

Binary Image Analysis

Week 04

Announcement

- Introduction of our course representatives
 - Duan Dao: u7236134@anu.edu.au
 - Maiteryi Singh: u7075106@anu.edu.au
- Lab Engagement: Ask questions related to your Lab assignment.
- Watch the video about how to write a good report.

Announcement: Mid-term Exam

EXAMS MANAGER

Semester 1 - Mid Semester, 2021 : Final Timetable

To view a different exam period, click [here](#).

Unit Codes

You can search for multiple units by putting a comma between your unit codes.

SEARCH : FINAL TIMETABLE

Displaying records 1 to 1 of 1

Exam Code	Exam Title	Date	Time	Writing Time (minutes)	Reading Time (minutes)	Venue	Exam Conditions
ENG6528_Semester 1	Computer Vision	Tuesday 20/04/2021	12:00pm	90	15	Online Exam - Wattle	Any material ,

Displaying records 1 to 1 of 1

Updated: 9 March 2021 / Responsible Officer: Registrar, Student Administration / Page Contact: [Examinations Officer](#)

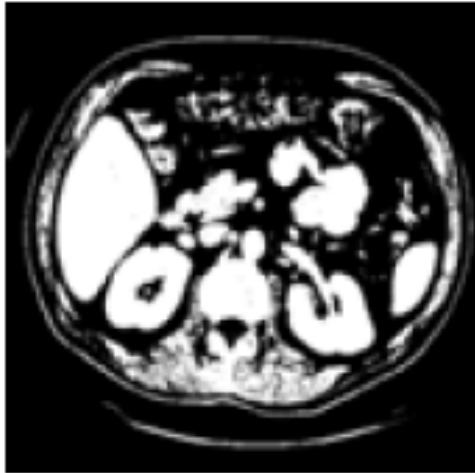
Announcement: Mid-term Exam

- Sample mid-term papers will be posted online.
- We will also provide answers in the video format. It requires students to check the answers by watching the video by yourself.

Contents

- Image threshold (histogram binarization)
- Mathematical Morphology

Why binary ?



0	0	0	0	0
1	1	1	1	1
2	2	2	2	2
3	3	3	3	3
4	4	4	4	4
5	5	5	5	5
6	6	6	6	6
7	7	7	7	7
8	8	8	8	8
9	9	9	9	9

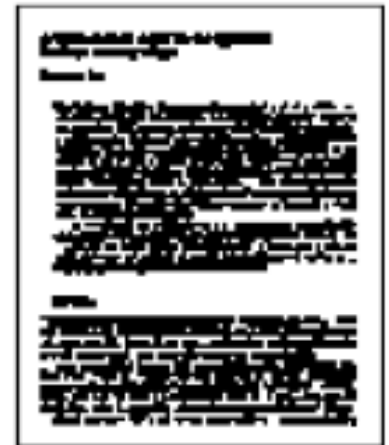
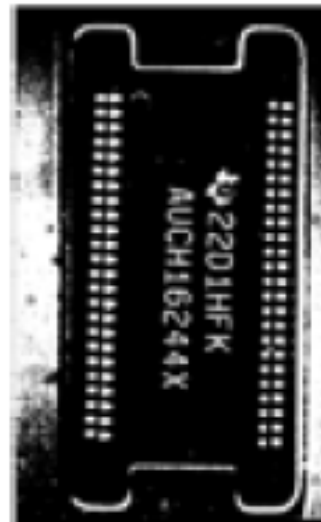
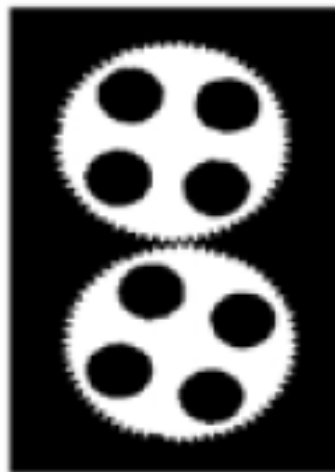


Image threshold (binarization)

- What is **Thresholding** ?
 - It is a pixel labeling operation.
 - It assigns a binary value to each pixel.
 - **Binary Value 1**: pixels have higher intensity values
 - **Binary Value 0**: pixels have lower intensity values



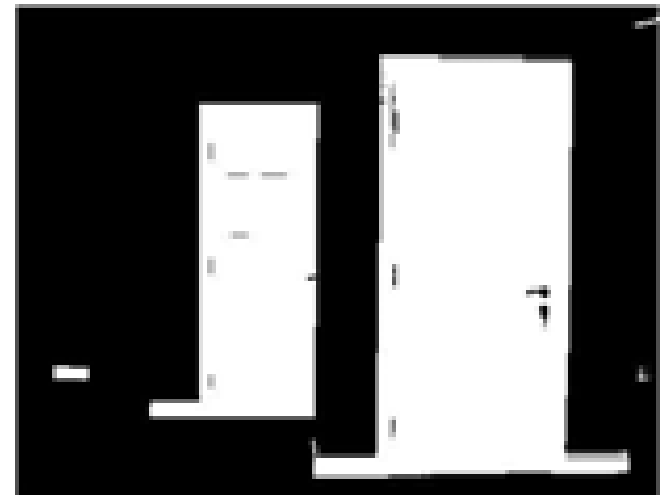
$T=128$ →



Thresholding

- Given a grayscale image or an intermediate matrix → threshold to create a binary output.

Example: intensity-based detection



```
fg_pix = find(im < 65);
```

Looking for dark pixels

Thresholding

- Given a grayscale image or an intermediate matrix \rightarrow threshold to create a binary output.

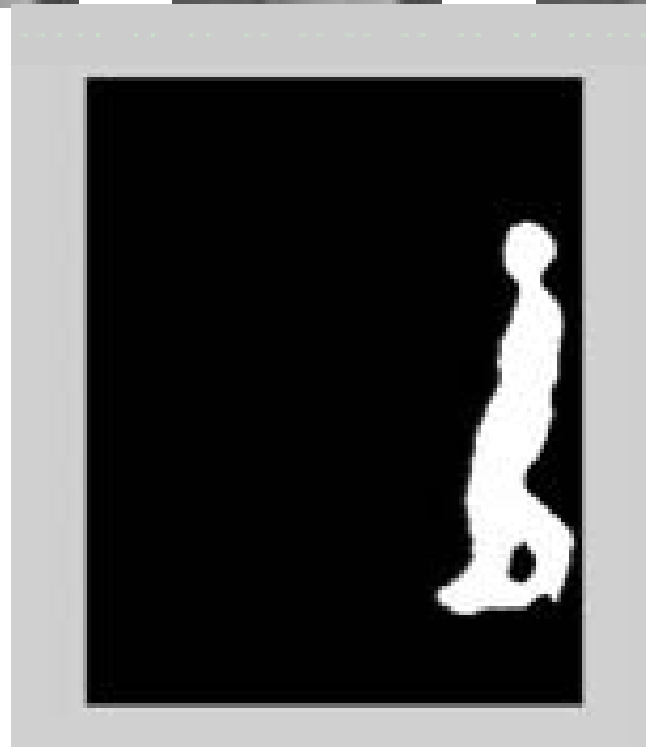
Example: background subtraction



Looking for pixels that differ significantly from the "empty" background.

```
fg_pix = find(diff > t);
```

Example using binary image analysis: Bg subtraction + blob detection



Thresholding

- Given a grayscale image or an intermediate matrix \rightarrow threshold to create a binary output.

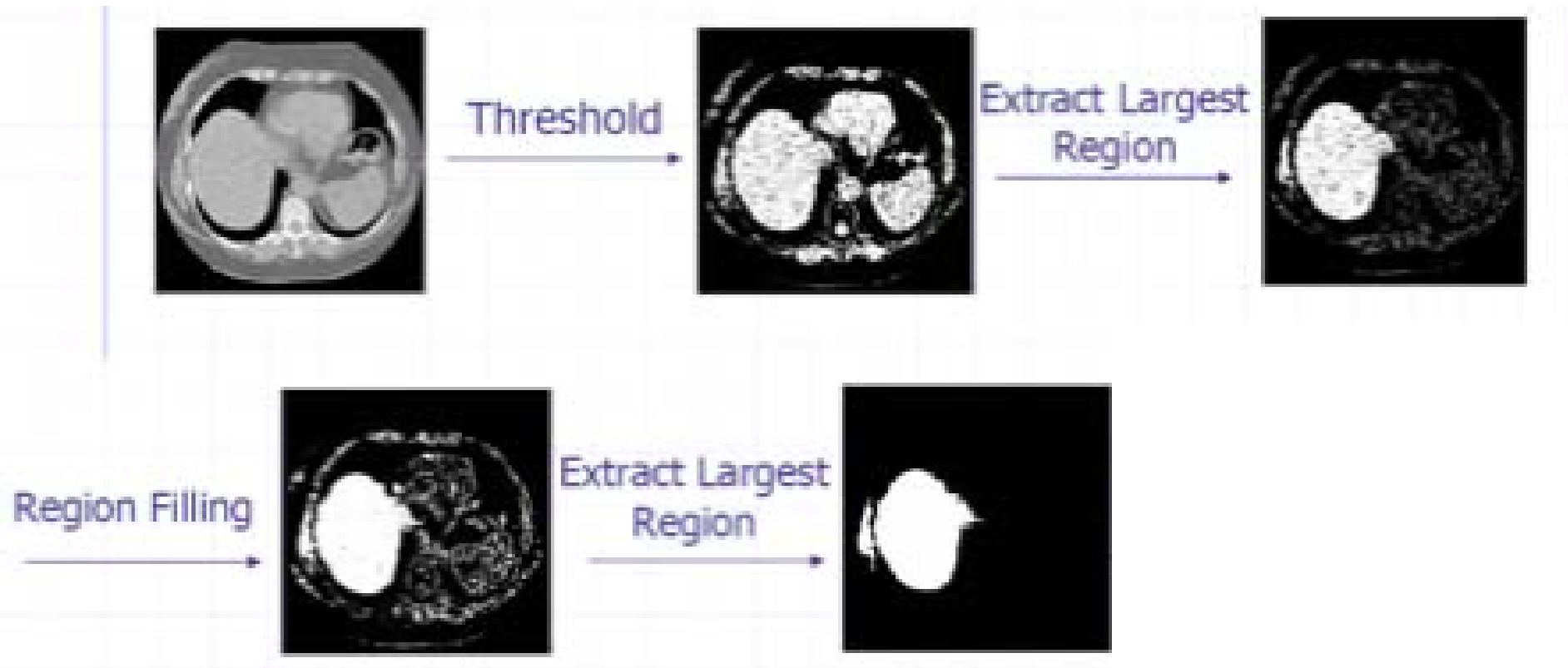
Example: color-based detection



```
fg_pix = find(hue > t1 & hue < t2);
```

Looking for pixels within a certain hue range.

Example using binary image analysis: segmentation of a liver

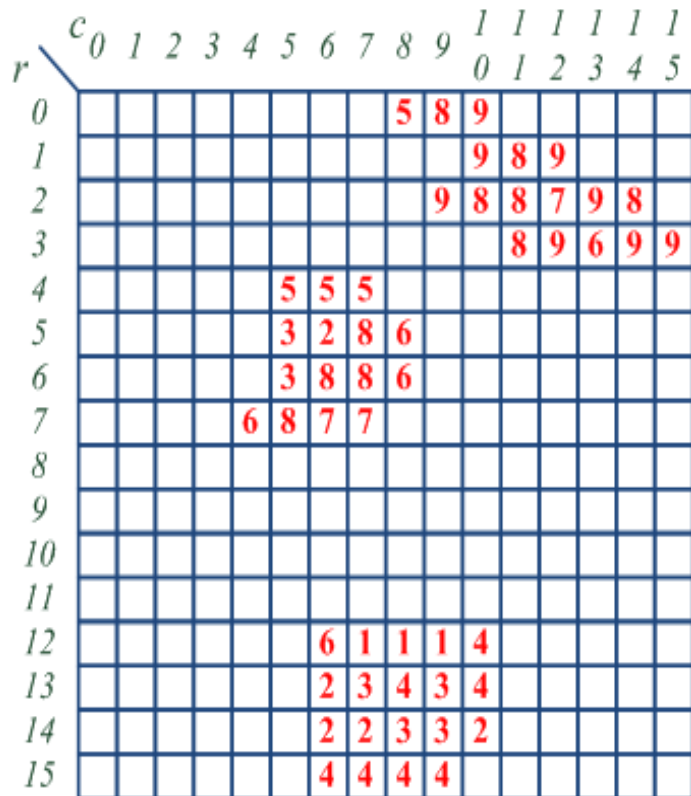


- Mathematical Formulation

$$B(r, c) = \begin{cases} 1 & \text{if } I(r, c) \geq T \\ 0 & \text{if } I(r, c) < T \end{cases}$$

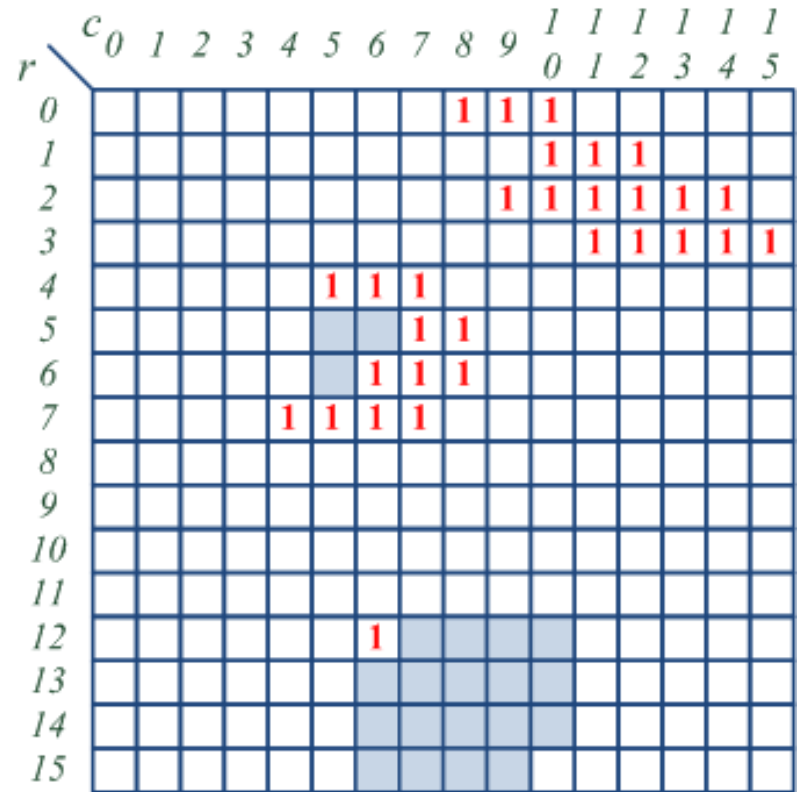
- (r, c) : row and column
- $I(.,.)$: gray-level intensity image
- T : intensity threshold
- $B(.,.)$: binary intensity image

How to select an appropriate threshold ?



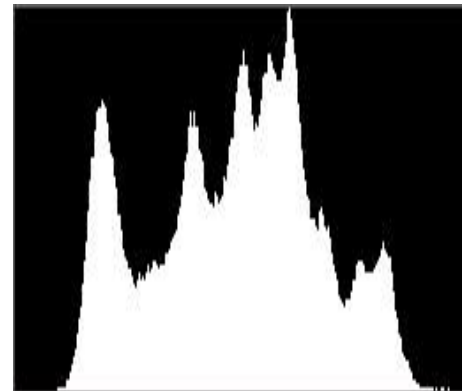
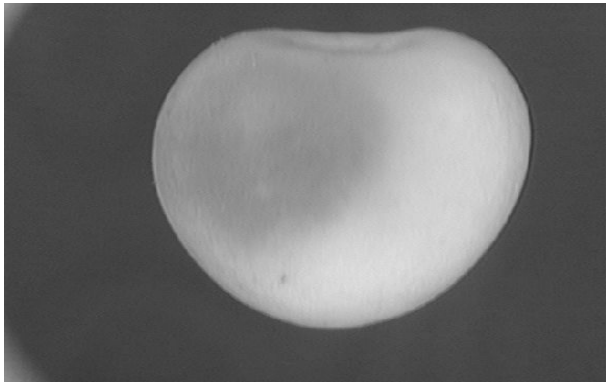
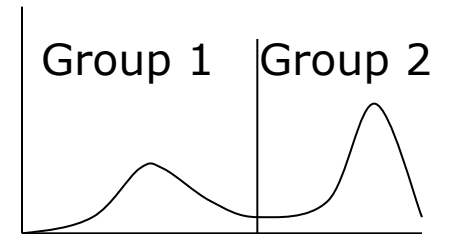
$I(.,.)$

$$T = 5$$



$B(.,.)$

- Approach: Histogram analysis



Where to pick an optimal threshold?

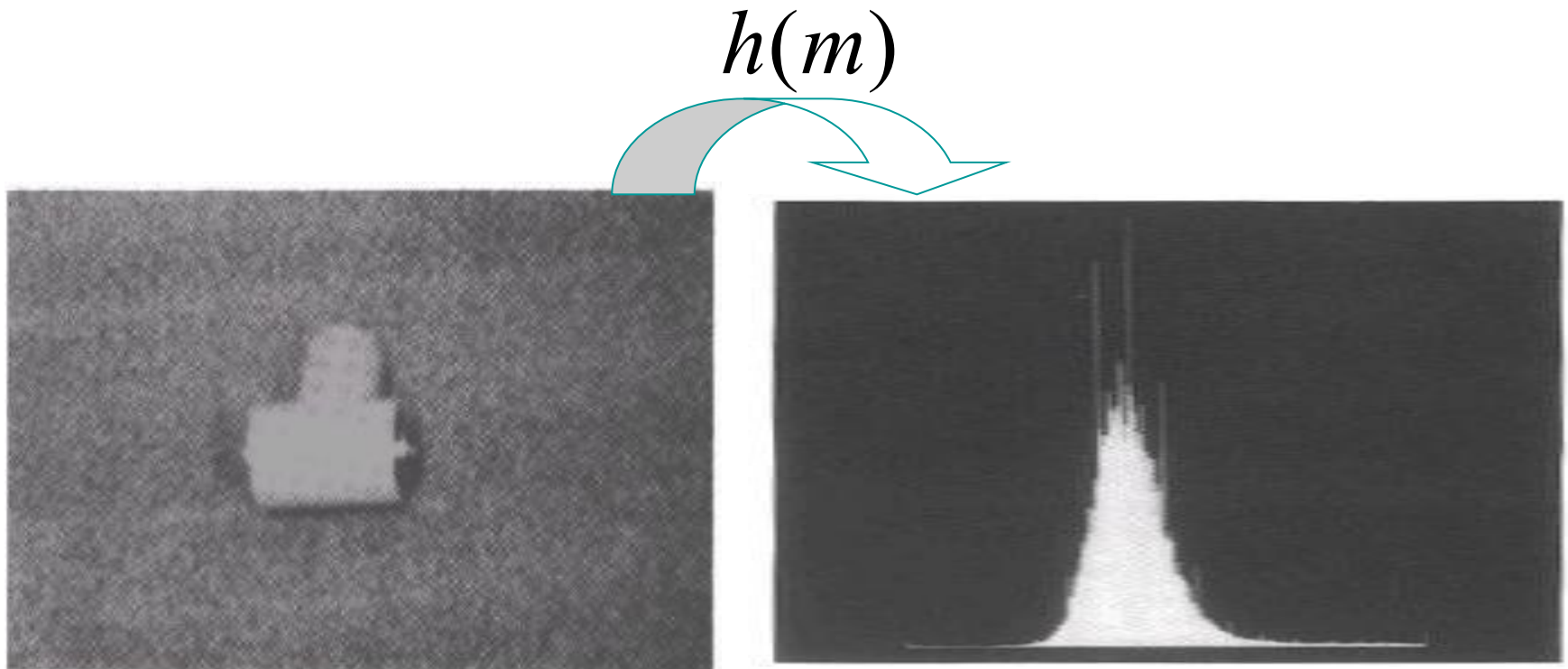


Figure 2.6 BNC T-connector against a dark background.

Figure 2.7 Histogram of the BNC T-connector image of Fig. 2.6.

Histogram

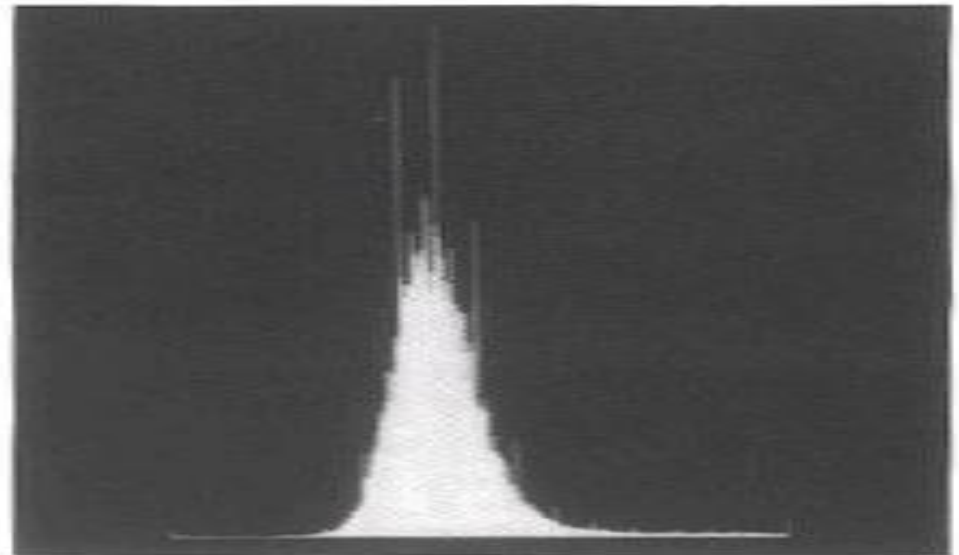
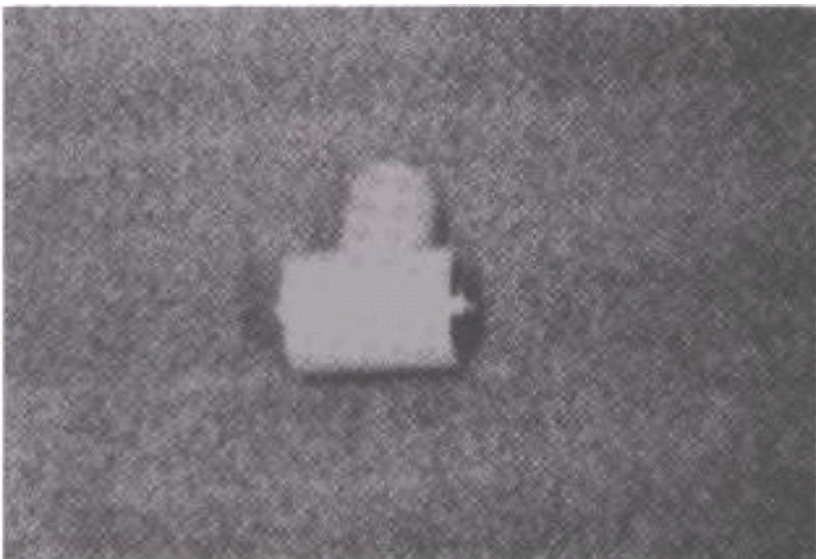
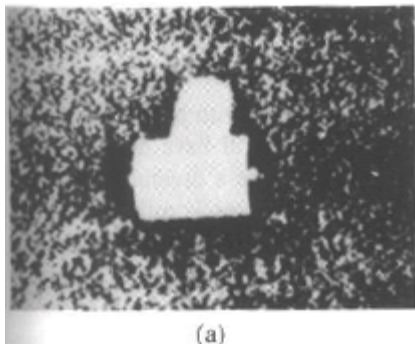
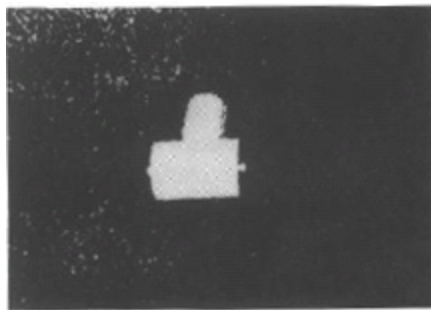


Figure 2.7 Histogram of the BNC T-connector image of Fig. 2.6.



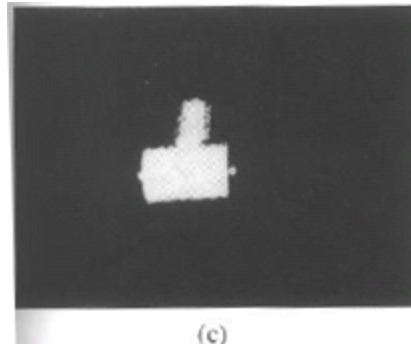
(a)

T=110



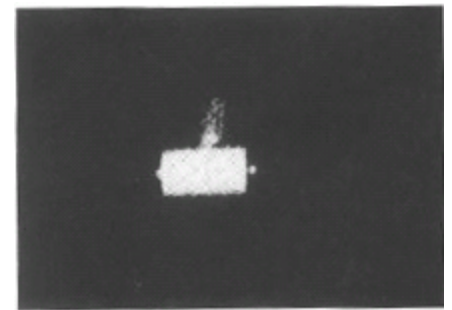
(b)

T=130



(c)

T=150



(d)

T=170

Basic Global Thresholding

Simple Idea:

1. Select an initial estimate for T .
2. Segment image using T into two groups G_1 and G_2 .
3. Compute the average gray level value as μ_1 and μ_2
4. Compute a new threshold value:

$$T = \frac{1}{2}(\mu_1 + \mu_2)$$

5. Repeat steps 2 through 4 until the difference in T in successive iteration is smaller than a predefined parameter T_0

How to find an optimal threshold ?

- There is no generic solution.
- The optimal solution is often problem-dependent;
- A heuristic binarisation algorithm based on K-L divergence:
 - fitting a 2-mode Gaussian mixture model to the histogram: minimizing K-L divergence.

Region Property Computation

Region property computation

- For each connected region, we can compute many of its properties, e.g.
 - Areas
 - Perimeter
 - Centre of gravity
 - circularity,
 - Major axis
 - Minor axis
 - mean and standard deviation of radial distance
 - bounding box
 - extremal axis length from bounding box
 - **second order moments** (row, column, mixed)
 - ...

Region properties

- Assume:

$b(i, j)$ is discrete,
only one object is in the image.

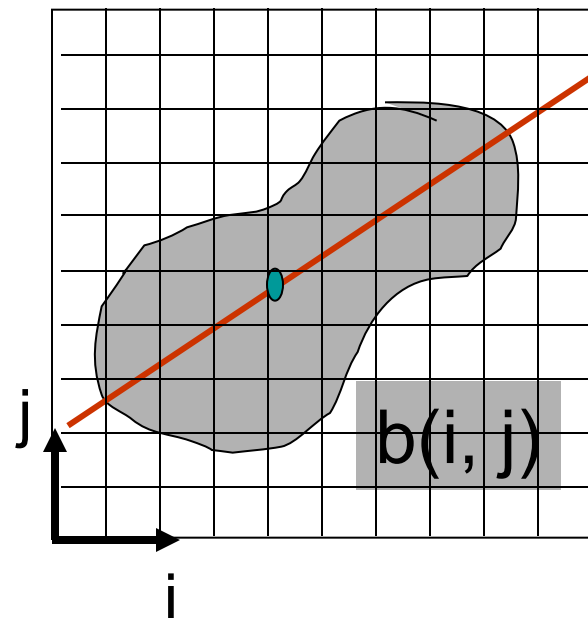
- Areas (0-th Moment) $A = \sum \sum b_{ij}$

- Center of Mass (First Moment)

$$\bar{x} = \frac{1}{A} \sum \sum i b_{ij} \quad \bar{y} = \frac{1}{A} \sum \sum j b_{ij}$$

- Second Moments:

$$a' = \sum \sum i^2 b_{ij} \quad b' = 2 \sum \sum ij b_{ij} \quad c' = \sum \sum j^2 b_{ij}$$



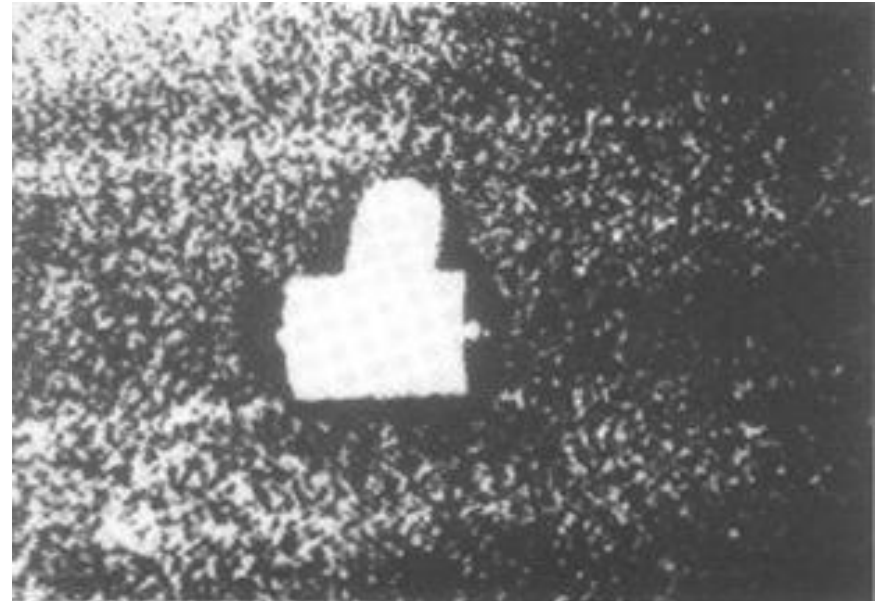
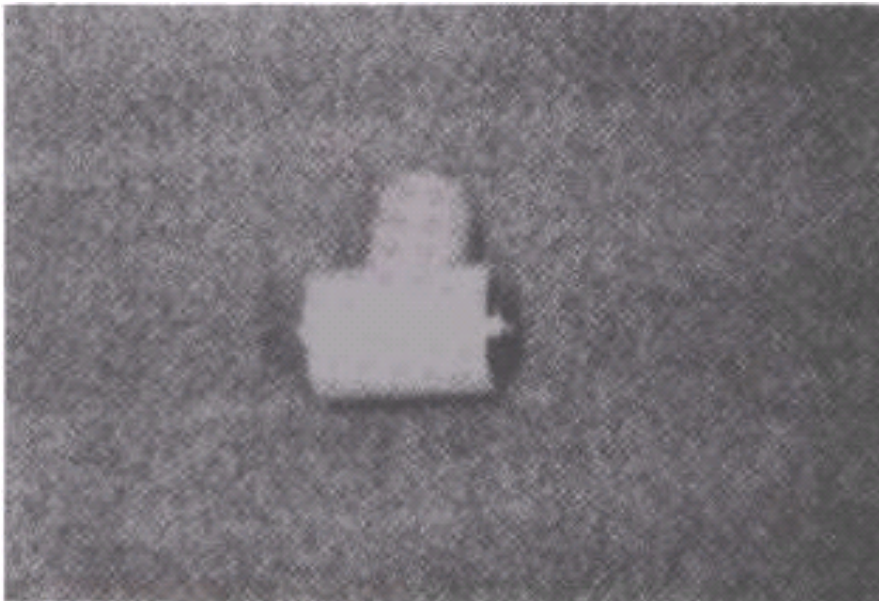
Note: a', b', c' are defined w.r.t origin

Mathematical Morphology

- **Morphology:** originally, a branch of biology science that studies the form and structure of animals and plants
- Mathematical Morphology in image processing is used to **extract image components** for representation and description of region shape, such as boundaries, skeletons, and the convex hull.

Motivation: remove small noisy regions

- Example result by a binarisation algorithm



Mathematical Morphology

In binary image processing, mathematical morphology consists of two basic operations,

dilation , erosion

and several composite operations

closing , opening, . . .

Logic Operations Involving Binary Image

- The principal logic operations used in image processing: AND, OR, and NOT(complement)
- Logic operations are performed on a pixel-wise basis, except the NOT operation.
- Their properties are summarized below.

Chapter 9 ■ Morphological Image Processing

TABLE 9.1
The three basic
logical operations.

p	q	$p \text{ AND } q \text{ (also } p \cdot q \text{)}$	$p \text{ OR } q \text{ (also } p + q \text{)}$	$\text{NOT } (p) \text{ (also } \bar{p} \text{)}$
0	0	0	0	1
0	1	0	1	1
1	0	0	1	0
1	1	1	1	0



Scanned with
CamScanner

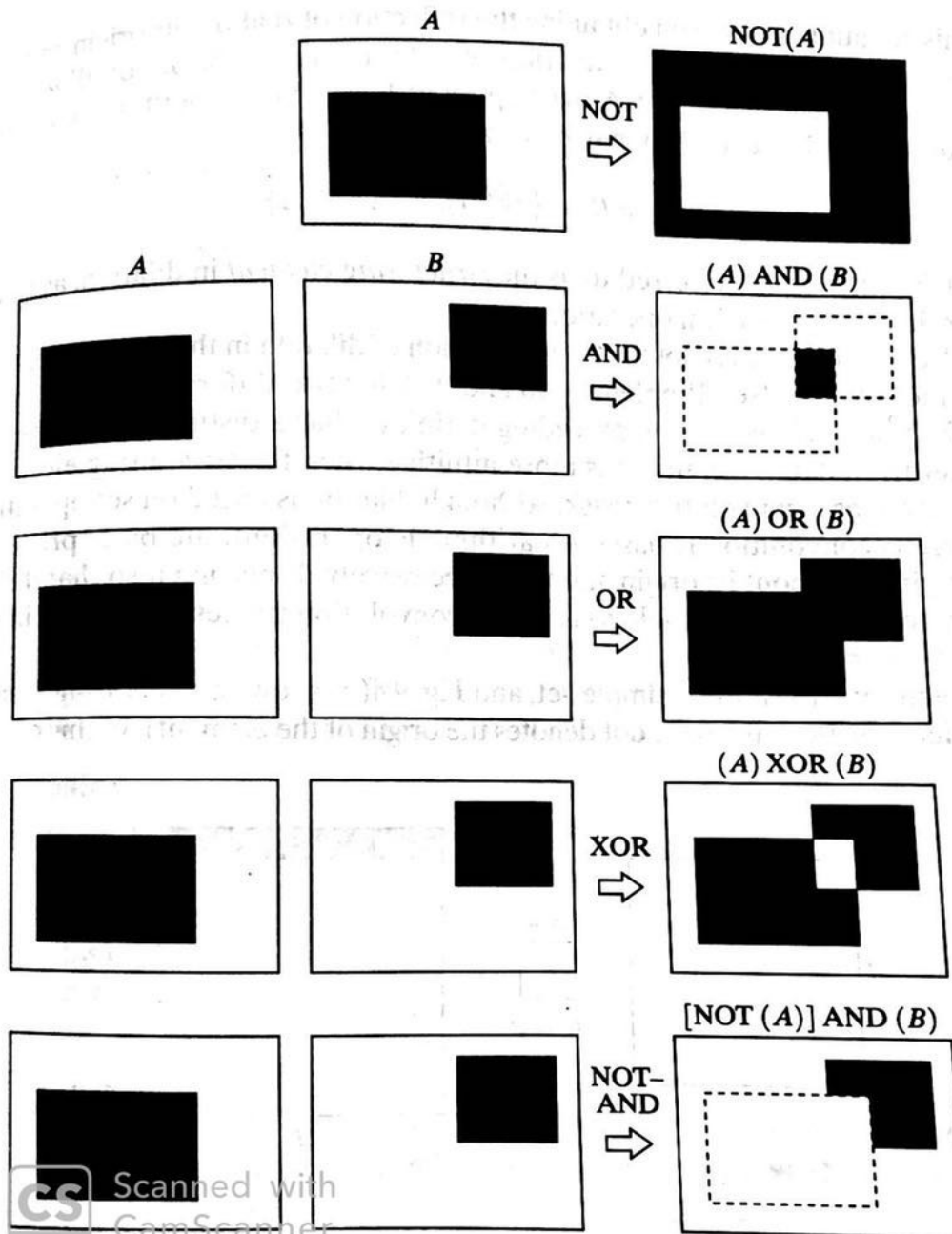


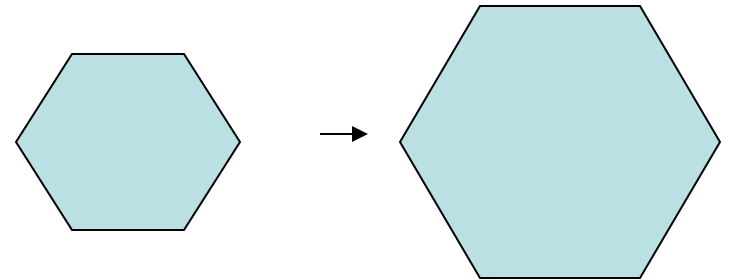
FIGURE 9.3 Some logic operations between binary images. Black represents binary 1s and white binary 0s in this example.

Dilation

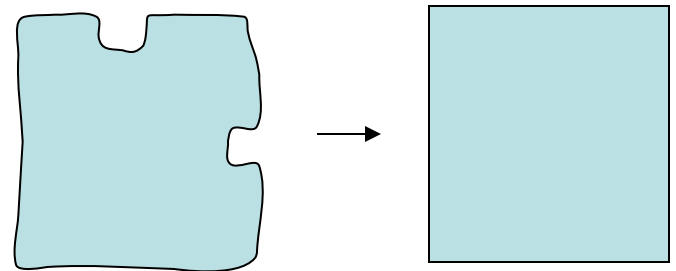
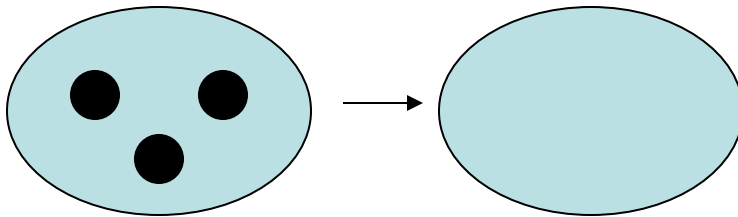
Dilation **expands** the connected sets of 1s of a binary image.

It can be used for

1. growing features



2. filling holes and gaps

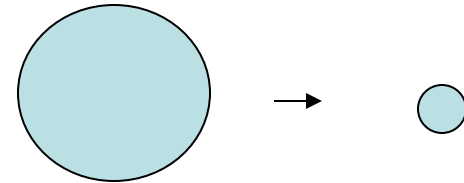
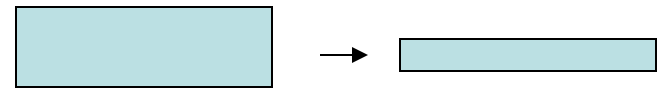


Erosion

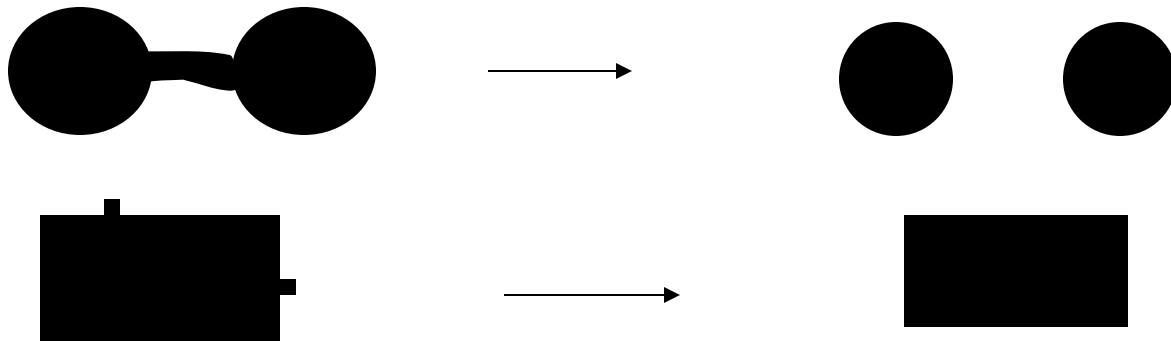
Erosion **shrinks** the connected sets of 1s of a binary image.

It can be used for

1. shrinking features



2. Removing bridges, branches and small protrusions



Structuring Elements

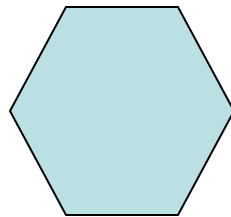
A **structuring element** is a shape mask used in the basic morphological operations.

They can be any shape and size that is digitally representable, and each has an **origin**.

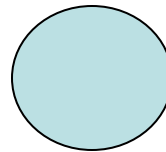


box

box(length,width)

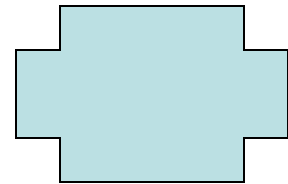


hexagon



disk

disk(diameter)



something

Opening and Closing

- **Closing** is the composite operation of **dilation** followed by **erosion** (with the same structuring element)
- **Opening** is the composite operation of **erosion** followed by **dilation** (with the same structuring element)

- Detailed explanations
 - Dilation
 - Erosion
 - Opening
 - Closing

Matlab

- `N = hist(Y,M)`
- `L = bwlabel (BW,N) ;`
- `STATS = regionprops (L,PROPERTIES) ;`
 - `'Area'`
 - `'Centroid'`
 - `'BoundingBox'`
 - `'Orientation', ...`
- `IM2 = imerode (IM,SE) ;`
- `IM2 = imdilate (IM,SE) ;`
- `IM2 = imclose (IM, SE) ;`
- `IM2 = imopen (IM, SE) ;`

DILATION

`dilate(B,S)` takes binary image B, places the origin of structuring element S over each 1-pixel, and **ORs** the structuring element S into the output image at the corresponding position.

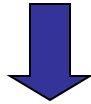
Dilation

- **Dilation** is the set of all points in the image, where the origin of the structuring element “hits” the foreground.
- Consider each foreground pixel in the input image
 - If the structuring element origin hits the foreground image, “OR” the structuring element to the image.
- **Input:**
 - **Binary Image**
 - **Structuring Element, containing only 1s!!**

Example for Dilation

Input image

0	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

1	1*	1
---	----	---



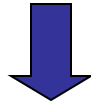
Output Image

	0								
--	---	--	--	--	--	--	--	--	--

Example for Dilation

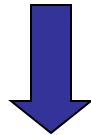
Input image

0	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

1	1	1
---	---	---



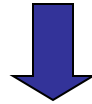
Output Image

	0	0							
--	---	---	--	--	--	--	--	--	--

Example for Dilation

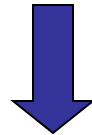
Input image

0	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

1	1	1
---	---	---



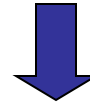
Output Image

	0	0	1						
--	---	---	---	--	--	--	--	--	--

Example for Dilation

Input image

0	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

1	1	1
---	---	---



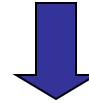
Output Image

	0	0	1	1					
--	---	---	---	---	--	--	--	--	--

Example for Dilation

Input image

0	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

1	1	1
---	---	---



Output Image

	0	0	1	1	1				
--	---	---	---	---	---	--	--	--	--

Example for Dilation

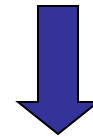
Input image

0	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

1	1	1
---	---	---



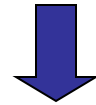
Output Image

	0	0	1	1	1	1			
--	---	---	---	---	---	---	--	--	--

Example for Dilation

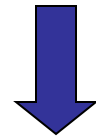
Input image

0	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

1	1	1
---	---	---



Output Image

	0	0	1	1	1	1	1		
--	---	---	---	---	---	---	---	--	--

Example for Dilation

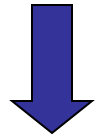
Input image

0	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

1	1	1
---	---	---



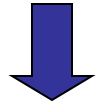
Output Image

	0	0	1	1	1	1	1	1	
--	---	---	---	---	---	---	---	---	--

Example for Dilation

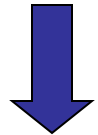
Input image

0	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

1	1	1
---	---	---



Output Image

	0	0	1	1	1	1	1	1	1
--	---	---	---	---	---	---	---	---	---

Example for Dilation

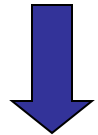
Input image

0	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

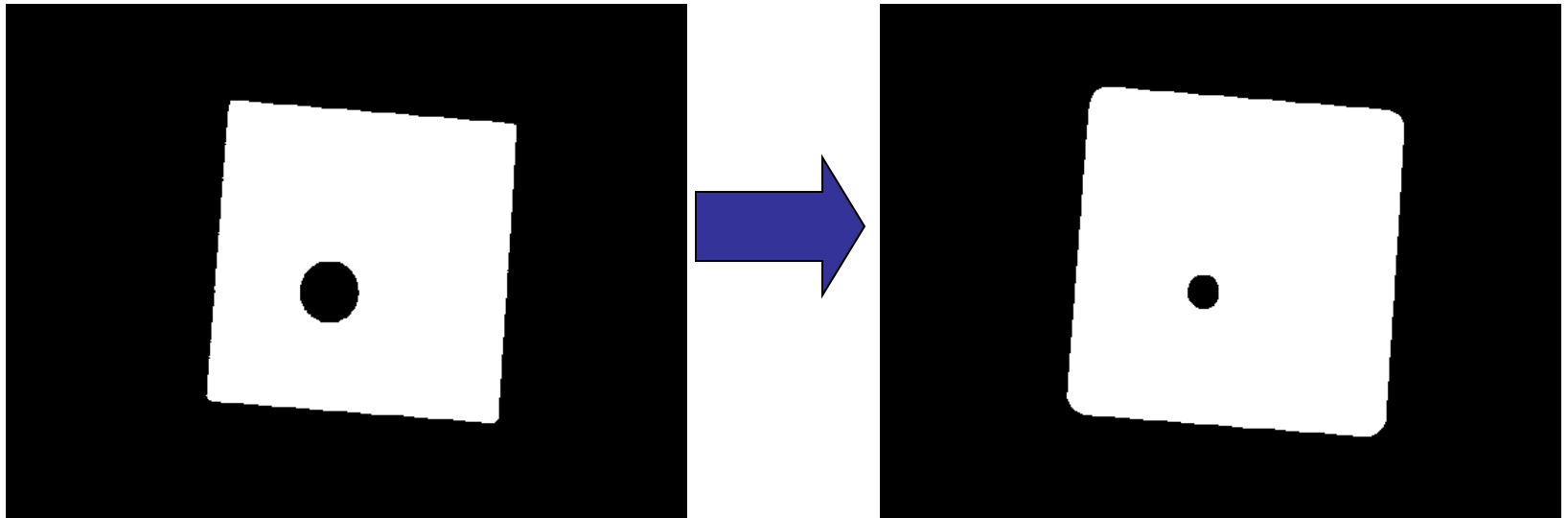
1	1	1
---	---	---



Output Image

0	0	0	1	1	1	1	1	1	1
---	---	---	---	---	---	---	---	---	---

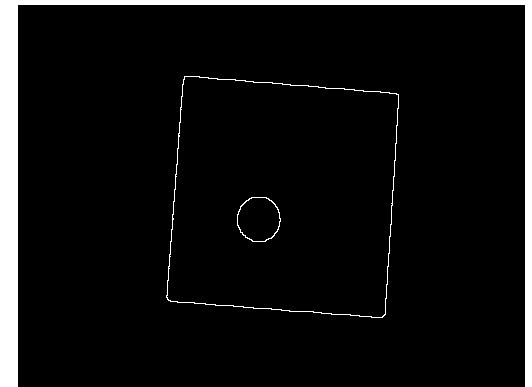
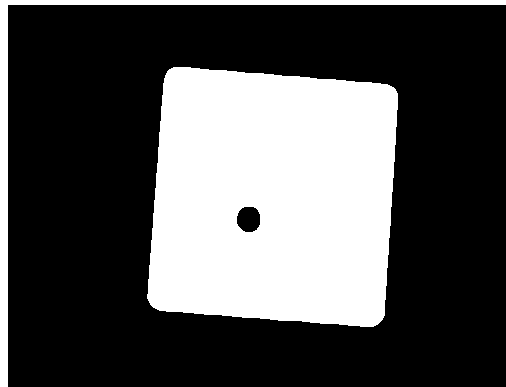
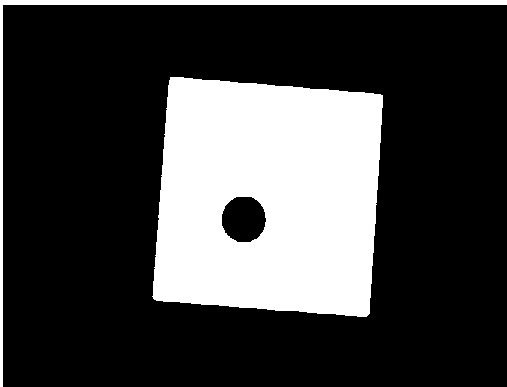
Another Dilation Example



- Image get lighter, more uniform intensity

Edge detection example

- Edge Detection
 1. Dilate input image
 2. Subtract input image from dilated image
 3. Edges remain!

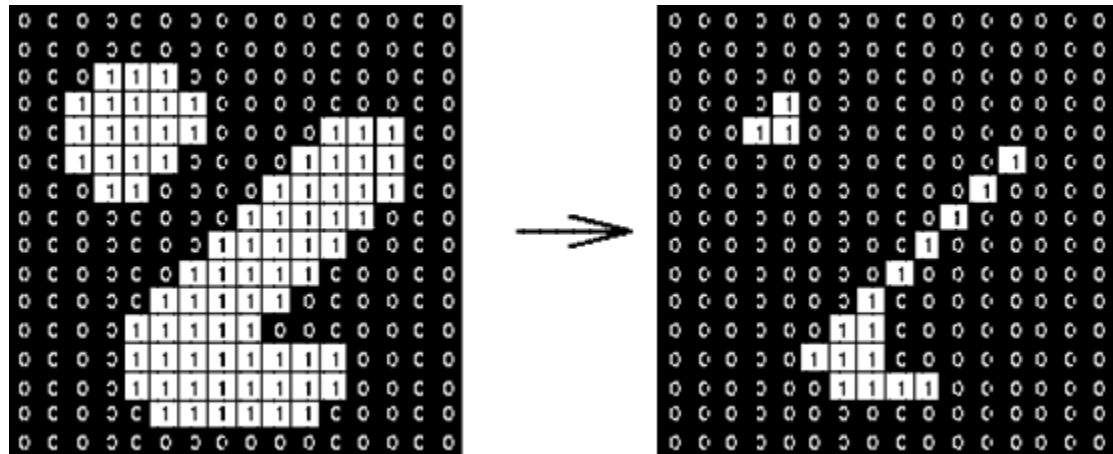


EROSION

erode(B,S) takes a binary image B, places the origin of structuring element S over every pixel position, and ORs a binary 1 into that position of the output image, if and only if every position of S (with a 1) covers a 1 in B.

Erosion

- **Erosion** is a basic morphological operation



- Applied **Structuring Element**:

1	1	1
1	1	1
1	1	1

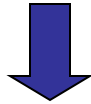
Set of coordinate points =

{ (-1, -1), (0, -1), (1, -1),
 (-1, 0), (0, 0), (1, 0),
 (-1, 1), (0, 1), (1, 1) }

Example for Erosion

Input image

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

1	1	1
---	---	---



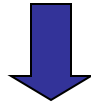
Output Image

	0								
--	---	--	--	--	--	--	--	--	--

Example for Erosion

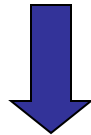
Input image

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

1	1	1
---	---	---



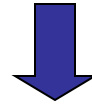
Output Image

	0	0							
--	---	---	--	--	--	--	--	--	--

Example for Erosion

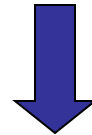
Input image

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

1	1	1
---	---	---



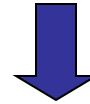
Output Image

	0	0	0						
--	---	---	---	--	--	--	--	--	--

Example for Erosion

Input image

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

1	1	1
---	---	---



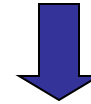
Output Image

	0	0	0	0					
--	---	---	---	---	--	--	--	--	--

Example for Erosion

Input image

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

1	1	1
---	---	---



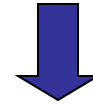
Output Image

	0	0	0	0	1				
--	---	---	---	---	---	--	--	--	--

Example for Erosion

Input image

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

1	1	1
---	---	---



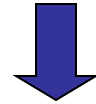
Output Image

	0	0	0	0	1	0			
--	---	---	---	---	---	---	--	--	--

Example for Erosion

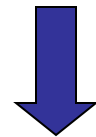
Input image

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

1	1	1
---	---	---



Output Image

	0	0	0	0	1	0	0		
--	---	---	---	---	---	---	---	--	--

Example for Erosion

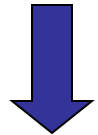
Input image

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring Element

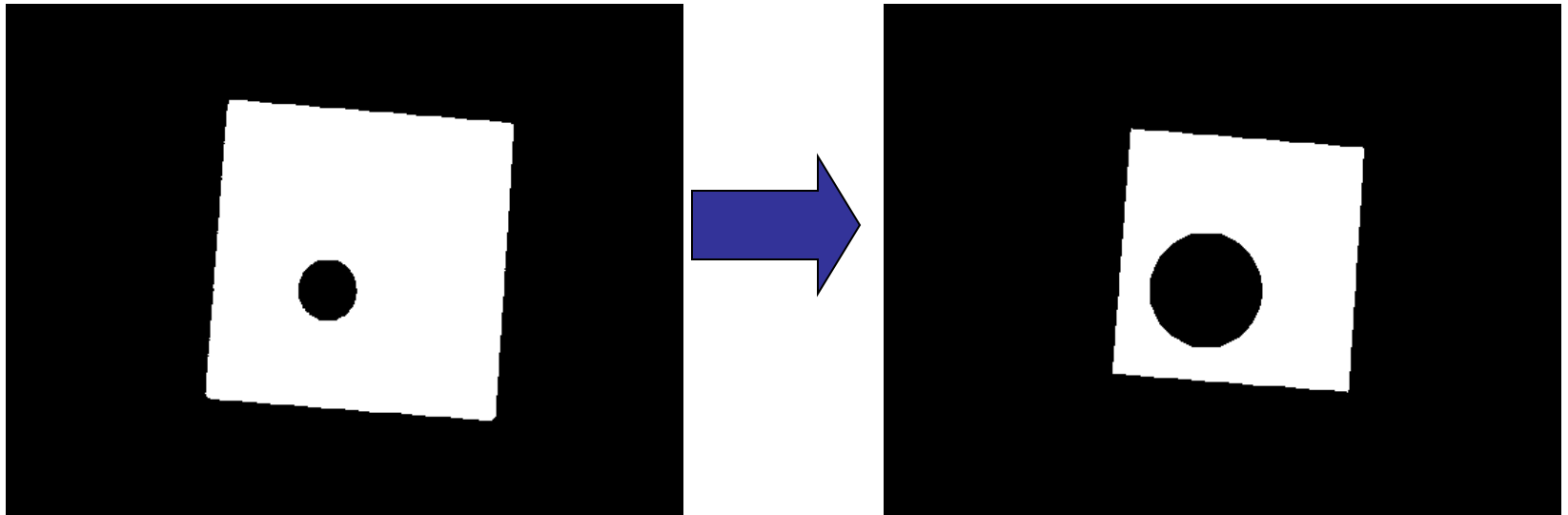
1	1	1
---	---	---



Output Image

	0	0	0	0	1	0	0	0	
--	---	---	---	---	---	---	---	---	--

An example of erosion



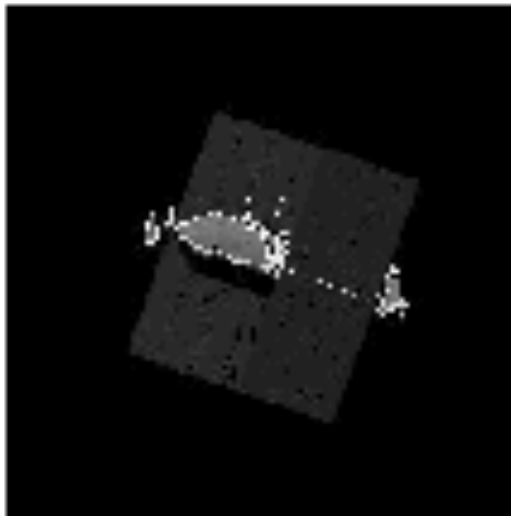
Binary image contour extraction

image



```
Erased=erode(image);  
Contour=  
double(image)-double(Erased);  
Contour=~Contour;
```

Contour



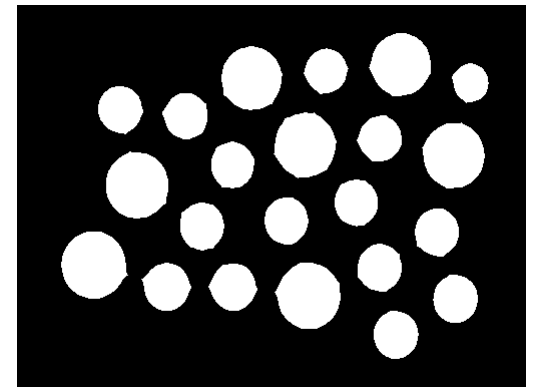
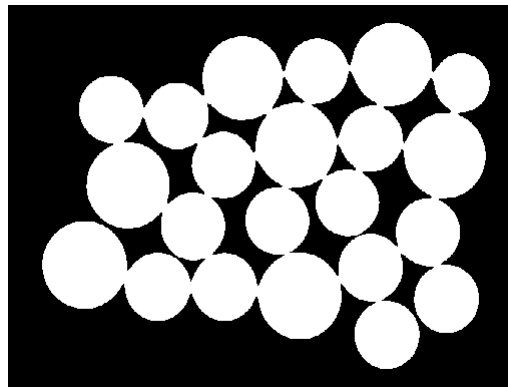
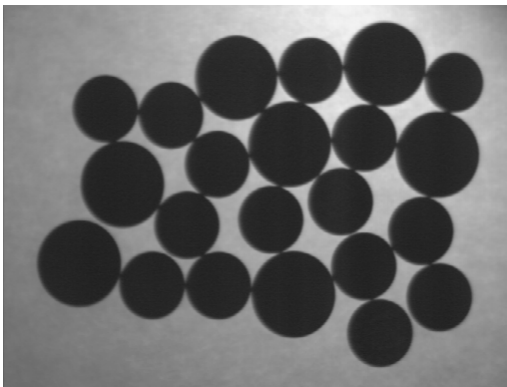
Satellite image
with c ontour .

Erosion can be
used to find
contour

Dilation can be
also used for it.

Counting Coins

- Counting coins is difficult because they touch each other!
- Solution: Binarization and Erosion separates them!



OPENING

Opening & Closing

- Important operations
- Derived from the two basic operations
 - Dilation
 - Erosion
- Usually applied to binary images.
- Opening and closing are dual operations

Opening & Closing

- Opening is the *dual* of closing:
- - *i.e.* opening the foreground pixels with a particular structuring element
 - is equivalent to closing the background pixels with the same element.

Opening

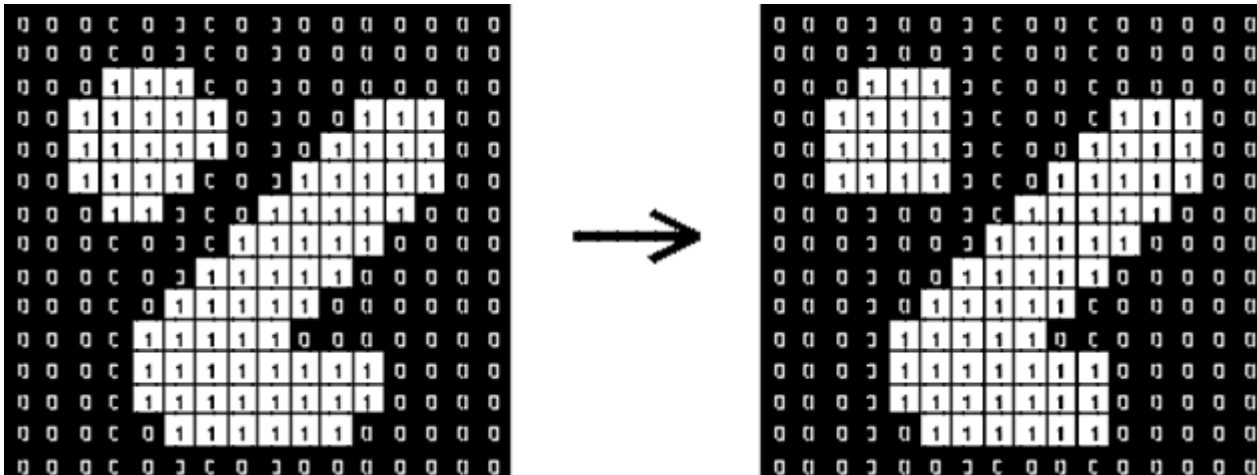
- Similar to Erosion
 - Spot and noise removal
 - Less destructive
- First Erosion, followed by dilation
- *the same structuring element for both operations.*
- Input:
 - Binary Image
 - Structuring Element, containing only 1s!

Opening

- Opening is **idempotent**: Repeated application has no further effects!

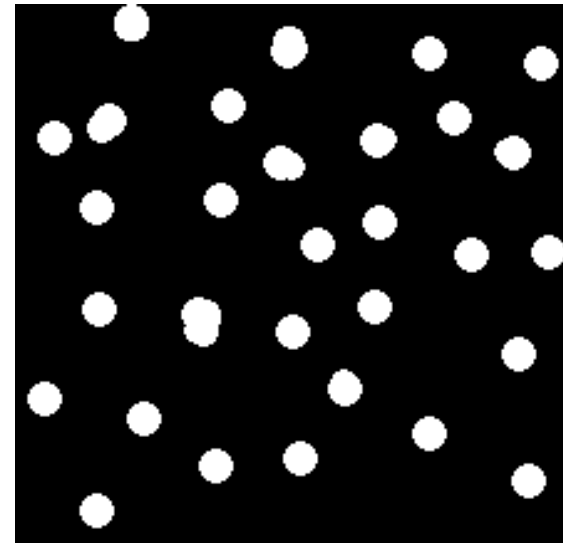
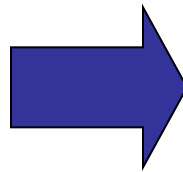
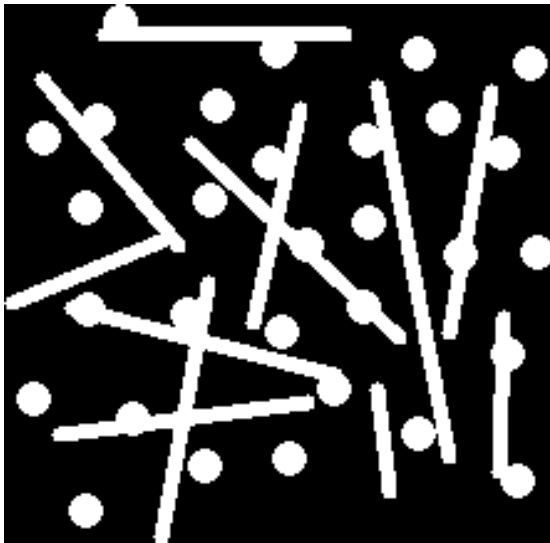
Opening

- Structuring element: 3x3 square



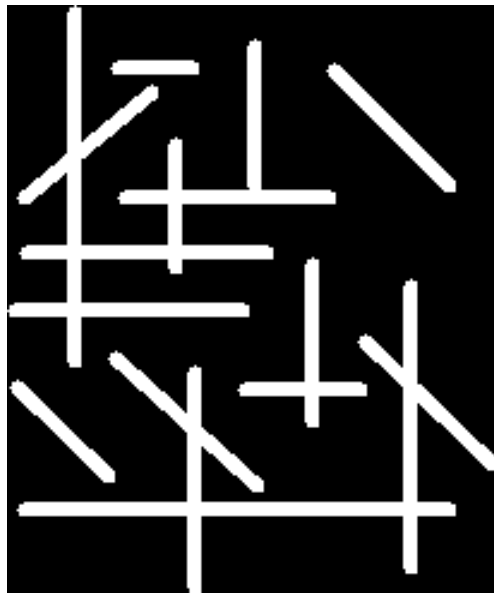
Opening Example

- Opening with a 11 pixel diameter disc



Opening Example

- 3x9 and 9x3 Structuring Element



15×9

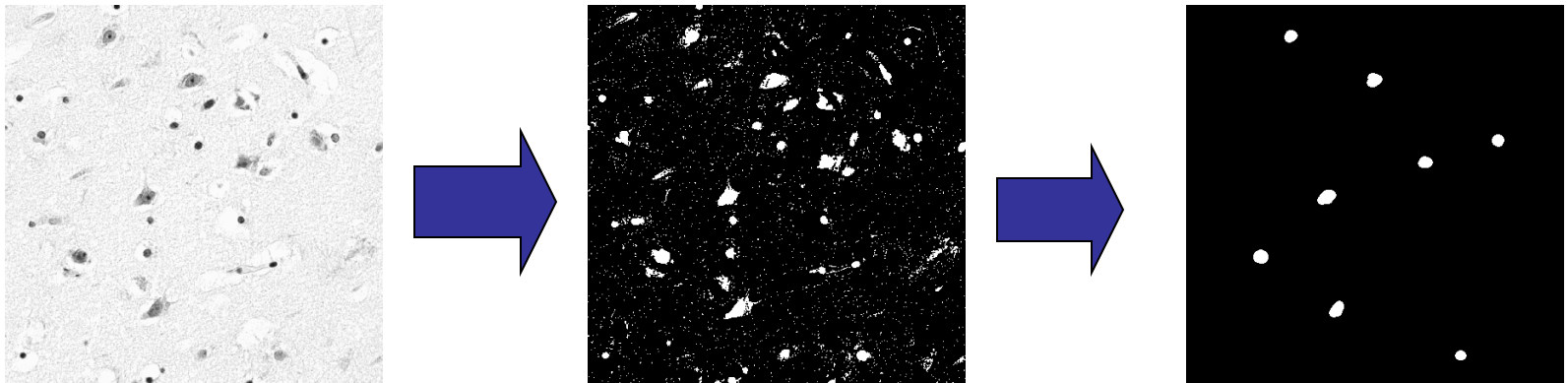


9×15



Use Opening for Separating Blobs

- Use large structuring element that fits into the big blobs
- Structuring Element: 11 pixel disc



Use Opening to extract corners



Original



Opening



Corners

1. What kind of structuring element was used in the opening?
2. How did we get the corners?

CLOSING

Closing

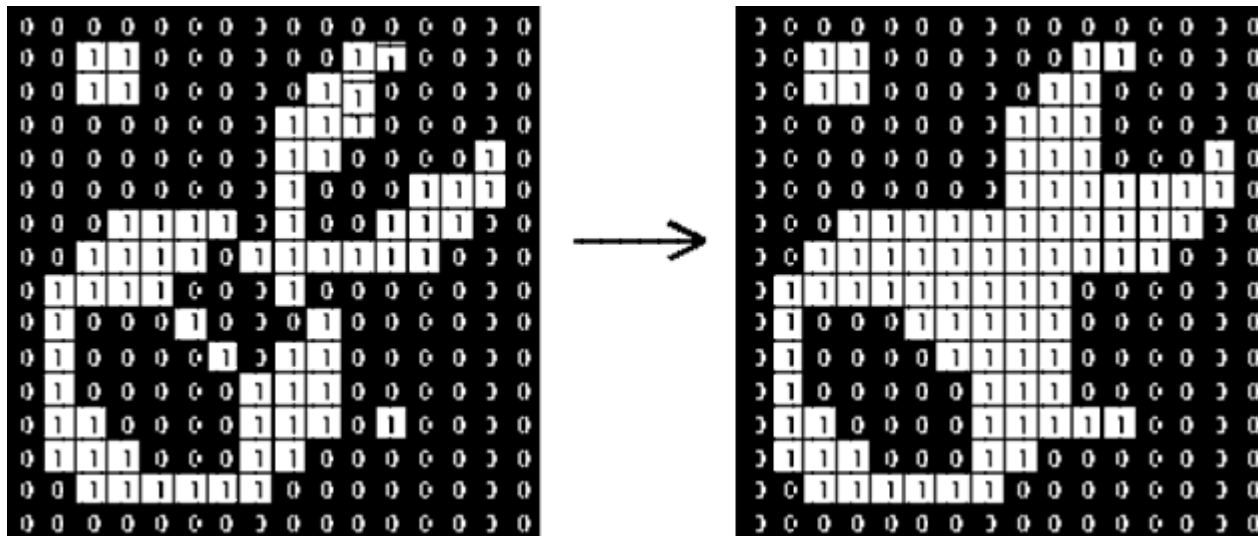
- Similar to Dilation
 - Removal of holes
 - Tends to enlarge regions, shrink background
- Closing is defined as a Dilatation, followed by an Erosion *using the same structuring element for both operations.*
- Dilation next erosion!
- Input:
 - Binary Image
 - Structuring Element, containing only 1s!

Closing

- Closing is **idempotent**: Repeated application of 'closing' has no further effects!

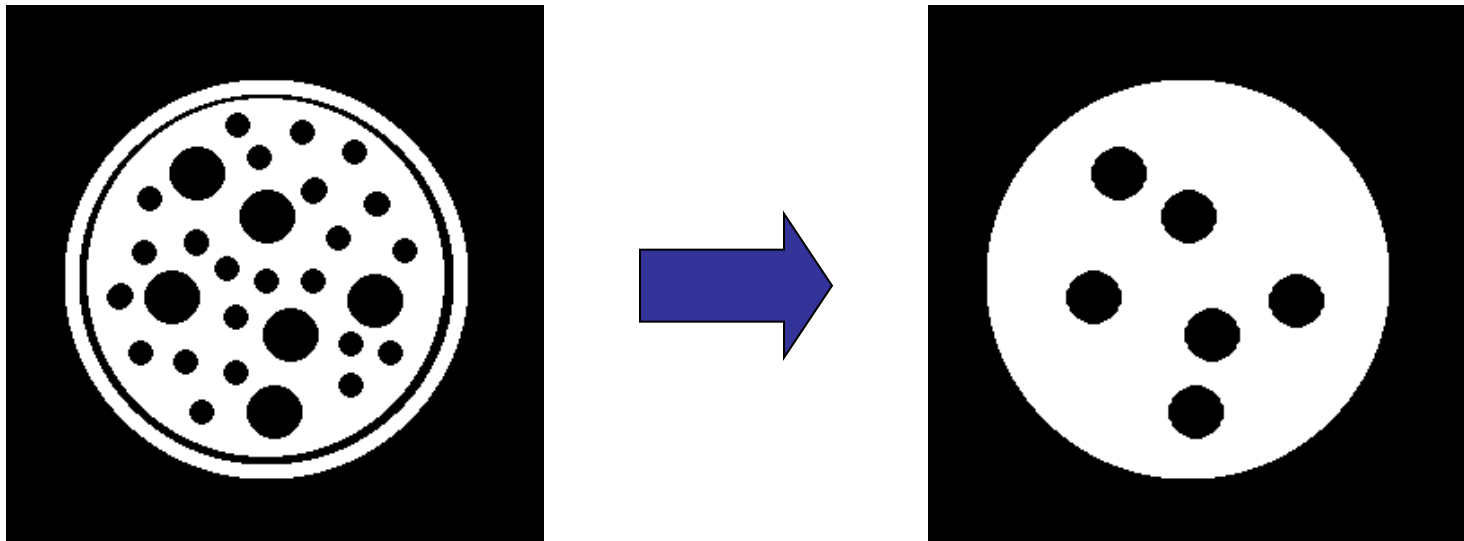
Closing

- Structuring element: 3x3 square



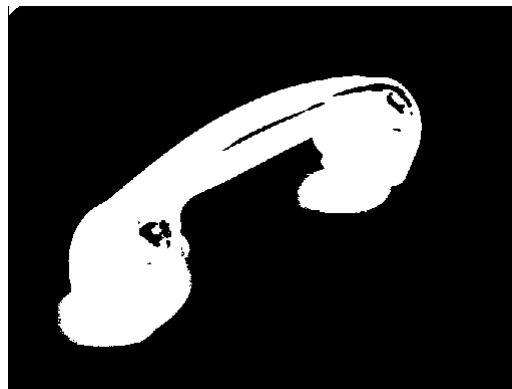
Closing Example

- Closing operation with a 22 pixel disc
- Closes small holes in the foreground



Closing Example

1. Threshold
2. Closing with disc of size 20



Threshold



closing⁸¹



Reading

- Chapter 9.1- Chapter 9.3, in Digital Image Processing 2nd edition.