# CSCI E-106: Section 13:

# 04/25/2019

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# (10.09) Reference Brand Preference Problem 6.5.

In a small-scale experimental study of the relation between degree of brand liking (Y) and moisture content  $(X_1)$  and sweetness  $(X_2)$  of the product, the following results were obtained from the experiment based on a completely randomized design (data are coded).

Please use datasets titled CH06PR05.txt when applicable

a Obtain the studentized deleted residuals and identify any outlying Y observations. Use the Bonferroni outlier test procedure with  $\alpha = .10$ . State the decision rule and conclusion.

```
#Load the data
dfCH10PR09 =read.delim(file="CH06PR05.txt", sep="", header = FALSE)
colnames(dfCH10PR09) =c("BrandLiking", "MoistureContent", "Sweetness")
#find our lmfit
lmCH10PR09 =lm(BrandLiking~MoistureContent+Sweetness, dfCH10PR09)
#calculate our deleted residuals using the rstudent function:
# this Returns the Studentized residuals based on rank-based estimation
deletedResiduals = rstudent(lmCH10PR09)
print(deletedResiduals)
                         2
             1
                                     3
                                                  4
                0.06128781 -1.36059879
                                        1.38602483 -0.36694571 -0.66490618
  -0.04085498
             7
                         8
                                     9
##
                                                 10
                                                             11
                                                                         12
  -0.76716157
               0.50461264
                            0.46506694 -0.60436295
                                                     1.82302030
##
            13
                        14
                                    15
                                                 16
## -1.13966417 -2.10272640 1.48973208 0.24572878
#you can round them to the 3rd to get smaller results
round(deletedResiduals,3)
                                                                       10
##
        1
                      3
                             4
                                    5
                                           6
                                                   7
                                                          8
## -0.041
          0.061 -1.361 1.386 -0.367 -0.665 -0.767 0.505 0.465 -0.604
##
       11
                     13
                            14
                                   15
                                          16
   1.823 0.978 -1.140 -2.103 1.490 0.246
```

```
#longer way to do this without the rstudent function
n = length(dfCH10PR09$BrandLiking)
# Number of regression parameters
p = 3
hii =hatvalues(lmCH10PR09)
ei = lmCH10PR09$residuals
SSE =anova(lmCH10PR09)[3,2]
deletedRes = ei*((n-p-1)/(SSE*(1-hii)-ei^2))^.5
round(deletedRes,3)
##
        1
                                    5
                                            6
                                                                       10
## -0.041 0.061 -1.361 1.386 -0.367 -0.665 -0.767 0.505 0.465 -0.604
##
       11
              12
                     13
                            14
                                   15
                                           16
## 1.823 0.978 -1.140 -2.103 1.490 0.246
#degrees of freedom
df = n-p-1
print(df)
## [1] 12
#t- value
t = qt(1-.10/(2*n), df = n-p-1)
print(t)
## [1] 3.307783
# finding our top 3 residuals
head(sort(abs(deletedRes), decreasing = TRUE),3)
##
         14
                  11
                           15
## 2.102726 1.823020 1.489732
```

 $H_0$ : Index 14 is not a outlier  $H_a$ : Index 14 is an outlier Decision Rule:  $|t14| \le 3.3$ , we conclude  $H_0$ . Otherwise,  $H_a$ 

Conclusion: if  $|t_i| \le 3.308$  conclude no outliers, otherwise conclude that i is an outlier. Since  $|t_14| = 2.103$  we can conclude no outliers

b. Obtain the diagonal elements of the hat matrix, and provide an explanation for the pattern in these elements.

```
#find diagonal elements
diagonalElements = hatvalues(lmCH10PR09)
print(diagonalElements)
##
              2
                      3
                             4
                                    5
                                           6
                                                  7
                                                                      10
       1
                                                         8
## 0.2375 0.2375 0.2375 0.2375 0.1375 0.1375 0.1375 0.1375 0.1375 0.1375
              12
                     13
                            14
                                   15
                                          16
## 0.1375 0.1375 0.2375 0.2375 0.2375
#check if they sum up to 3 (our Number of regression parameters)
sum(diagonalElements)
```

### ## [1] 3

Conclusion: Our elements seem to have the same two values showing that we do not have outliers.

c. Are any of the observations outlying with regard to their X values according to the rule of thumb stated in the chapter?

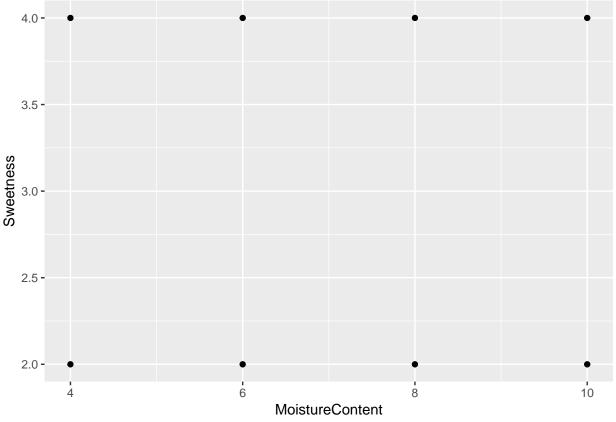
### Student's Solution Below

```
#mean leverage value
meanLev = p/n
hii > 2* meanLev
            2
                                         7
                                                                      12
##
      1
                  3
                        4
                              5
                                    6
                                               8
                                                          10
                                                                11
## FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
##
     13
           14
                 15
                       16
## FALSE FALSE FALSE
```

Conclusion: We see that none of the values are greater than 2 times the leverage so we say that we have no outliers.

d. Management wishes to estimate the mean degree of brand liking for moisture content  $X_1 = 10$  and sweetness  $X_2 = 3$ . Construct a scatter plot of  $X_2$  against  $X_1$  and determine visually whether this prediction involves an extrapolation beyond the range of the data. Also, use (10.29) to determine whether an extrapolation is involved. Do your conclusions from the two methods agree?

```
#scatter plot
ggplot(data=dfCH10PR09,aes(x=MoistureContent, y=Sweetness))+geom_point()
```



```
X = matrix(data=c(rep(1,n), dfCH10PR09$MoistureContent, dfCH10PR09$Sweetness),nrow=n,ncol=p)
X_new = matrix(data=c(1,10,3),nrow=1,ncol=p)
print(X_new)

## [,1] [,2] [,3]
## [1,] 1 10 3
h_newnew = X_new%*%solve(t(X)%*%X)%*%t(X_new)
print(h_newnew)

## [,1]
```

Conclusion: The values x1 = 10 and x2 = 3 are in the range so we do not have to do any extrapolation. And we see that the leverage point is in line with the existing leverage values.

e. The largest absolute studentized deleted residual is for case 14. Obtain the DFFITS, DFBETAS, and Cook's distance values for this case to assess the influence of this case. What do you conclude?

### Student's Solution Below

## [1,] 0.175

```
#obtain DFFITS
dffits_14 = dffits(lmCH10PR09)[14]
print(round(dffits_14,3))
## 14
## -1.174
```

```
#obtain DFBETAS
dfbetas_14 = dfbetas(lmCH10PR09)[14,]
print(round(dfbetas 14,3))
##
       (Intercept) MoistureContent
                                           Sweetness
##
             0.839
                                              -0.602
                             -0.808
#cooks distance
x = cbind(1,dfCH10PR09$MoistureContent,dfCH10PR09$Sweetness)
h = x\% *\% solve(t(x)\% *\% x)\% *\% t(x)
h_{diag} = diag(h)
sum_h = sum(h_diag)
MSE = SSE / lmCH10PR09$df.residual
cooksdistance = lmCH10PR09$residuals^2/(sum_h*MSE)*(h_diag/(1-h_diag)^2)
print(cooksdistance[14])
##
          14
## 0.3634123
```

Conclusion: The absolute value of dfits at 14 is bigger than 1 but is a bit close so it could be an influential case. But then when we look at the beta values none of them are near one so we see that this is not an influential case. From all of our reviews it seems that case 14 does seem to be an influential case.

f. Calculate the average absolute percent difference in the fitted values with and without case 14. What does this measure indicate about the influence of case 14?

### Student's Solution Below

```
predWith = fitted(lmCH10PR09)
fitWithout = lm(BrandLiking~MoistureContent+Sweetness, dfCH10PR09[-14,])
predWithout = predict(fitWithout, newdata =dfCH10PR09)

averageAbs = 100*mean(abs(predWith-predWithout)/predWith)
print(averageAbs)
```

## [1] 0.677679

Conclusion: So we can see here that the difference between the with and without case of 14 would be 68%.

g. Calculate Cook's distance  $D_i$  for each case and prepare an index plot. Are any cases influential according to this measure?

```
Di <- ((ei^2)/(p*MSE))*(hii/(1-hii)^2)
print(Di)
##
                            2
                                          3
                                                                     5
              1
## 0.0001877130 0.0004223542 0.1803921815 0.1862582123 0.0076655286
                            7
              6
                                         8
                                                       9
## 0.0245466787 0.0322971439 0.0143542862 0.0122308711 0.0204060192
##
             11
                           12
                                        13
                                                      14
                                                                    15
```

```
## 0.1498281704 0.0509831969 0.1318214458 0.3634123447 0.2106609008
## 16
## 0.0067576676
```

Conclusion: There are no influential points from the graphs.

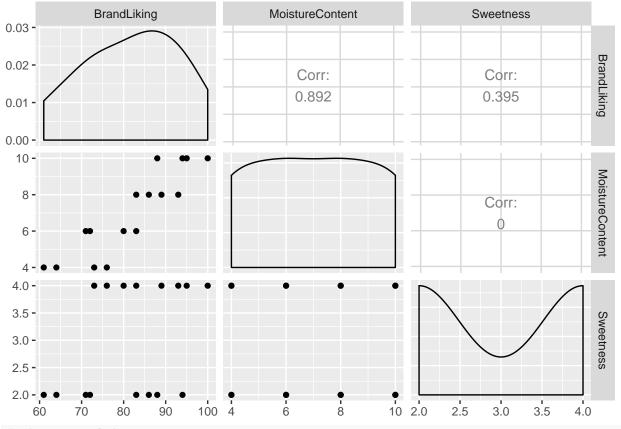
# (10.15) Reference Brand Preference Problem 6.5a.

a. What do the scatter plot matrix and the correlation matrix show about pairwise linear associations among the predictor variables?

## Student's Solution Below

```
#load the data
dfCH10PR15 =read.delim(file="CH06PR05.txt", sep="", header = FALSE)
colnames(dfCH10PR15) =c("BrandLiking", "MoistureContent", "Sweetness")
#plot the pairs (theres a few ways to do this)...
pairs(dfCH10PR15)
                                                   8
                                                                                90
       BrandLiking
                                                                                80
                                                                                20
0
                                                                            0
                0000
\infty
                              MoistureContent
9
              00
2
          0000
                  0 00
                                                                                3.0
                                                           Sweetness
        70
              80
                   90
                         100
                                                      2.0
                                                           2.5
                                                                 3.0
                                                                      3.5
                                                                            4.0
```

#or we could use ggpairs
library(GGally)
ggpairs(dfCH10PR15)



#matrix correlation

cor(dfCH10PR15)

## BrandLiking MoistureContent Sweetness
## BrandLiking 1.0000000 0.8923929 0.3945807
## MoistureContent 0.8923929 1.0000000 0.00000000
## Sweetness 0.3945807 0.0000000 1.00000000

Conclusion: We can see that there is no correlation between them.

b. Find the two variance inflation factors. Why are they both equal to 1?

## Student's Solution Below

library(car)

```
## Loading required package: carData
```

#find our lmfit
lmCH10PR15 =lm(BrandLiking~MoistureContent+Sweetness, dfCH10PR09)

#find our two variance inflation factors
vif(lmCH10PR15)

## MoistureContent Sweetness
## 1 1

# (10.27) Refer to the SENIC dataset in Appendix C.1 and Project 9.25.

SENIC DATASET DESCRIPTION: The primary objective of the Study on the Efficacy of Nosocomial Infection Control (SENIC Project) was to determine whether infection surveillance and control programs have reduced the rates of nosocomial (hospital-acquired) infection in United States hospitals. This data set consists of a random sample of 113 hospitals selected from the original 338 hospitals surveyed. Each line of the dataset has an identification number and provides information on 11 variables for a single hospital. The data presented here are for the 1975-76 study period.

Please use dataset titled APPENC01.txt when applicable

The regression model containing age, routine chest X-ray ratio, and average daily census in first-order terms is to be evaluated in detail based on the model-building data set.

a. Obtain the residuals and plot them separately against  $\hat{Y}$ , each of the predictor variables in the model, and each of the related cross-product terms. On the basis of these plots, should any modifications of the model be made?

```
#load the dataset and give it values
senic.df = read.table("APPENCO1.txt", header=FALSE, col.names = c("id", "los", "age", "infection_risk",
senic.df[ ,c('msa', 'region')] = list(NULL)
#we then see that we need to use cases 57 - 113 only in order to build our model properly
model.df = senic.df[57:113,]
attach(model.df)
model =lm(log10(los)~age+xray+adc, data = model.df)
lm = lm(los \sim (age + xray + adc)^2, senic.df)
#we can print out our residuals to show them which would satisfy the
#first question to obtain our residuals from the model
ei = model$residuals
print(round(ei,3))
                                                    63
##
               58
                      59
                              60
                                     61
                                             62
                                                            64
                                                                   65
                                                                          66
       57
##
   -0.086 -0.064 -0.004
                          0.068
                                  0.093
                                         0.015 -0.087
                                                        0.038
                                                              -0.095
                                                                      -0.030
##
       67
               68
                      69
                              70
                                     71
                                             72
                                                    73
                                                            74
                                                                   75
                                                                          76
##
    0.033
          -0.076
                 -0.052
                         -0.038
                                 -0.055
                                        -0.044
                                                 0.021
                                                        0.045
                                                                0.024
                                                                      -0.083
                      79
##
       77
                                                                   85
               78
                              80
                                     81
                                            82
                                                    83
                                                           84
                                                                          86
##
    0.033
          -0.073
                  -0.017
                          0.034
                                  0.091
                                        -0.052
                                                -0.034
                                                        0.041
                                                               -0.008
                                                                       0.017
                                                    93
                                                           94
                                                                   95
##
       87
               88
                      89
                              90
                                     91
                                            92
                                                                          96
##
   -0.113
           0.025
                   0.007
                          0.060
                                  0.016
                                         0.021
                                                 0.026 -0.022
                                                                0.043
                                                                      -0.010
                                                   103
                                                                  105
##
       97
               98
                      99
                             100
                                    101
                                           102
                                                          104
                                                                         106
                                                                       0.087
           0.081 -0.013 -0.007
                                  0.065
                                         0.040 -0.101
                                                        0.031
                                                               0.025
##
  -0.012
##
              108
                     109
      107
                            110
                                    111
                                           112
                                                   113
          0.013 -0.014 0.073 -0.049
## -0.037
                                        0.086
#now lets plot the points seperately against y hat
ggplot(model,aes(x=model$fitted.values, y=model$residuals))+
  geom_point()+ geom_smooth(method=lm)+xlab("Fitted Values")+ ylab("Residuals")
```

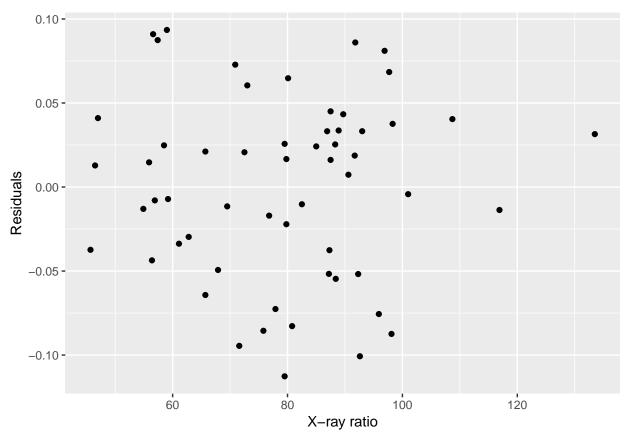
```
## Warning: Computation failed in `stat_smooth()`:
## 'what' must be a function or character string

0.10-
0.05-
-0.05-
-0.10-
0.99
1.0
1.1
```

```
ggplot(model,aes(x=xray, y=model$residuals))+ geom_point()+
  geom_smooth(method=lm)+xlab("X-ray ratio")+ ylab("Residuals")
```

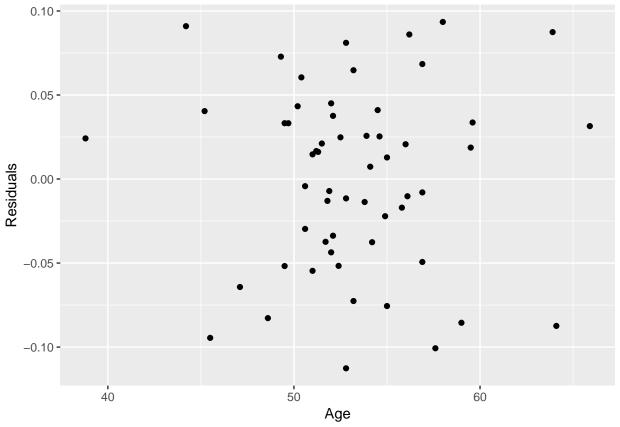
Fitted Values

```
## Warning: Computation failed in `stat_smooth()`:
## 'what' must be a function or character string
```



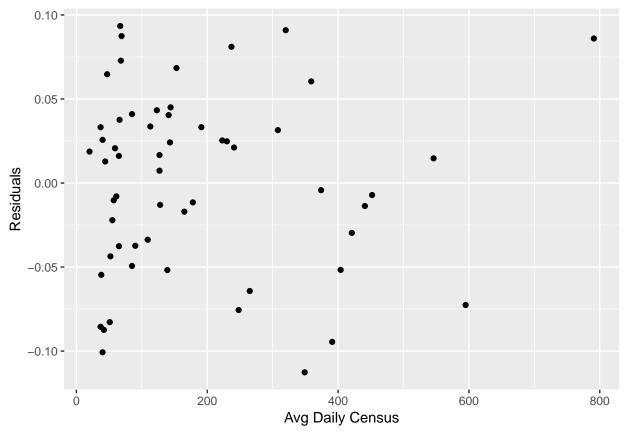
```
ggplot(model,aes(x=age, y=model$residuals))+ geom_point()+
  geom_smooth(method=lm)+xlab("Age")+ ylab("Residuals")
```

## Warning: Computation failed in `stat\_smooth()`:
## 'what' must be a function or character string



```
ggplot(model,aes(x=adc, y=model$residuals))+ geom_point()+
geom_smooth(method=lm)+xlab("Avg Daily Census")+ ylab("Residuals")
```

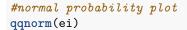
<sup>##</sup> Warning: Computation failed in `stat\_smooth()`:
## 'what' must be a function or character string



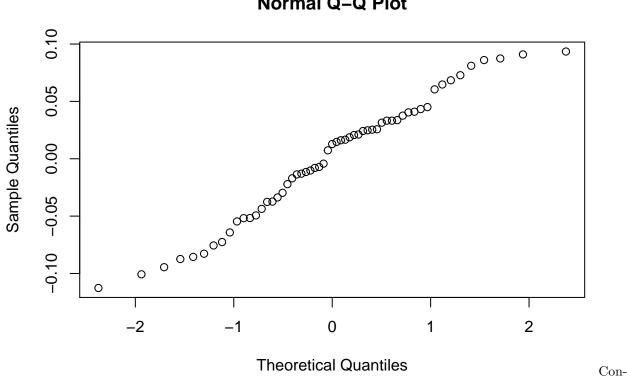
Conclusion: We say that our variances look to be ok and do not seem to show any certain pattern.

b. Prepare a normal probability plot of the residuals. Also obtain the coefficient of correlation between the ordered residuals and their expected values under normality. Test the reasonableness of the normality assumption, using Table B.6 and  $\alpha = .05$ . What do you conclude?

```
#first we want to show our expected values
MSE =anova(model)$"Mean Sq"[4]
k = rank(ei)
n = length(age)
expV = sqrt(MSE)*qnorm((k-.375)/(n+0.25))
print(round(expV,3))
                                      61
                                              62
                                                      63
                                                                     65
                                                                             66
##
       57
               58
                       59
                              60
                                                              64
##
   -0.077 -0.057 -0.005
                           0.066
                                   0.127
                                          0.002 -0.084
                                                          0.039
                                                                 -0.093 -0.028
##
       67
               68
                       69
                              70
                                      71
                                              72
                                                      73
                                                              74
                                                                     75
                                                                             76
    0.033 -0.066 -0.046 -0.036
                                  -0.053 -0.039
                                                  0.015
                                                          0.053
                                                                  0.017
                                                                        -0.071
##
                              80
                                      81
##
       77
               78
                       79
                                              82
                                                      83
                                                              84
                                                                     85
                                                                             86
##
    0.031
          -0.061
                  -0.022
                           0.036
                                   0.105
                                          -0.049
                                                 -0.031
                                                          0.046
                                                                 -0.010
                                                                          0.007
                                      91
                                                      93
                                                                     95
##
       87
               88
                       89
                              90
                                              92
                                                              94
                                                                             96
   -0.127
            0.022
                  -0.002
                           0.057
                                   0.005
                                          0.012
                                                  0.025
                                                         -0.025
                                                                  0.049
##
                                                                        -0.012
##
       97
               98
                       99
                             100
                                     101
                                             102
                                                     103
                                                            104
                                                                    105
                                                                            106
           0.077 -0.017 -0.007
   -0.015
                                   0.061
                                          0.043 - 0.105
                                                          0.028
                                                                  0.020
                                                                         0.093
##
      107
              108
                      109
                              110
                                     111
                                             112
                                                     113
## -0.033
            0.000 -0.020
                           0.071 -0.043
                                          0.084
                                                  0.010
```



# Normal Q-Q Plot

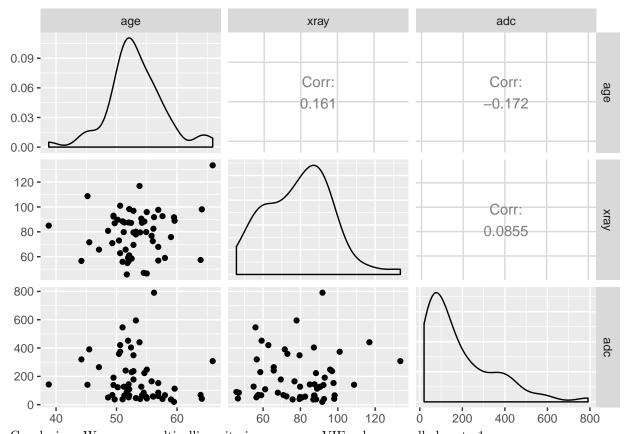


clusion:

H0: normal Ha: not normal We will conclude H0 in this case since our r=.990 based on table b.6 our rcritical is .98 so our errors are normally distributed.

c. Obtain the scatter plot matrix, the correlation matrix of the X variables, and the variance inflation factors. Are there any indications that serious multicollinearity problems are present? Explain.

```
#show our variance inflation factors
round(vif(model),3)
     age xray
                 adc
## 1.065 1.041 1.045
#scatter plot matrix
ourxvars =data.frame(age, xray, adc)
ggpairs(ourxvars)
```



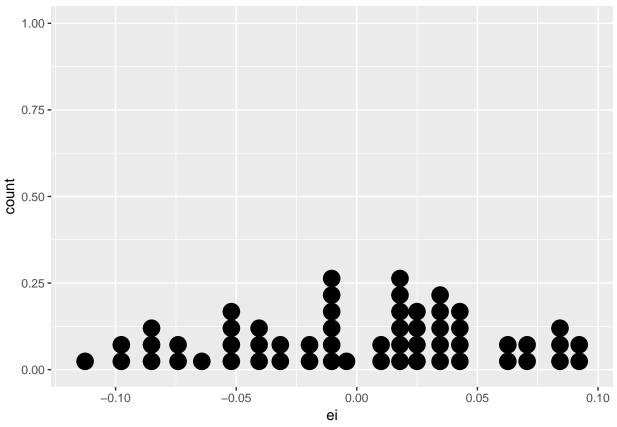
Conclusion: We see no multicollinearity issues as our VIF values are all close to 1.  $\,$ 

d. Obtain the studentized deleted residuals and prepare a dot plot of these residuals. Are any outliers present? Use the Bonferroni outlier test procedure with  $\alpha = .01$ . State the decision rule and conclusion.

```
#first lets find our hii
one =rep(1,length(los))
x_matrix =cbind(one, age, xray, adc)
x_matrix_trans =t(x_matrix)
h_matrix = x_matrix%*%(solve(x_matrix_trans%*%x_matrix))%*%x_matrix_trans
hii =diag(h_matrix)
print(round(hii,3))
   [1] 0.055 0.055 0.069 0.045 0.069 0.142 0.129 0.056 0.084 0.073 0.044
## [12] 0.037 0.051 0.032 0.048 0.055 0.031 0.026 0.213 0.055 0.055 0.133
## [23] 0.024 0.054 0.106 0.047 0.038 0.082 0.066 0.024 0.035 0.024 0.028
## [34] 0.043 0.039 0.035 0.031 0.030 0.040 0.033 0.023 0.037 0.051 0.093
## [45] 0.031 0.149 0.052 0.288 0.043 0.157 0.082 0.090 0.131 0.044 0.042
## [56] 0.288 0.067
#now we need to find the student deleted residuals
model.anova = anova(model)
ei = model$residuals
n = length(los)
p = 4
```

```
sse = model.anova$"Sum Sq"[4]
ti = ei*sqrt(((n-p-1)/(sse*(1-hii)-ei^2)))
print(round(ti,3))
##
       57
              58
                      59
                             60
                                     61
                                            62
                                                    63
                                                           64
                                                                   65
                                                                          66
## -1.617 -1.201 -0.079
                          1.274
                                 1.789
                                         0.284 -1.726
                                                        0.697 -1.826 -0.554
##
       67
              68
                                     71
                                                    73
                                                                  75
                      69
                             70
                                            72
                                                           74
                                                                          76
##
    0.611 -1.406 -0.959 -0.688 -1.014 -0.810
                                                0.385
                                                        0.823
                                                               0.489
                                                                     -1.561
##
       77
              78
                      79
                             80
                                     81
                                            82
                                                   83
                                                           84
                                                                  85
##
    0.614 -1.425 -0.309
                          0.622
                                 1.776 -0.959 -0.619
                                                        0.772 - 0.148
                                                                       0.302
##
       87
                      89
                             90
                                     91
                                            92
                                                    93
                                                           94
                                                                   95
## -2.145
           0.461
                   0.133
                          1.122
                                 0.295
                                         0.378
                                                0.469 -0.403
                                                               0.797 -0.187
##
       97
              98
                      99
                            100
                                    101
                                           102
                                                   103
                                                          104
                                                                 105
                                                                         106
## -0.209
           1.513 -0.239 -0.135
                                         0.790 -1.918 0.672 0.456
                                 1.195
                                                                     1.756
      107
             108
                     109
                            110
                                    111
                                           112
                                                   113
## -0.702 0.241 -0.263 1.358 -0.911
                                        1.889
                                               0.348
#prepare our dotplot
ggplot(model,aes(x = ei))+ geom_dotplot()
```

## `stat\_bindot()` using `bins = 30`. Pick better value with `binwidth`.



#now use the Bonferroni outlier test procedure with \$\alpha = .01\$

t\_crit = qt(1-.01/(2\*n),n-p-1)
print(round(t\_crit,3))

#### ## [1] 4.042

Conclusion: If our ti  $\leq$  t\_crit then we say no outliers. If our ti  $\geq$  t\_crit then we say there are outliers.

We can see that all of our abs(ti) <= 4.04 so we can conclude that there are no outliers.

#Obtain the diagonal elements of the hat matrix which weve already done

e. Obtain the diagonal elements of the hat matrix. Using the rule of thumb in the text, identify any outlying X observations.

### Student's Solution Below

```
print(round(hii,3))

## [1] 0.055 0.055 0.069 0.045 0.069 0.142 0.129 0.056 0.084 0.073 0.044

## [12] 0.037 0.051 0.032 0.048 0.055 0.031 0.026 0.213 0.055 0.055 0.133

## [23] 0.024 0.054 0.106 0.047 0.038 0.082 0.066 0.024 0.035 0.024 0.028

## [34] 0.043 0.039 0.035 0.031 0.030 0.040 0.033 0.023 0.037 0.051 0.093

## [45] 0.031 0.149 0.052 0.288 0.043 0.157 0.082 0.090 0.131 0.044 0.042

## [56] 0.288 0.067

#use rule of thumb to identify any outlying x observations

find_any_cases = which(hii> (2*p/n))

find_any_cases = find_any_cases+56

print(find_any_cases)

## [1] 62 75 102 104 106 112
```

#so we see that the following are cases that could have outlying observations as we can see in part f

f. Cases 62, 75, 106, and 112 are moderately outlying with respect to their X values, and case 87 is reasonably far outlying with respect to its Y value. Obtain DFFITS, DFBETAS, and Cook's distance values for these cases to assess their influence. What do you conclude?

```
#obtain DFFITS
dffits = dffits(lm)[c(62,75,87,106,112)]
print(dffits)
##
             62
                           75
                                                      106
                                                                    112
                 0.0008426962 -0.2337295766 0.9070194440 1.6461992492
## 0.3024343198
#obtain DFBETAS
df_{betas} = dfbetas(lm)[c(62,75,87,106,112),]
print(df_betas>2/sqrt(n))
##
       (Intercept)
                    age xray
                                adc age:xray age:adc xray:adc
## 62
            FALSE FALSE FALSE
                                       FALSE
                                               FALSE
                                                        FALSE
                                       FALSE
                                                        FALSE
## 75
            FALSE FALSE FALSE
                                               FALSE
## 87
            FALSE FALSE FALSE
                                       FALSE
                                               FALSE
                                                        FALSE
## 106
            FALSE TRUE TRUE FALSE
                                       FALSE
                                               FALSE
                                                        FALSE
## 112
            FALSE FALSE FALSE
                                       FALSE
                                                TRUE
                                                         TRUE
#cooks distance
cooks_dist = cooks_distance(lm)[c(62,75,87,106,112)]
```

```
f = pf(cooks_dist,p,n-p)
print(cooks_dist)

## 62 75 87 106 112
## 1.312777e-02 1.024143e-07 7.673756e-03 1.148007e-01 3.615651e-01
```

### (9.33) Case Study. Reference to Real estate sales Case Study 9.31.

The regression model identified in Case Study 9.31 is to be validated by means of the validation data set consisting of those cases not selected for the model building data set.

9.31. Residential sales that occurred during the year 2002 were available from a city in the Midwest. Data on 522 arms-length transactions include sales price, style, finished square feet, number of bedrooms, pool, lot size, year built, air conditioning, and whether or not the lot is adjacent to a highway. The city tax assessor was interested in predicting sales price based on the demographic variable information given above. Select a random sample of 300 observations to use in the model-building data set. Develop a best subset model for predicting sales price. Justify your choice of model. Assess your model's ability to predict and discuss its use as a tool for predicting sales price.

Data Set C.7. Real Estate Sales. Page 1353 The city tax assessor was interested in predicting residential home sales prices in a Midwestern city as a function of various characteristics of the home and surrounding property. Data on 522 arms-length transactions were obtained for home sales during the year 2002. Each line of the data set has an identification number and provides information on 12 other variables.

a. Fit the regression model identified in Case Study 9.31 to the validation data set. Compare the estimated regression coefficients and their estimated standard errors with those obtained in Case Study 9.31. Also compare the error mean square and coefficients of multiple determination. Does the model fitted to the validation data set yield similar estimates as the model fitted to the model-building data set?

### Solution Below

```
# Prep from 9.31

# Feature Engineering
age = 2002 - df_933$year
style1 = as.numeric(df_933$style == 7)
uniform = runif(nrow(df_933))
df_933_sorted = cbind(df_933, age, style1, uniform)
df_933_sorted = as.data.frame(df_933_sorted[order(uniform),])

# Partition Train and Test sets
trainSample = as.data.frame(df_933_sorted[1:300,])
valSample = as.data.frame(df_933_sorted[301:522,])

# To find the best model, basically fit the model and iteratively delete the insignificant variables

# Recall the factor variables: garage size, quality, style
summary(lm(log(salesPrice) ~ sqFt + nBeds + nBaths + ac + factor(garageSize) + pool + age + factor(qual)
```

```
##
## Call:
  lm(formula = log(salesPrice) ~ sqFt + nBeds + nBaths + ac + factor(garageSize) +
      pool + age + factor(quality) + style1 + lotSize + hwy, data = trainSample)
##
##
## Residuals:
                 10
                      Median
                                   30
                                           Max
## -0.52049 -0.10579 -0.00739 0.10699 0.52594
##
## Coefficients:
                        Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                       1.183e+01 1.135e-01 104.228 < 2e-16 ***
                       2.777e-04 2.870e-05
                                              9.676 < 2e-16 ***
## sqFt
## nBeds
                      -1.255e-02 1.256e-02 -0.999 0.31846
                       5.243e-02 1.696e-02
## nBaths
                                              3.091 0.00219 **
## ac
                       3.674e-02 3.167e-02
                                              1.160 0.24700
## factor(garageSize)1 4.109e-02 8.446e-02
                                              0.486 0.62703
## factor(garageSize)2 7.655e-02 8.123e-02
                                              0.942 0.34677
## factor(garageSize)3 2.182e-01 8.756e-02
                                              2.491 0.01329 *
## factor(garageSize)4 2.501e-02
                                  1.492e-01
                                              0.168 0.86696
                                             0.119 0.90521
## factor(garageSize)7 2.391e-02 2.006e-01
## pool
                       4.419e-02 3.809e-02
                                             1.160 0.24689
                      -3.667e-03 7.812e-04 -4.694 4.17e-06 ***
## age
## factor(quality)2
                      -2.199e-01 3.959e-02 -5.554 6.43e-08 ***
## factor(quality)3
                      -3.312e-01 5.568e-02 -5.949 7.94e-09 ***
## style1
                      -6.240e-02 3.197e-02 -1.952 0.05189 .
## lotSize
                       5.243e-06 8.724e-07
                                              6.010 5.71e-09 ***
## hwy
                      -1.420e-01 6.245e-02 -2.274 0.02372 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.1708 on 283 degrees of freedom
## Multiple R-squared: 0.8639, Adjusted R-squared: 0.8563
## F-statistic: 112.3 on 16 and 283 DF, p-value: < 2.2e-16
summary(lm(log(salesPrice) ~ sqFt + nBaths + ac + factor(garageSize) + pool + age + factor(quality) + s
##
## Call:
## lm(formula = log(salesPrice) ~ sqFt + nBaths + ac + factor(garageSize) +
##
      pool + age + factor(quality) + style1 + lotSize + hwy, data = trainSample)
##
## Residuals:
##
       Min
                 1Q
                      Median
                                   30
## -0.54910 -0.10282 -0.00634 0.10769 0.50579
##
## Coefficients:
                        Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                       1.183e+01 1.134e-01 104.397 < 2e-16 ***
                       2.695e-04 2.750e-05
                                              9.800 < 2e-16 ***
## sqFt
## nBaths
                       4.772e-02 1.630e-02
                                              2.929 0.00368 **
                       3.417e-02 3.157e-02
                                              1.082 0.27997
## ac
## factor(garageSize)1 3.073e-02 8.382e-02
                                              0.367
                                                     0.71418
## factor(garageSize)2
                       6.795e-02 8.077e-02
                                              0.841 0.40090
## factor(garageSize)3 2.107e-01 8.724e-02
                                             2.415 0.01635 *
```

```
## factor(garageSize)4 2.007e-02 1.491e-01 0.135 0.89302
## factor(garageSize)7 3.310e-02 2.004e-01 0.165 0.86892
## pool
                       4.446e-02 3.809e-02
                                            1.167 0.24404
## age
                      -3.673e-03 7.812e-04 -4.702 4.03e-06 ***
## factor(quality)2
                      -2.268e-01 3.899e-02 -5.817 1.62e-08 ***
## factor(quality)3
                      -3.397e-01 5.503e-02 -6.172 2.31e-09 ***
## style1
                      -6.109e-02 3.194e-02 -1.913 0.05680 .
## lotSize
                       5.200e-06 8.714e-07
                                            5.967 7.17e-09 ***
## hwy
                      -1.444e-01 6.240e-02 -2.314 0.02139 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.1708 on 284 degrees of freedom
## Multiple R-squared: 0.8635, Adjusted R-squared: 0.8563
## F-statistic: 119.7 on 15 and 284 DF, p-value: < 2.2e-16
summary(lm(log(salesPrice) ~ sqFt + nBaths + ac + pool + age + factor(quality) + style1 + lotSize+ hwy,
##
## Call:
## lm(formula = log(salesPrice) ~ sqFt + nBaths + ac + pool + age +
##
      factor(quality) + style1 + lotSize + hwy, data = trainSample)
##
## Residuals:
       Min
                     Median
                 1Q
                                   30
                                           Max
## -0.56512 -0.10969 -0.01351 0.11222 0.50999
##
## Coefficients:
##
                    Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                    1.197e+01 8.971e-02 133.448 < 2e-16 ***
## sqFt
                    2.794e-04 2.752e-05 10.151 < 2e-16 ***
## nBaths
                    4.339e-02 1.663e-02
                                         2.610 0.00953 **
## ac
                    4.276e-02 3.196e-02
                                         1.338 0.18194
                    3.932e-02 3.923e-02
                                          1.002 0.31702
## pool
                   -4.367e-03 7.863e-04 -5.554 6.33e-08 ***
## age
## factor(quality)2 -2.829e-01 3.804e-02 -7.437 1.18e-12 ***
## factor(quality)3 -4.105e-01 5.471e-02 -7.503 7.76e-13 ***
## style1
                   -4.556e-02 3.243e-02 -1.405 0.16119
                                         6.386 6.78e-10 ***
## lotSize
                   5.645e-06 8.840e-07
## hwy
                   -1.506e-01 6.423e-02 -2.345 0.01969 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.1766 on 289 degrees of freedom
## Multiple R-squared: 0.8515, Adjusted R-squared: 0.8463
## F-statistic: 165.7 on 10 and 289 DF, p-value: < 2.2e-16
summary(lm(log(salesPrice) ~ sqFt + nBaths + ac + age + factor(quality) + style1 + lotSize+ hwy, data=t.
##
## Call:
## lm(formula = log(salesPrice) ~ sqFt + nBaths + ac + age + factor(quality) +
      style1 + lotSize + hwy, data = trainSample)
## Residuals:
```

```
Median
                 1Q
                                   3Q
## -0.52934 -0.11514 -0.01392 0.11084 0.50866
## Coefficients:
##
                     Estimate Std. Error t value Pr(>|t|)
                    1.197e+01 8.971e-02 133.450 < 2e-16 ***
## (Intercept)
                    2.787e-04 2.751e-05 10.130 < 2e-16 ***
## sqFt
                    4.555e-02 1.649e-02
## nBaths
                                          2.763 0.00609 **
## ac
                    4.374e-02 3.194e-02
                                           1.369 0.17196
## age
                   -4.333e-03 7.856e-04 -5.516 7.68e-08 ***
## factor(quality)2 -2.846e-01 3.800e-02 -7.489 8.38e-13 ***
## factor(quality)3 -4.128e-01 5.466e-02
                                         -7.552 5.61e-13 ***
                   -4.679e-02 3.241e-02 -1.444 0.14988
## style1
## lotSize
                    5.586e-06 8.821e-07
                                          6.333 9.12e-10 ***
                   -1.528e-01 6.420e-02 -2.380 0.01795 *
## hwy
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.1766 on 290 degrees of freedom
## Multiple R-squared: 0.851, Adjusted R-squared: 0.8463
## F-statistic:
                 184 on 9 and 290 DF, p-value: < 2.2e-16
trainModel = lm(log(salesPrice) ~ sqFt + nBaths + ac + age + factor(quality) + style1 + lotSize+ hwy, d
# Preliminary Analysis
#summary(df_933)
\#lapply(df_933, mode)
#lapply(df_933, class)
testModel = lm(log(salesPrice) ~ sqFt + nBaths + ac + age + factor(quality) + style1 + lotSize+ hwy, da
summary(trainModel)
##
## Call:
## lm(formula = log(salesPrice) ~ sqFt + nBaths + ac + age + factor(quality) +
##
       style1 + lotSize + hwy, data = trainSample)
##
## Residuals:
##
       Min
                      Median
                 1Q
                                   3Q
## -0.52934 -0.11514 -0.01392 0.11084 0.50866
##
## Coefficients:
##
                     Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                    1.197e+01 8.971e-02 133.450 < 2e-16 ***
## sqFt
                    2.787e-04 2.751e-05 10.130 < 2e-16 ***
## nBaths
                    4.555e-02 1.649e-02
                                          2.763 0.00609 **
## ac
                    4.374e-02 3.194e-02
                                          1.369 0.17196
                   -4.333e-03 7.856e-04 -5.516 7.68e-08 ***
## factor(quality)2 -2.846e-01 3.800e-02 -7.489 8.38e-13 ***
## factor(quality)3 -4.128e-01 5.466e-02 -7.552 5.61e-13 ***
## style1
                   -4.679e-02 3.241e-02 -1.444 0.14988
## lotSize
                    5.586e-06 8.821e-07
                                          6.333 9.12e-10 ***
## hwy
                   -1.528e-01 6.420e-02 -2.380 0.01795 *
```

```
## ---
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
## Residual standard error: 0.1766 on 290 degrees of freedom
## Multiple R-squared: 0.851, Adjusted R-squared: 0.8463
## F-statistic:
                   184 on 9 and 290 DF, p-value: < 2.2e-16
summary(valSample)
##
                       salesPrice
                                             sqFt
                                                            nBeds
           id
##
    Min.
            :
              2.0
                     Min.
                             : 84000
                                        Min.
                                               : 980
                                                        Min.
                                                                :0.000
##
    1st Qu.:154.2
                     1st Qu.:183480
                                        1st Qu.:1694
                                                        1st Qu.:3.000
    Median :266.5
                     Median :231500
                                        Median:2092
                                                        Median :3.000
            :260.5
##
    Mean
                     Mean
                             :269237
                                        Mean
                                               :2243
                                                                :3.509
                                                        Mean
    3rd Qu.:380.5
                                        3rd Qu.:2602
##
                     3rd Qu.:314625
                                                        3rd Qu.:4.000
##
                             :920000
    Max.
            :522.0
                     Max.
                                        Max.
                                               :4973
                                                        Max.
                                                                :6.000
##
        nBaths
                            ac
                                          garageSize
                                                              pool
##
            :0.000
                             :0.0000
                                               :0.000
                                                                 :0.0000
    Min.
                     Min.
                                        Min.
                                                         Min.
##
    1st Qu.:2.000
                     1st Qu.:1.0000
                                        1st Qu.:2.000
                                                         1st Qu.:0.00000
##
                                        Median :2.000
                                                         Median :0.00000
    Median :3.000
                     Median :1.0000
##
    Mean
            :2.662
                             :0.8604
                                               :2.081
                                                                 :0.05856
                     Mean
                                        Mean
                                                         Mean
##
    3rd Qu.:3.000
                     3rd Qu.:1.0000
                                        3rd Qu.:2.000
                                                         3rd Qu.:0.00000
            :7.000
##
    Max.
                     Max.
                             :1.0000
                                        Max.
                                               :5.000
                                                         Max.
                                                                 :1.00000
##
         year
                       quality
                                          style
                                                          lotSize
##
                                                              : 6746
    Min.
            :1885
                    Min.
                            :1.000
                                     Min.
                                             :1.000
                                                       Min.
##
    1st Qu.:1957
                    1st Qu.:2.000
                                      1st Qu.:1.000
                                                       1st Qu.:18188
    Median:1966
                    Median :2.000
                                     Median :3.000
                                                       Median :22079
##
##
    Mean
            :1967
                    Mean
                            :2.212
                                     Mean
                                             :3.523
                                                       Mean
                                                               :24027
    3rd Qu.:1980
                                      3rd Qu.:7.000
                                                       3rd Qu.:26692
##
                    3rd Qu.:3.000
##
    Max.
            :1997
                            :3.000
                                     Max.
                                                       Max.
                                                               :86248
                    Max.
                                             :7.000
##
                                             style1
                                                              uniform
         hwy
                             age
            :0.00000
                       Min.
                                  5.0
                                                :0.0000
                                                                   :0.6009
    Min.
                                         Min.
                                                           Min.
    1st Qu.:0.00000
                       1st Qu.: 22.0
                                         1st Qu.:0.0000
                                                           1st Qu.:0.6986
    Median :0.00000
                       Median: 36.0
                                         Median : 0.0000
                                                           Median: 0.8021
##
##
    Mean
            :0.01351
                       Mean
                               : 34.7
                                                :0.3018
                                                                   :0.7996
                                         Mean
                                                           Mean
    3rd Qu.:0.00000
                       3rd Qu.: 45.0
                                         3rd Qu.:1.0000
                                                           3rd Qu.:0.8944
            :1.00000
                               :117.0
                                                 :1.0000
                                                                   :0.9983
    Max.
                       Max.
                                         Max.
                                                           Max.
```

# **ANALYSIS**

 $R^2$  value for the training model was slightly higher and we see that the  $R^2$  value for the validation model dropped. We can further analyze the variables in the model summaries. Comparing the variables, we see some notable differences. Specifically: number of baths, AC, style1 (our dummy variable), highway.

b. Calculate the mean squared prediction error (9.20) and compare it to MSE obtained from the model-building data set. Is there evidence of a substantial bias problem in MSE here?

#### Solution Below

anova(trainModel)

```
## Analysis of Variance Table

##
## Response: log(salesPrice)

## Df Sum Sq Mean Sq F value Pr(>F)

## sqFt 1 43.391 43.391 1391.6554 < 2.2e-16 ***
```

```
## nBaths
                     1 1.973
                                1.973
                                        63.2801 4.052e-14 ***
## ac
                       0.526
                                0.526
                                        16.8628 5.231e-05 ***
                                        53.7339 2.297e-12 ***
## age
                       1.675
                                1.675
                     2 2.507
## factor(quality)
                                1.254
                                        40.2106 3.862e-16 ***
## style1
                       0.202
                                0.202
                                         6.4696
                                                  0.01149 *
## lotSize
                                        37.5772 2.864e-09 ***
                     1
                       1.172
                                1.172
## hwy
                       0.177
                                0.177
                                         5.6658
                                                  0.01795 *
                     1
## Residuals
                   290 9.042
                                0.031
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
(MSE = anova(trainModel)[9,3])
## [1] 0.03117945
# See MSE is ~0.033
MSE = paste0(signif(MSE, digits=4))
predsTest = predict(trainModel, valSample)
(MSPR = sum((log(valSample$salesPrice) - predsTest)^2)/(nrow(valSample)))
## [1] 0.03193739
MSPR = paste0(signif(MSPR, digits=4))
```

### **ANALYSIS**

The MSE obtainined from the model-building set is 0.03118 and the mean squared prediction error is 0.03194. We see that the two values are fairly similar, with variations between the two being small. There is no evidence of a substantial bias problem in the MSE.