P14. 
$$D = \beta \begin{pmatrix} \frac{1}{2} & 0 \\ 0 & \frac{1}{2} \end{pmatrix}$$
,  $z = e^{iQ} \beta \leq u(1)$ 

(a) 
$$d \in D$$
  $u = \begin{pmatrix} d & \beta \\ -\overline{\beta} & \overline{d} \end{pmatrix} \in Su(2)$   $|d|^{\frac{1}{2}}|B|^{2} = 1$ 

$$udu^{-1} = \begin{pmatrix} x & \beta \\ -\overline{\beta} & \overline{x} \end{pmatrix} \begin{pmatrix} \frac{2}{9} & \frac{2}{9} \end{pmatrix} \begin{pmatrix} \overline{d} & -\beta \\ \overline{\beta} & x \end{pmatrix}$$

$$= \left(\begin{array}{cc} \overline{\alpha} \, \overline{\beta} \, \left(-\overline{2} + \overline{\beta}\right) & \overline{\alpha} \, \overline{\beta} \, \left(-\overline{2} + \overline{\beta}\right) \\ \overline{\alpha} \, \overline{\beta} \, \left(-\overline{2} + \overline{\beta}\right) & \overline{\alpha} \, \overline{\beta} \, \left(-\overline{2} + \overline{\beta}\right) \end{array}\right) \in D$$

$$N_{\text{Sup}}(D) = \sum_{i=1}^{\infty} \binom{20}{07}, 3600, 505 \binom{0}{30}, 4600$$

(b) 
$$N_{SU(2)}(D)/D = \begin{cases} (\frac{2}{5}) D = (\frac{1}{5}) D \end{cases}$$

$$\begin{pmatrix} 0 & -\frac{1}{2} \\ \frac{1}{2} & 0 \end{pmatrix} D = \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix} D \quad \begin{cases} \frac{1}{2} & \mathbb{Z}_2 \end{cases}$$

$$\begin{pmatrix} a & o \\ o & \overline{a} \end{pmatrix} \begin{pmatrix} \overline{a} & \overline{a} \\ \overline{o} & \overline{a} \end{pmatrix} \begin{pmatrix} \overline{\overline{d}} & \overline{a} \\ \overline{o} & \overline{a} \end{pmatrix} = \begin{pmatrix} \overline{a} & \overline{o} \\ \overline{o} & \overline{a} \end{pmatrix}$$

$$\begin{pmatrix} 0 & -\overline{\lambda} \\ \lambda & 0 \end{pmatrix} \begin{pmatrix} \overline{\lambda} & 0 \\ 0 & \overline{\lambda} \end{pmatrix} \begin{pmatrix} \overline{\lambda} & 0 \\ 0 & \overline{\lambda} \end{pmatrix} = \begin{pmatrix} \overline{\lambda} & 0 \\ 0 & \overline{\lambda} \end{pmatrix}$$

(d) should at least comain  $(\frac{1}{5}\frac{2}{1})$ , and some

$$a=\begin{pmatrix}0,\frac{7}{2}\\-\frac{7}{2}\end{pmatrix}$$
 then it contains  $a^2=\begin{pmatrix}-1&0\\0&-1\end{pmatrix}$ 

( Nsup)(D)/D is not a subgroup of Su(2)
or Nsup(D))

PIJ.

Ge-set X. p: Ge -> Sx

(a) effective  $\iff \phi$  injective, i.e.  $\phi(g) = 1$  iff g = 1  $\forall g \neq 1$ .  $\exists x \in S, t$ .  $g = x_1 = x_2 \neq x_1 \iff \forall g \neq 1$ .  $\phi(g) = 1$  if g = 1permutation  $\phi(g) = 1$  if g = 1  $\phi(g) = 1$  if g = 1  $\phi(g) = 1$  if g = 1  $\phi(g) = 1$  if g = 1

(b)  $\$ \$ i \}$  are ineffective  $V \$ \in G$   $\$ i \$ x = \$ i \cdot x' = x'$ \$ \$ i x = \$ x = x'

=> 9:3=88: V86G

trivial to show fgit is a group

=> H= 18i: 8ix=x \forall x \in X \in A G

(C) define the action  $G/H \times X \longrightarrow X$  (gH).x:=gx

HXEX, S.+ (gH) x = X ( gx = X ( gt H ( gt gt = H = 1 G/H

Plb. X a finite G set.

G-action transitive => one orbit = X

Burnside's Lemma = (G(=Z)xf|
jeG

If all f's have fixed points. I  $|x^{\delta}| > \frac{1}{366} = |G|$  equality holds iff  $\forall f. |X^{\delta}| = 1$ 

But 1xe = 1x1 > 1

=> | x ==> for some 9.