$$T(B) \cdot \overline{U}_{i} = [M_{T}(B)J_{i} \cdot \overline{U}_{j} = \overline{M_{T}(B)}_{3} \cdot \overline{U}_{j}$$

$$= \overline{T(B)U_{i}} = \overline{M_{T}(B)}_{j} \cdot \overline{U}_{j}$$

$$= M_{T}(B) = M_{T}^{*}(B)$$

$$\stackrel{(4)}{=} M_{T}^{*}(B) = S(M_{T}(B))S^{-1}$$

$$\stackrel{(4)}{=} M_{T}^{*}(B) = S(M_{T}(B))S^{-1}$$

P17.11> (T(8).4)(U)= Tw(8).4(Tv(8-1)v)

$$\begin{array}{rcl}
\widetilde{(\Upsilon(R_1)(\Upsilon(R_2) \phi))}(\omega) &=& T_{\omega}(R_1) \cdot (\widetilde{\Upsilon(R_2) \phi}) \; (T_{\omega}(R_1^{-1}) \cdot \nu) \\
&=& T_{\omega}(R_1) \; T_{\omega}(R_1) \; \forall \; (T_{\omega}(R_2^{-1}) \; T_{\omega}(R_2^{-1}) \; \nu) \\
&=& T_{\omega}(R_1) \; \forall \; (T_{\omega}(R_1, R_1^{-1}) \; \nu) \\
&=& T_{\omega}(R_1, R_2^{-1}) \; \nu) \\
&=& \left(\widetilde{\Upsilon}(R_1) + T_{\omega}(R_1, R_2^{-1}) \; \nu\right)
\end{array}$$

(2) V* = Hom (V, k) & V* & K Twaces trivially on K.

Pep. in (1) becomes

 $(T(x) \cup (y) = v_i(T(x)^{-1} \cup y)$

which is exactly the dual rep.

(3) V with basis tuis. W & was

Hom (U, W) & Matmin(C)

(T(8).4)(U)= TW(8).4(TV(8-1)V)

take $\phi = eai$, eai(Uj) = War bij

Tuj = zkij ui

 $\forall v_j: [\tilde{T}(s) e_{ai}J(v_j) = T_w b) \{e_{ai}(\sum_{k} [W(s)^T J_{kj}v_k)\}$

= Twb)·(Z[M&)]Jkj eai(Uk))

= Twl8) (ZIMB) JK Wasik)

= Tw (8). [M8)]] ij Wa

= [MG)] J & J & B ba Wb

= = [M(8)] ba [M(8)] jj ebj (vj)

= = [[M &] { a [M &) t', J]; e b ; (v))

= Topeai = Z[Mer]ba[Mert,]ki ebk

P18 (V. W) = 1 = 1 = < T(8) V, T(8) W>