

$$\begin{aligned}
I1(p) &\triangleq && [\text{Associated variable: } \textit{outcome}[p]] \\
&&& (\textit{outcome}[p] \neq \text{BLANK}) \Rightarrow \exists B \in \mathcal{B} : (B.qrm \subseteq B.vot) \wedge (B.dec = \textit{outcome}[p])
\end{aligned}$$

$$\begin{aligned}
I2(p) &\triangleq && [\text{Associated variable: } \textit{lastTried}[p]] \\
&&& \wedge \textit{owner}(\textit{lastTried}[p]) = p \\
&&& \wedge \forall B \in \mathcal{B} : (\textit{owner}(B.bal) = p) \Rightarrow \\
&&& \quad \wedge B.bal \leq \textit{lastTried}[p] \\
&&& \quad \wedge (\textit{status}[p] = \textit{trying}) \Rightarrow (B.bal < \textit{lastTried}[p])
\end{aligned}$$

$$\begin{aligned}
I3(p) &\triangleq && [\text{Associated variables: } \textit{prevBal}[p], \textit{prevDec}[p], \textit{nextBal}[p]] \\
&&& \wedge \textit{prevBal}[p] = \textit{MaxVote}(\infty, p, \mathcal{B}).bal \\
&&& \wedge \textit{prevDec}[p] = \textit{MaxVote}(\infty, p, \mathcal{B}).dec \\
&&& \wedge \textit{nextBal}[p] \geq \textit{prevBal}[p]
\end{aligned}$$

$$\begin{aligned}
I4(p) &\triangleq && [\text{Associated variable: } \textit{prevVotes}[p]] \\
&&& (\textit{status}[p] \neq \textit{idle}) \Rightarrow \\
&&& \quad \forall v \in \textit{prevVotes}[p] : \wedge v = \textit{MaxVote}(\textit{lastTried}[p], v.pst, B) \\
&&& \quad \wedge \textit{nextBal}[v.pst] \geq \textit{lastTried}[p]
\end{aligned}$$

$$\begin{aligned}
I5(p) &\triangleq && [\text{Associated variables: } \textit{quorum}[p], \textit{voters}[p], \textit{decree}[p]] \\
&&& (\textit{status}[p] = \textit{polling}) \Rightarrow \\
&&& \wedge \textit{quorum}[p] \subseteq \{v.pst : v \in \textit{prevVotes}[p]\} \\
&&& \wedge \exists B \in \mathcal{B} : \wedge \textit{quorum}[p] = B.qrm \\
&&& \quad \wedge \textit{decree}[p] = B.dec \\
&&& \quad \wedge \textit{voters}[p] \subseteq B.vot \\
&&& \quad \wedge \textit{lastTried}[p] = B.bal
\end{aligned}$$

$$\begin{aligned}
I6 &\triangleq && [\text{Associated variable: } \mathcal{B}] \\
&&& \wedge B1(\mathcal{B}) \wedge B2(\mathcal{B}) \wedge B3(\mathcal{B}) \\
&&& \wedge \forall B \in \mathcal{B} : B.qrm \text{ is a majority set}
\end{aligned}$$

$$\begin{aligned}
I7 &\triangleq && [\text{Associated variable: } \mathcal{M}] \\
&&& \wedge \forall \textit{NextBallot}(b) \in \mathcal{M} : (b \leq \textit{lastTried}[\textit{owner}(b)]) \\
&&& \wedge \forall \textit{LastVote}(b, v) \in \mathcal{M} : \wedge v = \textit{MaxVote}(b, v.pst, \mathcal{B}) \\
&&& \quad \wedge \textit{nextBal}[v.pst] \geq b \\
&&& \wedge \forall \textit{BeginBallot}(b, d) \in : \exists B \in \mathcal{B} : (B.bal = b) \wedge (B.dec = d) \\
&&& \wedge \forall \textit{Voted}(b, p) \in \mathcal{M} : \exists B \in \mathcal{B} : (B.bal = b) \wedge (p \in B.vot) \\
&&& \wedge \forall \textit{Success}(d) \in \mathcal{M} : \exists p : \textit{outcome}[p] = d \neq \text{BLANK}
\end{aligned}$$