(1) 
$$u = \begin{pmatrix} d \beta \\ -\beta^* d^* \end{pmatrix} (d)^2 + (\beta)^2 = 1$$

$$tr u = tr u^*$$

$$(i\sigma^2) u (i\sigma^2)^{-1} = u^*$$

- (2) eigenvalues of unitaries  $|\lambda| = 1$ tr  $u = e^{i\theta_1} + e^{i\theta_2}$ tr  $u^{\#} = \bar{e}^{i\theta_1} + e^{-i\theta_2}$ in general not the same.
- (3)  $tru = \sum_{i=1}^{n} e^{i\theta_{i}} & (\pi e^{i\theta_{i}} = 1 \neq 0 \text{ } \Sigma \theta_{i} = 0 \text{ } \text{ } \text{ } \text{ } e^{-i\theta_{i}}$   $tru^{*} = \sum_{i=1}^{n} e^{-i\theta_{i}}$

in general not the same.

(1) Consider left cosets H & &H (84H)

right cosets H & H&

both partition &. ("[G:HJ=2]

=> &H=H&

(1) G/2(G) = (g-2(G)) > Cyclic

table they are in some cosets.

WLOG. a= qm2, = qm3(G) b= qm22 = qm2(G)

 $ab = \beta^{m} Z_{1} \beta^{n} Z_{2} = \beta^{m+n} Z_{1} Z_{2} = \beta^{n+m} Z_{2} Z_{3}$   $= \beta^{n} Z_{1} \beta^{m} Z_{1} = ba$ 

=> G abelian,

P14. (1) AEGL. BESL

det (BABT) = det (A) = 1

BABTESL

o) Verify specifically. or use the feet that [Sn: An] = 2

and the statement of P13(1).

P15. (1) [91,82] = 8,8, 8, 8, 827

 $g[a,b]g^{\dagger} = gaba^{\dagger}b^{\dagger}g^{\dagger} = [gag^{\dagger}(gbg^{\dagger}(gbg^{\dagger}(ga^{\dagger}ga^{$ 

Then any products of the generators  $T_i = [a_i, b_j] \in CG, GJ$   $q(\pi \ Ti)g^{-1} = \pi \ g \ Tig^{-1} \in [G, GJ]$   $=> g[G, GJg^{-1} = [G, GJ] \quad \forall g \in G.$ 

(L) HUG, (G/H abelian) => [G.G] CH.

(a) 
$$\Rightarrow$$
:  $(aH) \cdot (bH) = abH = (bH) \cdot (aH) = baH (a.beg)$ 

=>  $abh_1 = bah_2$  (h: eH)

=>  $a^{-1}b^{-1}ab = h_2 \cdot h_1^{-1} \in H$ 
 $\Rightarrow (a^{-1}b^{-1}) \in H$ 

(b)  $\Leftarrow$ : [a, b]  $\in$  H  $\Rightarrow$  aba = b = h  $\in$  H  $\Rightarrow$  a = b = b = a = b = d =