(1)
$$u = (d \beta)$$
 $(d)^2 + (\beta)^2 = 1$

(2) eigenvalues of unitaries
$$|\lambda|=1$$

 $tru=e^{i\theta_1}+e^{i\theta_2}$

in general not the same.

(3) tru =
$$\sum_{i=1}^{N} e^{i\theta_i}$$
 & ($Te^{i\theta_i} = 1 \neq 0 \sum_{i=1}^{N} \sum_{i=1}^{N} e^{i\theta_i}$)

in general not the same

(1) Consider left cosets H & &H (8#H)

right cosets H&H&

both partition G. (: [G:HJ=2]

=> &H = H&

G/2(G) = 292(G) > Cyclic

 $\forall a,b \in G$ they are in some cosets: WLOG $a = g^m + c \in g^m + 2(G)$ $b = g^m + 2c \in f^m + 2(G)$

ab = 8 2, 9 22 = 8 4 3, 72 = 3 4 22 3 = gⁿz₂g^mz, = ba

⇒ Gabelian,

o) Verify specifically or use the feat that [Sn: An] = 2

and the statement of P13(1)

aca, b]g= qaba+b+g= (3a8), (8b8), (3a+8), (3a+8)

= [gag , gbg] E [G. G]

Then any products of the generators ti= [a, b] & CG. G]

g(π τί)g=π gτg + € [G.G]

(b) Hag, (G/H abelian) => [G.G] CH.

(a) = (aH) (bH) = abH = (bH) (aH) = baH (a.666)

=> abh; = bahz

ChieHI

=> a b ab = hz hi EH

. ⇒ [at . bt] ∈ H

(b) &: [a, b] +H

=> abatbt=h eH

 $= a^{-1}b^{-1} = b^{-1}a^{-1}h$

=> a b H = b a H

 $\Rightarrow (a^{-1}H) \cdot (b^{-1}H) = (b^{-1}H) \cdot (a^{-1}H).$

=> G/H abelian.