## P8106\_midterm

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```
library(corrplot)
library(tidyverse)
library(caret)
library(mgcv)
library(patchwork)
library(rpart)
library(rpart.plot)
library(party)
library(randomForest)
library(ranger)
library(e1071)
library(pdp)
library(earth)
library(splines)
library(pdp)
library(ggplot2)
library(gridExtra)
library(glmnet)
library(MASS)
library(pROC)
library(vip)
library(AppliedPredictiveModeling)
library(klaR)
```

## import and Data

```
set.seed(4195)
load("recovery.Rdata")
dat <- dat[sample(1:10000, 2000),]
dat <- dat[,-1]%>% #ignore the id variable
    mutate(study = case_when( # from character variable to a numeric variable
    study == "A" ~ 1,
    study == "B" ~ 2,
    study == "C" ~ 3)) %>%
    mutate(
    gender = as.factor(gender),
    race = as.factor(race),
    smoking = as.factor(smoking),
    hypertension = as.factor(diabetes),
```

```
vaccine = as.factor(vaccine),
    severity = as.factor(severity),
    study = as.factor(study)
)
skimr::skim_without_charts(dat)
```

Table 1: Data summary

Name	dat
Number of rows	2000
Number of columns	15
Column type frequency:	
factor	8
numeric	7
Group variables	None

## Variable type: factor

skim_variable	n_missing	$complete\_rate$	ordered	n_unique	top_counts
gender	0	1	FALSE	2	0: 1009, 1: 991
race	0	1	FALSE	4	1: 1246, 3: 439, 4: 221, 2: 94
smoking	0	1	FALSE	3	0: 1209, 1: 583, 2: 208
hypertension	0	1	FALSE	2	0: 1030, 1: 970
diabetes	0	1	FALSE	2	0: 1722, 1: 278
vaccine	0	1	FALSE	2	1: 1189, 0: 811
severity	0	1	FALSE	2	0: 1804, 1: 196
study	0	1	FALSE	3	2: 1152, 3: 432, 1: 416

## Variable type: numeric

skim_variable	n_missing	complete_rate	mean	sd	p0	p25	p50	p75	p100
age	0	1	60.08	4.58	45.0	57.00	60.0	63.0	77.0
height	0	1	170.10	5.89	151.4	166.20	170.3	174.1	189.3
weight	0	1	79.92	6.99	57.5	75.00	79.9	84.7	104.2
bmi	0	1	27.67	2.65	19.7	25.80	27.6	29.4	37.1
SBP	0	1	130.43	8.06	104.0	125.00	130.0	136.0	156.0
LDL	0	1	110.30	20.22	47.0	96.75	110.0	124.0	172.0
$\underline{\text{recovery}\_\text{time}}$	0	1	41.83	27.05	2.0	28.00	38.5	49.0	365.0

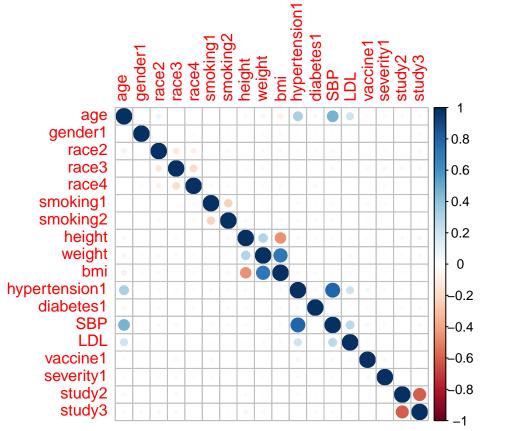
## Create x and y matrixs for modeling

```
traindata <- createDataPartition(dat$recovery_time, p = 0.7, list = FALSE)
traindataset <- dat[traindata,]
testdataset <- dat[-traindata,]
#train
x = model.matrix(recovery_time ~ ., dat)[traindata,-1]
y = traindataset$recovery_time

#test
x_test = model.matrix(recovery_time ~ ., dat)[-traindata,-1]
y_test = testdataset$recovery_time</pre>
```

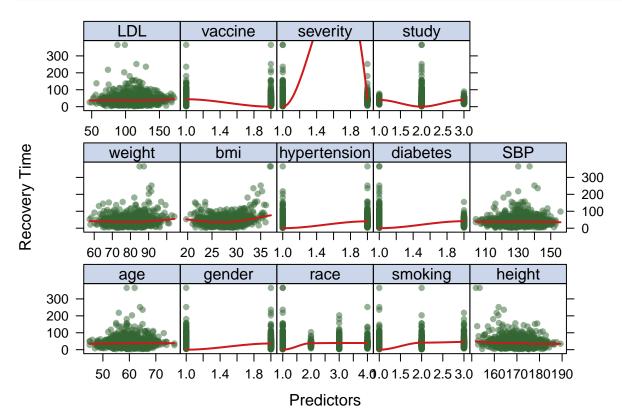
## Exploratory analysis and data visualization:





```
# create dataset for exploratory analysis and data visualization
traindataset1 <- traindataset%>%
    mutate(
    gender = as.numeric(gender),
    race = as.numeric(race),
    smoking = as.numeric(smoking),
    hypertension = as.numeric(hypertension),
```

```
diabetes = as.numeric(diabetes),
vaccine = as.numeric(vaccine),
severity = as.numeric(severity),
study = as.numeric(study))
```



## Model training:

#### Fit a linear model:

```
set.seed(4195)
# Fit a linear regression model
lm.fit <- train(recovery_time ~ age + gender + race + smoking + height + weight +</pre>
                bmi + hypertension + diabetes + SBP + LDL + vaccine +
                severity + study,
              data = traindataset,
              method = "lm",
              trControl = ctrl)
# model summary
summary(lm.fit$finalModel)
##
## Call:
## lm(formula = .outcome ~ ., data = dat)
##
## Residuals:
##
      Min
               1Q Median
                                     Max
## -82.006 -12.582 -0.872
                           9.012 235.079
## Coefficients:
                  Estimate Std. Error t value Pr(>|t|)
## (Intercept) -2.580e+03 1.888e+02 -13.666 < 2e-16 ***
                                     1.666 0.09600 .
                 2.584e-01 1.551e-01
## age
## gender1
               -5.893e+00 1.245e+00 -4.733 2.44e-06 ***
## race2
              -4.165e+00 2.869e+00 -1.452 0.14676
                3.060e-01 1.556e+00 0.197 0.84412
## race3
               -7.088e-01 2.041e+00 -0.347 0.72838
## race4
## smoking1
               4.534e+00 1.398e+00 3.242 0.00122 **
               1.021e+01 2.083e+00 4.900 1.07e-06 ***
## smoking2
                1.509e+01 1.111e+00 13.586 < 2e-16 ***
## height
## weight
               -1.639e+01 1.176e+00 -13.934 < 2e-16 ***
## bmi
                4.892e+01 3.366e+00 14.534 < 2e-16 ***
## hypertension1 2.698e+00 2.066e+00 1.306 0.19168
## diabetes1 -3.749e-01 1.819e+00 -0.206 0.83674
## SBP
               1.498e-02 1.356e-01 0.110 0.91205
## LDL
              -4.738e-02 3.187e-02 -1.486 0.13739
## vaccine1
               -6.875e+00 1.280e+00 -5.373 9.07e-08 ***
                8.467e+00 2.130e+00
## severity1
                                      3.975 7.40e-05 ***
## study2
                2.775e+00 1.573e+00
                                     1.764 0.07788 .
## study3
                -9.477e-01 1.900e+00 -0.499 0.61805
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Residual standard error: 23.25 on 1383 degrees of freedom
## Multiple R-squared: 0.2404, Adjusted R-squared: 0.2305
## F-statistic: 24.31 on 18 and 1383 DF, p-value: < 2.2e-16
```

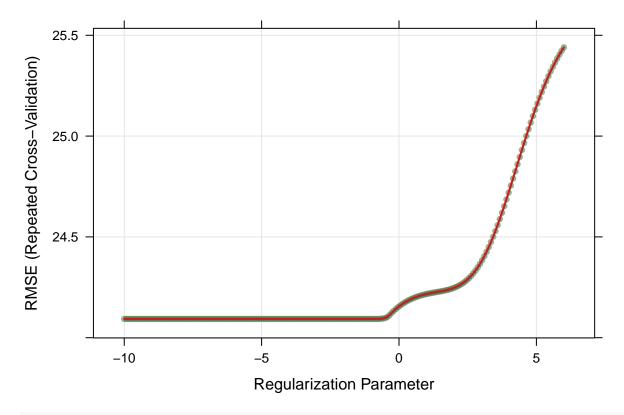
```
# RMSE
test_pred_lm <- predict(lm.fit, newdata = testdataset)
test_rmse_lm <- sqrt(mean((test_pred_lm -y_test)^2))
test_rmse_lm

## [1] 24.21453</pre>
RMSE = 24.214526
```

### Fit Ridge Regression

```
Length Class
                   -none-
                              numeric
## a0
             100
## beta
            1800
                   dgCMatrix
                              S4
## df
             100
                              numeric
                   -none-
## dim
              2
                    -none-
                              numeric
## lambda
             100
                    -none-
                              numeric
                   -none-
## dev.ratio
            100
                              numeric
## nulldev
              1 -none-
                              numeric
## npasses
               1 -none-
                              numeric
## jerr
               1 -none-
                              numeric
## offset
               1 -none-
                              logical
## call
                              call
              5 -none-
## nobs
## lambdaOpt 1 -none-
18 -none-
## nobs
               1 -none-
                              numeric
                             numeric
                            character
## problemType 1 -none-
                              character
              2 data.frame list
## tuneValue
## tuneval 1 -none 0 -none-
               1 -none-
                              logical
                              list
```

plot(ridge.fit,xTrans =log)



```
ridge.fit$bestTune
```

```
## alpha lambda
## 116     0 0.4705896

# RMSE

test_pred_ridge <- predict(ridge.fit, newdata = data.frame(x_test))
test_rmse_ridge <- sqrt(mean((test_pred_ridge -y_test)^2))
test_rmse_ridge

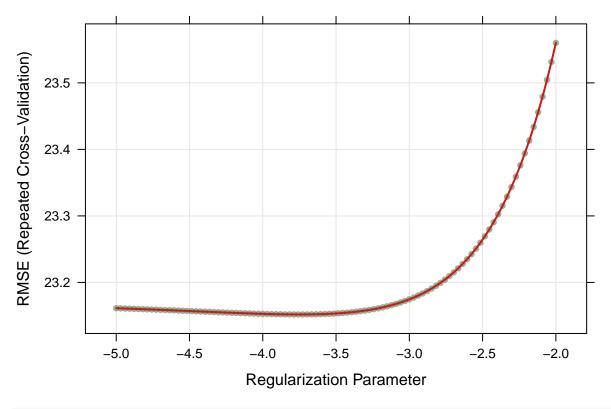
## [1] 26.43512

RMSE = 26.4351178</pre>
```

#### Fit Lasso model:

##		Length	Class	Mode
##	a0	93	-none-	numeric
##	beta	1674	${\tt dgCMatrix}$	S4
##	df	93	-none-	numeric
##	dim	2	-none-	numeric
##	lambda	93	-none-	numeric
##	dev.ratio	93	-none-	numeric
##	nulldev	1	-none-	numeric
##	npasses	1	-none-	numeric
##	jerr	1	-none-	numeric
##	offset	1	-none-	logical
##	call	5	-none-	call
##	nobs	1	-none-	numeric
##	lambdaOpt	1	-none-	numeric
##	xNames	18	-none-	${\tt character}$
##	${\tt problemType}$	1	-none-	${\tt character}$
##	tuneValue	2	${\tt data.frame}$	list
##	obsLevels	1	-none-	logical
##	param	0	-none-	list

## plot(lasso.fit,xTrans =log)



## lasso.fit\$bestTune

```
## alpha lambda
## 42 1 0.02334025
```

```
# view performance on the test set (RMSE)
lasso_pred <- predict(lasso.fit, newdata = data.frame(x_test))
test_rmse_lasso<- sqrt(mean((lasso_pred - y_test)^2))
test_rmse_lasso</pre>
## [1] 24.34447
```

RMSE = 24.3444707

#### Fit Elastic net model:

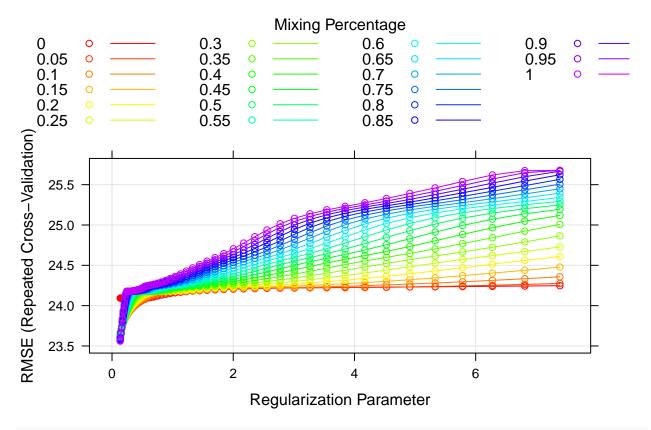
## Warning in nominalTrainWorkflow(x = x, y = y, wts = weights, info = trainInfo, : ## There were missing values in resampled performance measures.

```
# view the model summary
summary(enet.fit$finalModel)
```

```
##
             Length Class
                             Mode
## a0
             93 -none-
                             numeric
## beta
            1674 dgCMatrix S4
             93
## df
                  -none-
                             numeric
## dim
              2 -none-
                             numeric
## lambda
             93 -none-
                             numeric
## dev.ratio
             93 -none-
                             numeric
             1 -none-
## nulldev
                            numeric
## npasses
              1 -none-
                            numeric
## jerr
              1 -none-
                            numeric
## offset
              1 -none-
                             logical
## call
              5 -none-
                            call
## nobs
              1 -none-
                           numeric
## lambdaOpt 1 -none-
## xNames 18 -none-
                           numeric
                           character
## problemType 1 -none-
                            character
## tuneValue
             2 data.frame list
## obsLevels
              1 -none-
                            logical
## param
               0 -none-
                             list
```

```
enet.fit$bestTune
```

```
## alpha lambda
## 1001 1 0.1353353
```

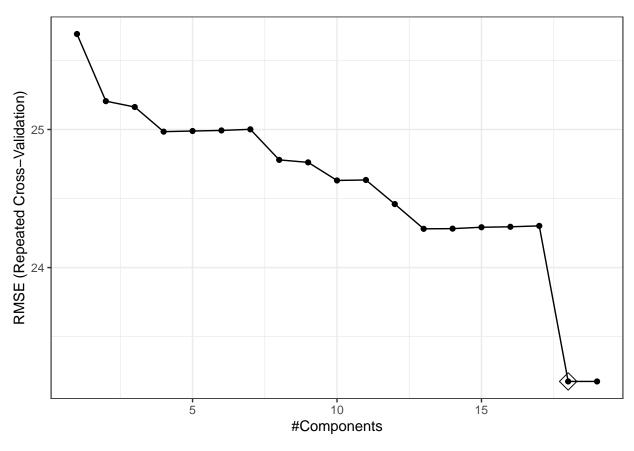


coef(enet.fit\$finalModel, enet.fit\$bestTune\$lambda)

```
## 19 x 1 sparse Matrix of class "dgCMatrix"
##
## (Intercept)
                 -971.60882559
## age
                    0.24586872
## gender1
                   -5.74078448
## race2
                   -3.14016554
## race3
                   -0.25586131
## race4
## smoking1
                    4.04765122
## smoking2
                   10.25806216
## height
                    5.59355972
## weight
                   -6.32138317
## bmi
                   20.09733437
                    2.47119605
## hypertension1
## diabetes1
                   -0.12472863
## SBP
                    0.01248712
## LDL
                   -0.03516016
## vaccine1
                   -6.80532972
## severity1
                    8.35373727
```

```
## study2
                   2.81593202
## study3
                  -0.40909368
# view performance on the test set (RMSE)
enet_pred <- predict(enet.fit, data.frame(x_test))</pre>
test_rmse_enet <- sqrt(mean((enet_pred - y_test)^2))</pre>
test_rmse_enet
## [1] 25.35936
# calculate RMSE
sqrt(mean((enet_pred - y_test)^2))
## [1] 25.35936
RMSE = 25.3593609
Fit a PCR model
set.seed(4195)
pcr.fit <- train(x, y,</pre>
                method = "pcr",
                tuneGrid = data.frame(ncomp = 1:19),
                trControl = ctrl,
                preProcess = c("center", "scale"))
# model summary
summary(pcr.fit$finalModel)
           X dimension: 1402 18
## Data:
## Y dimension: 1402 1
## Fit method: svdpc
## Number of components considered: 18
## TRAINING: % variance explained
             1 comps 2 comps 3 comps 4 comps 5 comps 6 comps 7 comps
##
            12.51500 22.141
                               31.18 38.300
                                                 45.194
                                                         51.708
                                                                  57.806
## .outcome 0.01676
                                                           6.979
                                                                    7.018
                        4.682
                                 5.10
                                          6.685
                                                  6.797
##
            8 comps 9 comps 10 comps 11 comps 12 comps 13 comps 14 comps
## X
           63.619
                    69.264
                               74.69
                                           79.98
                                                    84.69
                                                              88.94
                                                                        92.93
## .outcome 8.773
                       8.844
                                 10.23
                                           10.24
                                                    11.57
                                                              12.90
                                                                        12.95
##
            15 comps 16 comps 17 comps 18 comps
## X
               96.76
                         98.96
                                   99.99
                                           100.00
## .outcome
               13.02
                         13.06
                                   13.08
                                             24.04
```

ggplot(pcr.fit, highlight = TRUE) + theme\_bw()



```
# RMSE

test_pred_pcr <- predict(pcr.fit, newdata = data.frame(x_test))

test_rmse_pcr <- sqrt(mean((test_pred_pcr -y_test)^2))

test_rmse_pcr</pre>
```

## [1] 24.21453

RMSE = 24.214526

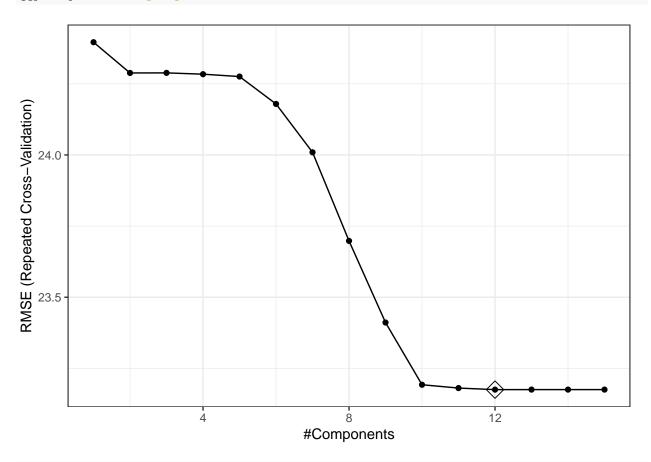
## Fit a Partial least squares model(PLS):

## Data: X dimension: 1402 18

## Y dimension: 1402 1
## Fit method: oscorespls

```
## Number of components considered: 12
## TRAINING: % variance explained
             1 comps 2 comps
                                        4 comps 5 comps
##
                               3 comps
                                                           6 comps
                                                                     7 comps
## X
               8.308
                        14.97
                                  22.46
                                           31.92
                                                    36.72
                                                             41.27
                                                                       47.00
                                                                       16.75
##
  .outcome
              12.019
                        13.09
                                  13.19
                                           13.28
                                                    13.81
                                                              14.93
##
             8 comps 9 comps 10 comps 11 comps
                                                   12 comps
## X
               50.70
                        54.04
                                   57.10
                                             62.31
                                                       67.54
               19.99
                        22.55
                                   23.94
                                             24.03
                                                       24.04
## .outcome
```

```
ggplot(pls.fit, highlight = TRUE) + theme_bw()
```



```
# view performance on the test set (RMSE)
pls_pred <- predict(pls.fit, data.frame(x_test))
test_rmse_pls <- sqrt(mean((pls_pred - y_test))^2)
test_rmse_pls</pre>
```

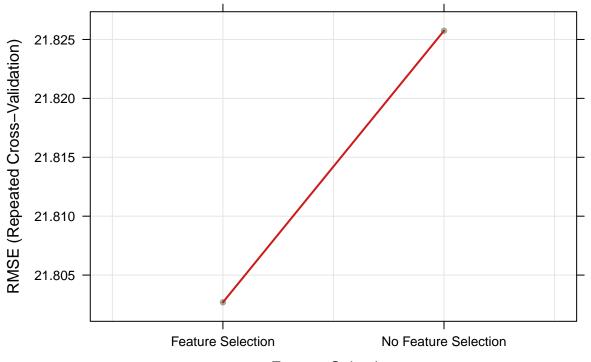
## [1] 1.030057

 $\mathrm{RMSE} = 1.0300573$ 

Fit a Generalized additive model (GAM):

```
set.seed(4195)
# fit GAM using default setting
gam.fit <- train(x, y, # test dataset
               method = "gam",
               trControl = ctrl)
# view the model summary
summary(gam.fit$finalModel)
##
## Family: gaussian
## Link function: identity
##
## Formula:
## .outcome ~ gender1 + race2 + race3 + race4 + smoking1 + smoking2 +
      hypertension1 + diabetes1 + vaccine1 + severity1 + study2 +
      study3 + s(age) + s(SBP) + s(LDL) + s(bmi) + s(height) +
##
##
      s(weight)
##
## Parametric coefficients:
               Estimate Std. Error t value Pr(>|t|)
               42.69008 1.72989 24.678 < 2e-16 ***
## (Intercept)
## gender1
               -6.03913 1.11580 -5.412 7.33e-08 ***
## race2
               -2.36813
                          2.58265 -0.917 0.35934
                                   0.673 0.50093
## race3
                        1.39612
                0.93986
## race4
               -1.38293 1.83233 -0.755 0.45053
## smoking1
               5.06298 1.25663 4.029 5.91e-05 ***
## smoking2
              1.12341
## hypertension1 3.51457
                                   3.128 0.00179 **
## diabetes1 -0.03949 1.63164 -0.024 0.98069
## vaccine1
               -6.89201 1.15163 -5.985 2.76e-09 ***
## severity1
               9.97838 1.90893 5.227 1.99e-07 ***
## study2
                2.29649
                          1.41166
                                   1.627 0.10401
## study3
               -1.06735
                        1.70593 -0.626 0.53164
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Approximate significance of smooth terms:
                 edf Ref.df
                               F p-value
                      9 0.00 0.3983
## s(age)
            4.614e-08
## s(SBP)
           2.185e-08
                         9 0.00 0.5511
## s(LDL)
           3.601e-08
                        9 0.00 0.4010
## s(bmi)
           8.925e+00
                         9 72.01 <2e-16 ***
                         9 0.00 0.9094
## s(height) 6.577e-09
## s(weight) 5.300e+00
                         9 1.24 0.0435 *
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## R-sq.(adj) = 0.383
                      Deviance explained = 39.5%
## GCV = 441.96 Scale est. = 433.38
```





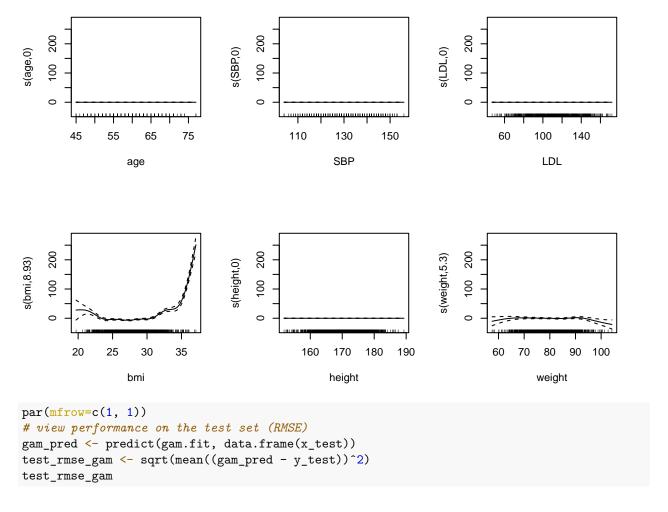
**Feature Selection** 

```
gam.fit$bestTune
```

```
## select method
## 2 TRUE GCV.Cp
```

#### gam.fit\$finalModel

```
##
## Family: gaussian
## Link function: identity
##
## Formula:
##
   .outcome ~ gender1 + race2 + race3 + race4 + smoking1 + smoking2 +
       hypertension1 + diabetes1 + vaccine1 + severity1 + study2 +
##
##
       study3 + s(age) + s(SBP) + s(LDL) + s(bmi) + s(height) +
##
       s(weight)
##
## Estimated degrees of freedom:
## 0.00 0.00 0.00 8.93 0.00 5.30 total = 27.23
##
## GCV score: 441.9595
par(mfrow=c(2, 3))
plot(gam.fit$finalModel)
```



## [1] 0.3650951

RMSE for gaml= 0.3650951

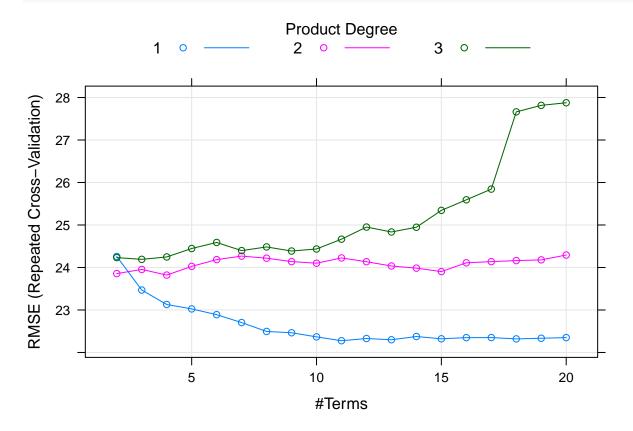
#### Fit a Multivariate adaptive regression spline (MARS) model:

## Warning in nominalTrainWorkflow(x = x, y = y, wts = weights, info = trainInfo, : ## There were missing values in resampled performance measures.

# # view the model summary summary(mars.fit\$finalModel)

```
## Call: earth(x=matrix[1402,18], y=c(30,118,49,41,...), keepxy=TRUE, degree=1,
##
               nprune=11)
##
               coefficients
##
## (Intercept)
                 -34.958407
## gender1
                  -5.877791
## smoking2
                   9.425191
## vaccine1
                  -6.573231
## severity1
                   9.512094
## h(bmi-23.9)
                   9.037401
## h(bmi-28.6)
                   5.225776
## h(32-bmi)
                   9.704445
## h(bmi-32)
                   7.002485
## h(bmi-34.3)
                 -51.894845
## h(bmi-35.2)
                 156.582406
## Selected 11 of 23 terms, and 5 of 18 predictors (nprune=11)
## Termination condition: Reached nk 37
## Importance: bmi, vaccine1, gender1, smoking2, severity1, age-unused, ...
## Number of terms at each degree of interaction: 1 10 (additive model)
## GCV 447.0747
                   RSS 608162.2
                                    GRSq 0.3642685
                                                      RSq 0.3822897
```

#### plot(mars.fit)



```
varImp(mars.fit)
## earth variable importance
             Overall
##
             100.000
## bmi
## vaccine1
            17.904
## gender1
              11.429
## smoking2
             5.528
## severity1 0.000
# view performance on the test set (RMSE)
mars_pred <- predict(mars.fit, data.frame(x_test))</pre>
test_rmse_mars <- sqrt(mean((mars_pred - y_test))^2)</pre>
test_rmse_mars
## [1] 0.498946
RMSE = 0.498946
```

## Model comparison:

## Number of resamples: 50

## ## MAE ##

## **Boxplot**

## Models: linear, ridge, lasso, enet, pcr, pls, gam, mars

## linear 12.45434 14.36326 15.46439 15.39960 16.07453 18.33422 ## ridge 12.51644 14.17746 15.06231 15.26539 16.16693 18.84820

## lasso 12.33922 14.21415 15.22249 15.24308 15.99849 18.22015 ## enet 12.24497 13.83944 14.84224 14.99155 15.87681 18.51202

Min. 1st Qu. Median

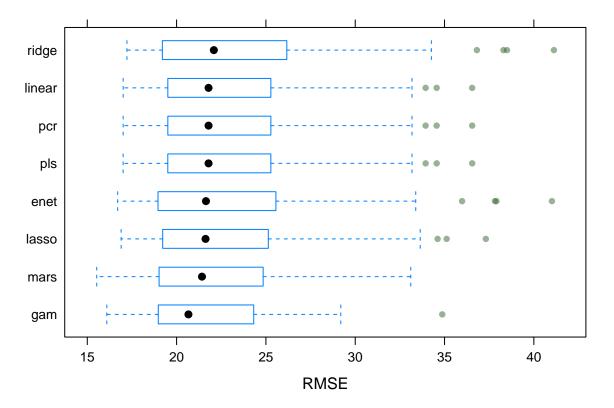
Mean 3rd Qu.

0

0

```
12.45434 14.36326 15.46439 15.39960 16.07453 18.33422
## pcr
          12.45441 14.36526 15.46680 15.40030 16.07406 18.34113
                                                                    0
## pls
## gam
          11.79423 13.82056 14.66266 14.56811 15.29117 17.21988
                                                                    0
          10.94788 13.88167 14.64942 14.54511 15.38748 17.06443
## mars
                                                                    0
##
## RMSE
##
                    1st Qu.
                              Median
                                         Mean 3rd Qu.
## linear 17.00778 19.53498 21.78932 23.17550 25.20443 36.54660
  ridge
          17.22035 19.23008 22.08552 24.09320 26.04269 41.12200
                                                                    0
          16.89531 19.27019 21.62040 23.15185 25.12814 37.31288
                                                                    0
## lasso
## enet
          16.70205 19.04394 21.64395 23.56012 25.43298 41.01151
                                                                    0
          17.00778 19.53498 21.78932 23.17550 25.20443 36.54660
                                                                    0
##
  pcr
  pls
          17.00605 19.53420 21.78871 23.17539 25.20385 36.54796
##
                                                                    0
          16.09422 19.04722 20.66361 21.80269 24.29060 34.87183
                                                                    0
  gam
          15.52845 19.02786 21.42099 22.27648 24.80028 33.10796
                                                                    0
##
  mars
##
## Rsquared
##
                Min.
                        1st Qu.
                                   Median
                                                Mean
                                                       3rd Qu.
## linear 0.06296364 0.14590446 0.1926016 0.2129520 0.2526136 0.4770537
         0.02164192 0.09911699 0.1239995 0.1346198 0.1703316 0.3108875
## lasso 0.06270494 0.14415659 0.1975179 0.2118501 0.2536393 0.4576479
## enet
          0.04215195 0.13506557 0.1664189 0.1765881 0.2217879 0.3575522
          0.06296364 0.14590446 0.1926016 0.2129520 0.2526136 0.4770537
## pcr
          0.06300174 0.14592884 0.1926212 0.2129513 0.2525843 0.4769383
## pls
## gam
          0.03495173 0.18162408 0.2514815 0.2958699 0.3515494 0.6687155
## mars
          0.03294532 0.14345855 0.2403353 0.2747823 0.3541213 0.6495820
```

#### bwplot(resamp, metric = "RMSE")



# choose GAM model