# **OCTOSELECTOR: Efficient and Effective Batch-Aware Model Selection for Large Language Models**

#### **Abstract**

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Large Language Models (LLMs) vary significantly in metrics such as accuracy, latency, and cost, making it challenging for users and applications to decide which model to invoke for each query. This paper presents OctoSelector, a framework for LLM selection that satisfies user-defined objectives and constraints across multiple metrics. In the preprocessing phase, OctoSelector learns difficulty-aware representations of queries based on both input and output complexity, clustering them into iso-difficulty groups to enable efficient performance estimation across multiple LLMs. During inference, OctoSelector supports LLM selection for both batched and query-at-a-time workloads, formulating it as an Integer Linear Programming (ILP) problem that optimizes a user-defined objective (e.g., minimizing cost or latency, or maximizing accuracy) while enforcing constraints on other metrics. We evaluate OctoSelector on two types of tasks: NL2SQL using the Spider and BIRD benchmarks, and sentiment analysis using the IMDb benchmark. When optimizing for cost under accuracy and latency constraints, OctoS-ELECTOR achieves up to a 67.7% cost reduction on NL2SQL tasks for batched workloads compared to state-of-the-art approaches.

#### **ACM Reference Format:**

# 1 Introduction

In recent years, large language models (LLMs) have become a core component in a wide range of natural language applications, data-driven tasks, such as data wrangling [11, 13, 14, 33, 48], tabular data treatment [8, 32, 35], and Text-to-SQL [18, 19, 21, 29, 30, 47]. While much research focused on improving model architectures or training pipelines, an equally critical challenge arises: given a pool of advanced LLMs, how can we systematically select the most suitable ones to achieve both cost efficiency and performance effectiveness in applications.

Compared to open-source LLMs, proprietary LLMs such as GPT [4], Gemini [1], and Claude [2] offer several key advantages. These models exhibit strong generalization capabilities and state-of-the-art performance across diverse tasks, largely due to their massive parameter scales and proprietary training pipelines. More importantly, they are easily accessible via API, requiring no infrastructure management, model training, or fine-tuning from the user. By typically

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just specifying a model name users can invoke powerful LLMs while offloading concerns such as versioning, scaling, and maintenance.

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Despite their advantages, proprietary LLMs exhibit varying performance in terms of accuracy, latency, and pricing, making model selection a non-trivial decision. The primary concern with proprietary LLMs lies in their API usage cost, which can be substantial at scale. For example, OpenAI offers multiple LLM APIs, with GPT-40 reported to perform better on complex tasks than GPT-40-mini but at  $16\times$  the cost [3]. Similarly, Opus, part of Anthropic's Claude 3.5 model achieves higher accuracy on various benchmarks than the lightweight version Haiku but can be 18 to  $60\times$  more expensive [5].

A naive strategy that sends all queries to the most powerful model can lead to excessive costs, while processing easy queries with expensive models wastes budget without meaningful accuracy gain. Conversely, complex queries may fail when routed to lightweight models resulting in inaccurate outputs and wasted latency. As a result, inefficient model selection can lead to rapidly accumulating wasted cost and latency, posing a major bottleneck for scalable applications when processing large volumes of data.

Prior Work on LLM Routing: Recent work has investigated LLM routing strategies to reduce inference costs while maintaining task performance. A straightforward method called HybridLLM [17] classifies queries into two categories-easy and hard-and routes them to small or large LLMs accordingly, based on estimated difficulty. In contrast to the binary difficulty classification used in prior work, Smoothie [24] adopts a clustering-based retrieval approach: it identifies k nearest neighbor queries in an embedding space and routes the input to the LLM that achieved the best performance on these similar queries. Another line of work adopts cascade execution strategies such as FrugalGPT [12] and Automix [6], where a query is first processed by a small and cheap model, and only escalated to a more powerful LLM if the initial response is verified to be unsatisfied in term of accuracy or confidence. Although this reduces the number of expensive model calls, it introduces additional latency and redundant computation, especially when large portions of queries eventually require escalation. A recent strategy is GraphRouter [20] that introduces a set-level routing framework using a graph neural network (GNN), where tasks, queries, and LLMs are represented as nodes. Edges between queries and LLMs encode performance and cost.

Our goal in this paper is to develop an LLM routing strategy for situations when LLM invocations are used as inference mechanisms within data processing systems (e.g., ThalamusDB [26]) or in data science applications where such inferences must be performed over a large batch of tasks. We further wish to design routing strategies that empower users to explore tradeoffs across diverse metrics – cost, accuracy, and latency – inherent in different LLMs. In particular, the routing strategy must allow specification of constraints over one or more metrics, and choose LLMs such that those constraints

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Compared Aspect	HybridLLM	FrugalGPT	GraphRouter	Automix	Smoothie	RouteLLM	OctoSel.(our)
Support batch-level routing	-	-	-	-	-	-	✓
Input-output difficulty-aware feature encoding	-	-	-	-	-	-	✓
Clustering-based routing strategy	-	-	-	-	✓	-	✓
Objective optimization (e.g., cost-efficient)	✓	✓	$\checkmark$	✓	-	✓	✓
Support user-specified constraints	-	-	-	-	-	-	✓
Cross-model routing across multiple LLMs	-	✓	$\checkmark$	✓	✓	-	✓
Single-stage routing architecture(vs. cascade)	$\checkmark$	-	✓	-	$\checkmark$	✓	✓

Table 1: Comparison between OCTOSELECTOR and representative LLM routing systems. ✓ indicates that the feature is supported, while - denotes absence.

are met in aggregate over the entire workload, while optimizing other metrics.

Existing approaches (with the exception of GraphRouter) operate at the individual query level, selecting an LLM per query in isolation without considering global routing efficiency across the entire query set. GraphRouter, while it enables global optimization over a single objective such as minimizing cost, it lacks support for multi-objective routing with constraints, such as jointly optimizing for cost while satisfying accuracy or latency requirements. Furthermore, while GraphRouter makes decisions at the global (set) level, the routing mechanisms uses a single query for each LLM invocation which ignores the potential benefit of batching multiple queries into one prompt, in terms of overall cost and latency reduction.

Table 1 summarizes a comparative analysis between OctoSelector-the routing mechanism proposed in this paper with representative LLM routing frameworks across different dimensions.

Our Approach - OctoSelector: We propose OctoSelector, a framework for cost-efficient and performance-aware LLM model selection. OctoSelector addresses several challenges that arise in tackling the problem of LLM router under cost-performance trade-offs. First, it supports an effective feature representation of input queries that captures their relative difficulty with respect to a specific task domain. Without such a representation, it would be difficult to distinguish which queries can be handled by lightweight models and which require more capable LLMs. Second, it supports effective ways to determine how well different LLMs perform for queries of varying levels of difficulty across diverse metrics. Third, it supports ways to batch queries into single prompts and to assign batches to models so as to jointly optimize for performance, cost, and latency across the entire workload. Unlike heuristic-based routing, this approach allows for globally coordinated decisions that can leverage batching opportunities and model capabilities more effectively.

OCTOSELECTOR operates in two phases: the *pre-processing* and the *inference* phases. In the *pre-processing* phase, OCTOSELECTOR learns a feature extraction model from training dataset of natural language queries, which produces vector representations that encode the relative difficulty of each query within a given task domain. In OCTOSELECTOR, difficulty is treated as an abstract concept rather than an actual class label. We identify the source of difficulty by task type: for code generation and text generation, the difficulty often arises from both the input prompt (including query

and task instruction) and the expected response as output, which may be long or structurally complex. In contrast, for task domain like sentiment analysis, where outputs are typically short (e.g., a label or scalar value), difficulty is largely derived from the semantic ambiguity or complexity of the input query itself. Depending on the task type, the feature extraction model is trained on the input query alone or jointly with the expected output, capturing the aspects of difficulty that are most relevant to the task. Using these difficulty-aware features, we cluster the queries in the training set with similar complexity. We operate under the assumption that LLMs tend to exhibit similar performance across queries of similar difficulty. This enables us to approximate query-level performance (e.g., cost, latency, accuracy) using cluster-level statistics, reducing the need for exhaustive model-query evaluation. The resulting performance estimates are stored in a lookup table, which will be referenced during inference.

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In the *inference* phase, given a set of incoming (development) queries, OctoSelector formulates the query-to-model assignment as an integer linear programming (ILP) problem, jointly optimizing for cost, latency, and accuracy under user-defined constraints. Unlike prior work that routes queries individually, OctoSelector employs a batching strategy: multiple queries that share same context and instructions are grouped into a single prompt, enabling significant cost and latency savings while preserving task feasibility. Furthermore, it supports streaming inferences when queries arrive sequentially and LLM assignment decision must be made at query arrival time. In this setting, we adopt a local optimization strategy based on linear programming, leveraging cluster-level performance estimates to make real-time decisions.

Contributions: This paper's contributions are summarized as follows. We 1) formalize the model selection problem in a general form (Sec. 2); 2) develop OCTOSELECTOR a general framework for query-level LLM selection that balances cost, latency, and performance under user-defined constraints; 3) develop a difficulty-aware query feature representation, leveraging unsupervised clustering to approximate query-level performance metrics using cluster-level statistics, which enables cost-efficient and scalable estimation (Sec. 3.1); 4) develop an integer linear programming (ILP) based inference time optimization strategy for model selection, both for batched and streaming settings (Sec. 4); 5) Evaluate OCTOSELECTOR for two case studies – NL2SQL tasks and sentiment analysis (Sec. 5), and conduct comprehensive experiments to evaluate OCTOSELECTOR in these domains, demonstrating up to 70% cost reduction while

maintaining or improving task feasibility compared to single-LLM execution baselines.

# 2 Problem Setting

Let L be an LLM model that takes a natural language question q as input and returns a natural language response r as output. We denote one invocation of the LLM L on a prompt q as L(q) = r. Considering a workload  $Q = \{q_1, q_2, \ldots, q_n\}$ , a set of candidate LLMs  $\mathcal{L} = \{L_1, L_2, \ldots, L_m\}$ , we aim to design a good plan that assigns one LLM  $L_i \in \mathcal{L}$  per question  $q_j \in Q$  satisfying user-defined constraints while optimizing user-defined objectives.

We first introduce three metrics used to define the constraints or objectives, i.e., cost, latency, and accuracy of an LLM invocation, denoted by C(q, L), T(q, L), and A(q, L), respectively.

Cost C(q, L) per LLM invocation on question q using LLM L is determined by the number of tokens in the input q and the response L(q). In particular, C(q, L) = L.IC \* Tok(q) + L.OC \* Tok(L(q)), where  $Tok(\cdot)$  denotes the number of tokens, and L.IC and L.OC denote the unit cost for input and output tokens, respectively. For example, IC is \$0.15 and OC is \$0.60 per one million tokens for gpt-40-mini [3]. Latency T(q, L) is defined as the time between sending a prompt and receiving the response, consisting of network transmission overhead and the model's internal processing time. Accuracy A(q, L) per LLM invocation is defined as a boolean function that returns True if the response L(q) matches the groundtruth answer of q, and False otherwise. Based on the metrics defined for a single LLM invocation, it is straightforward to extend them to the query workload Q, where cost, latency, and accuracy are defined as the average values over all invocations on Q. Let  $C(Q, \mathcal{L})$ ,  $T(Q,\mathcal{L})$ , and  $A(Q,\mathcal{L})$  denote the average cost, latency, and accuracy over the workload Q paired with LLMs from  $\mathcal{L}$ , where  $C(Q,\mathcal{L}) = \frac{\sum_{q \in Q} C(q,f(q))}{|Q|}$ , and f(q) denotes the LLM  $L \in \mathcal{L}$  assigned to q by OctoSelector. (The definitions for the other metrics are analogous and are omitted here.)

#### 2.1 Problem Formulation

Given a query workload  $Q = \{q_1, q_2, \ldots, q_n\}$ , a set of LLMs  $\mathcal{L} = \{L_1, L_2, \ldots, L_m\}$ , and predefined metrics  $C(Q, \mathcal{L})$ ,  $T(Q, \mathcal{L})$ , and  $A(Q, \mathcal{L})$ , we present the high-level problem formulation by first discussing the possible combinations of constraints and objectives based on these three metrics, and then by relaxing the LLM assignment problem under both batching and query at a time scenarios. **Space of Constraints and Objectives.** We describe below three cases supported in OctoSelector, based on the number of constraints and objectives.

- (1) Single objective. Given a workload Q and LLMs  $\mathcal{L}$ , users may specify an objective from one of the metrics  $C(Q,\mathcal{L})$ ,  $T(Q,\mathcal{L})$ , or  $A(Q,\mathcal{L})$ , and optionally place the remaining (partial) metrics as constraints. For example, one may maximize accuracy  $A(Q,\mathcal{L})$  while constraining cost  $C(Q,\mathcal{L})$  and/or latency  $T(Q,\mathcal{L})$  under user-defined thresholds (e.g.,  $C(Q,\mathcal{L}) \leq \sigma_C$ ).
- (2) Multi-objectives. Users are also allowed to set more than one objective with optional constraints. For example, one can simultaneously maximize accuracy  $A(Q, \mathcal{L})$  and minimize cost  $C(Q, \mathcal{L})$  while constraining latency  $T(Q, \mathcal{L})$  under thresholds (e.g.,  $T(Q, \mathcal{L}) \leq \sigma_T$ ).

(3) Zero-objective. Users may also specify only constraints without an explicit objective. For example, one may require staying within a cost budget and ensuring a minimum acceptable accuracy without caring about latency. In this case, any feasible solution suffices, and OctoSelector returns one from the pareto solution set, i.e., one that dominates the others, if such a solution exists.

While we focus on describing solutions for the single-objective case, which is most commonly used in practice, we also discuss our approaches to support other cases in Section 4.

Batching Strategy. For a given set of queries, we refer to *batching* as a strategy that grouping a subset of queries into a single prompt for LLM invocation. The batching strategy follows the policy that queries within one prompt should a shared context and instruction, e.g., for NL2SQL tasks, only two questions from the same database can potentially share the same schema description. As a result, executing prompt with multiple queries will reduce the cost and latency, compared with same queries but each one in single prompt. We formulate the optimization problem under this batching strategy in section 4.

# 2.2 Applicable Tasks in OctoSelector

Consider a task consisting of n queries,  $Q = \{q_1, q_2, \ldots, q_n\}$ . We classify the task as either an *independent task* or a *dependent task*. **Independent Task**. For any  $q_i \in Q$ , and any  $Q_s \subseteq Q \setminus \{q_i\}$ , the outcome of  $q_i$  cannot be inferred from the outcomes of q', i.e.,  $L_j(q'), q' \in Q_s$ . A task being independent implies, none of its queries can be eliminated or derived by answering other queries in the task. Example of such independent task include NL2SQL and sentiment analysis.

**Dependent Task.** A task Q is considered dependent task if there exists a query  $q_i \in Q$  and a subset  $Q_s \subseteq Q_i \setminus \{q_i\}$  s.t. outcome of  $q_i$  can be inferred from the output of  $q' \in Q_s$ . An example of such a task is a set of Entity Resolution(ER) [15, 22, 43]. Note that when  $q_i$  correspond to ER queries, queries can be eliminated due to transitivity or anti-transitivity to optimize LLM invocations.

In OctoSelector, we focus on independent tasks, and leave the study of dependent tasks as future work. We evaluate OctoSelector through two case studies: NL2SQL, which translates natural language into SQL, and sentiment analysis, which classifies text sentiment. Evaluation results from both are presented in section 5.

# 3 OctoSelector: Pre-Processing

Let the training data set at the pre-processing state consist of a set of natural language queries  $Q_{\text{train}} = \{q_1, \cdots, q_n\}$  and let their ground-truth answers be  $A_{\text{train}} = \{a(q_1), \cdots, a(q_n)\}$ ), where  $a(q_i)$  refers to the (ground-truth) output of  $q_i$ . The pre-processing pipeline of OctoSelector transforms query/answer pairs in such an input and output training data into a a numerical features that capture the level of difficulty of the queries. Based on such a feature representation, OctoSelector clusters the queries creating groups

<sup>&</sup>lt;sup>1</sup>While OctoSelector assumes the availability of ground truth for model evaluation, this is not strictly necessary. In cases where ground truth is unavailable, a committee of expert techniques can be employed on a sample to estimate each model's performance. Such an approach has been extensively studied in ML literature, with solutions based on EM-based latent truth discovery [XX]. In this work we maintain the simplifying assumption about availability of ground truth since our contributions – optimizing the cost/quality/latency tradeoffs of a workload – do not rely on the mechanism used to calibrate/profile models.

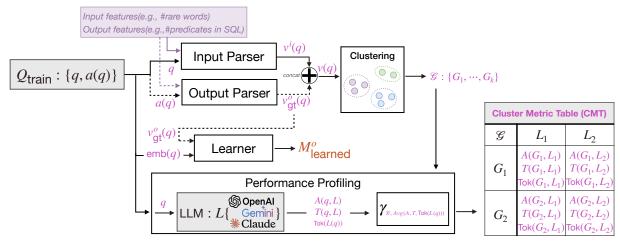


Figure 1: Pre-Processing Component Diagram

 $\mathcal{G}: \{G_1, \dots, G_k\}$  of queries that have a similar levels of difficulty. The queries in a group are executed over the various target LLMs to gather statistics about their performance resulting in a profile of the LLM based on the training data. These performance statistics are then summarized into a Cluster Metric Table (CMT) which will be used during inference time in assigning optimal LLMs to execute for each query. We describe the different components of the pre-processing pipeline in more detail below.

# 3.1 From Queries to Clusters

The first step of pre-processing is to extract and represent queries based on features. In OctoSelector, difficulty features for a query can be derived from input for tasks such as classification, or from both input and output, for generative tasks such as code generation. Features capturing query difficulty, in general, are domain and task specific, though OctoSelector supports a set of default features which can be used. A set of such default features (which we used for both NL2SQL and sentiment analysis tasks) is listed in Table 2. These features correspond to commonly used indicators of linguistic complexity [23, 40] that capture the syntactic and semantic difficulty of the query. OctoSelector supports parse rules to extract such default features from input queries. Such features extracted from a query q are referred to as input features of q denoted as  $v^i(q)$ , short as  $v^i$ .

Features derived from the output, a(q) to a query q, used in OctoSelector are denoted as  $v^o$ . Note that since the a(q) is available in training data, during pre-processing, the output features  $v^o$  can be derived from the corresponding outputs. Such features would not be available during the inference phase, and, thus, as discussed in the following subsection, we will learn an additional model to estimate the output feature values from the input query q.

Output features are task-dependent and capture the domain-related difficulty revealed from the answer to the query. The output features we used in OctoSelector for the NL2SQL task are shown in Table 3 which are based on the complexity of SQL constructs used in the SQL output.

Although OctoSelector provides a set of default input-derived difficulty features (which can be used broadly across diverse tasks), a set of output-derived features (intended for capturing the difficulty of translating a specific NL query into SQL), such features are customizable and changeable based on the specificity of the task. The final feature representation of query q is formed by concatenating the input and output vectors:  $v(q) = [v^i; v^o]$ . Or  $v(q) = [v^i]$  alone when output features are not used in tasks such as sentiment analysis.

Once the feature representation v(q) for a query q has been determined, the second step of pre-processing applies unsupervised learning to cluster the feature vectors v(q). This clustering process is motivated by the observation that for a given task, LLM performance varies significantly across queries of different difficulty levels. By clustering queries in the feature space, we naturally partition them into groups  $\mathcal{G}:\{G_1,...,G_k\}$  of queries of similar level of difficulty. OctoSelector employs K-Means clustering [37, 38] as its default algorithm. We determine the optimal number of clusters k through the elbow method [16]. The chosen k corresponds to the elbow point where increasing the number of clusters results in only a small improvement in clustering quality, as measured by the reduction in intra-cluster variance.

# 3.2 Output Model Learner

During pre-processing, input and output (ground truth answers) are both available in the training dataset. We could,thus, extract difficulty-related features from both input and output, and learn clusters over such a feature representation. Development data during inference, however, only contains query input. So, if output features were used to create clusters of similar difficulty to help choose an LLM, we need a mechanism to determine the output feature values from the input. OctoSelector supports a model learning step (referred to as Learner in the diagram 1) that learns a model  $M^o_{\rm learned}$ , which is used to predict the output feature values based on input query during inference time.

The *Learner* is a supervised learning model. In NL2SQL task, we use the Random Forest model, where the training input are

Table 2: Linguistic Features and corresponding definitions

	D C ::: (0 1)		
Linguistic Features	Definition (Scale)		
Rare Word Proportion	Proportion of low-frequency words		
Kare Word Proportion	in the input text.		
	Flesch-Kincaid Grade [45] Level es-		
Readability Score	timating reading difficulty (higher		
·	= harder).		
	For multi-sentence inputs, this is de-		
	fined as the mean number of tokens		
Average Sentence Length	per sentence. For single-sentence in-		
	puts, it reduces to the total number		
	of words in the input.		
	Maximum depth of the syntactic		
Parse Tree Depth	parse tree [39] (captures structural		
	complexity).		
	Ratio of subordinate clauses to to-		
Subordinate Clause Ratio	tal sentences (e.g., "although", "be-		
	cause").		
Part of Speech(POS) ratios	Proportion of each POS tag (adjec-		
	tive, adverb, verb, noun) relative to		
	the total number of words in the in-		
	put.		

embedded queries  $\operatorname{emb}(q), q \in Q_{train}$  and training target are  $v_{\operatorname{gt}}^o$ . For the training input, the word-embedding approach (e.g., TF-IDF [44]) is necessary to apply on each natural language query, as the Random Forest model requires numerical input.

#### 3.3 Profiling and Cluster Metric Table (CMT)

LLM Performance Profiling. For each natural language query q in the training data  $Q_{\rm train}$ , we profile all candidate LLMs by measuring each invocation's performance in terms of accuracy A(q,L), latency T(q,L), and query's response L(q) token length, noted as  ${\rm Tok}(L(q))$ . Note that the output token length is used for computing the cost following the method described in section 2.

The prompt that are used for LLM invocation and metric computations are task-dependent. In general, prompt should include task instruction, necessary context, and query (question). For instance, in NL2SQL, the instruction might be "convert this natural language query to SQL", and the context is query associated table schema. For sentiment analysis in movie reviews, the context we used is external information, such as the movie storyline description from IMDB. The latency and cost metrics definitions are as defined in section 2, while the accuracy is task-dependent or decided by users.

In OctoSelector, we adopt *Execution Accuracy (EX)* [36, 46] as the evaluation metric for NL2SQL task. This metric measures whether the execution result of the SQL query generated by the LLM  $L_j(q)$  is identical to that of the ground truth SQL query  $R_{gt}(q)$  on the associated database. Formally,  $A(q, L_j) = EX(L_j(q), R_{gt}(q))$ , where  $EX(\cdot)$  is an indicator function returning 1 if the two execution results are identical, and 0 otherwise. For sentiment analysis, if the class label is a discrete numerical values (e.g.,a rating score), we adopt mean-squared-error (MSE) as the accuracy metric, to measure the distance between the ground truth class label and

Table 3: SQL Syntax Features and corresponding definitions

Feature Group	Feature Name	Definition		
	Num Predicates	Number of predicates in WHERE clause.		
Clause	Num Nested Queries	Number of nested sub- queries in the SQL state- ment.		
Complexity	Num GROUP BY	Number of GROUP BY clauses.		
	Num HAVING	Number of HAVING constraints used.		
	Has ORDER BY	Binary indicator for presence of ORDER BY clause.		
	Has LIMIT	Binary indicator for presence of LIMIT constraint.		
	Has DISTINCT	Binary indicator for use of DISTINCT keyword.		
	Has LIKE	Binary indicator for use of LIKE operator.		
SQL	Num SQL Concepts	Total number of unique SQI syntax used in the query.		
Concept Richness	Num Joins	Number of join operations (e.g., INNER JOIN, LEFT JOIN).		
	Num Aggregations	Number of aggregation functions (e.g., SUM, AVG).		
	Num Logical Ops	Number of logical operators (e.g., AND, OR, NOT).		
Schema Diversity	Num Distinct Attrs	Number of distinct attributes accessed in the query.		

the model's prediction. When the class label is categorical (e.g., positive/negative sentiment), we instead measure accuracy by the proportion of exact matches between predicted and ground-truth labels.

*CMT Construction.* We construct Cluster Metric Table (CMT) to enable efficient query-level performance estimation via cluster-level approximation. This approach leverages the iso-difficulty property of clusters in  $\mathcal{G}$ : queries within each cluster exhibit similar LLM performance characteristics, while inter-cluster differences reflect varying difficulty levels.

Given the performance profile of training queries  $q_i \in Q_{train}$  on each LLM  $L_j$  (i.e., accuracy, latency, and output size), we define **cluster-level metrics**. For example, the cluster-level accuracy of  $L_j$  on cluster  $G_k$  is

$$A(G_k, L_j) = \frac{1}{|G_k|} \sum_{q \in G_k} A(q, L_j),$$

where  $|G_k|$  is the number of queries in cluster  $G_k$ . Analogously, we define cluster-level latency and cluster-level output token length.

During inference, we estimate the expected accuracy, cost, and latency of a query q by locating the cluster it belongs to based on

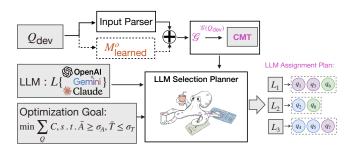


Figure 2: Inferencing in OctoSelector

its feature vector v(q). Specifically, the accuracy of q on an LLM  $L_j$  is approximated by the accuracy of  $L_j$  on the cluster:

$$A(q, L_j) \approx A(G_i, L_j), \text{ where } v(q) \in G_i, G_i \in \mathcal{G}, j \in \{1, \dots, m\}.$$

The same approximation applies to latency and output token length. The CMT stores the aggregated performance result from profiling for all  $G_i \in \mathcal{G}$  and  $L_j \in L$ , allowing efficient lookup at inference time.

# 4 OctoSelector: Inference with Batching Strategy

The inference process in OctoSelector (Figure 2) takes as input a development dataset of natural language queries ( $Q_{\text{dev}}$ ) and user-specified optimization objectives (e.g., minimizing cost) and constraints (e.g., average accuracy per query  $\geq$  X, average latency per query  $\leq$  Y second) to generate an LLM assignment plan that allocates queries to different LLMs.

In this phase, each query  $q \in Q_{\text{dev}}$  is transformed into a feature vector using the input and output parsers (Figure 1). Query q is then assigned to its respective cluster based on its feature representation v(q). The inference task is, thus, transformed into a set of group of queries, with each group corresponding to one cluster. The selection planner takes such an input and uses the cluster metric table (Figure 1), learned during pre-processing, to assign queries to LLMs. It postulates the LLM assignment task as an an Integer Linear Programming (ILP) problem to satisfy the user-defined constraints. The exact formulation of the problem will be described in Section 4.3.

It is straightforward to see that grouping queries with shared context into a single prompt reduces both cost and latency. For instance, in the NL2SQL task, queries from the same database reuse identical schema descriptions; batching them ensures the schema is transmitted only once, thereby lowering token cost and response time.

We first define the notion of a batch and the procedure for batch creation (Section 4.1). We then describe how to compute batch-level metrics—accuracy, latency, and cost (Section 4.2). Finally, we present our LLM assignment problem formulation and solution approach (section 4.3).

# 4.1 Batch Definition and Creation

For each invocation to LLM, the expected prompts are assumed to contain a set of instructions and context, referred to as *preamble*,  $D: \{D_1, \dots, D_M\}$ , which should associate with one or multiple queries

in the dataset. For example, in the NL2SQL task, the preamble consists of the task instruction and the database schema.

**Batch Definition**. A batch b is defined as one or a group of queries that share the same preamble, and can thus be jointly processed within a single LLM invocation. In OctoSelector, each batch b contains at most  $n_s$  queries.

While each LLM enforces a maximum prompt length, these limits are typically very large (e.g., 128k tokens for GPT-40 at Tier 1 [4] and up to 200k tokens per minute for Claude Haiku 3.5 [2]). For short-query workloads such as NL2SQL, this constraint rarely limits the choice of  $n_s$ . However, in tasks with longer queries or more complex preambles, the prompt length may still impose a non-trivial bound on  $n_s$ . In practice, the effective upper bound on  $n_s$  is often determined empirically: batching too many queries together can cause semantic interference and degraded performance well before the raw prompt-length limit is reached. Similar effects have been reported in prior studies on long-context usage and prompt packing, which show that quality loss arises primarily from information dilution and cross-query interference rather than exceeding context length [12, 34].

**Batch Creation.** We consider the following inputs for batch creation: a set of natural language queries for inference:  $Q_{\text{dev}}: \{q_1, \cdots, q_n\}$ , their assicoated preambles,  $D: \{D_1, \cdots, D_M\}$ , LLMs  $L: \{L_1, \cdots, L_m\}$ , iso-difficulty clusters  $G: \{G_1, \cdots, G_k\}$ , and the Cluster Metric Table (CMT), which summarizes the cluster-level performance of different LLMs. Based on these inputs, we now describe the batch creation procedure.

Let  $Q_{(D_i,G_j)}$  be the queries that share a preamble  $D_i$  and are grouped in cluster  $G_j$ . Inside preamble  $D_i$ , for every cluster  $G_j$  we slice its queries into blocks of exactly  $n_s$  queries each (last block, refer to as *left over*, may have  $< n_s$  queries). This process creates

$$\lceil \frac{|Q(D_i,G_j)|}{n_s} \rceil + \mathbf{left} \ \mathbf{over}_{ij}$$

number of batches for the given preamble  $D_i$  and cluster  $G_j$ , where the  $|\cdot|$  denotes the numbers of queries. We refer to a batch, b, created through the above described process that contains  $n_s$  queries, i.e.,  $|b| = n_s$ , a as *full pure batch*.

Dealing with Under-filled batches. Both left-over batches and clusters containing fewer than  $n_s$  queries will produce under-filled batches. We consider two strategies for handling them:

- Retain as-is: Each under-filled batch is kept without merging. This may result in up to k × M under-filled batches, where k is the number of clusters and M is the number of preambles.
- (2) *Merge:* Inside the same preamble, greedily merge underfilled batches from different clusters to form filled batches of size  $n_s$ . This yields *mixed batches*, as opposed to *pure batches* formed without merging. While this strategy reduces the total number of batches compared to (1), it may still result in up to M under-filled batches in the worst case.

In order to minimize the total number of batches, we choose the merge strategy as a default. In general, two types of batches may arise in OctoSelector: *full pure batches* that contain  $n_s$  number of queries belonging to a given cluster, and *residual batches*, which

may either be mixed batches or under-filled pure batches. We next describe how performance and cost metric described earlier for queries can be extended to corresponding concepts for batches. These metrics will be used in formulating the LLM selection challenge as an ILP problem (Section 4.3).

# 4.2 Batch based Metrics

In this section we describe how accuracy, latency, and cost can be computed for different LLMs based on the corresponding metrics defined for queries for both *full pure batches* and *residual batches*.

**Batch Accuracy**. Batch accuracy measures the average accuracy of individual queries within a batch. Estimating batch accuracy can be challenging due to two reasons: First, LLM performance is affected by the hallucination problem [25], making it challenging to determine whether accuracy variations stem from batching or model instability. Second, while query batching can provide beneficial cross-query context, it also risks attention dilution [7, 28]. Given these uncertainties which are difficult to model, we adopt a simplified approach that treats each query as independent and compute batch accuracy as the average accuracy of its constituent queries. Given a batch b and an LLM  $L_j$ , the batch accuracy can be computed as follows:

$$A(b, L_j) = \frac{1}{|b|} \sum_{i=1}^{k} n_i A(G_i, L_j)$$
 (1)

where  $n_i$  is the number of queries of cluster  $G_i$  in the batch, and the set of clusters are  $G_1, G_2, \ldots, G_k$ .

Our experimental results will show that while LLM behavior could deviate from the idealistic setting of queries being considered as independent, the mapping of batches to LLMs OctoSelector achieves (while modeling batch accuracy as the average accuracy of independent queries) brings significant cost-savings while ensuring desired accuracy levels.

**Batch Latency**. Following Section 2, latency consists of network transmission time and LLM processing time. For modeling purposes, we adopt two key assumptions: (1) Network overhead is constant per prompt for each LLM provider, since each invocation requires only one request-response cycle regardless of query count inside the batch; and (2) Processing time scales linearly with input and output token size, reflecting the sequential token processing behavior of LLMs [27, 41]. These assumptions preserve computational tractability while accounting for batch size effects.

Let Preamble(b) denote the shared preamble of batch b (e.g., NL2SQL instructions + database schema), and let  $n_i(b)$  be the number of queries in b that belong to cluster  $G_i$ , note that  $n_i(b) \leq n_s$ . Define  $\mu_j^{\rm in}(G_i)$  as the *per-query* average input-token count (*excluding the preamble*) for cluster  $G_i$ , and  $\mu_j^{\rm out}(G_i)$  as the *per-query* average output-token count for model  $L_j$  on cluster  $G_i$  (both estimated offline in CMT), where by previous notation in Section 2  $\mu_j^{\rm out}(G_i) = {\rm Tok}(L_j(q \in G_i))$ .

For batch b executed on  $L_j$ , we use the following unified latency model:

$$T(b, L_j) = \theta_j^{\text{in}} \left[ \text{Tok}(\text{Preamble}(b)) + \sum_{i=1}^K n_i(b) \, \mu_j^{\text{in}}(G_i) \right]$$
$$+ \theta_j^{\text{out}} \sum_{i=1}^K n_i(b) \, \mu_j^{\text{out}}(G_i) + T_{\text{network}}(L_j)$$
(2)

Here,  $\operatorname{Tok}(\cdot)$  is the model-specific tokenizer;  $\operatorname{Tok}(\operatorname{Preamble}(b))$  can be computed exactly once for each preamble and cached;  $(\theta_j^{\operatorname{in}}, \theta_j^{\operatorname{out}})$  are the input/output per-token coefficients, and  $T_{\operatorname{network}}(L_j)$  is the fixed network latency per invocation.

We empirically determine the coefficient value  $\theta_j^{\rm in}$ ,  $\theta_j^{\rm out}$  and  $T_{\rm network}(L_j)$  in the *Performance Profiling* module, where we measure the latency across varying batch sizes estimate the parameters via linear regression.

**Batch Cost.** The batching strategy reduces cost by allowing multiple queries to share same instruction and context within a single prompt. For a batch of size |b|, this avoids repeating the shared preamble |b|-1 times compared to single-query execution.

The cost for processing batch b on LLM  $L_i$  is computed as:

$$C(b, L_j) = L_j . IC \left[ \text{Tok}(\text{Preamble}(b)) + \sum_{i=1}^K n_i(b) \, \mu_j^{\text{in}}(G_i) \right]$$

$$+ L_j . OC \sum_{i=1}^K n_i(b) \, \mu_j^{\text{out}}(G_i), \tag{3}$$

where  $L_j.IC$  and  $L_j.OC$  is the input and output unit price of LLM  $L_j$ , respectively. Other terms are reused from latency model in Eq. 2.

Full Pure versus Residual Batches. The above models for accuracy, cost, and latency apply for both full pure, as well as, residual batches. When batches are full, we can significantly simplify the the expressions. For instance, for pure batches, the expression for simply reduces to  $A(G_i, L_i)$ , the accuracy for a query in the cluster for a given LLM. Likewise the latency expression Eq. 2 can be simplified by replacing the term  $\sum_{i=1}^{K} n_i(b)$  by  $n_s$ , the size of the full batches, across all clusters. We further approximate Tok(Preamble(b)) in the expressions above for latency and cost for a full pure cluster by a cluster-level average for  $G_i$ , which can be computed offline. With such a replacement, latency for a full batch and cost of a full batch on a given LLM  $L_i$  depends only on  $(G_i, n_s)$ . Such an approximation essentially treats expected latency and cost of any two full batches belonging to the same cluster on the same LLM as being equal its value is considered as the expected latency/cost. We refer to the corresponding cost and latency for a pure full batch belong to cluster  $G_i$  on LLM  $L_j$  by  $C_{fp}(G_i, L_j)$  and  $T_{fp}(G_i, L_j)$  respectively. Note that instead of approximating batch latency/cost as above, we could use the actual composition of the batch to better estimate cost and latency. We will discuss our rationale for estimating the metrics as above in next section.

### 4.3 LLM Assignment Problem

We now formulate the LLM assignment problem, which is a mapping of batch to LLM based on the competing criteria - cost, accuracy, latency. The LLM assignment problem can be expressed

as an optimization problem wherein we optimize one (or more of the metrics) and specify constraints on the other. We focus in OctoSelector on the variant where we minimize total cost, while putting constraints on accuracy and latency, defined by  $\sigma_A$  and  $\sigma_T$ , respectively. These constraints are on the average overall queries (expected sense) based on the LLM profile learned during the preprocessing phase. To formalize the assignment problem, let us define the following notations.

Batch Assignment An assignment of batches to LLM is expressed as  $\{L_1: \mathcal{B}_1, \cdots, L_m: \mathcal{B}_m\}$ , where,  $\mathcal{B}_i$  is the set of batches assigned to LLM  $L_i$ , for all  $i = \{1, 2, \dots, m\}$ . Since a batch is assigned to a single LLM,  $\mathcal{B}_i \cap \mathcal{B}_j = \emptyset$ ,  $i \neq j$ , and  $\bigcup \mathcal{B}_i$  covers all batches,  $\forall i, j \in \{1, \cdots m\}$ .

Full pure batches assignment variables. We denote by  $x_{i,j} \in \mathbb{N}^+$  the numbers of full pure batches originating from cluster  $G_i$  that are assigned to LLM  $L_j$ .

Residual batches assignment variables. Let  $y_{b,j} \in \{0,1\}$  be the binary decision variable for residual batches, i.e.,  $b \in \mathcal{B}^{\text{res}}$  assigned to LLM  $L_j$ . Each residual batch is assigned to exactly one LLM, i.e.,  $\sum_{j=1}^m y_{b,j} = 1$ .

Note that for an given batch assignment, the total number of batches assigned to LLM  $L_j$ , denoted as  $|\mathcal{B}_j|$ , is the sum of the number of full pure batches and the number of residual batches assigned to  $L_j$ . Specifically,  $|B_j| = \sum_{i=1}^K x_{i,j} + \sum_{b \in \mathcal{B}^{\text{res}}} y_{b,j}$ .

Example of Assignment Assume inside preamble  $D_1$  we have : cluster ID  $G_1$  contains full pure batches:  $\{b_1,b_2,b_3,b_4\}$ , and residual batches:  $\{b_5,b_6\}$ , which will be assigned to LLM  $L_1,L_2$ . If an example of assignment plan leads to variable solution as:  $x_{1,1}=3$ ,  $x_{1,2}=1$ , and  $y_{b_5,1}=0$ ,  $y_{b_5,2}=1$ ,  $y_{b_6,1}=1$ ,  $y_{b_6,2}=0$ , this indicating that, any three batches inside the  $G_1$  will be assigned to  $L_1$ , and the rest will be assigned to  $L_2$ , and for residual batches,  $b_5$  will be assigned to  $L_2$ , wherein  $b_6$  will be assigned to  $L_1$ .

Given an assignment plan  $\mathcal{A}$ , we can determine the cost, accuracy and latency using the models described in section 4.2 based with the assignment variables.

In particular, the cost of a given assignment corresponds to the cost of assigning  $x_{i,j}$  full batches from cluster  $G_i$  to LLM  $L_j$ , plus the cost of any residual batches assigned to it. Thus, the total cost of an assignment can be expressed as:

$$cost(\mathcal{A}) = \sum_{i=1}^{K} \sum_{j=1}^{m} x_{i,j} C_{fp}(G_i, L_j) + \sum_{b \in \mathcal{B}^{res}} \sum_{j=1}^{m} y_{b,j} C(b, L_j)$$
 (4)

In the formula above, the cost of  $\mathcal{A}$ , is computed by adding up the costs of assigning  $x_{i,j}$  full batches of queries belonging to cluster  $G_i$  to LLM  $L_j$  with the cost of residual batch assignments to various LLMs. We can similarly compute the accuracy and latency metrics

for an assignment  $\mathcal{A}$  as follows:

$$\operatorname{accuracy}(\mathcal{A}) = \frac{1}{N} \left[ \sum_{i=1}^{K} \sum_{j=1}^{m} x_{i,j} \, n_s \, A(G_i, L_j) + \sum_{b \in \mathcal{A}: i=1}^{m} \sum_{j=1}^{m} y_{b,j} \sum_{i=1}^{K} n_i(b) \, A(G_i, L_j) \right]$$
(5)

latency(
$$\mathcal{A}$$
) =  $\frac{1}{N} \left[ \sum_{i=1}^{K} \sum_{j=1}^{m} x_{i,j} T_{\text{fp}}(G_i, L_j) + \sum_{b \in \mathcal{B}^{\text{res}}} \sum_{j=1}^{m} y_{b,j} T(b, L_j) \right],$ 
(6)

where  $T(b, L_j)$  and  $C(b, L_j)$  are the unified batch latency (Eq. 2) and batch cost (Eq. 3), respectively. The terms  $T_{\rm fp}(G_i, L_j)$  and  $C_{\rm fp}(G_i, L_j)$  are full pure batch latency and cost expression, obtained by instantiating a full pure batch from cluster  $G_i$  with  $|b| = n_s$  and replacing Tok(Preamble(b)) by the cluster-level average token length on preambles (detailed in subsection 4.2.

We can now formulate the optimization problem as:

$$\begin{aligned} \min \cot(\mathcal{A}), & \text{s.t. accuracy}(\mathcal{A}) \geq \sigma_A, \text{ latency}(\mathcal{A}) \leq \sigma_T & \text{ (7)} \\ & \text{and} \\ & \sum_{j=1}^m x_{i,j} = \left| \mathcal{B}^{\text{full pure}} \in G_i \right|, \quad i = 1, \dots, K, \\ & \sum_{j=1}^m y_{b,j} = 1, \forall \, b \in \mathcal{B}^{\text{res}}, \\ & x_{i,j} \in \mathbb{N}^+, \, y_{b,j} \in \{0,1\}, \end{aligned}$$

where the expression  $cost(\mathcal{A})$ ,  $accuracy(\mathcal{A})$ ,  $latency(\mathcal{A})$  follow the formulation in Eq. 4-6, respectively.

The Eq. 7 minimizes total cost by summing contributions from full pure batches and residual batches. Accuracy and latency constraints are enforced at the *query* level: full pure terms are count-weighted via  $x_{i,j}$  (each full batch from  $G_i$  contributes  $n_s$  queries), while residual terms average over the actual composition of each residual batch via  $y_{b,j}$ . The assignment constraints ensure that all full pure batches originating from each cluster are accounted for and that every residual batch is routed to exactly one LLM.

Note that in the above characterization, we have assumed the cost, quality, and latency of a given full pure batch of queries from the same cluster assigned to the same LLM to be essentially equal. While this assumption is necessary for our approach to ensure accuracy, as our method is based on iso-difficulty clustering, it is not strictly required for latency or cost. In practice, latency and cost depend on the input and output sizes of the prompt. Since we know the actual sizes of the batches, we could in principle adopt a more fine-grained model that expresses the individual cost of each full pure batch, similar to our treatment of residual batches. However, doing so would require introducing a binary assignment variable for every batch, specifically, the full pure batch assignment variable  $x_{i,j}$ becomes  $x_{b,j} \in \{0,1\}$ . If a cluster  $G_i$  contains  $|\mathcal{B}_i^{\text{full pure}}|$  numbers of full pure batches, individual assignment variable numbers of  $x_{b,j}$  equal to the  $|\mathcal{B}_i^{\text{full pure}}|$ . Instead, by assuming that full pure batches from the same cluster share the same metrics, we reduce the numbers of full pure batches assignment variables to  $x_{i,j}$ . Within the cluster  $G_i$ , numbers of variables  $x_{i,j}$  is bounded by numbers of

candidate LLMs m, and overall number of variable  $x_{i,j}$  is bounded by Km, where K is the total cluster number.

#### 5 Evaluation

# 5.1 Experimental Setup

**Evaluation Tasks & Benchmarks** We evaluate OctoSelector on two tasks, *NL2SQL* and *sentiment analysis*. NL2SQL is chosen for its importance in democratizing access to databases. Additionally, to measure the complexity per NL2SQL task, it considers syntax features from both the input (e.g., linguistic features in Table 2) and the output (e.g., SQL complexity in Table 3), making it a representative task for evaluation. We evaluate NL2SQL using two popular benchmarks, Spider [46] and BIRD [31].

Spider Benchmark. We employ 7,000 queries from the Spider training set (train\_spider) in the pre-processing stage to compute the cluster metric table, and 1,034 queries from the development set for inference.

BIRD Benchmark. Compared with Spider, queries in BIRD exhibit higher complexity with larger table schemas [36]. In OctoSelector, 9,428 queries from the training set are used for pre-processing, and 1,534 queries from the development set are employed for inference.

We evaluate the second task, sentiment analysis, using the IMDb benchmark [42], where each task predicts a movie's rating score based on its corresponding review.

IMDb Benchmark [42]. The IMDb dataset consists of movie reviews labeled with sentiment (rating scores from 1 to 10) for sentiment analysis tasks. We use 4,000 reviews with labels during the pre-processing stage in OctoSelector and another 1,000 reviews without labels for inference.

Candidate LLMs We evaluate OctoSelector using proprietary LLMs listed in Table 4, chosen for their popularity in real-world data processing tasks and accessibility through commercial APIs. OCTOSELECTOR works when taking all LLMs listed in Table 4 as the LLM pool. However, in a collection of models, if a small subset exhibits dominated performance (e.g., lower cost and higher accuracy), it can obscure the observations for the remaining majority of models, since those dominated models are unlikely to be selected. For example, as will be shown later, Gemini models are overall faster and cheaper than Claude models, resulting in few Claude models being selected and, consequently, limited observations for them. Therefore, to increase the diversity of observations, we group all LLMs from the same provider into one LLM pool used in Oc-TOSELECTOR and for other baselines. This allows us to make more fine-grained observations across models from different providers, which is also also a common practical setting to select models from the same provider.

**Baselines.** We consider the following three baselines to compare against OctoSelector:

**Baseline 1:** Our first baseline is the *single LLM approach*, which uses a single LLM to process all queries in the same batch created by OctoSelector.

**Baseline 2:** The second baseline is an improved version of the first one. Instead of using a single LLM to process all queries in one batch, it selects the cheapest LLM from the candidate models that

LLM	Company	Input Price/1M	Output Price/1M
GPT-4o Mini	OpenAI	0.15	0.6
GPT-3.5 Turbo	OpenAI	3	6
GPT-40	OpenAI	2.5	10
Gemini 1.5 Flash 8B	Google	0.0375	0.15
Gemini 1.5 Flash	Google	0.075	0.3
Gemini 1.5 Pro	Google	1.25	5
Claude 3.5 Haiku	Anthropic	0.8	4
Claude 3.5 Sonnet	Anthropic	3	15

Table 4: LLM Pricing Comparison (March 2025 rates)

satisfy the user-specified constraints. How these constraints are set will be clarified shortly in the evaluation setup.

Baseline 3: The third baseline is GraphRouter [20], which is designed for assigning LLMs per query by optimizing an objective (e.g., minimize cost) under user-specified constraints, a setting similar to OctoSelector. Since GraphRouter shows better performance than HybridLLM [17] and FrugalGPT [12], we only compared against GraphRouter [20]. However, GraphRouter natively does not support batching. We extend it with a batching mechanism to enable a fair comparison with OctoSelector, and denote this enhanced version as *GraphRouter Plus* or *GR+*. Specifically, given the LLM assignments produced by GraphRouter, we first group queries into clusters such that queries within the same cluster share the same LLM assignment. We then apply the same batching strategy as in OctoSelector to create batches for each cluster, allowing queries with the same assigned LLM and shared context to be batched together, thereby reducing cost and latency.

**Evaluation Setups.** While OctoSelector supports flexible optimization objectives over various metrics such as cost, latency, and accuracy, we focus on minimizing cost while constraining accuracy  $(\sigma_A)$  and latency  $(\sigma_T)$  in our evaluation. This setup is common for LLM-powered tasks, where the goal is to minimize cost while ensuring that accuracy (and/or latency) meets user-specified thresholds.

The accuracy threshold  $\sigma_A$  for a benchmark is defined over a range [l,r], where l and r denote the lowest and highest accuracy of Baseline 1 (i.e., using a fixed LLM for all queries) when employing different LLMs from the candidate pool. For example, consider  $\sigma_A$  for Spider in Table 5, which spans [0.661, 0.815], where 0.661 and 0.815 correspond to the accuracies of Baseline 1 using GPT-3.5-Turbo and GPT-40, respectively. All baselines have no meaningful data points outside this range, and the same applies to OctoSelector. For example, the highest possible accuracy that OctoSelector can achieve is by employing the best model (e.g., GPT-40 among all OpenAI models) to execute every single query. We enforce a similar constraint range on latency, defined by the smallest and largest latency of Baseline 1 when using different LLMs.

We further discretize each range into 20 evenly spaced values, resulting in a total of 400 combinations of accuracy and latency test pairs.

# 5.2 Feasibility Regions

We first define the feasibility for OCTOSELECTOR as follows. If the LLM assignment plan created by a method has estimated accuracy and latency that both satisfy a given constraint pair on accuracy and latency  $(\sigma_A, \sigma_T)$ , we call such a plan feasible on  $(\sigma_A, \sigma_T)$ .

Ranchmark Constraints

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	Dencimark	Constraints	Kanges			
	Spider	$\sigma_A$	[0.661, 0.815]			
		$\sigma_T(\mathrm{sec})$	[0.248, 0.583]			
	BIRD	$\sigma_A$	[0.398, 0.485]			
		$\sigma_T(\mathrm{sec})$	[0.457, 0.974]			
	IMDb	$\sigma_A$	[1.98, 3.51]			
		$\sigma_T(\mathrm{sec})$	[0.421, 1.71]			
ble 5: Constraint value range of accuracy $(\sigma_A)$ and laten						

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 $ncy(\sigma_T)$ across benchmarks.

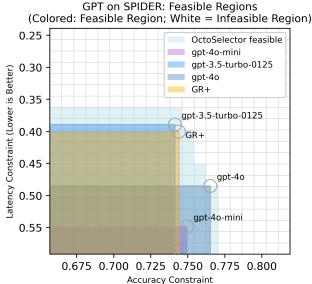


Figure 3: Feasible region of LLMs from OpenAI provider compared with OctoSelector. The circled points of each GPT model denote the single LLM baseline result performance of average accuracy and latency value.

Consider the space of constraint pairs specified in Table 5, where we have  $20 \times 20$  ( $\sigma_A$ ,  $\sigma_T$ ) pairs per benchmark. We define the *feasi*bility region for a method as the set of feasible constraint pairs, and further define the *feasibility rate* (%) as the number of feasible constraint pairs over the total number of pairs (i.e., 400). Figure 3 shows the feasibility regions of each single LLM (provided by OpenAI) compared with OctoSelector on the Spider benchmark. The three circled points for each LLM represent the corresponding average accuracy and latency of Baseline 1 (single LLM), and we consider the bottom-left area of each circled point as the feasibility region of the corresponding LLM. The light blue area in Figure 3 denotes the feasibility region of OctoSelector, which is strictly larger than any of the three individual feasibility regions. For Baseline 2, defined as the union of the three feasibility regions (in this case, gpt-4o-mini, gpt-3.5, and gpt-4o), it always selects the cheapest model. The corresponding assignment plan of Baseline 2 is thus the cheapest feasible solution to the given constraint pair. We list the exact feasibility rates of the baselines for each LLM provider across

all benchmarks in Table 6, where OctoSelector has the highest feasibility rates than all baselines for all LLMs.

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# **Evaluation Results**

For each LLM provider, we first compute each LLM's feasibility region within the constraint ranges shown in Table 5. Each cell in the feasibility region in Figure 3 corresponds to a constraint pair  $(\sigma_A, \sigma_T)$ , for which OctoSelector returns an LLM assignment plan that satisfies the pair while minimizing cost.

Experiment 1: Feasibility Rate. We first measure the feasibility rate, defined as the percentage of queries that satisfy the specified constraints across all baselines using different LLMs, as shown in Table 6. A higher feasibility rate indicates a better approach, as it reflects a greater ability to find assignment plans that fit more queries within the given constraints. In this experiment, OctoSe-LECTOR has the highest feasibility rate among all baselines across all LLMs, demonstrating its great capability to offer an effective plan.

Experiment 2: Baseline 1 vs. OctoSelector. We compare OctoS-ELECTOR against Baseline 1, i.e., the single-LLM method, in Figure 4. The y-axis shows the percentage of cost reduction, defined as  $(1 - \frac{C_{\text{OCTOSelector}}}{C_{\text{baseline}}}) \times 100\%$ . We report the cost reduction that is averaged over all cells within the feasible ranges per method, that is, over the queries that satisfy both constraints for the enumerated constraint pairs. The x-axis shows the compared single-LLM model names. OctoSelector has a significantly lower cost than the single-LLM method. In particular, on the Spider benchmark, within the feasibility region of the LLM gpt-40, OctoSelector achieves an average cost reduction of 81.5% compared to the cost incurred by a single-LLM gpt-40 invocation. In addition, OctoSelector achieves 40-95% cost savings; especially on the IMDb benchmark, the highest saving reaches 95.1% compared to gpt-3.5-turbo.

Experiment 3: Baseline 2 vs. OctoSelector. We compare OctoS-ELECTOR with Baseline 2 in Figure 5. Recall that Baseline 2 is an improvement over the single LLM method, where it selects the model with the lowest cost from the candidates that satisfy the constraints (i.e., among the union of feasibility regions of all candidate LLMs from the same provider). We similarly report the average cost reduction, and observe a substantial improvement with Oc-TOSELECTOR. Across benchmarks, OctoSelector achieves 30.8% to 68% cost reduction, with particularly high savings on the IMDb benchmark, where the average reduction exceeds 60%.

Experiment 4: Baseline 3 vs. OctoSelector. We compare Baseline 3, GraphRouter Plus (GR+), with OctoSelector, and report the average cost reduction in Figure 6. OctoSelector achieves significant cost reductions across all three benchmarks and all LLM providers. The peak saving of 94.8% occurs on the IMDb benchmark when compared with GPT models. This is because GraphRouter tends to select gpt-3.5 for most queries, which is relatively expensive according to the pricing table 4.

Experiment 5: Effect of Number of Query Clusters. We conduct an ablation study to examine how the number of query clusters affects the performance of OctoSelector, and report the average cost reduction by comparing with OctoSelector against the improved single LLM method (i.e., Baseline 2) in Figure 7. As shown, the average cost reduction of the LLM assignment plans generated

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GPT Gemini Claude 3 5 Union GR+ OctoSel 1.5-flash-8b 1.5-flash 1.5-pro Union GR+ OctoSel haiku sonnet Union GR+ OctoSel 40-mini 40 28 5% 3.8% 3.8% 1 5% Spider 5.5% 27 5% 19 5% 32.0% 30.2% 42.0% 75.0% 76.0% 84 3% 76% 94.5% 0.2% 4.5% 6.0% 9.4% 0.0% 18.0% 18.0% 28.0% 24% 2.0% 12.0% 12.0% 10.5% 16.0% 4.8% 40.5% 43.0% 56.8% 37.7% IMDb 85.5% 90.2% 90.0% 94.8% 86.5% 95.0% 4 8% 40.0% 72.0% 76.0% 9.5% 79.0% 46.8% 66.5% 66.5% 48% 76.0%

Table 6: Feasibility rate (%) across benchmarks, compared OctoSelector with three baselines: single-model, cheapest feasible solution on union of feasible regions, and GraphRouter plus.

Cost Reduction (%) on Each Feasible Region of Single-LLMs Baselines

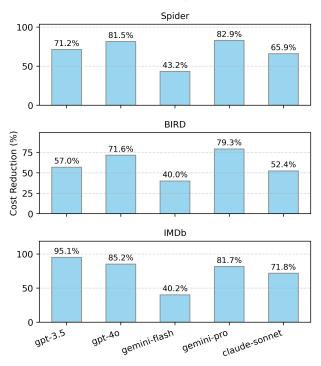


Figure 4: Cost reduction (in percentage) compared with single-LLM baselines on their correspond feasible regions.

by OctoSelector compared against Baseline 2 is stable across different numbers of query clusters, indicating the robustness of OctoSelector with respect to query complexity clusters.

# 5.4 Query-at-a-time Scenario

While OctoSelector is designed to batch processing a workload of LLM queries, the iso-difficulty clusters and the LLM metadata in the form of CMT can be useful when queries arrive sequentially and the LLM invocation cannot be batched. In such a query-at-a-time setting, we still associate one or more constraints  $\sigma_M$  on a metric  $\mathcal{M}$ , where  $\mathcal{M}$  is one of accuracy, latency and cost metrics. The goal is to assign the LLM that satisfies the constraint, while optimizing on the metric on which the constraint is not defined. For instance, if a query specifies  $\sigma_T$  and  $\sigma_A$  but not  $\sigma_C$ , then the solution first looks for a feasible solution that meets latency and quality constraint, and, if multiple LLMs based on CMT meet the criteria, we choose

OctoSel Cost Reduction (%) Compared to Cheapest Feasible Solution

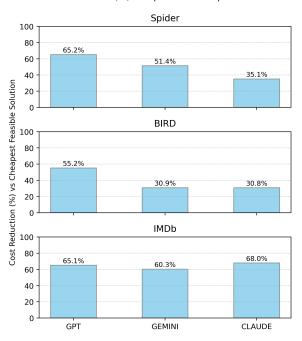


Figure 5: Cost reduction (in percentage) compared to the cost of cheapest feasible solution on the union feasibility regions of (same provider's) single LLMs.

the least cost one. To evaluate the cluster-based LLM assignment strategy of OctoSelector in the query-at-a-time setting, we created a workload with constraints on accuracy and latency, with the objective of minimizing cost. We compared OctoSelector with a strategy of choosing a single LLM and compared the two in the context of (a) cost-reduction using OctoSelector compared to using a single LLM, and (b) reduction in the number of queries that experience constraint violation using OctoSelector compared to using a single LLM. Figure 8 plots the percentage reduction for both cost (blue bars) and violations (orange bars) of OctoSelec-TOR compared to all the LLMs we considered. Compared to all all lowest-cost models (i.e., gpt-4o-mini, gemini-1.5-flash-8b, and claude-haiku), OctoSelector maintain a similar lowest-cost level, while reducing the violation rate for infeasible queries (by using the more expensive model, when need arises). For other models, cost reduction reaches more than 90% on expensive model such as gpt-40 and gemini-1.5-pro. We observed that, OctoSelector

OctoSel Cost Reduction (%) Compared to GraphRouter Plus

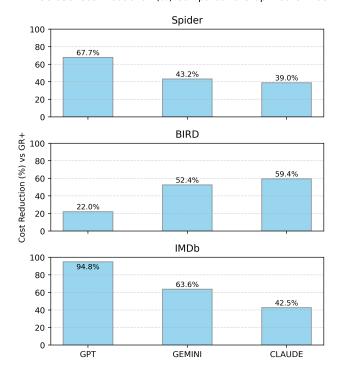


Figure 6: Cost reduction (in percentage) compared to the cost of GraphRouter Plus (GR+) on the GR+'s feasibility regions

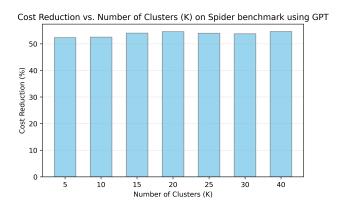


Figure 7: Cost reduction on different cluster numbers K

can always gain either from cost savings or reducing violation rate for infeasible queries across all three benchmarks compared with single LLM baselines.

#### 6 Conclusion

In this paper, we introduced OctoSelector, a framework for LLM selection across diverse tasks. OctoSelector first models query difficulty by extracting features from both input and output, and groups queries into iso-difficulty clusters. Based on this clustering, it formulates LLM assignment as an integer linear programming

Query-at-a-time cost and violation comparison

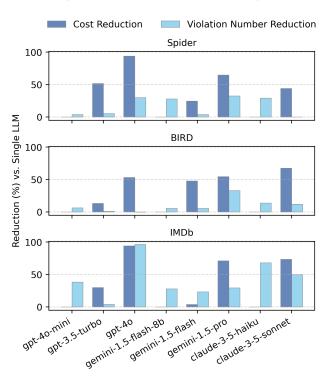


Figure 8: Query-at-a-time scenario: Cost reduction (in percentage) compared with single-LLM baselines on their correspond feasible regions.

problem that jointly optimizes for accuracy, latency, and cost. We proposed batching strategy for LLM assignment—leveraging shared context to reduce overhead—and query-at-a-time scenarios, where a weighted penalties are applied to handle violation on constraints . Experimental results demonstrate that OCTOSELECTOR consistently achieves higher feasibility rates and better cost-effectiveness than the baselines, without compromising performance.

While OctoSelector allows adding new LLMs and workloads, there are several directions of future work. In OctoSelector batching scenario, we ignore the *order* of queries within a batch. However, the *order* is demonstrated as a possible factors that may affect the query response [10]. Another direction for enhancing OctoSelector is the implementation of guardrail mechanisms [9] for LLM response validation.

Moreover, we considered only independent tasks in the paper. When tasks are dependent such as entity resolution(ER), where transitivity exist in ER, numbers of questions(NL query) to ask (whether two attributes are the same) can be reduced according to previous questions result, given the transitivity property. This is challenging since the property of saving the executed queries should be considered within a closed loop of post-optimization factors.

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