# HedonicModel3:SND

luismor

3/26/2021

# VARIABLES SELECTION

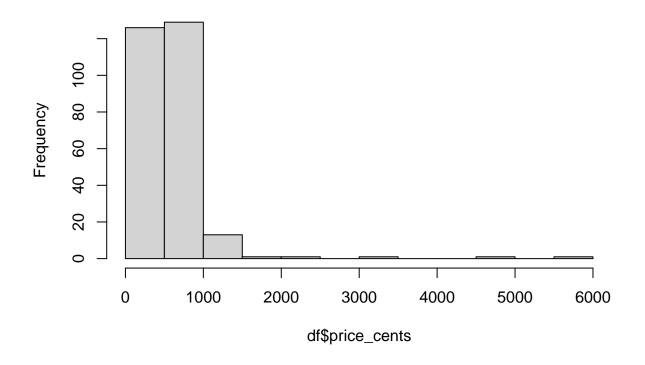
# Loading the data

# Visualization

head(df)

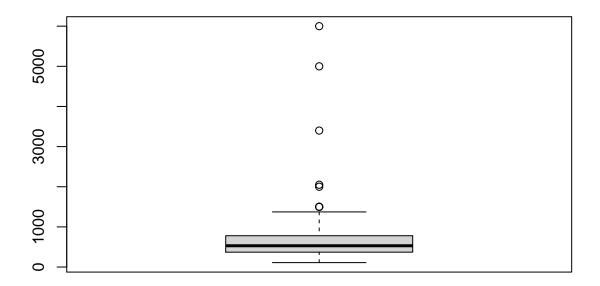
```
library(ggplot2)
library(corrplot)
library(tidyverse)
library(MASS)
```

# Histogram of df\$price\_cents



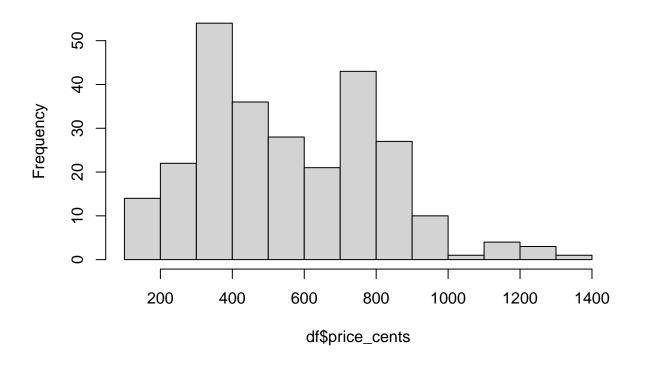
#The histogram shows a positive skweness (positioned to the left). There are many outliers that should

gcaja <- boxplot(df\$price\_cents)</pre>

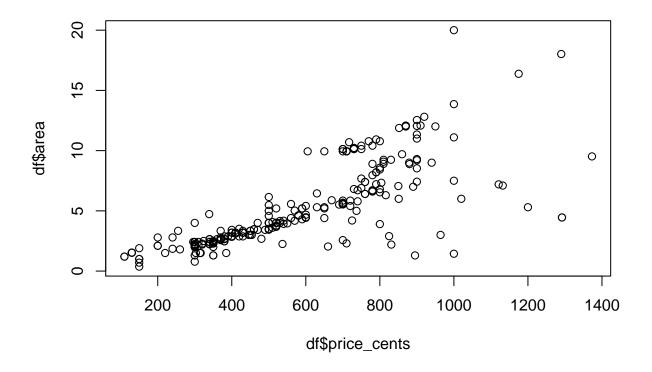


```
df<-df[!(df$price_cents %in% gcaja$out),]
hist(df$price_cents)</pre>
```

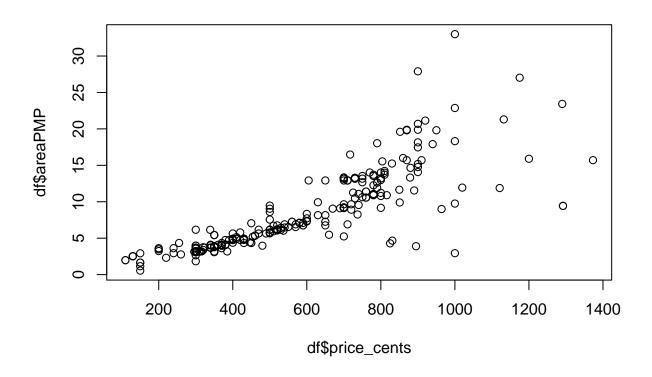
# Histogram of df\$price\_cents



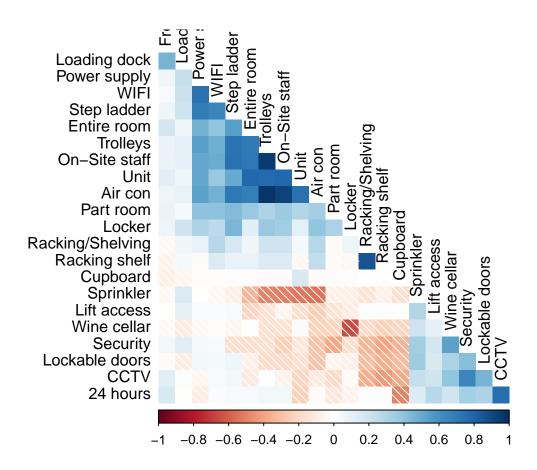
plot(df\$price\_cents,df\$area)



plot(df\$price\_cents,df\$areaPMP)



```
#Deleting outlyers
```



 ${\it \#The\ correlation\ matrix\ indicates\ the\ presence\ of\ strong\ autocorrelation\ between\ some\ variables.\ We\ shown in the correlation in the correlation of\ strong\ autocorrelation\ between\ some\ variables.\ We\ shown in the correlation\ some\ some\ variables.\ We\ shown in the correlation\ some\ variables.\ We\ shown in the correlation\ some\ some$ 

```
library(PanJen)

## Loading required package: mgcv

## Loading required package: nlme

## Attaching package: 'nlme'

## The following object is masked from 'package:dplyr':

## ## collapse

## This is mgcv 1.8-33. For overview type 'help("mgcv-package")'.

formBase <- formula(price_cents~ area + areaPMP + PMP, data=df)
summary(gam(formBase, method="GCV.Cp",data=df))

## ## Family: gaussian</pre>
```

## Link function: identity

```
##
## Formula:
## price_cents ~ area + areaPMP + PMP
## Parametric coefficients:
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) -59.593
                          72.420 -0.823 0.41133
                                     2.665 0.00817 **
## area
                 35.856
                            13.452
## areaPMP
                16.905
                            8.384
                                     2.016 0.04479 *
                            42.456
                                    4.399 1.58e-05 ***
## PMP
                186.786
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## R-sq.(adj) = 0.708
                         Deviance explained = 71.2%
## GCV = 18893 Scale est. = 18606
PanJenArea <-fform(data=df, "area", formBase)
                         BIC ranking (BIC)
                 AIC
## smoothing 3258.29 3294.28
                                       1.0
## x^2
            3275.67 3297.12
                                       2.0
            3284.31 3305.77
## log(x)
                                       3.0
## sqr(x)
            3294.63 3316.09
                                       4.5
## x+x^2
             3294.63 3316.09
                                       4.5
## 1/x
             3345.91 3367.37
                                       6.0
                                       7.5
## base
             3350.62 3368.50
                                       7.5
## x
             3350.62 3368.50
## [1] "Smoothing is a semi-parametric and data-driven transformation, please see Wood (2006) for an el
## [1] "please note that you included area in the base-formula and it is also the variable you test"
PanJenArea<-fform(data=df, "areaPMP", formBase)</pre>
##
                         BIC ranking (BIC)
                 AIC
## x^2
             3267.93 3289.39
                                       1.0
             3271.05 3292.50
                                       2.5
## sqr(x)
## x+x^2
             3271.05 3292.50
                                       2.5
## smoothing 3258.79 3299.90
                                       4.0
## log(x)
            3281.79 3303.25
                                       5.0
## base
             3350.62 3368.50
                                       6.5
## x
             3350.62 3368.50
                                       6.5
                                       8.0
## 1/x
             3348.06 3369.51
## [1] "Smoothing is a semi-parametric and data-driven transformation, please see Wood (2006) for an el
## [1] "please note that you included areaPMP in the base-formula and it is also the variable you test"
PanJenArea<-fform(data=df,"PMP",formBase)</pre>
##
                 AIC
                         BIC ranking (BIC)
## base
             3350.62 3368.50
             3350.62 3368.50
                                       1.5
```

3.0

4.5

## smoothing 3334.21 3371.24

## sqr(x)

3351.12 3372.58

```
## x+x^2 3351.12 3372.58      4.5
## x^2 3351.32 3372.77      6.0
## log(x) 3351.40 3372.86      7.0
## 1/x 3351.76 3373.21      8.0
## [1] "Smoothing is a semi-parametric and data-driven transformation, please see Wood (2006) for an el.
## [1] "please note that you included PMP in the base-formula and it is also the variable you test"

df$areaPMP2 <- df$areaPMP^2
df$area2 <- df$area^2</pre>
```

## Training and test sample division

### Variables selection

#### AIC forward selection

```
Modelzero <- lm(price_cents~1,data=Training)
   summary(Modelzero)

FitAll = lm(price_cents ~ ., data=Training)
   formula(FitAll)

model.forward <- step(Modelzero,direction="forward",scope=formula(FitAll))</pre>
```

```
summary(model.forward)
```

```
##
## Call:
## lm(formula = price_cents ~ areaPMP + areaPMP2 + Trolleys + Locker +
```

```
##
       'Lift access' + 'Part room' + 'Step ladder' + '24 hours' +
##
       'Power supply' + 'Wine cellar' + CCTV + 'Racking shelf' +
##
       'Lockable doors' + 'Entire room' + 'On-Site staff' + PMP,
##
       data = Training)
##
## Residuals:
      Min
                10 Median
                                30
                                      Max
## -299.85 -31.73
                      2.00
                            40.91 351.25
##
## Coefficients:
                     Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                     720.7162
                                116.6113
                                           6.181 4.54e-09 ***
## areaPMP
                      71.6360
                                  3.7315 19.198 < 2e-16 ***
## areaPMP2
                      -1.3958
                                  0.1442 -9.682 < 2e-16 ***
## Trolleys
                     283.4565 101.7978
                                          2.785 0.005965 **
## Locker
                     -276.1819
                                 47.6418 -5.797 3.18e-08 ***
## 'Lift access'
                    -180.0903
                                 74.2699 -2.425 0.016357 *
## 'Part room'
                     -304.9518
                                 49.7279 -6.132 5.82e-09 ***
## 'Step ladder'
                                          4.843 2.85e-06 ***
                     259.4567
                                 53.5774
## '24 hours'
                   -1072.1018
                               146.1035 -7.338 8.37e-12 ***
## 'Power supply'
                    -143.2721
                                 43.3152 -3.308 0.001147 **
## 'Wine cellar'
                     -159.1852
                                 52.1847 -3.050 0.002650 **
## CCTV
                                          6.274 2.79e-09 ***
                     915.6844
                                145.9520
## 'Racking shelf'
                                 95.1061
                                           4.335 2.49e-05 ***
                     412.2588
## 'Lockable doors' -220.1758
                               59.1372 -3.723 0.000267 ***
## 'Entire room'
                     138.1340
                                 41.2172
                                          3.351 0.000990 ***
## 'On-Site staff'
                     -284.5849
                               105.1520 -2.706 0.007491 **
## PMP
                       61.8493
                                 33.3704
                                          1.853 0.065545 .
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 82.69 on 171 degrees of freedom
## Multiple R-squared: 0.8992, Adjusted R-squared: 0.8898
## F-statistic: 95.36 on 16 and 171 DF, p-value: < 2.2e-16
predict.for.tr <- predict(model.forward, newdata = Training)</pre>
training.for.mse <- mean((predict.for.tr - Training*price_cents)^2)
paste("Training MSE error:", training.for.mse)
## [1] "Training MSE error: 6218.84749850434"
predict.for.tst <- predict(model.forward, newdata = Test)</pre>
test.for.mse <- mean((predict.for.tst - Test$price_cents)^2)</pre>
paste("Test MSE error:", test.for.mse)
```

AIC backward selection

## [1] "Test MSE error: 33491.9618712716"

```
model.backward <- stepAIC(FitAll, trace=TRUE, direction="backward")</pre>
```

#### summary(model.backward)

```
##
## Call:
## lm(formula = price_cents ~ area + PMP + areaPMP + Locker + 'Racking shelf' +
      'Part room' + 'Entire room' + 'Wine cellar' + 'Air con' +
      '24 hours' + 'Lift access' + Security + CCTV + 'Lockable doors' +
##
      'On-Site staff' + Trolleys + 'Step ladder' + 'Power supply' +
##
      areaPMP2 + area2, data = Training)
##
##
## Residuals:
      Min
               1Q Median
                               ЗQ
                                     Max
## -257.51 -30.02
                     0.81
                            34.30 316.43
##
## Coefficients:
##
                     Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                    1390.3759 197.4060
                                         7.043 4.68e-11 ***
                                43.6297 -4.744 4.47e-06 ***
## area
                    -206.9883
## PMP
                              72.7750 -2.653 0.008749 **
                    -193.0689
                                         7.278 1.26e-11 ***
## areaPMP
                    199.3332
                               27.3882
                    -241.9684 48.4049 -4.999 1.45e-06 ***
## Locker
## 'Racking shelf'
                    428.3879 92.3749 4.637 7.08e-06 ***
## 'Part room'
                   -322.5346 57.5388 -5.606 8.42e-08 ***
                    123.9874 41.3909 2.996 0.003157 **
## 'Entire room'
## 'Wine cellar'
                    -118.8612 54.6932 -2.173 0.031171 *
## 'Air con'
                    -264.9318 182.8798 -1.449 0.149306
## '24 hours'
                   -1036.5202 187.1490 -5.538 1.17e-07 ***
## 'Lift access'
                    -234.0499
                               90.2713 -2.593 0.010366 *
## Security
                    -221.1852 121.1279 -1.826 0.069629 .
## CCTV
                     873.3448
                               200.5938 4.354 2.33e-05 ***
## 'Lockable doors' -226.9956
                               68.0640 -3.335 0.001051 **
## 'On-Site staff'
                   -422.2022
                                105.1282 -4.016 8.93e-05 ***
## Trolleys
                     680.5225 198.6777 3.425 0.000773 ***
## 'Step ladder'
                     280.5002 55.6191 5.043 1.18e-06 ***
## 'Power supply'
                               46.5463 -3.408 0.000820 ***
                    -158.6295
                                0.6519 -6.885 1.12e-10 ***
## areaPMP2
                      -4.4883
                                         4.836 3.00e-06 ***
## area2
                       8.0578
                                 1.6664
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 77.89 on 167 degrees of freedom
## Multiple R-squared: 0.9127, Adjusted R-squared: 0.9022
## F-statistic: 87.27 on 20 and 167 DF, p-value: < 2.2e-16
predict.bck.tr <- predict(model.backward, newdata = Training)</pre>
training.bck.mse <- mean((predict.bck.tr - Training$price_cents)^2)</pre>
paste("Training MSE error:", training.bck.mse)
```

### **Summary**

```
## [1] "Training MSE error: 5388.60327239268"

predict.bck.tst <- predict(model.backward, newdata = Test)

test.bck.mse <- mean((predict.bck.tst - Test$price_cents)^2)
paste("Test MSE error:", test.bck.mse)

## [1] "Test MSE error: 47216.582975243"</pre>
```

# Ridge and Lasso regularizations

```
library(glmnet)

## Loading required package: Matrix

## ## Attaching package: 'Matrix'

## The following objects are masked from 'package:tidyr':

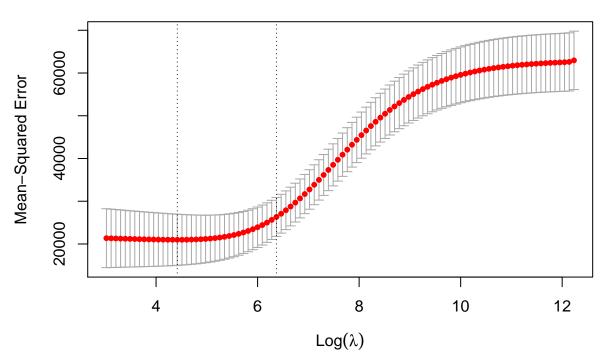
## expand, pack, unpack

## Loaded glmnet 4.0-2

# Convert into a matrix train and test data
train.mat <- model.matrix(price_cents ~ ., data = Training)
test.mat <- model.matrix(price_cents ~ ., data = Test)</pre>
```

## Ridge

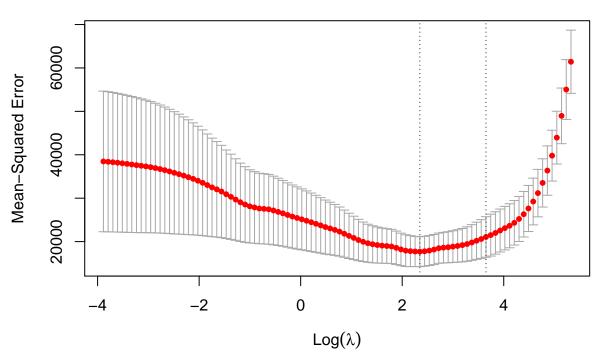
## 



```
paste("Best lambda:", cv.ridge$lambda.min)
## [1] "Best lambda: 82.8962040386565"
paste("Best lambda + y sd:", cv.ridge$lambda.1se)
## [1] "Best lambda + y sd: 584.816330737625"
# Training the model
mod.ridge.train <- glmnet(x = train.mat, y = Training$price_cents, alpha = 0,</pre>
                          lambda = cv.ridge$lambda.1se)
dim(coef(mod.ridge.train))
## [1] 29 1
coef(mod.ridge.train, s = "lambda.1se")
## 29 x 1 sparse Matrix of class "dgCMatrix"
##
## (Intercept)
                      519.9546855
## (Intercept)
## area
                        9.5555486
```

```
## PMP
                     16.1704369
## areaPMP
                      6.7590258
## Locker
                     -61.7338679
## Cupboard
## 'Racking shelf'
                     50.3237893
## 'Part room'
                    -32.9606682
## 'Entire room'
                     32.8389610
## Unit
                     35.1664430
## 'Wine cellar'
                     62.8528510
## 'Air con'
                     14.7398559
## '24 hours'
                     -68.5651762
## 'Lift access'
                     -93.5450013
## Security
                      3.9605439
## 'Loading dock'
                     11.4918662
## CCTV
                      -37.0390277
## 'Lockable doors'
                       3.2126782
## 'On-Site staff'
                     17.2551282
## 'Free Parking'
                      4.0930558
## Trolleys
                     15.4875343
## 'Step ladder'
                       17.0748527
## 'Racking/Shelving' 50.3044594
## Sprinkler
                      -3.3464127
## 'Power supply'
                      3.2118782
## WIFI
                       -2.5807604
## areaPMP2
                       0.1792083
## area2
                        0.4311332
# Training predictions
pred.ridge <- predict(mod.ridge.train, newx = train.mat)</pre>
# Training error (MSE)
tr.ridge.mse <- mean((pred.ridge - Training$price_cents)^2)</pre>
paste("Training MSE error:", tr.ridge.mse)
## [1] "Training MSE error: 22768.5893704842"
#Test predictions: using training model
pred.test.ridge <- predict(mod.ridge.train,newx = test.mat)</pre>
test.ridge.mse <- mean((pred.test.ridge - Test$price_cents)^2)</pre>
paste("Test MSE error:",test.ridge.mse)
## [1] "Test MSE error: 29051.6852001325"
Lasso
cv.lasso <- cv.glmnet(x = train.mat, y = Training$price_cents, alpha = 1,</pre>
                      lambda = NULL, type.measure="mse")
plot(cv.lasso)
```

## 26 26 26 26 24 23 22 20 16 12 10 6 3 1 1 1



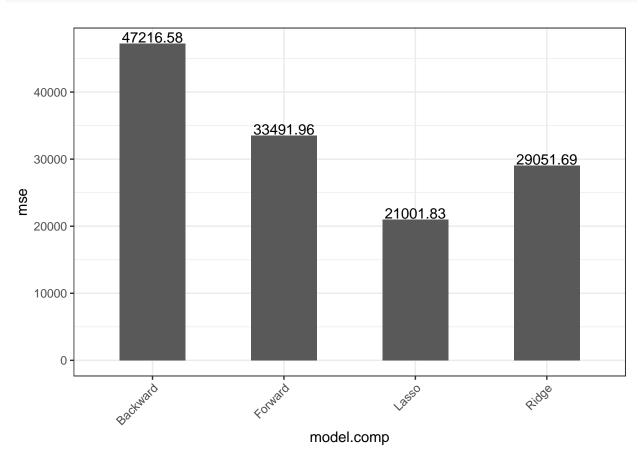
```
paste("Best lambda:", cv.lasso$lambda.min)
## [1] "Best lambda: 10.4603145174933"
paste("Best lambda + y sd:", cv.lasso$lambda.1se)
## [1] "Best lambda + y sd: 38.4770092814394"
# Training the model
mod.lasso.train <- glmnet(x = train.mat, y = Training$price_cents, alpha = 1,</pre>
                          lambda = cv.lasso$lambda.1se)
dim(coef(mod.lasso.train))
## [1] 29 1
coef(mod.lasso.train, s = "lambda.1se")
## 29 x 1 sparse Matrix of class "dgCMatrix"
##
## (Intercept)
                      311.40725
## (Intercept)
## area
```

```
## PMP
## areaPMP
                     31.04453
## Locker
                     -17.87422
## Cupboard
## 'Racking shelf'
## 'Part room'
## 'Entire room'
                       56.28222
## Unit
## 'Wine cellar'
## 'Air con'
## '24 hours'
## 'Lift access'
## Security
## 'Loading dock'
## CCTV
## 'Lockable doors'
## 'On-Site staff'
## 'Free Parking'
## Trolleys
## 'Step ladder'
## 'Racking/Shelving'
## Sprinkler
## 'Power supply'
## WIFI
## areaPMP2
## area2
# Training predictions
pred.lasso <- predict(mod.lasso.train, newx = train.mat)</pre>
# Training error (MSE)
tr.lasso.mse <- mean((pred.lasso - Training$price_cents)^2)</pre>
paste("Training MSE error:", tr.lasso.mse)
## [1] "Training MSE error: 19127.0633609672"
#Test predictions: using training model
pred.test.lasso <- predict(mod.lasso.train, newx = test.mat)</pre>
test.lasso.mse <- mean((pred.test.lasso - Test$price_cents)^2)</pre>
paste("Test MSE error:",test.lasso.mse)
## [1] "Test MSE error: 21001.8332374298"
Comparing results
df_compar <- data.frame(model.comp = c("Forward", "Backward", "Ridge", "Lasso"),</pre>
```

ggplot(data = df\_compar, aes(x = model.comp, y = mse)) + geom\_col(width = 0.5) +

mse = c(test.for.mse, test.bck.mse, test.ridge.mse, test.lasso.mse))

```
geom_text(aes(label = round(mse, 2)), vjust = -0.1) + theme_bw() + theme(axis.text.x = element_text
hjust = 1))
```



### Linear Model

##

## areaPMP

## Locker

## Unit

1.791 20.350 < 2e-16 \*\*\*

29.668 6.038 8.45e-09 \*\*\*

Estimate Std. Error t value Pr(>|t|)

-126.104 33.151 -3.804 0.000194 \*\*\*

## (Intercept) 264.617 18.179 14.556 < 2e-16 \*\*\*

36.447

179.120

```
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 125.3 on 184 degrees of freedom
## Multiple R-squared: 0.7509, Adjusted R-squared: 0.7468
## F-statistic: 184.9 on 3 and 184 DF, p-value: < 2.2e-16
lmodel.Test <- lm (price_cents ~ areaPMP + Locker + Unit, data = Test)</pre>
summary(lmodel.Test)
##
## Call:
## lm(formula = price_cents ~ areaPMP + Locker + Unit, data = Test)
##
## Residuals:
##
      Min
               1Q Median
                               ЗQ
                                      Max
## -517.05 -57.83 -10.30 51.64 517.17
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 236.428
                           30.289
                                   7.806 3.53e-11 ***
                            3.121 12.038 < 2e-16 ***
## areaPMP
                37.576
## Locker
                -5.139
                           59.003 -0.087 0.93083
## Unit
               132.255
                           45.755 2.890 0.00508 **
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 138.7 on 72 degrees of freedom
## Multiple R-squared: 0.7319, Adjusted R-squared: 0.7207
## F-statistic: 65.52 on 3 and 72 DF, p-value: < 2.2e-16
```