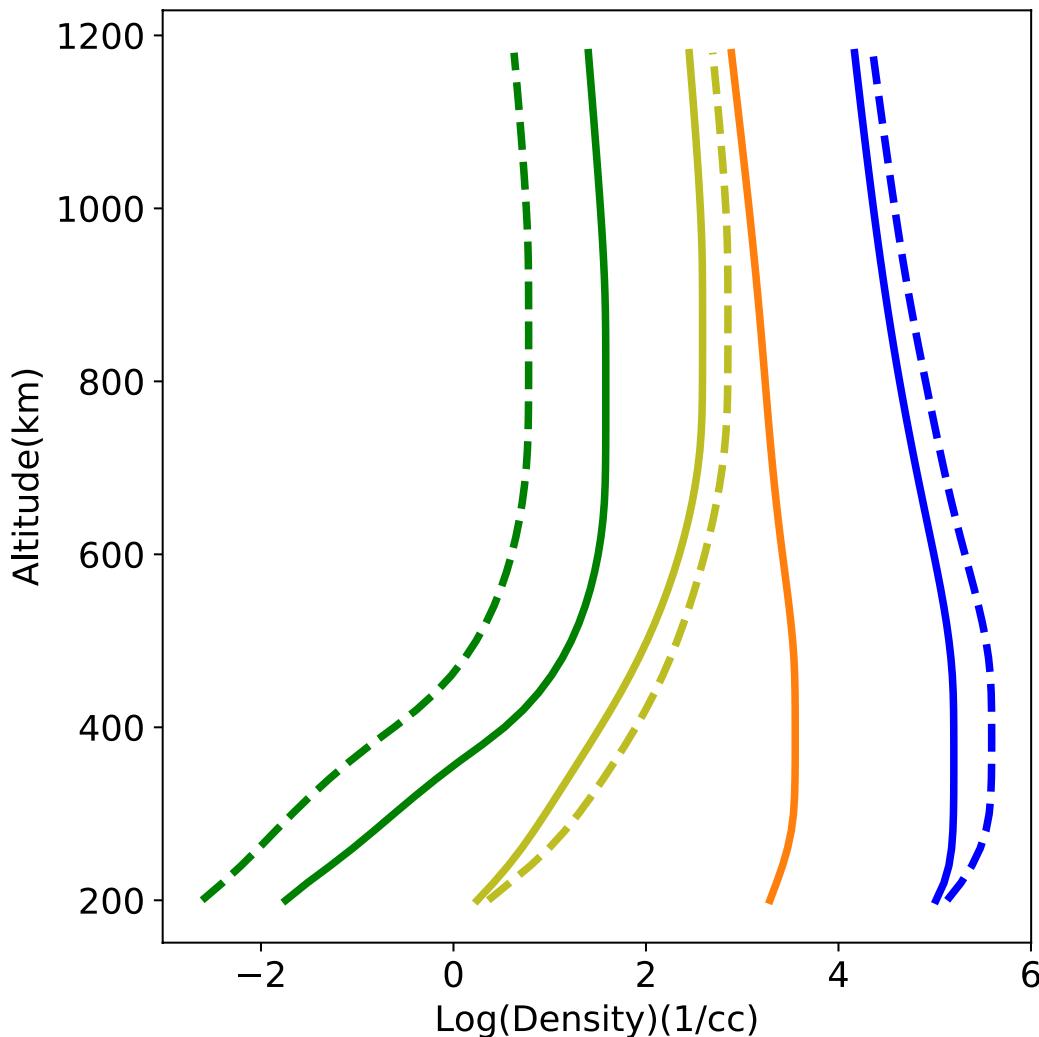
ECE ILLINOIS





# What causes these differences?

  
— : 7iPWOM  
- - - - : 3iPWOM

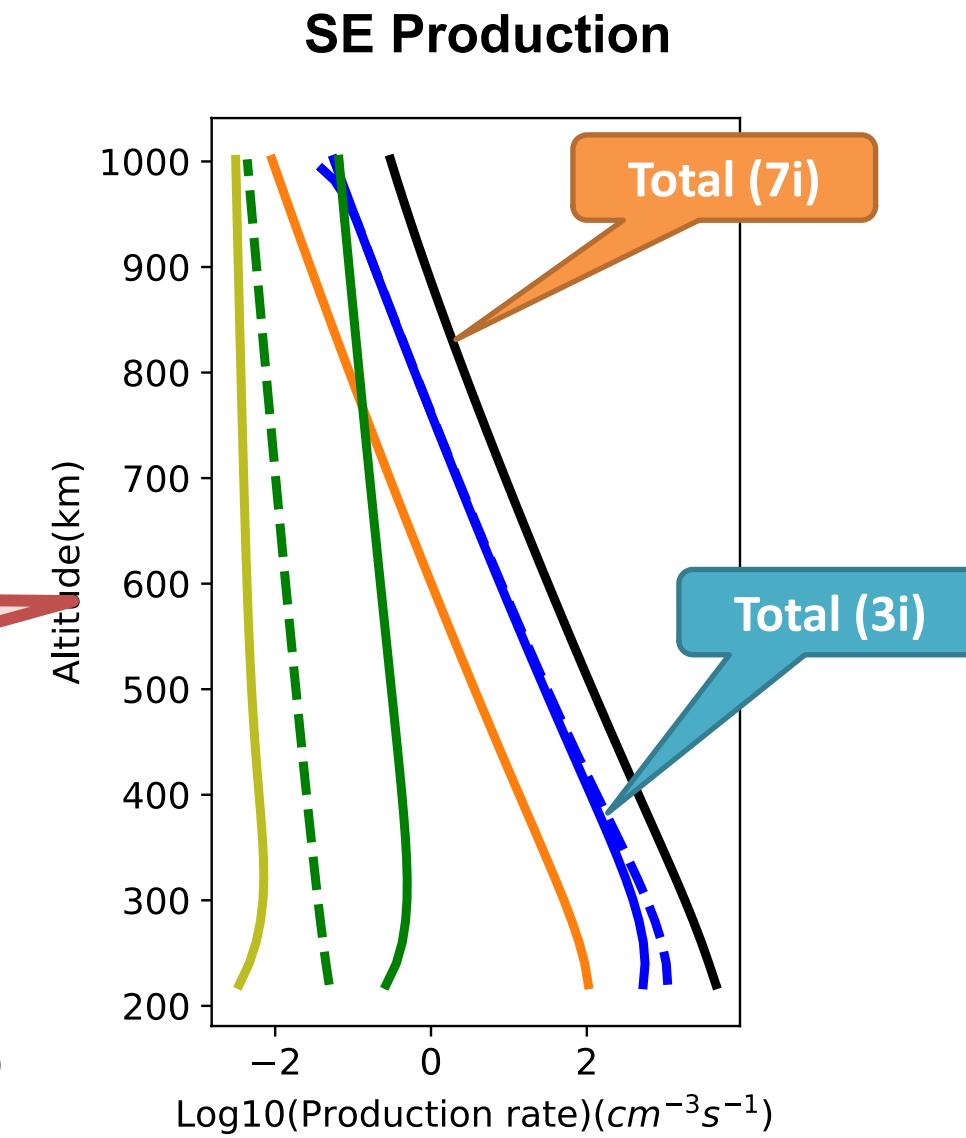
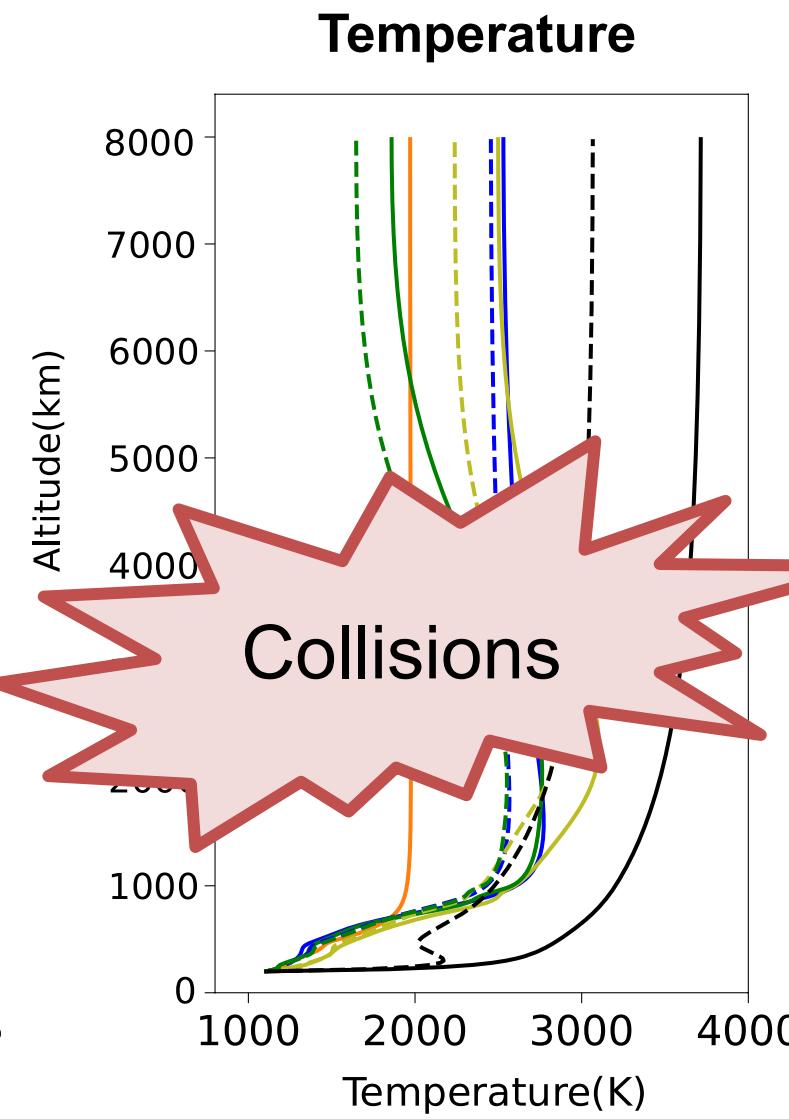
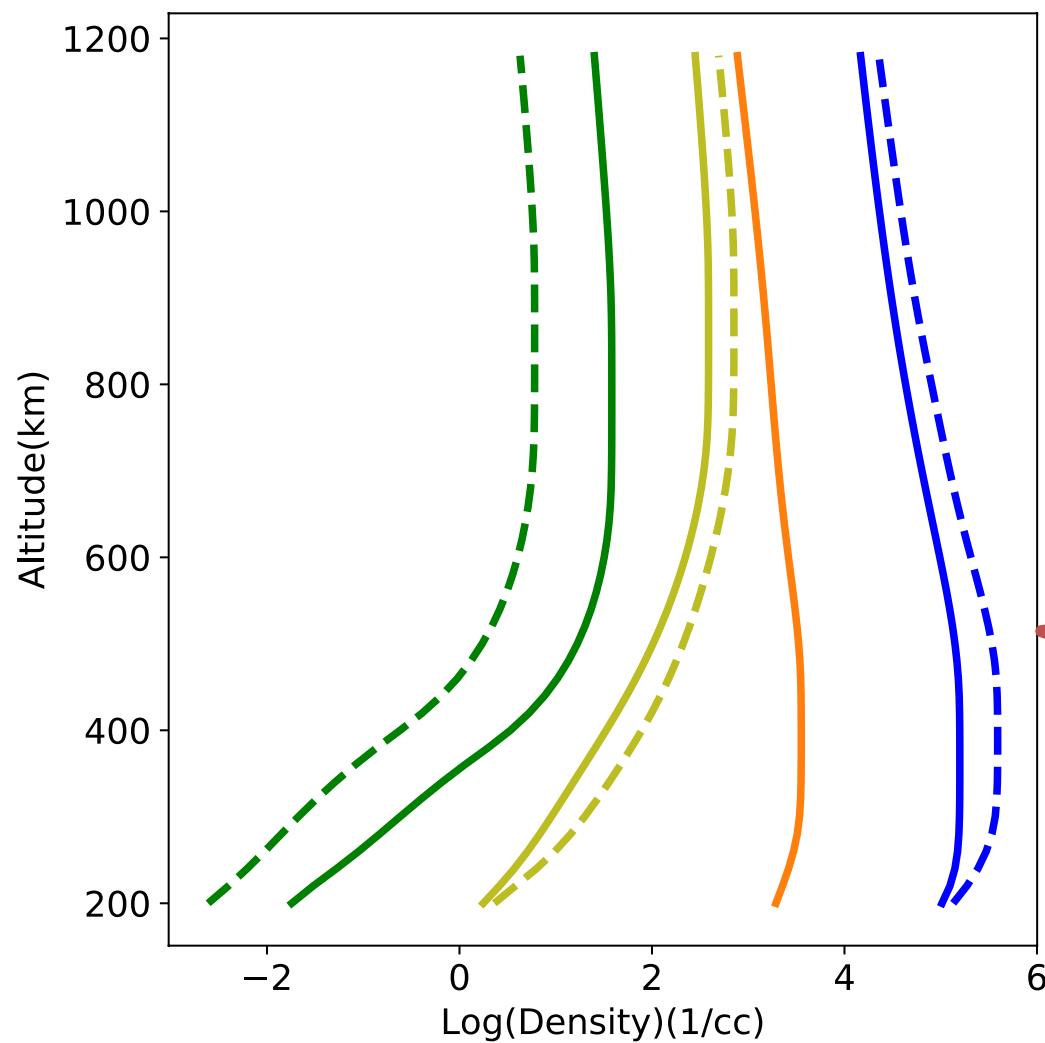


Presence of **N<sup>+</sup>** and molecular species leads to :

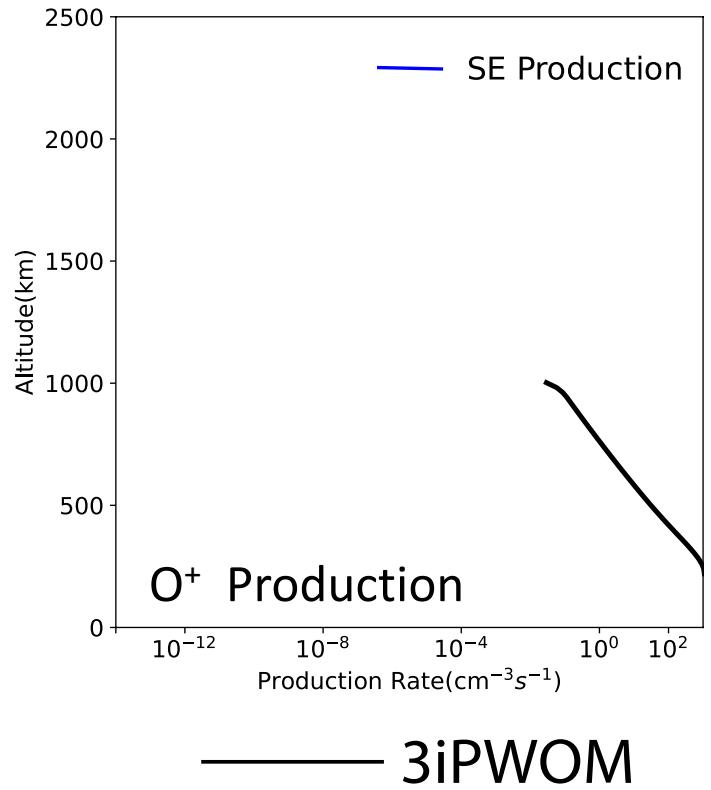
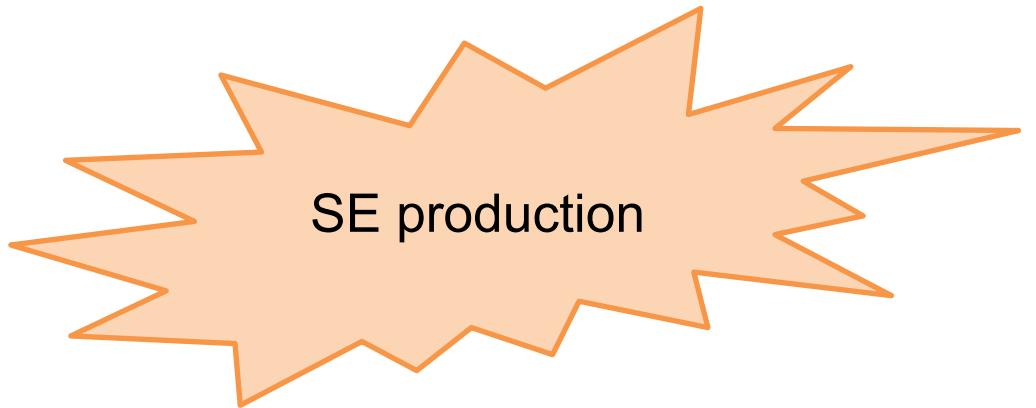
- A significant increase (~1 an order of magnitude) in **He<sup>+</sup>** density.
- **H<sup>+</sup>** solution improves as compared with measurements
- **O<sup>+</sup>** density profile better matches the data, and the density is a factor 2 larger.
- **N<sup>+</sup>** profile matches observations
- **All species show an increase in temperature/energy.**

# What causes these differences?

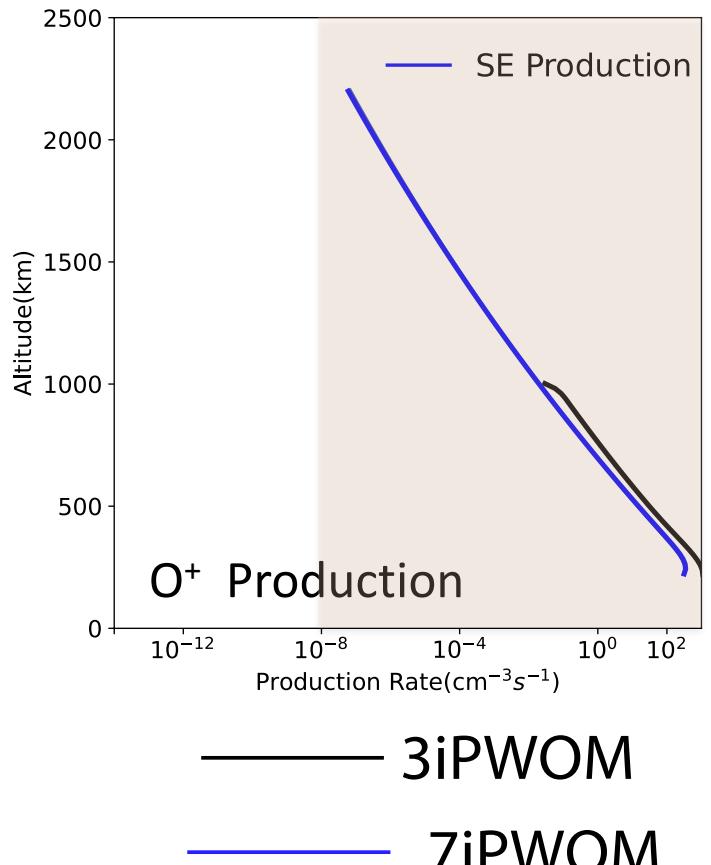
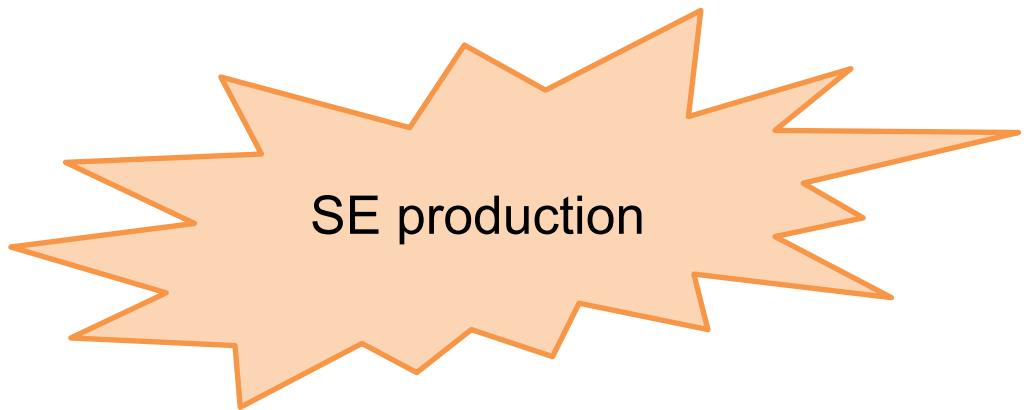
— : 7iPWOM  
--- : 3iPWOM



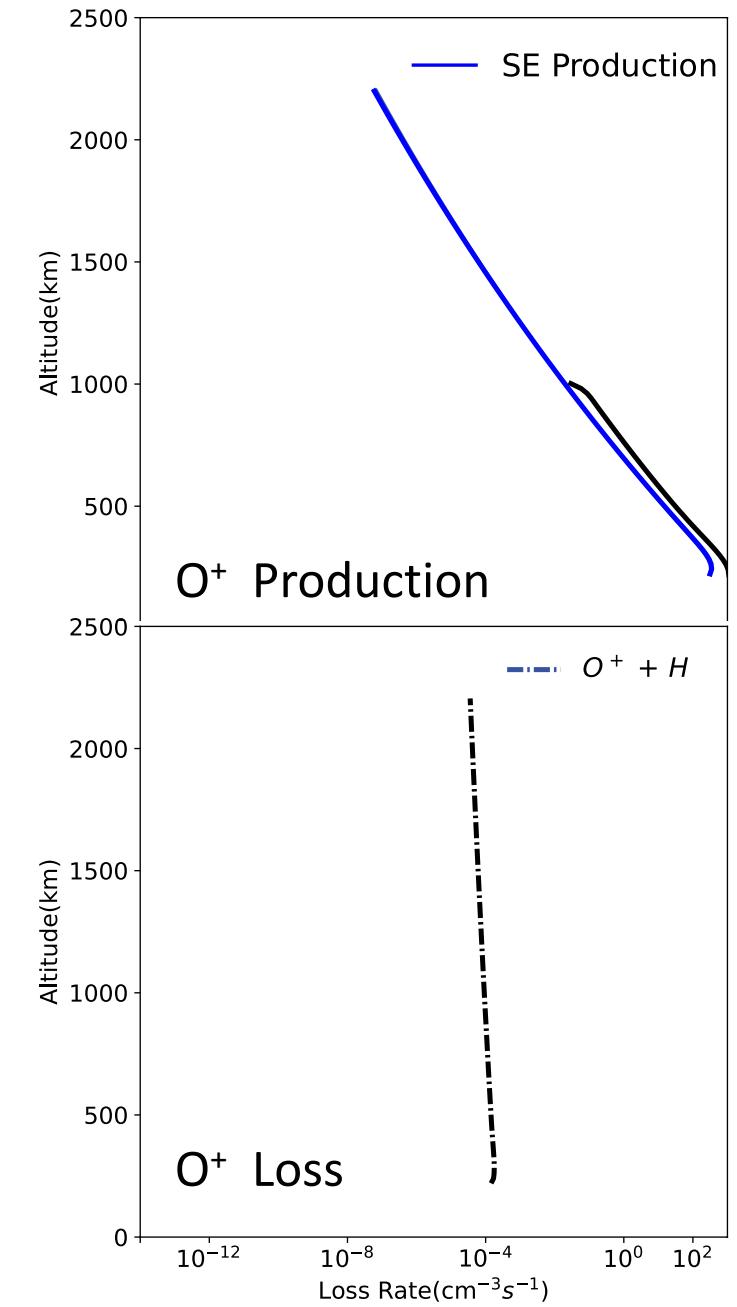
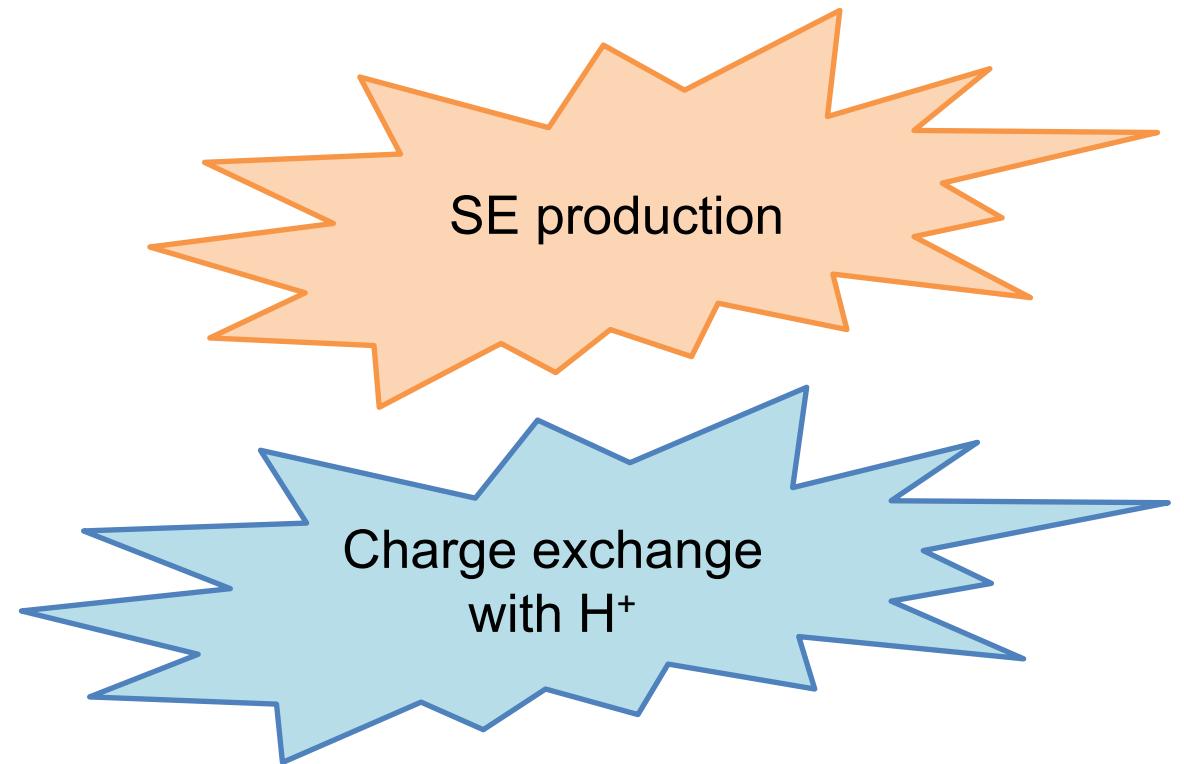
# Chemistry?



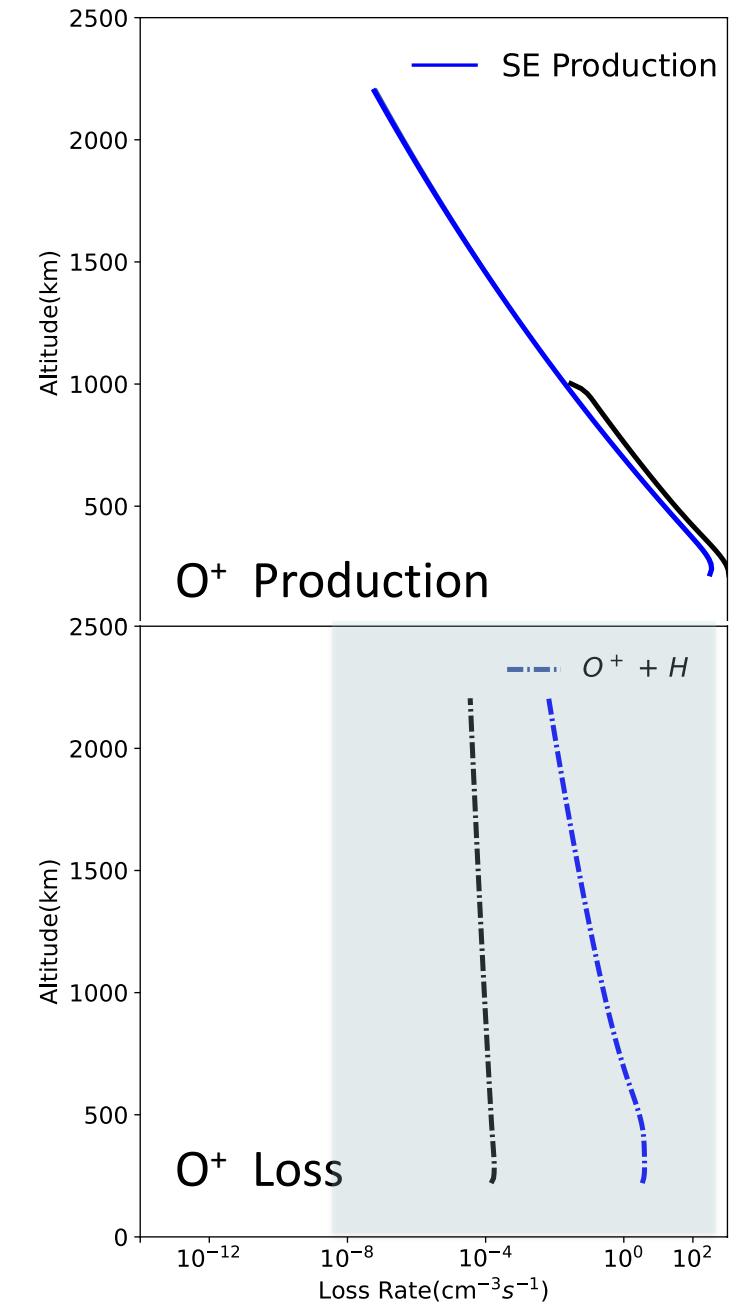
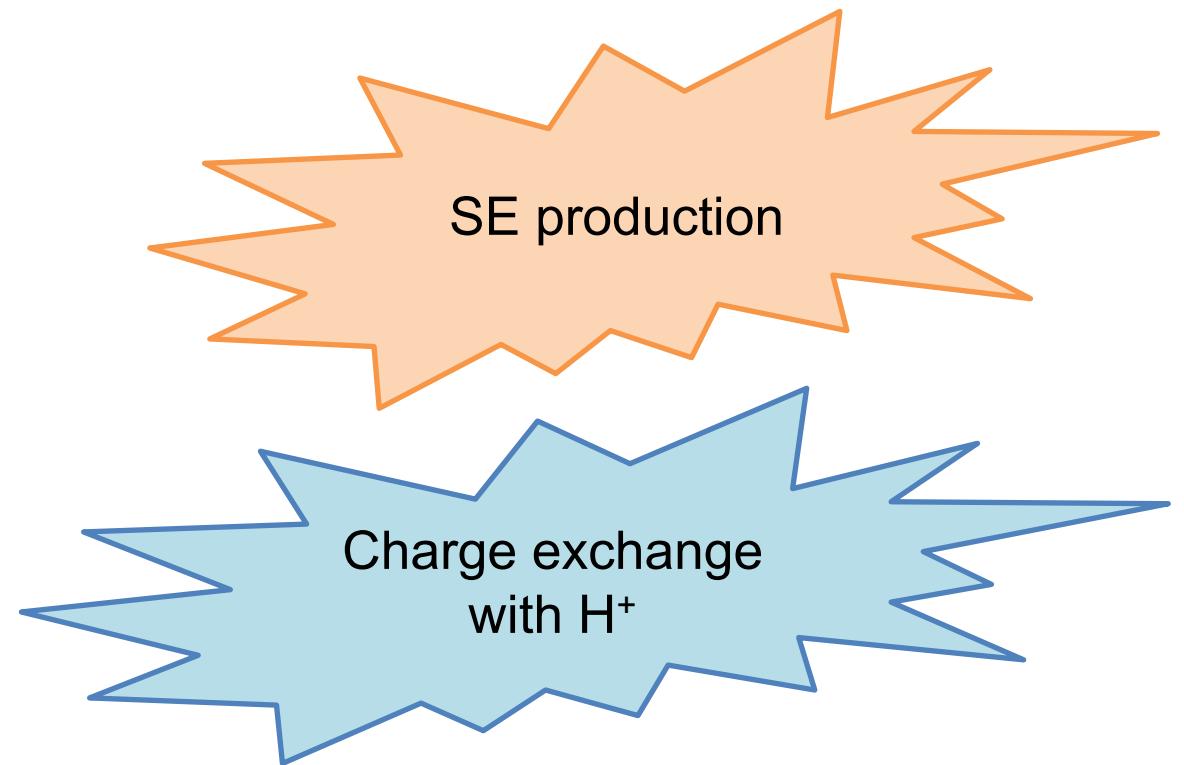
# Chemistry?



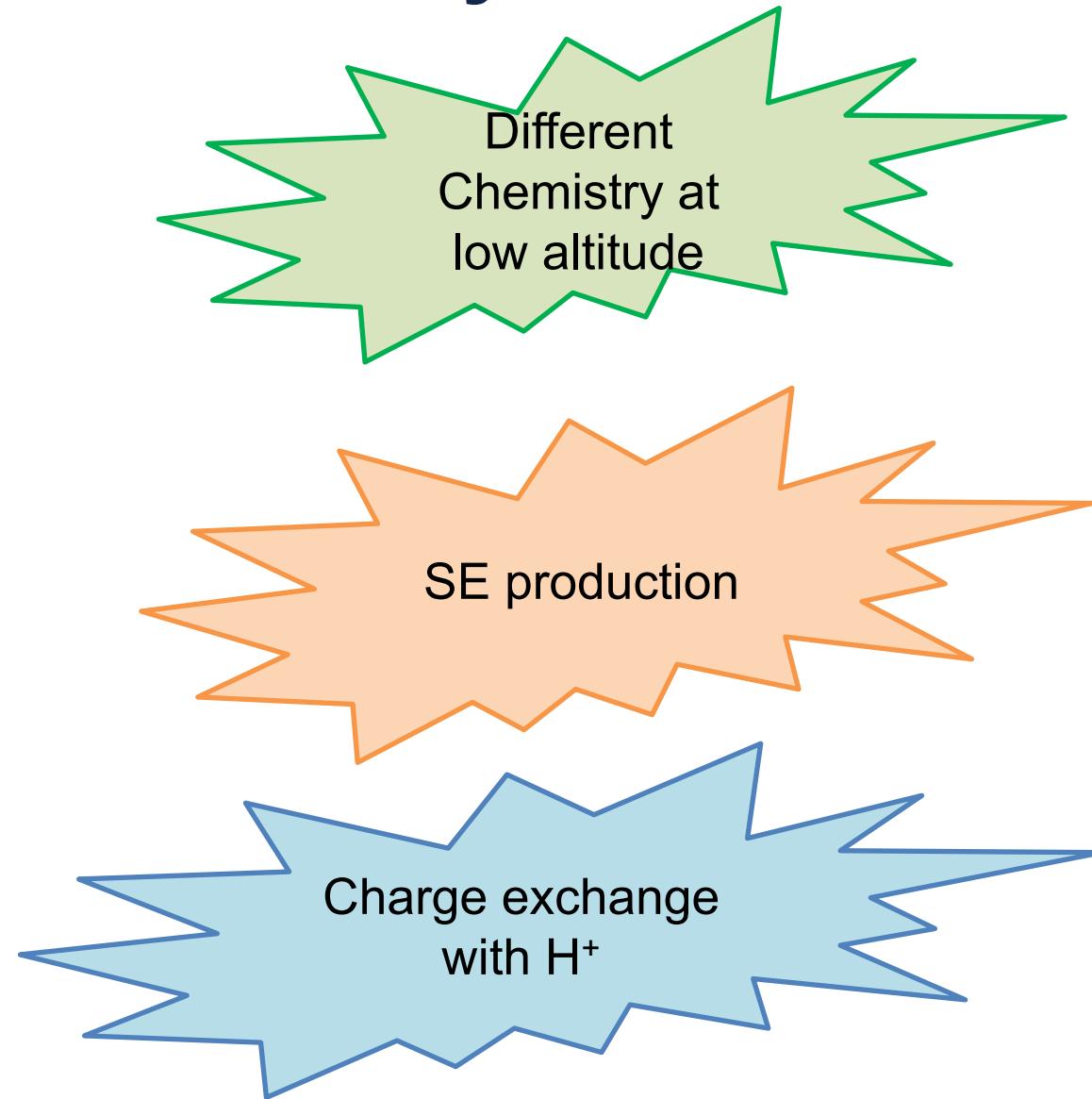
# Chemistry?



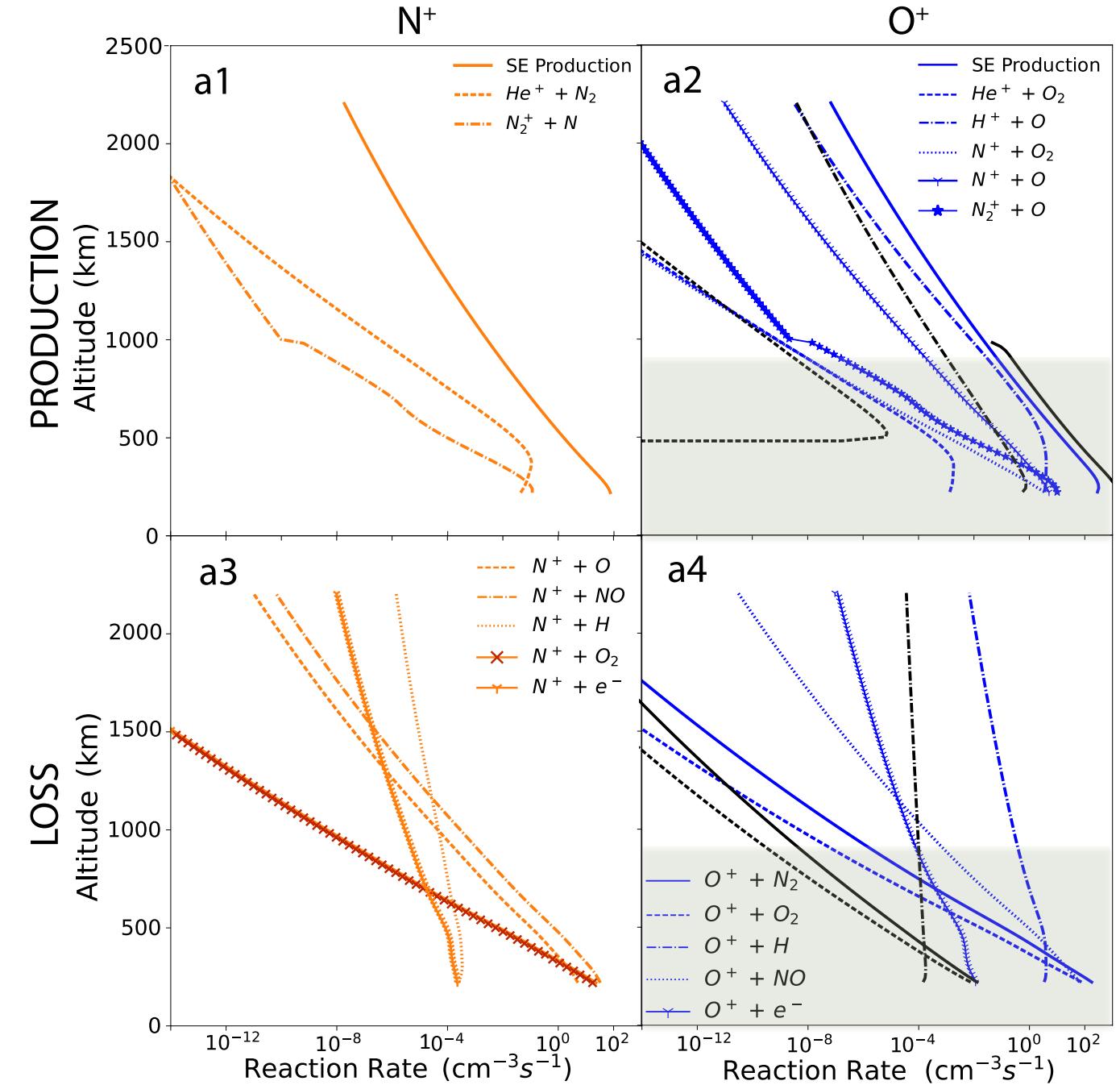
# Chemistry?



# Chemistry?



(a) Production and Loss



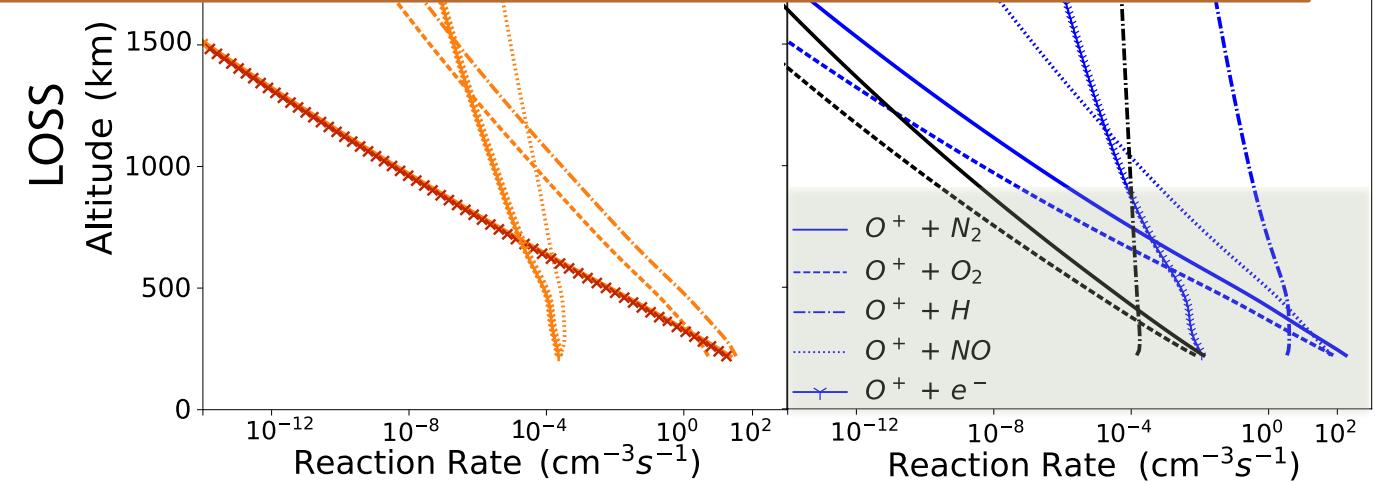
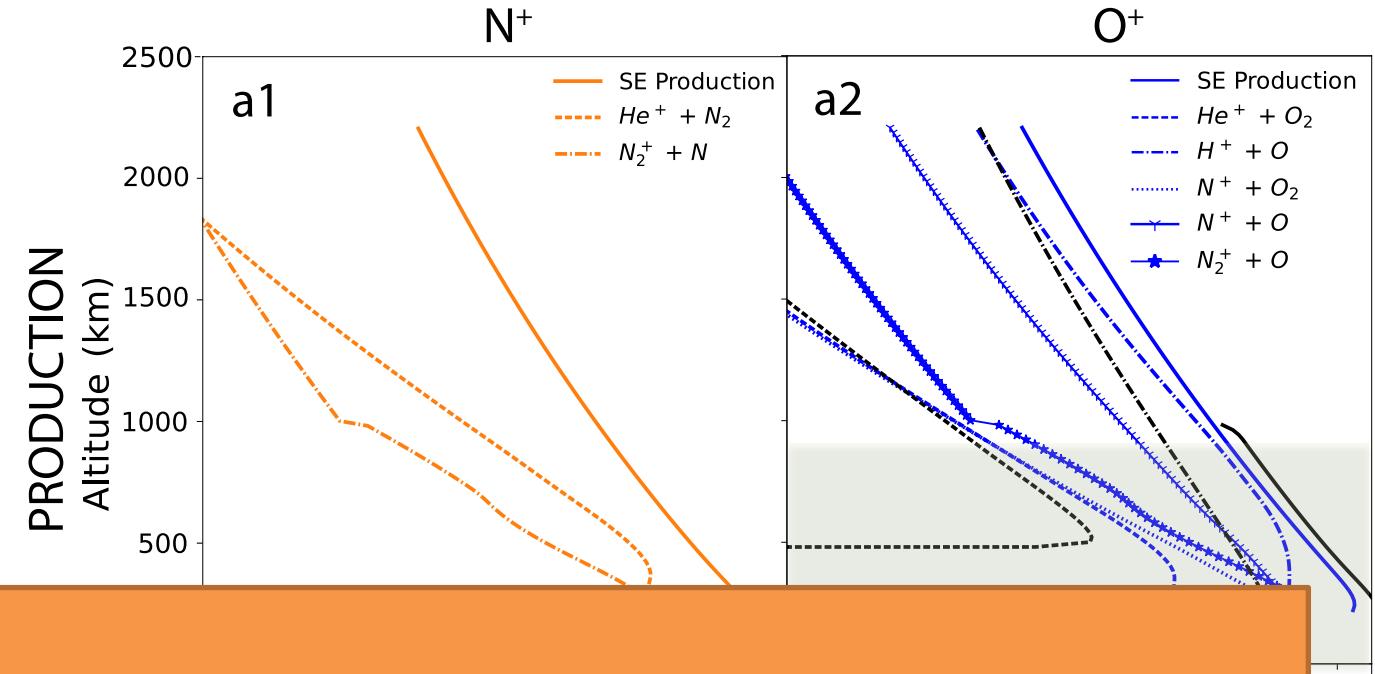
# Chemistry?

Different  
Chemistry at  
low altitude

How about the transport of molecular ions?

Charge exchange  
with  $H^+$

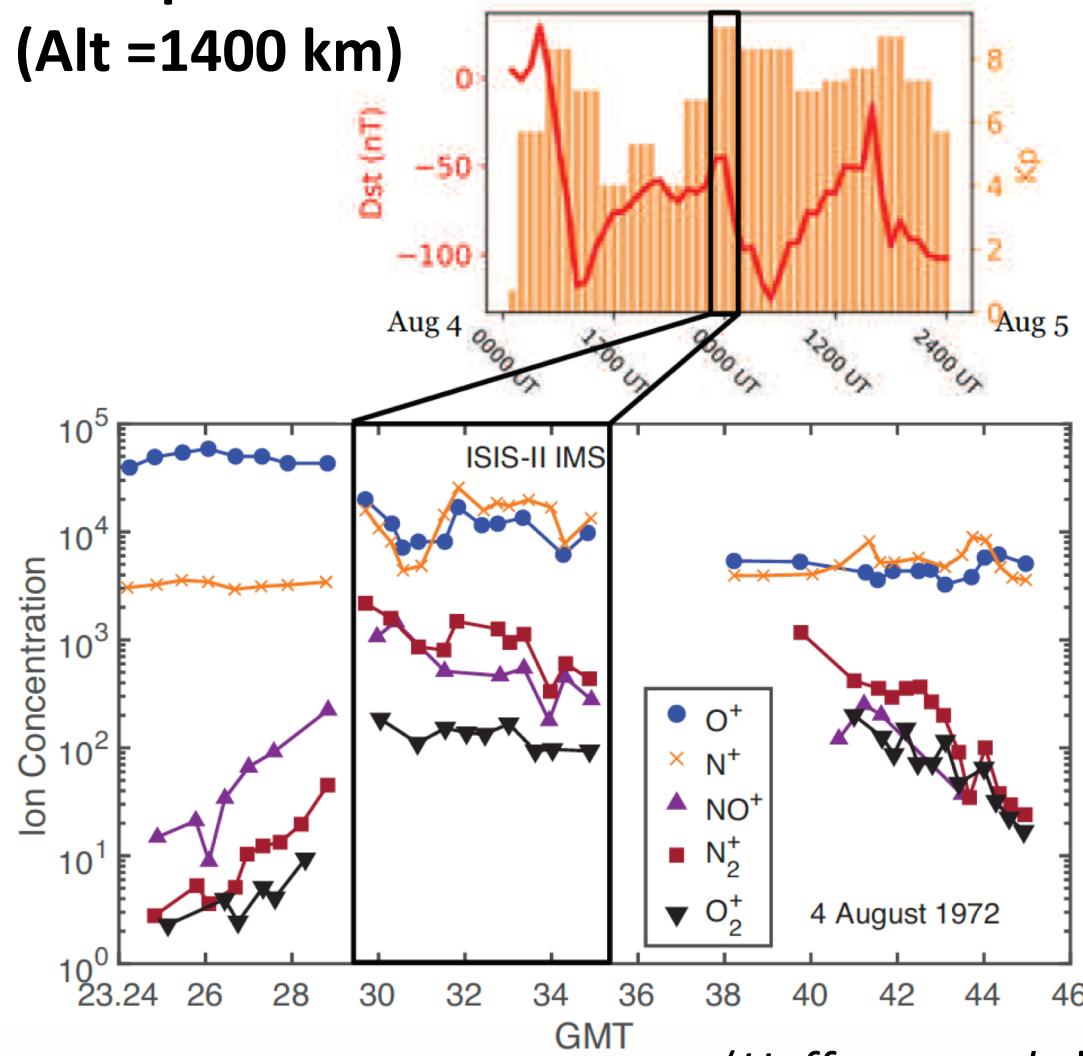
(a) Production and Loss



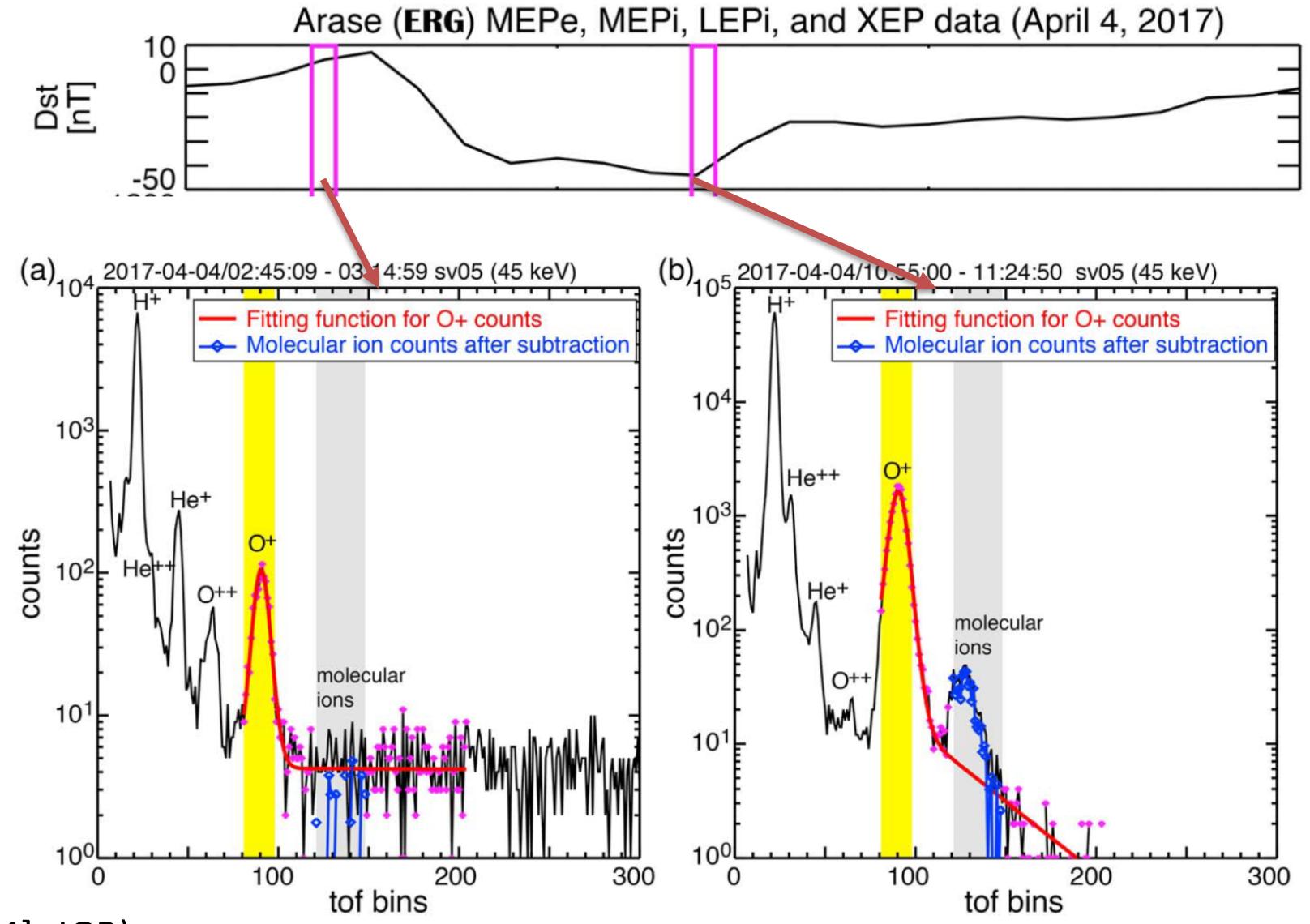
# Observations of Molecular Ions

Inner Magnetosphere

Ionosphere  
(Alt = 1400 km)



(Hoffman et al., [1974], JGR)

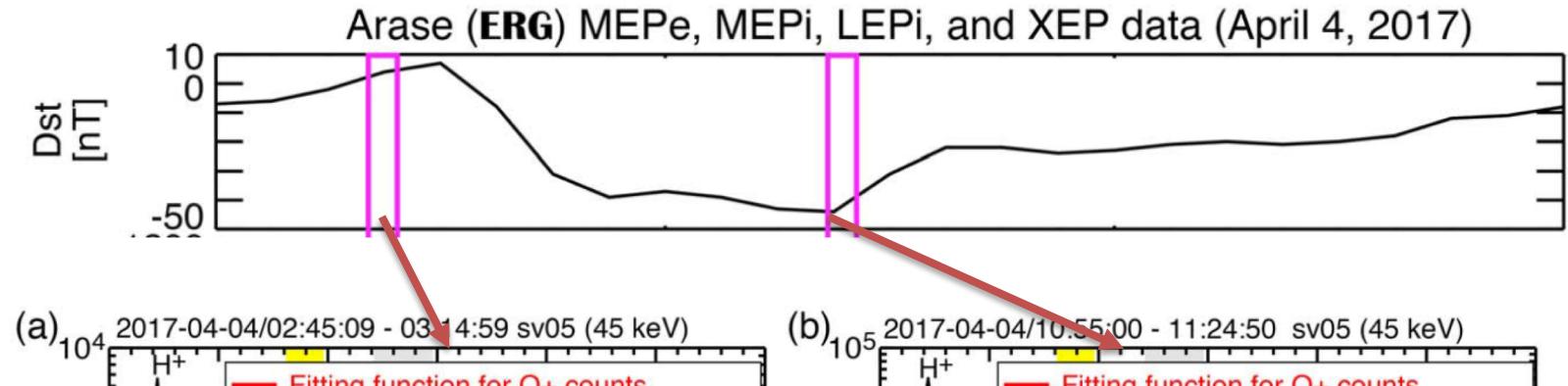
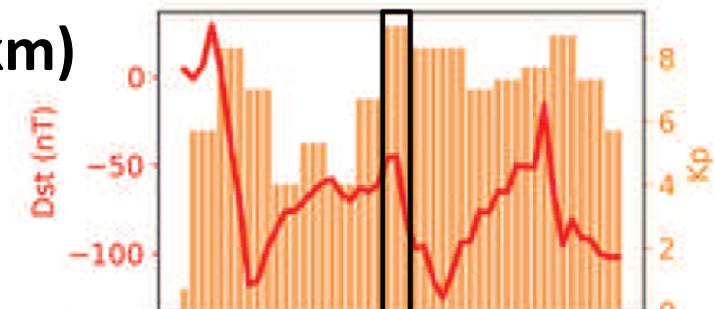


(Seki et al., [2019], GRL)

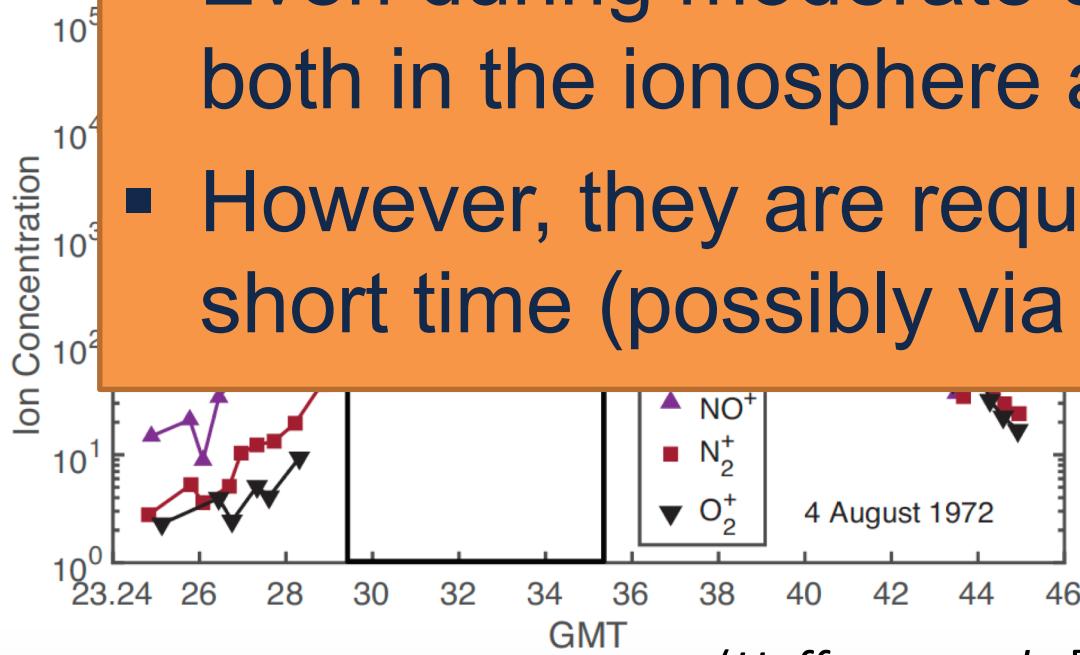
# Observations of Molecular Ions

Inner Magnetosphere

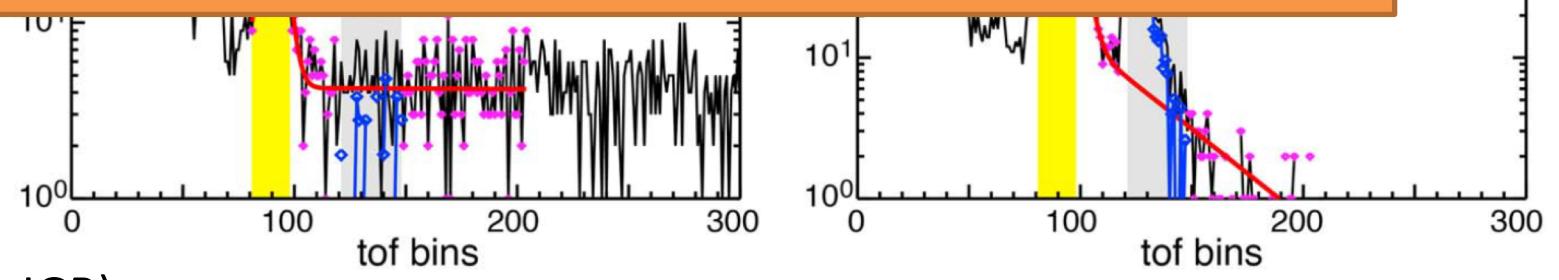
Ionosphere  
(Alt = 1400 km)



- Even during moderate storms, **molecular ions are observed** both in the ionosphere and the magnetosphere.
- However, they are required to obtain sufficient energy in a very short time (possibly via **wave particle interactions**).

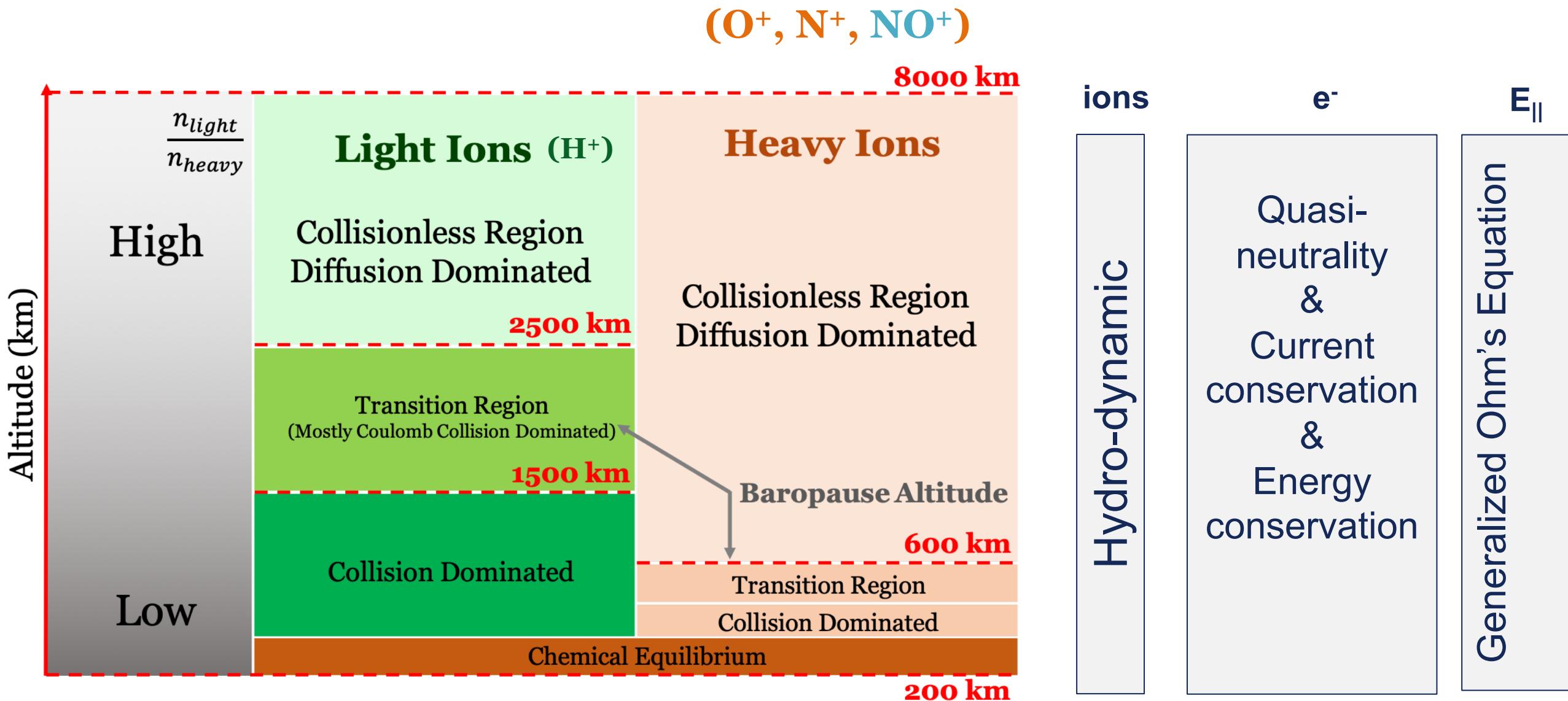


(Hoffman et al., [1974], JGR)



(Seki et al., [2019], GRL)

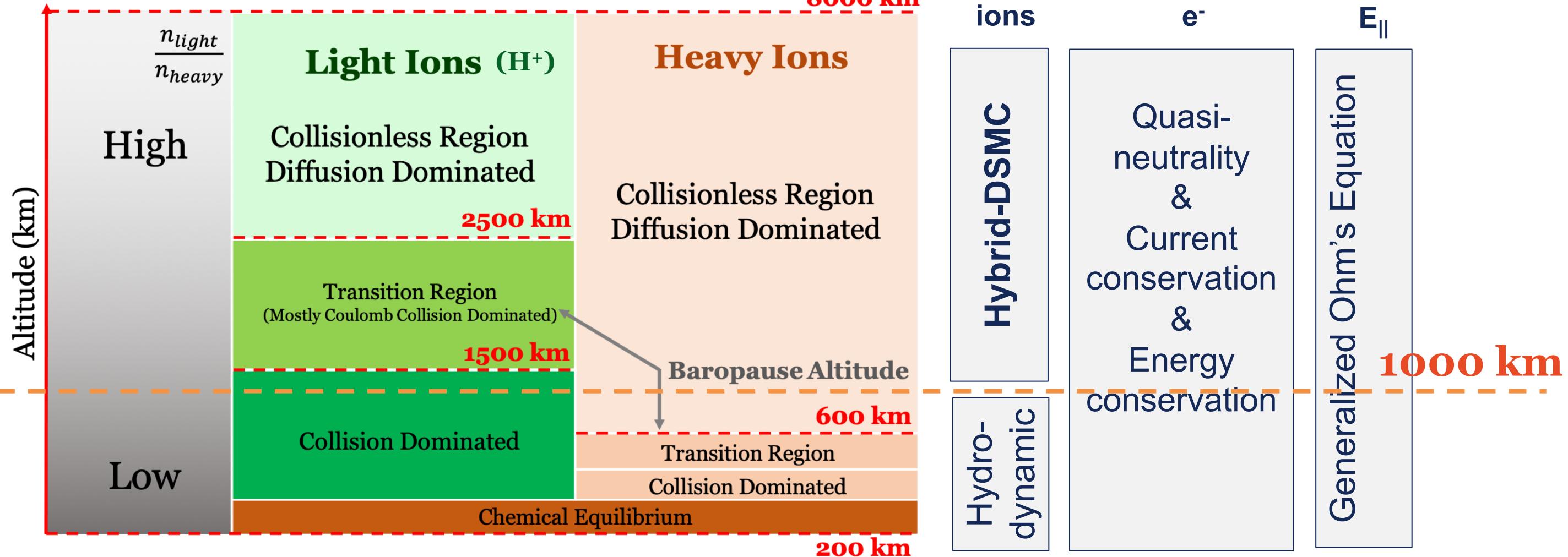
# Our approach: 7iPWOM



# Our approach: 7iPWOM

$$m \frac{\partial v_{\parallel}}{\partial t} - qE_{\parallel} + \frac{GmM_{planet}}{r^2} + \mu \frac{\partial B}{\partial s} = 0$$

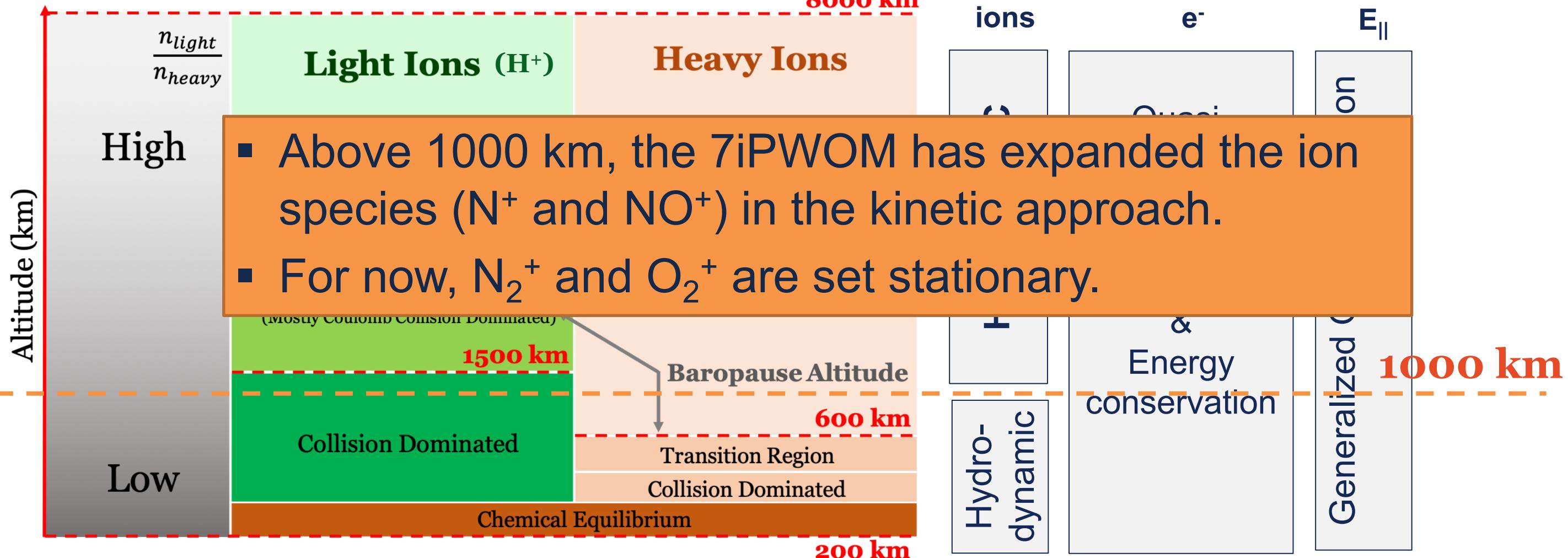
$(O^+, N^+, NO^+)$   
8000 km



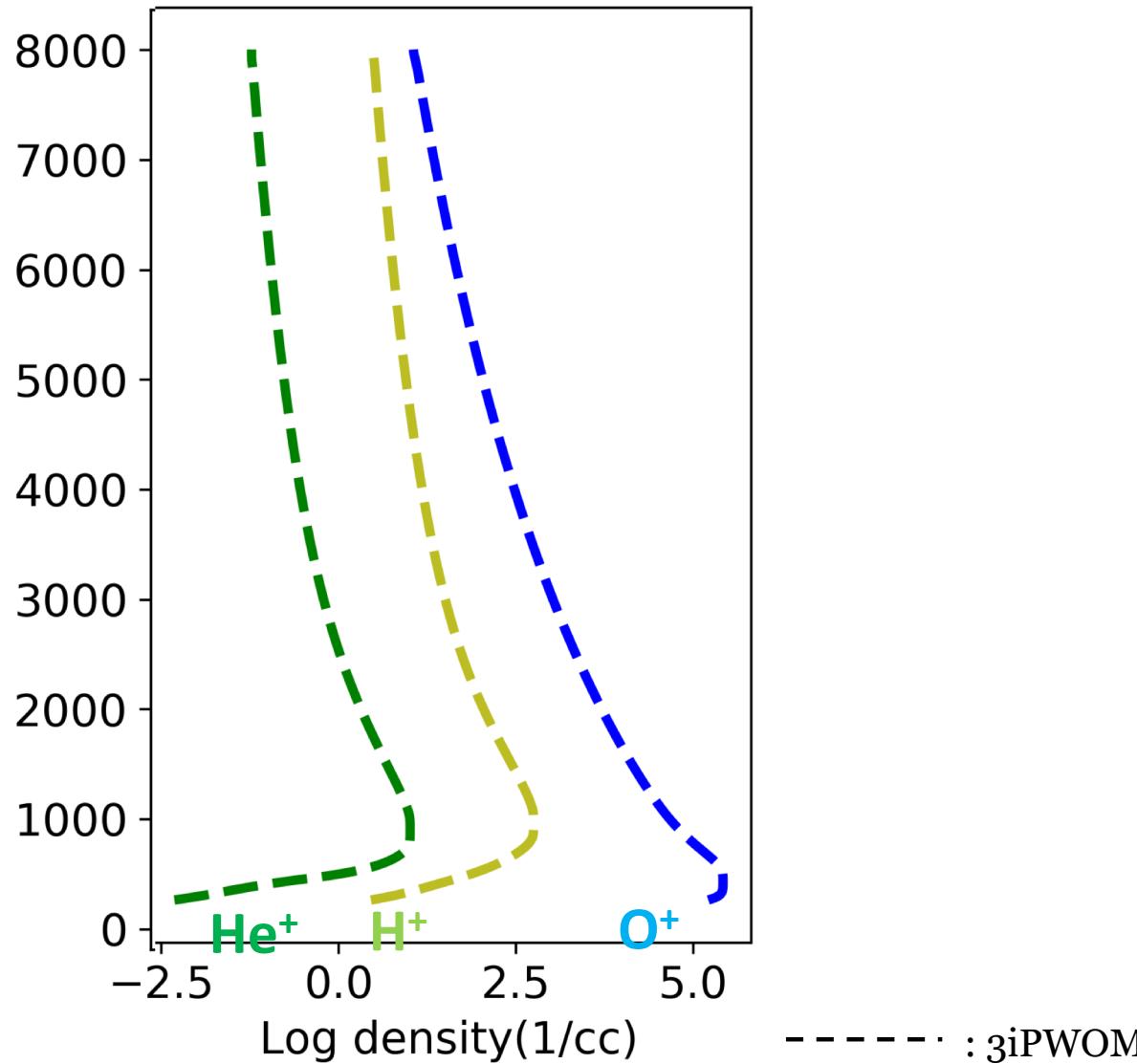
# Our approach: 7iPWOM

$$m \frac{\partial v_{\parallel}}{\partial t} - qE_{\parallel} + \frac{GmM_{planet}}{r^2} + \mu \frac{\partial B}{\partial s} = 0$$

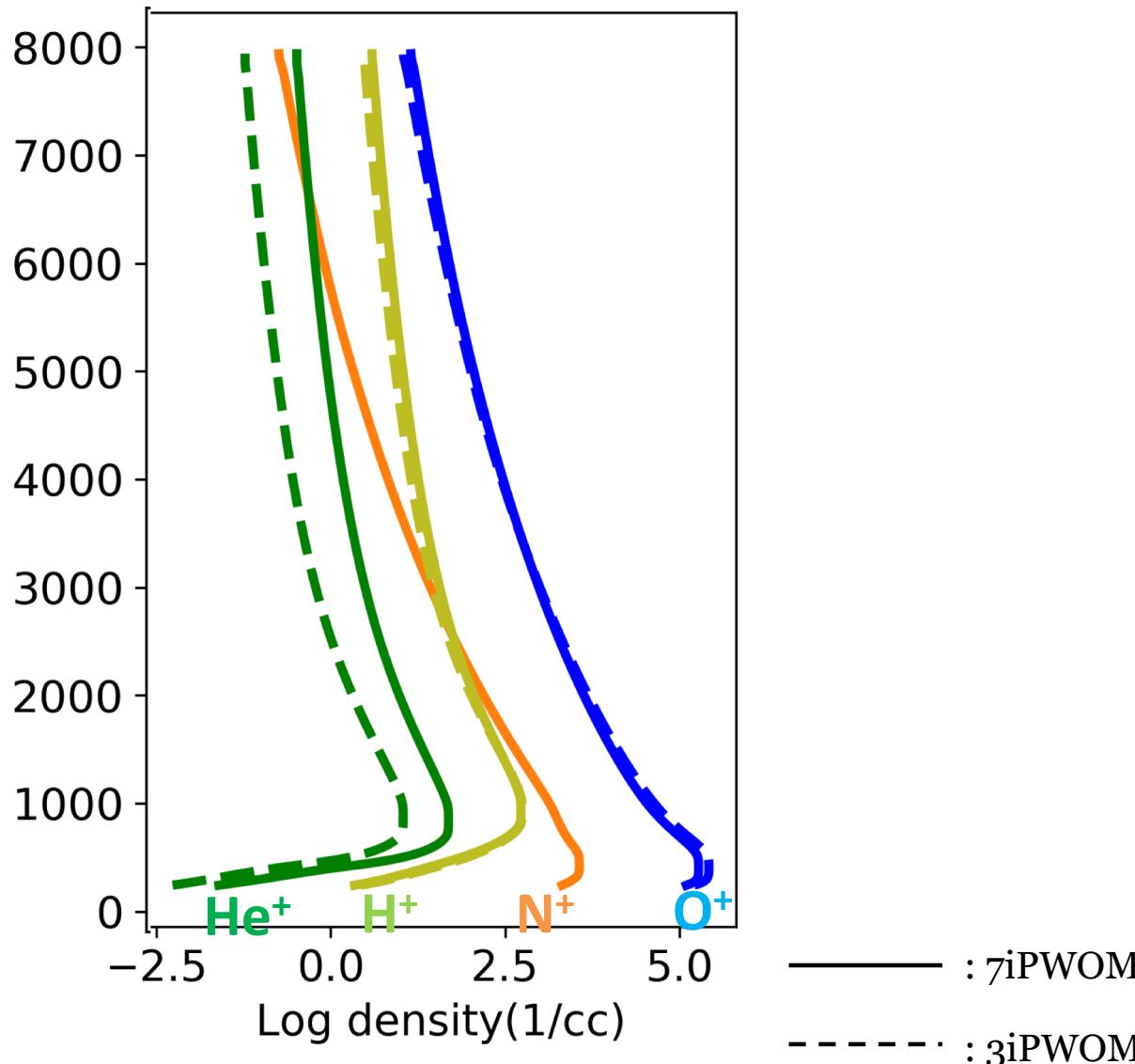
(O<sup>+</sup>, N<sup>+</sup>, NO<sup>+</sup>)  
8000 km



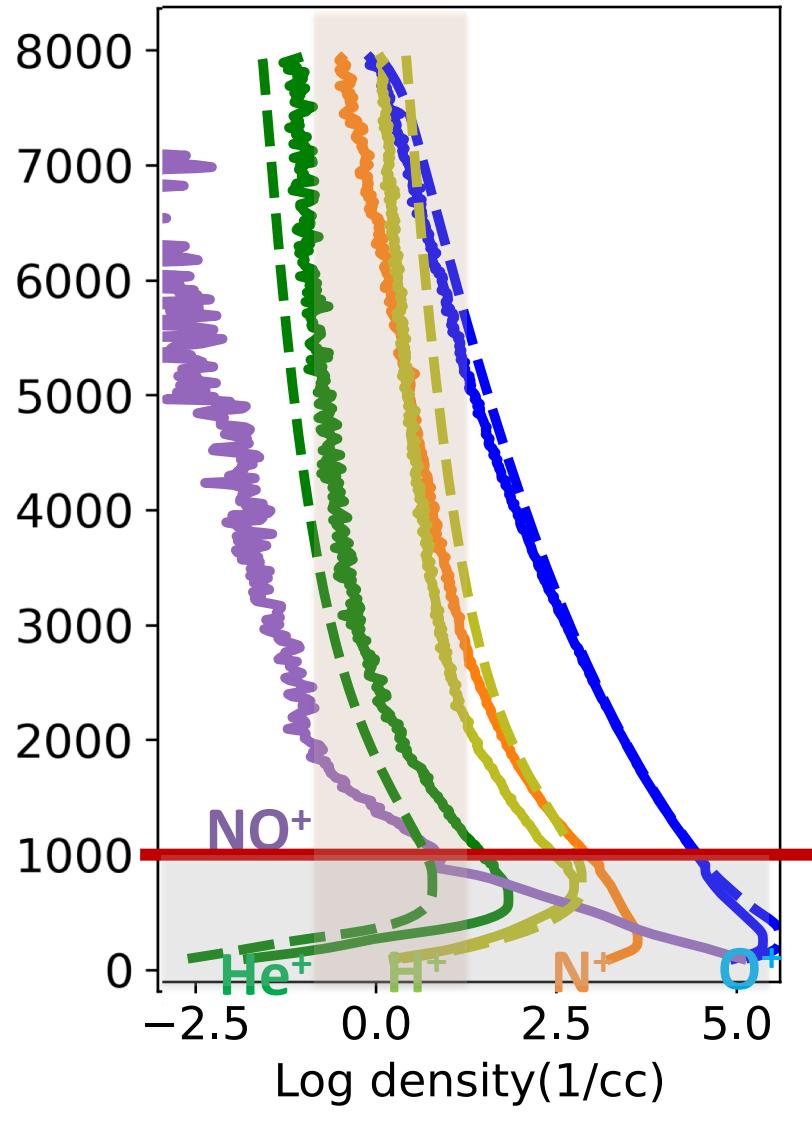
# Steady State: 3iPWOM Fluid Solution



# Steady State: 7iPWOM Fluid Solution (static $\text{NO}^+$ )



# 7iPWOM Fluid + Kinetic Solution (Dynamic NO<sup>+</sup>)



$n(NO^+)$  is still important in the kinetic solution

$n(NO^+)$  is comparable with  $n(He^+)$  below 1000 km altitude

This simulation required increased resolution

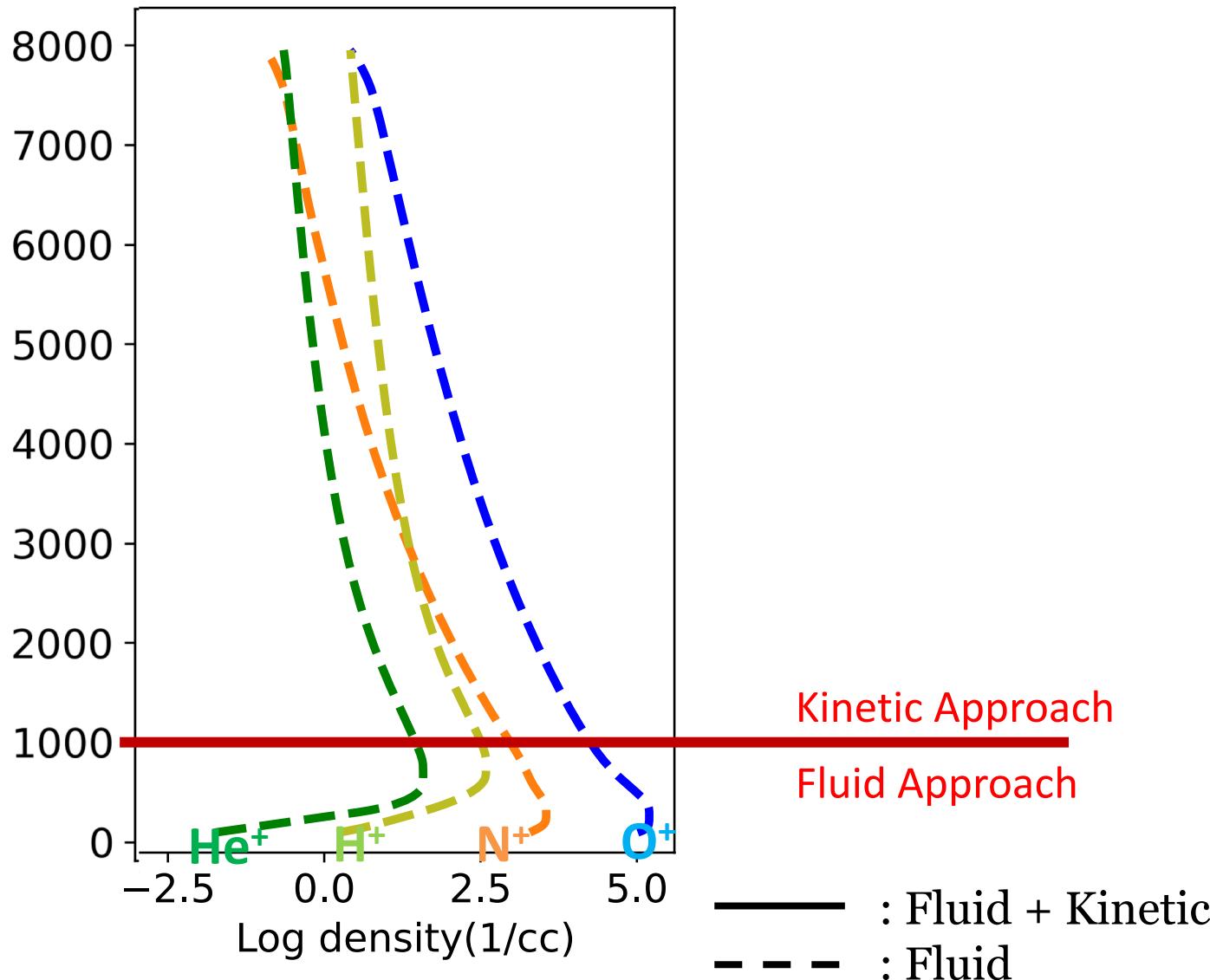
Kinetic Approach

Fluid Approach

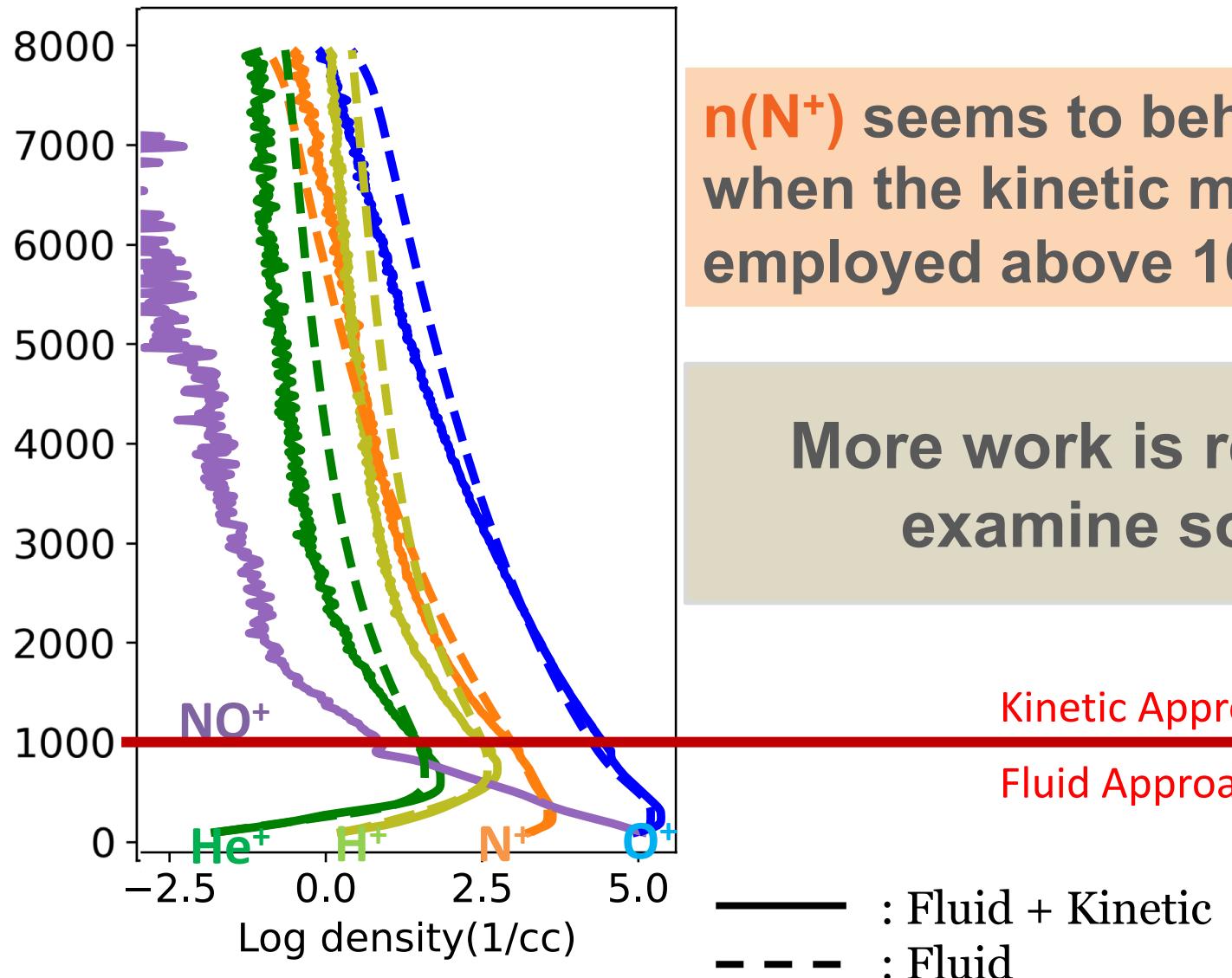
— : 7iPWOM

- - - : 3iPWOM

# Compare (Fluid + Kinetic) vs (Fluid) Solution



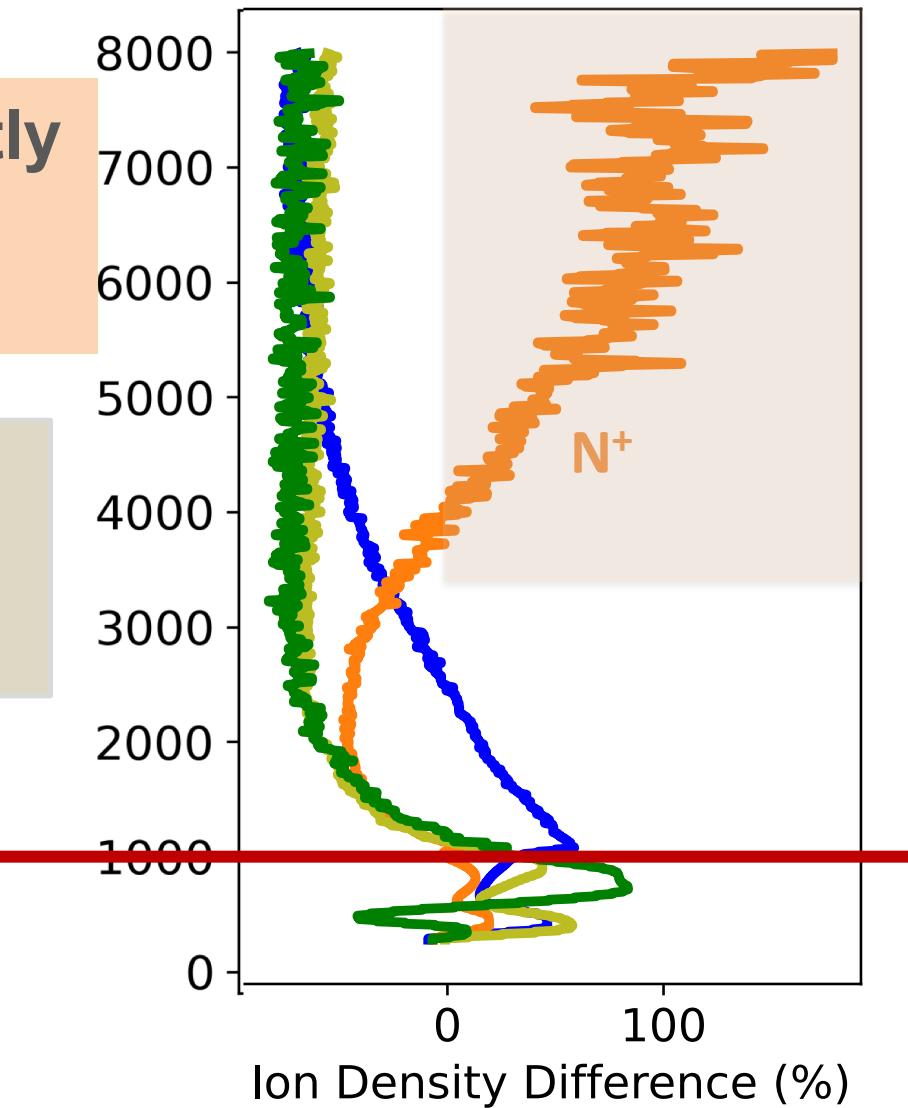
# Compare (Fluid + Kinetic) vs (Fluid) Solution



$n(\text{N}^+)$  seems to behave differently when the kinetic model is employed above 1000 km.

More work is required to examine solution

Kinetic Approach  
Fluid Approach



# Summary and Future work

- **N<sup>+</sup> ions are a key species** in the ionosphere and their presence alter the outflow for all conditions.
- Comparison with **available data below 1200km**, 7iPWOM shows **tremendous improvement** of the outflow solution when N<sup>+</sup> is included.
- Preliminary simulations using the kinetic 7iPWOM suggest that **molecular ions could also play an important role** in the local transport of all species [*more work to be done here*].
- The molecular ions, such as NO<sup>+</sup>, need to acquire sufficient energy in a very short time to escape from the ionosphere, and the energization of molecular ions, via wave particle interaction, are still under investigation.