

1 New Figure 2

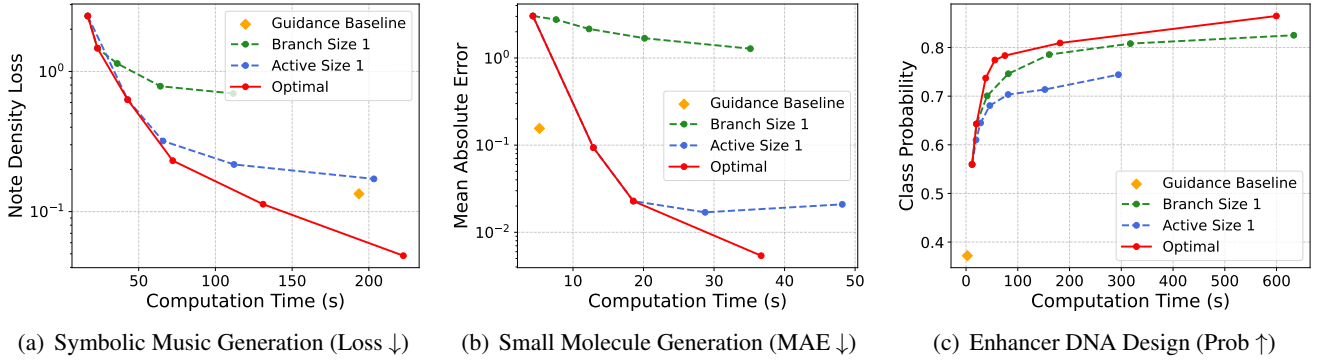


Figure 1: **SPS outperforms the guidance baseline, with the optimization effect of the objective function following a scaling behavior with inference time.** We evaluate SPS with varying active set and branch-out sizes. “**Optimal**” refers to the combination of active set and branch-out sizes that achieve the best performance within the same inference time. The optimal line shows that SPS outperforms the guidance baseline and the scaling behavior of inference time.

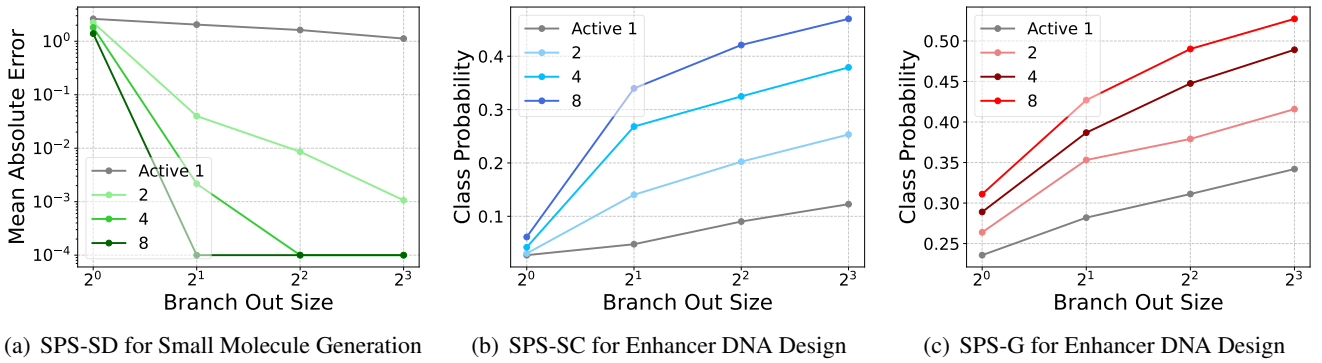


Figure 2: **Scaling Behavior with Fixed Active or Branch-Out Size:** Increasing either the active size or the branch-out size enhances performance. (a): The MAEs are capped at 10^{-4} ; (b) & (c): The results are for Class 3 in DNA enhancer design with strength 20 for SPS-G.

2 New Figure 3

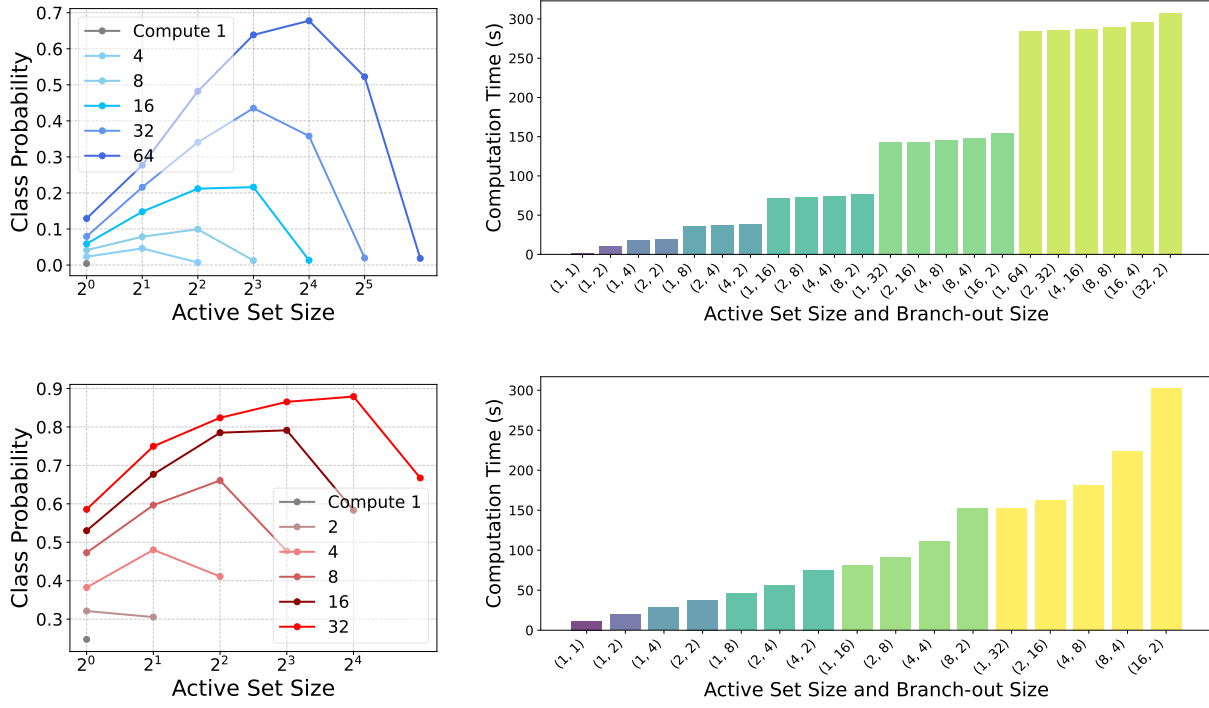


Figure 3: **Trade-Off between Active Set Size A and Branch-Out Size K with Fixed Computation:** SPS-SC (Top) and SPS-G (Bottom) vary (A, K) with fixed total compute $A * K$ for DNA enhancer design. Performance peaks when A and K are in the moderate range. Fixed $A * K$ can be viewed as a fixed computation budget where the actual inference time is shown on the right. The results are for Class 1 and $\gamma = 20$ for SPS-G.