Real rep. M=(8) = 8M(8)57 + + (\*)

 $\overline{T}(\mathcal{E}) \cdot \overline{v_i} = [N_{\overline{i}}(\mathcal{E})]_i \cdot \overline{v_j} = \overline{N_{\overline{i}}(\mathcal{E})}_{ji} \cdot \overline{v_j}$ 

= T&2 U; = M(&); U;

 $\stackrel{(*)}{=} M_{\tau}^{*}(\theta) = S M_{\tau}(\delta) S^{-1}$ 

P20 113 (T(8) 4) (U)= TW(B) 4(TU(8-1)V)

 $[\widehat{T}(\mathcal{G}_{1})(\widehat{T}(\mathcal{G}_{2}), \phi)](\omega) = T_{1}(\mathcal{G}_{1}) \cdot (\widehat{T}(\mathcal{G}_{2}), \phi) \cdot (T_{1}(\mathcal{G}_{1}^{-1}) \cdot \psi)$ 

= Tw(f,) Tw(f,) & ( Tv (827) Tv (827)0)

. = Twich & + (Tuc(8, 2)) ) )

 $= \left(\frac{2}{T} \left( \frac{2}{S} \left( \frac{1}{S} \right) \right) + \frac{1}{T} \left( \frac{1}{S} \left( \frac{1$ 

 $(\tau_{(e)}, \phi_{(v)}) = \tau_{(e)}, \phi_{(v)} = \phi_{(v)}$ 

(2) V\* = Hom (V, k) 4 V\* & K Twaces trivially

Pep. in (1) becomes  $(T(x) \cup_{i}^{*})(v_{i}) = v_{i}^{*}(T(x)^{T} \cdot v_{i})$ 

which is exactly the dual rep we

discussed in the learne.

(3) V with basis tuit. W & was

Hom (U, W) & Matmin(C)

(一味) ゆ)(ひ)= ていより・サイナンターンン

take  $\phi = eai$ , eai(Uj) = Wasij

To vj = 2 Maj ut

θυς: [ T(8) ea; J(υς) = Twb) {ea; ( Z [M(8) ] Jkj v ) }

= Twb) ( Z[M&) ] Ly ea: (Vk))

= Twif) (ZIMB) Juj Wasik)

= Two (F): [MB) ] Jij Wa

= [MG) ] JOJEMB ba Wb

= 2 [M(8)] ba [M(8) -1] ij ebj (Uj)

= Z[M&)Jba [M&) tr, Jj; eb; (v))

Theai = Z[MB] Joa [MB) to, Jk; ebk

21 ( v. w? = 10 2 ( Tb) v. Tb) w>

This is the unitirization discussed in the

lecture. <u, w>2 = Jdg < Tby, TB, w>,