

Section 2.

1. $T = \begin{bmatrix} \lambda & 0 \\ 0 & \lambda \end{bmatrix}$, $\lambda \in \mathbb{R} \setminus \{0\}$.

2. Let $g(x) = 3x^T A x$. $f(g(x)) = 2\sin(g(x))$.

$$\begin{aligned} \nabla_x f(x) &= \frac{df}{dg} \frac{dg}{dx} = 2\cos(3x^T A x) \cdot 3(A + A^T)x \\ &= 6\cos(3x^T A x)(A + A^T)x. \end{aligned}$$

