

Section 3.

$$1. P(S=s|X=x) = \frac{P(X=x|S=s) P(S=s)}{P(X)}$$

$$2. X=AB: \quad (\underline{2}, 1) \quad (\underline{2}, 3) \quad (\underline{4}, 1) \quad (\underline{4}, 3)$$

$$X=AC: \quad (\underline{2}, 2) \quad (\underline{2}, 3) \quad (\underline{4}, 2) \quad (\underline{4}, 3)$$

$$X=BC: \quad (\underline{1}, 2) \quad (\underline{1}, 3) \quad (\underline{3}, 2) \quad (\underline{3}, 3)$$

$$\therefore P(S=5) = \frac{4}{12} = \frac{1}{3}.$$

$$3. P(C \text{ flipped} | S=5) = \frac{2}{4} = \frac{1}{2}.$$

$$P(C \text{ flipped}) = P(X=AC) + P(X=BC) = \frac{2}{3} < P(C \text{ flipped} | S=5) < P(C \text{ flipped})$$

$$4. P(C \text{ flipped} | S=7) = \frac{1}{2}.$$

$$P(C \text{ flipped} | S=3) = \frac{1}{2} = P(C \text{ flipped} | S=7).$$

$$P(C \text{ flipped} | S=4) = 1 > P(C \text{ flipped} | S=7).$$

$$P(C \text{ flipped} | S=5) = \frac{1}{2} = P(C \text{ flipped} | S=7).$$

$$P(C \text{ flipped} | S=6) = 1 > P(C \text{ flipped} | S=7).$$

$$P(C \text{ flipped} | S=7) < P(C \text{ flipped}).$$

