## Problem 07

Construct a nontrivial homomorphism from the quaternion group to the Klein four group,

$$\phi: Q \to \mathbb{Z}_2 \times \mathbb{Z}_2.$$

Show its kernel  $\ker \phi$  and image  $\operatorname{im} \phi$ .

## Problem 08

Show that the following diagram commutes if and only if  $k_1 = k_2 \mod N$ .

$$\mathbb{Z}_{N} \xrightarrow{m_{k_{1}}} \mathbb{Z}_{N} 
\downarrow \psi \qquad \qquad \downarrow \psi 
\mu_{N} \xrightarrow{p_{k_{2}}} \mu_{N}$$