Pao Real rep:
$$M_{7}(B) = 8M_{7}(B) e^{-1} + 4 e^{-1}$$
 $T(B) \cdot \overline{v_{i}} = [M_{7}(B)J_{j} : \overline{v_{j}} = M_{7}(B)J_{j} : \overline{v_{j}}$
 $= \overline{T(B)}v_{i} = M_{7}(B)J_{j} : \overline{v_{j}}$
 $\Rightarrow M_{7}(B) = M_{7}(B)J_{7}(B) = M_{7}(B)$
 $\stackrel{*}{=} M_{7}(B) = SM_{7}(B)S^{-1}$

₹21 117 (T(87.4)(U)= Tw(8).4(TU(8-1)V)

$$\begin{split} \left[\widehat{T}(\mathcal{G}_{1}) \left(\widehat{T}(\mathcal{G}_{1}) + \emptyset \right) (\mathcal{O}) &= T_{W}(\mathcal{G}_{1}) \cdot (\widehat{T}(\mathcal{G}_{2}) + \emptyset) \left(T_{V}(\mathcal{G}_{1}^{-1}) \cdot V \right) \\ &= T_{W}(\mathcal{G}_{1}) T_{W}(\mathcal{G}_{2}) + \left(T_{V}(\mathcal{G}_{1}^{-1}) T_{V}(\mathcal{G}_{2}^{-1}) U \right) \\ &= T_{W}(\mathcal{G}_{1} + \mathcal{G}_{2}) + \left(T_{V}(\mathcal{G}_{1}, \mathcal{G}_{2}^{-1}) U \right) \\ &= \left[\widehat{T}(\mathcal{G}_{1}, \mathcal{G}_{2}) + \mathcal{G}(\mathcal{O}) \right], \quad \text{and} \end{split}$$

 $(\stackrel{\sim}{\tau}_{(e)} \cdot \not=)_{(U)} = \tau_{(e)} \cdot \not= (\tau_{(e)} \cdot \not= \phi_{(U)})$

(T'(f) V^* = Hom (V, k) $V^* \otimes K$ Twaces trivially on K.

Pep-in (1) becomes $(T^*(f) V^*_i)(V_j) = V^*_i(T(f)^{1} \cdot V_j)$

which is exactly the dual rep we discussed in the learne.

(3) V with basis tuit. W & was

Hom (U, W) & Matmin(C)

(T(8).4)(U)= Tw(8).4(TV(8-1)V)

take $\phi = eai$, eai(Uj) = Wasij

Tuj = zkij ui

$$\begin{split} \forall \, v_j : & \left[\, \stackrel{\sim}{T}(8) \, e_{ai} J(v_j) = \, T_w B \right) \, \left(\, e_{ai} (\, \sum_k \left[M(8)^\intercal J_{kj} v_k \, \right) \, \right) \\ & = \, T_w (8) \cdot \left(\, \sum_k \left[M(8)^\intercal J_{kj} \, v_k \, \right) \, \right) \\ & = \, T_w (8) \cdot \left(\, \sum_k \left[M(8)^\intercal J_{kj} \, w_k \, e_{ai} \, (v_k) \, \right) \, \right) \\ & = \, T_w (8) \cdot \left[M(8)^\intercal J_{ij} \, w_k \, e_{ai} \, e_{ai} \, e_{ai} \, (v_k) \, e_{ai} \, e_{ai}$$

722 (V. W) = 1 2 < T(F) V. T(F) W>

This is the unitirization discussed in the lecture. CU, w>2 = Jdg < Tby, Tb, w>,