

TESTING FUNDAMENTAL PHYSICS WITH BLACK HOLES

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TESTS OF GENERAL RELATIVITY

- 1915 → General Relativity (Einstein)
- 1919 → Deflection of light by Sun (Eddington)
- 1960s-Present → Solar System Experiments
- 1970s-Present → Binary Pulsars

Tests in the weak field regime

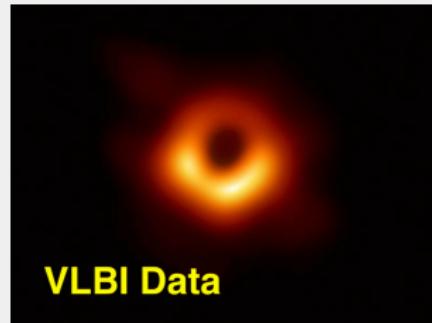
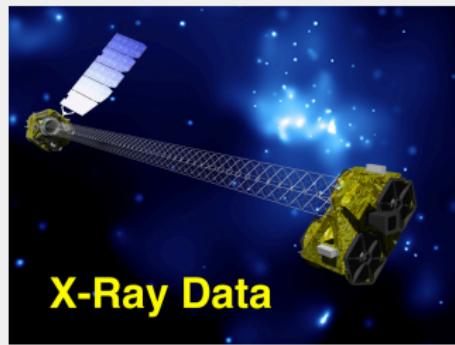
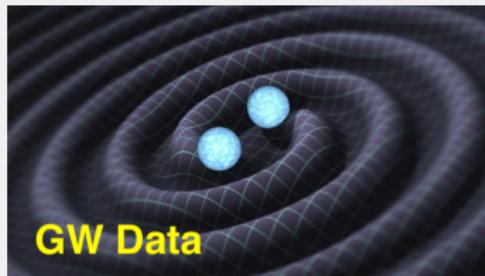
- 2000s-Present → Cosmological Tests

Tests on large scales

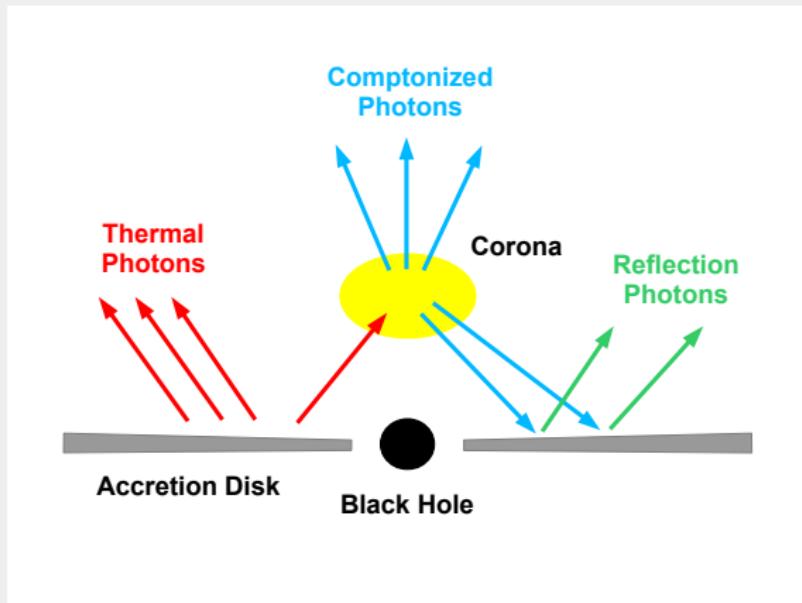
TESTS OF GENERAL RELATIVITY

■ 2010s-Present → Black Holes, Neutron Stars

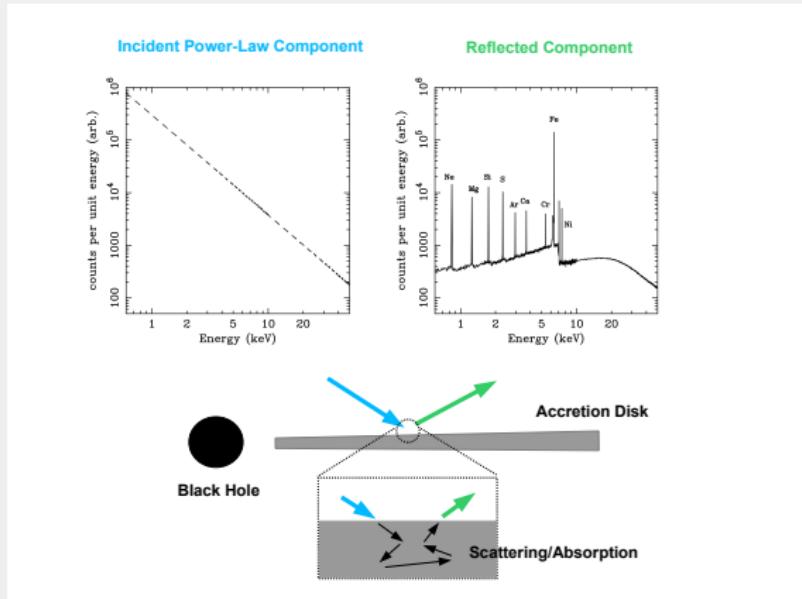
Tests in the strong field regime



DISK-CORONA MODEL



REFLECTION SPECTRUM



THEORETICAL MODELS

Fundamental Physics

- 1) Spacetime Metric
- 2) Particle Motion
- 3) Fundamental Constants
- 4) Atomic Energy Levels
- 5) ...

Astrophysical Model

- 1) Accretion Disk
- 2) Coronal Geometry



**Theoretical Predictions
of the Properties of the
Reflection and Thermal
Photons**

THEORETICAL MODELS

Standard Physics

Fundamental Physics

- 1) Kerr Spacetime
- 2) Geodesic Motion
- 3) Same Atomic Physics as in our Laboratories on Earth

Astrophysical Model

- 1) Accretion Disk
- 2) Coronal Geometry



**Theoretical Predictions
of the Properties of the
Reflection and Thermal
Photons**

OUR MODELS

- **RELXILL_NK** (Bambi et al. 2017; Abdikamalov et al. 2019)
Reflection spectrum of a thin accretion disk
- **NKBB** (Zhou et al. 2019)
Thermal spectrum of a thin accretion disk

OUR MODELS

Tests of Fundamental Physics:

- Kerr spacetime \Rightarrow **Kerr hypothesis**
- Geodesic motion \Rightarrow **Weak Equivalence Principle**
- Atomic physics
 \Rightarrow **Local Lorentz Invariance and Local Position Invariance**

How CAN WE TEST GENERAL RELATIVITY?

- **Top-down approach:** we test a specific alternative theory of gravity against Einstein's theory of General Relativity
Problems:
 - ▶ A large number of theories of gravity...
 - ▶ Usually we do not know their rotating black hole solutions...
- **Bottom-up approach:** we parametrize possible deviations from General Relativity with a number of phenomenological “deformation parameters”

BOTTOM-UP APPROACH

- Parametrized Post-Newtonian (PPN) formalism
- Weak field limit: $M/r \ll 1$
- Solar System experiments

$$\begin{aligned} ds^2 = & - \left(1 - \frac{2M}{r} + \beta \frac{2M^2}{r^2} + \dots \right) dt^2 \\ & + \left(1 + \gamma \frac{2M}{r} + \dots \right) (dx^2 + dy^2 + dz^2) \end{aligned}$$

$|\beta - 1| < 2.3 \cdot 10^{-4}$ (Lunar Laser Ranging experiment)

$|\gamma - 1| < 2.3 \cdot 10^{-5}$ (Cassini spacecraft)

In the General Relativity (Schwarzschild metric), $\beta = \gamma = 1$

BLACK HOLES IN GENERAL RELATIVITY

- “No-Hair Theorem” $\rightarrow M, J, Q (a_* = J/M^2)$
- Uncharged black holes \rightarrow Kerr solution
- Clear predictions on particle motion

ASTROPHYSICAL BLACK HOLES

It is remarkable that the spacetime metric around astrophysical black holes formed from gravitational collapse of stars/clouds should be **well approximated** by the “ideal” Kerr metric

- Initial deviations → Quickly radiated away by GWs
- Accretion disk, nearby stars → Negligible
- Electric charge → Negligible

BLACK HOLES BEYOND GENERAL RELATIVITY

Macroscopic deviations from the Kerr metric are predicted in many models

- Quantum gravity effects (information paradox)
 - ▶ Mathur (Fuzzballs)
 - ▶ Dvali & Gomez
 - ▶ Giddings
 - ▶ ...
- Modified theories of gravity
 - ▶ Einstein-dilaton-Gauss-Bonnet gravity
 - ▶ Chern-Simons gravity
 - ▶ Lorentz-violating theories
 - ▶ ...
- Presence of exotic matter
 - ▶ Hairy black holes (Herdeiro & Radu)
 - ▶ ...

TESTING THE KERR HYPOTHESIS

There are several parametric black hole spacetimes in the literature. Johannsen metric¹:

$$\begin{aligned} ds^2 &= -\frac{\tilde{\Sigma}(\Delta - a^2 A_2^2 \sin^2 \theta)}{B^2} dt^2 + \frac{\tilde{\Sigma}}{\Delta A_5} dr^2 + \tilde{\Sigma} d\theta^2 \\ &\quad - \frac{2a[(r^2 + a^2)A_1 A_2 - \Delta]\tilde{\Sigma} \sin^2 \theta}{B^2} dt d\phi \\ &\quad + \frac{[(r^2 + a^2)^2 A_1^2 - a^2 \Delta \sin^2 \theta]\tilde{\Sigma} \sin^2 \theta}{B^2} d\phi^2, \\ \tilde{\Sigma} &= r^2 + a^2 \cos^2 \theta, \quad \Delta = r^2 - 2Mr + a^2, \\ B &= (r^2 + a^2)A_1 - a^2 A_2 \sin^2 \theta \end{aligned}$$

¹Johannsen, PRD 88, 044002 (2013)

TESTING THE KERR HYPOTHESIS

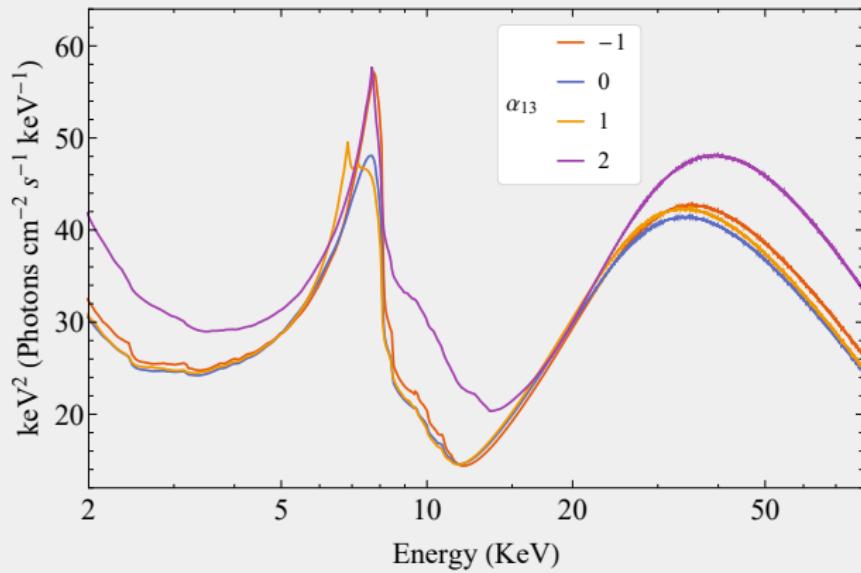
The functions f , A_1 , A_2 , and A_5 are defined as

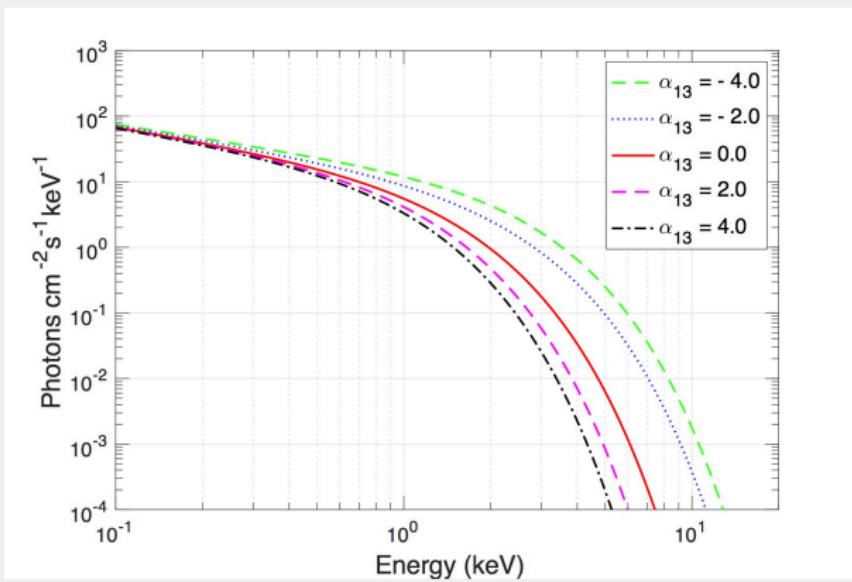
$$\begin{aligned} f &= \sum_{n=3}^{\infty} \epsilon_n \frac{M^n}{r^{n-2}}, \quad A_1 = 1 + \sum_{n=3}^{\infty} \alpha_{1n} \left(\frac{M}{r}\right)^n, \\ A_2 &= 1 + \sum_{n=2}^{\infty} \alpha_{2n} \left(\frac{M}{r}\right)^n, \quad A_5 = 1 + \sum_{n=2}^{\infty} \alpha_{5n} \left(\frac{M}{r}\right)^n \end{aligned}$$

There are 4 infinite sets of “deformation parameters”:

$$\{\epsilon_n\}, \quad \{\alpha_{1n}\}, \quad \{\alpha_{2n}\}, \quad \{\alpha_{5n}\}$$

If all deformation parameters vanish, we recover the Kerr solution

Impact of the deformation parameter α_{13} 

Impact of the deformation parameter α_{13} 

RESULTS

SOURCES ANALYZED (BHBS)

Sources analyzed with `RELXILL_NK` and `NKBB`

- **4U 1630–472:** Tripathi et al., ApJ 913, 79 (2021)
- **Cygnus X-1;** Liu et al., PRD 99, 123007 (2019); Zhang et al., PRD 103, 024055 (2021)
- **EXO 1846–031:** Tripathi et al., ApJ 913, 79 (2021)
- **GRS 1716–249:** Zhang et al., ApJ 924, 72 (2022)
- **GRS 1739–278:** Tripathi et al., ApJ 913, 79 (2021)
- **GRS 1915+105;** Zhang et al., ApJ 875, 41 (2019); ApJ 884, 147 (2019); Tripathi et al., JCAP 01 (2022) 019
- **GS 1354–645:** Xu et al., ApJ 865, 134 (2018)
- **GX 339–4:** Wang et al., JCAP 05 (2020) 026; Tripathi et al., ApJ 907, 31 (2021)
- **LMC X-1:** Tripathi et al., ApJ 897, 84 (2020)
- **Swift J1658–4242:** Tripathi et al., ApJ 913, 79 (2021)

SOURCES ANALYZED (AGN)

Sources analyzed with [RELXILL_NK](#)

- **1H0419–577**: [Tripathi et al., ApJ 874, 135 \(2019\)](#)
- **1H0707–495**: [Cao et al., PRL 120, 051101 \(2018\)](#)
- **Ark 120**: [Tripathi et al., ApJ 874, 135 \(2019\)](#)
- **Ark 564**: [Tripathi et al., PRD 98, 023018 \(2018\)](#)
- **Fairall 9**: [Liu et al., ApJ 896, 160 \(2020\)](#)
- **MCG–6–30–15**: [Tripathi et al., ApJ 875, 56 \(2019\)](#)
- **Mrk 335**: [Choudhury et al., ApJ 879, 80 \(2019\)](#)
- **PKS 0558–504**: [Tripathi et al., ApJ 874, 135 \(2019\)](#)
- **Swift J0501.9–3239**: [Tripathi et al., ApJ 874, 135 \(2019\)](#)
- **Ton S180**: [Tripathi et al., ApJ 874, 135 \(2019\)](#)

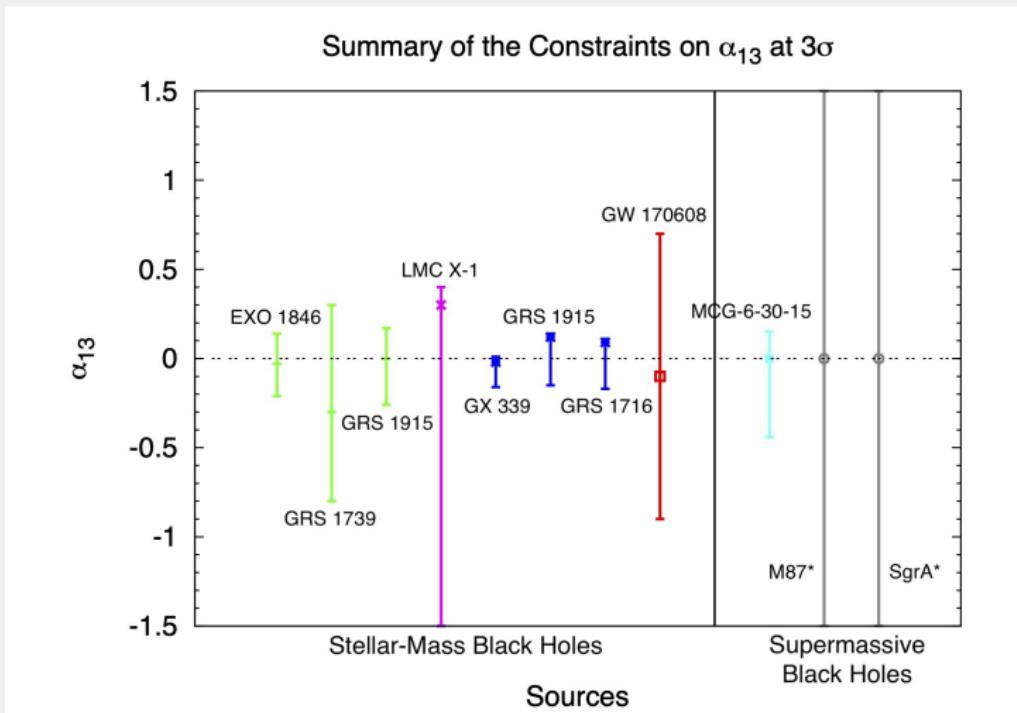
TESTS ON SPECIFIC GRAVITY THEORIES

Theories constrained with [RELXILL_NK](#)

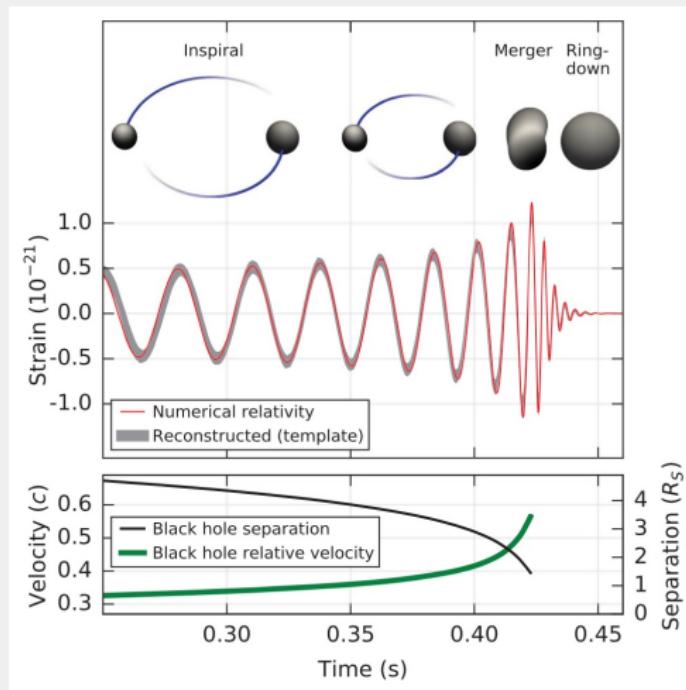
- **Einstein-Maxwell-Dilaton-Axion Gravity:**
[Tripathi et al., JCAP 07 \(2021\) 002](#)
- **Asymptotically Safe Quantum Gravity:**
[Zhou et al., JCAP 01 \(2021\) 047](#)
- **Kaluza-Klein Gravity:**
[Zhu et al., EPJC 80, 622 \(2020\)](#)
- **Conformal Gravity:**
[Zhou et al., PRD 98, 024007 \(2018\); EPL 125, 30002 \(2019\)](#)

AGNOSTIC TESTS

Constraints on the Johannsen deformation parameter α_{13}



GW TESTS



Abbott et al. PRL 116, 061102 (2016)

EM TESTS VS GW TESTS

EM Tests:

- Particle motion
- Non-gravitational physics in strong gravitational fields

EM tests are more suitable to study the interactions between the matter and gravity sectors

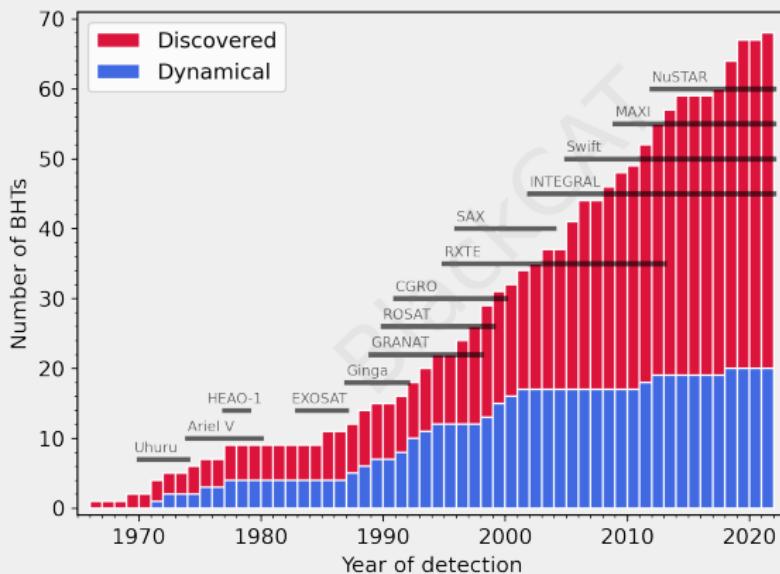
GW Tests:

- Dynamical regime

GW tests are more suitable to study the gravity sector itself

NUMBER OF SOURCES: STELLAR-MASS BHs IN XRBs

- $10^8 - 10^9$ stellar-mass black holes in the Galaxy (estimate)
- We know less than 100 objects
- We have a spin measurement from about 30 objects

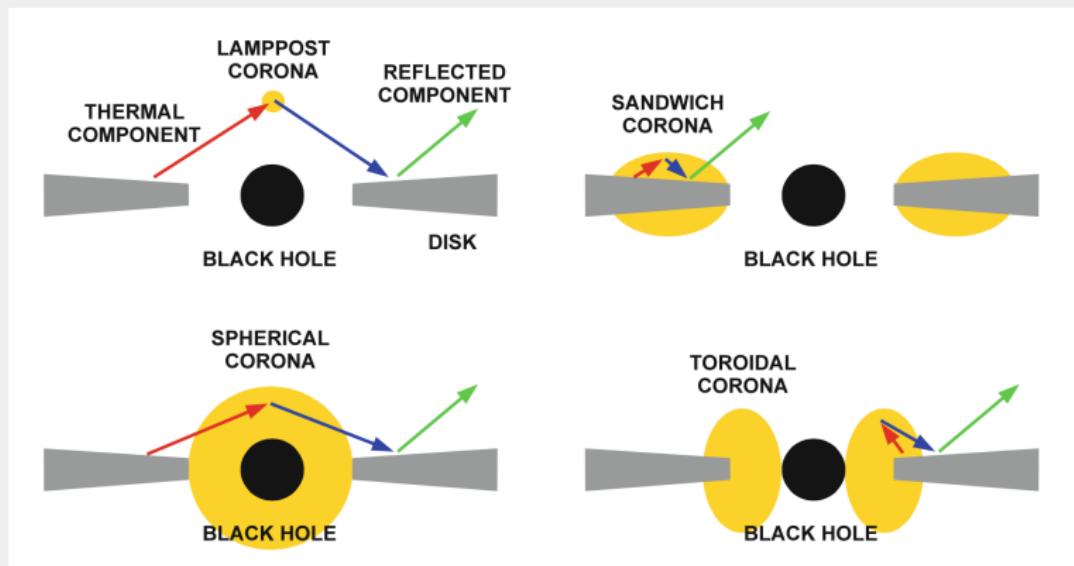


SOURCE SELECTION

- Source selection for X-ray Reflection Spectroscopy
 - 1. Prominent iron line
 - 2. High spin ($a_* > 0.9$)
 - 3. Compact corona close to the black hole
 - 4. Bright source
 - 5. $L \sim 0.05 - 0.30 L_{\text{Edd}}$ ($R_{\text{in}} = R_{\text{ISCO}}$)
 - 6. High resolution at the iron line + Data up to 50-100 keV (e.g. *XMM-Newton* + *NuSTAR*)
 - 7. Constant flux

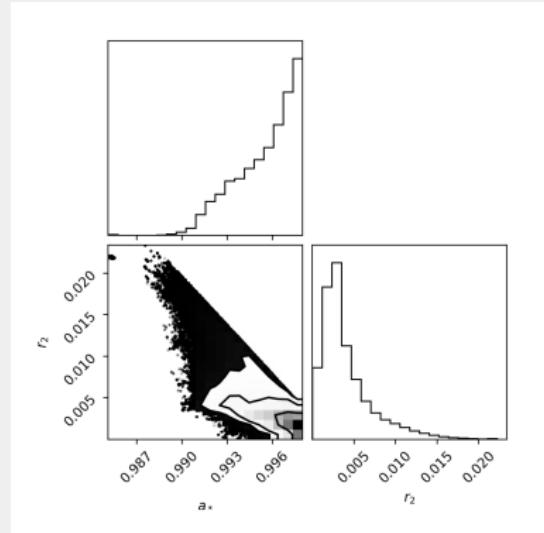
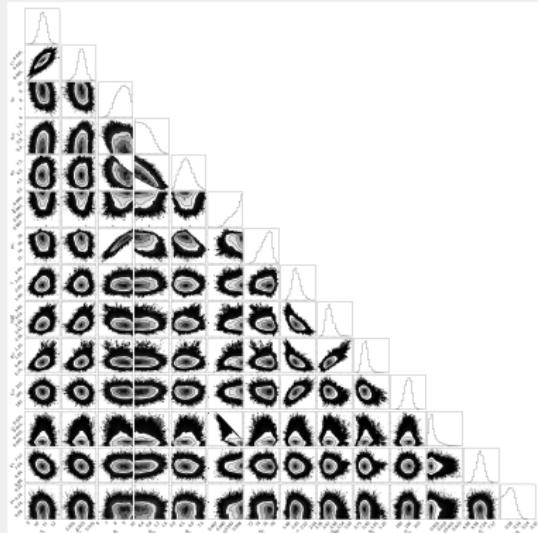
THANK YOU!

CORONAL MODELS



EINSTEIN-MAXWELL-DILATON-AXION GRAVITY

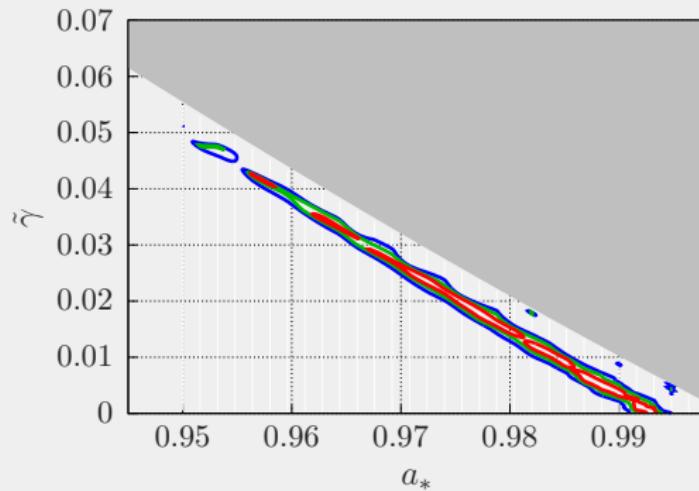
NuSTAR observation of EXO 1846–031
Constraint: $r_2 < 0.011$ (90% CL)



ASYMPTOTICALLY SAFE QUANTUM GRAVITY

Suzaku observation of GRS 1915+105

Constraint: $\tilde{\gamma} < 0.047$ (90% CL)



CONFORMAL GRAVITY

NuSTAR observation of GS 1354–645
Constraint: $L/M < 0.12$ (99% CL)

