

Homework9

General Edge Detection

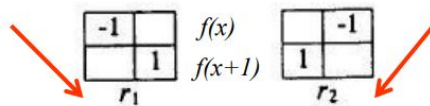
Description

You are to implement following edge detectors with thresholds :

To implement each operator, we follow the method introduced in the lecture slide.

(a) Robert's Operator

$$f'(x) \approx f(x+1) - f(x)$$



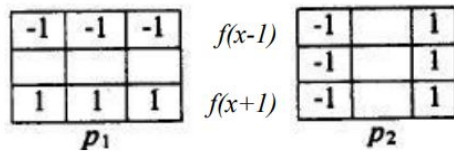
$$\text{gradient magnitude: } \sqrt{r_1^2 + r_2^2}$$

```
int r1 = ori.at<uchar>(i + 1, j + 1) - ori.at<uchar>(i, j);
int r2 = ori.at<uchar>(i + 1, j) - ori.at<uchar>(i, j + 1);
int gradient = sqrt(r1 * r1 + r2 * r2);
if (gradient >= threshold) {
    output.at<uchar>(i, j) = 0;
}
else {
    output.at<uchar>(i, j) = 255;
}
```

(For more information, please refer to lines 14~28.)

(b) Prewitt's Edge Detector

$$f'(x) \approx f(x+1) - f(x-1)$$



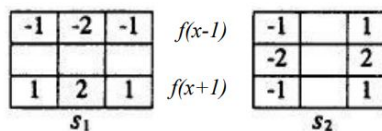
$$\text{gradient magnitude: } \sqrt{p_1^2 + p_2^2}$$

```
int p1 = (array[0][0] + array[0][1] + array[0][2]) * -1 + array[2][0] + array[2][1] + array[2][2];
int p2 = (array[0][0] + array[1][0] + array[2][0]) * -1 + array[0][2] + array[1][2] + array[2][2];
int gradient = sqrt(p1 * p1 + p2 * p2);
if (gradient >= threshold) {
    output.at<uchar>(i, j) = 0;
}
else {
    output.at<uchar>(i, j) = 255;
}
```

(For more information, please refer to lines 30~97.)

(c) Sobel's Edge Detector

$$f'(x) \approx f(x+1) - f(x-1)$$



$$\text{gradient magnitude: } \sqrt{s_1^2 + s_2^2}$$

```
int s1 = - array[0][0] - (array[0][1]*2) - array[0][2] + array[2][0] + (array[2][1]*2) + array[2][2];
int s2 = - array[0][0] - (array[1][0]*2) - array[2][0] + array[0][2] + (array[1][2]*2) + array[2][2];
int gradient = sqrt(s1 * s1 + s2 * s2);
if (gradient >= threshold) {
    output.at<uchar>(i, j) = 0;
}
else {
    output.at<uchar>(i, j) = 255;
}
```

(For more information, please refer to lines 99~166.)

(d) Frei and Chen's Gradient Operator

$$f(x-1) \begin{bmatrix} -1 & -\sqrt{2} & -1 \\ & & \\ & & \end{bmatrix} \quad \begin{bmatrix} -1 & & 1 \\ -\sqrt{2} & & \sqrt{2} \\ -1 & & 1 \end{bmatrix}$$

$$f(x+1) \begin{bmatrix} 1 & \sqrt{2} & 1 \\ & & \\ & & \end{bmatrix} \quad \begin{bmatrix} 1 & & -1 \\ \sqrt{2} & & -\sqrt{2} \\ 1 & & 1 \end{bmatrix}$$

$$f_1 \quad f_2$$

gradient magnitude: $\sqrt{f_1^2 + f_2^2}$ $f'(x) \approx f(x+1) - f(x-1)$

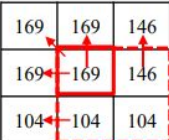
```
int f1 = -array[0][0] - (array[0][1] * sqrt(2)) - array[0][2] + array[2][0] + (array[2][1] * sqrt(2)) + array[2][2];
int f2 = -array[0][0] - (array[1][0] * sqrt(2)) - array[2][0] + array[0][2] + (array[1][2] * sqrt(2)) + array[2][2];
int gradient = sqrt(f1 * f1 + f2 * f2);
if (gradient >= threshold) {
    output.at<uchar>(i, j) = 0;
}
else {
    output.at<uchar>(i, j) = 255;
}
```

(For more information, please refer to lines 168~235.)

(e) Kirsch's Compass Operator

$$\begin{matrix} \begin{bmatrix} -3 & -3 & 5 \\ -3 & & 5 \\ -3 & -3 & 5 \end{bmatrix} & \begin{bmatrix} -3 & 5 & 5 \\ -3 & & 5 \\ -3 & -3 & -3 \end{bmatrix} & \begin{bmatrix} 5 & 5 & 5 \\ -3 & & -3 \\ -3 & -3 & -3 \end{bmatrix} & \begin{bmatrix} 5 & 5 & -3 \\ 5 & & -3 \\ -3 & -3 & -3 \end{bmatrix} \\ k_0 & k_1 & k_2 & k_3 \\ \begin{bmatrix} 5 & -3 & -3 \\ 5 & & -3 \\ 5 & -3 & -3 \end{bmatrix} & \begin{bmatrix} -3 & -3 & -3 \\ 5 & & -3 \\ 5 & 5 & -3 \end{bmatrix} & \begin{bmatrix} -3 & -3 & -3 \\ -3 & & -3 \\ 5 & 5 & 5 \end{bmatrix} & \begin{bmatrix} -3 & -3 & -3 \\ -3 & & 5 \\ -3 & 5 & 5 \end{bmatrix} \\ k_4 & k_5 & k_6 & k_7 \end{matrix}$$

gradient magnitude: $\max_{n,n=0,\dots,7} k_n$



```
int k[8];
//array[i][j]
k[0] = (-3) * (array[0][0] + array[0][1] + array[1][0] + array[2][0] + array[2][1]) + (5) * (array[0][2] + array[1][2] + array[2][2]);
k[1] = (-3) * (array[0][0] + array[1][0] + array[2][0] + array[2][1] + array[2][2]) + (5) * (array[0][1] + array[0][2] + array[1][2]);
k[2] = (-3) * (array[1][0] + array[1][2] + array[2][0] + array[2][1] + array[2][2]) + (5) * (array[0][0] + array[0][1] + array[0][2]);
k[3] = (-3) * (array[2][0] + array[2][1] + array[2][2] + array[1][2] + array[0][2]) + (5) * (array[0][0] + array[0][1] + array[1][0]);
k[4] = (-3) * (array[0][1] + array[0][2] + array[2][1] + array[2][2] + array[1][2]) + (5) * (array[0][0] + array[1][0] + array[2][0]);
k[5] = (-3) * (array[0][0] + array[0][1] + array[0][2] + array[1][2] + array[2][2]) + (5) * (array[1][0] + array[2][0] + array[2][1]);
k[6] = (-3) * (array[0][0] + array[0][1] + array[0][2] + array[1][0] + array[1][2]) + (5) * (array[2][0] + array[2][1] + array[2][2]);
k[7] = (-3) * (array[0][0] + array[0][1] + array[0][2] + array[1][0] + array[2][0]) + (5) * (array[2][1] + array[2][2] + array[1][2]);

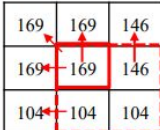
int gradient = -1;
for (int a = 0; a < 8; a++) {
    if (k[a] > gradient) {
        gradient = k[a];
    }
}
if (gradient >= threshold) {
    output.at<uchar>(i, j) = 0;
}
else {
    output.at<uchar>(i, j) = 255;
}
```

(For source code, please refer to lines 237~319.)

(f) Robinson's Compass Operator

$$\begin{matrix} \begin{bmatrix} -1 & & 1 \\ -2 & & 2 \\ -1 & & 1 \end{bmatrix} & \begin{bmatrix} 1 & 2 \\ -1 & 1 \end{bmatrix} & \begin{bmatrix} 1 & 2 & 1 \\ & & \\ & & \end{bmatrix} & \begin{bmatrix} 2 & 1 \\ 1 & -1 \\ -1 & -2 \end{bmatrix} \\ r_0 & r_1 & r_2 & r_3 \\ \begin{bmatrix} 1 & & -1 \\ 2 & & -2 \\ 1 & & -1 \end{bmatrix} & \begin{bmatrix} -1 & -2 \\ 1 & -1 \end{bmatrix} & \begin{bmatrix} -1 & -2 & -1 \\ & & \\ & & \end{bmatrix} & \begin{bmatrix} -2 & -1 \\ -1 & 1 \\ 1 & 2 \end{bmatrix} \\ r_4 & r_5 & r_6 & r_7 \end{matrix}$$

gradient magnitude: $\max_{n,n=0,\dots,7} r_n$



(For source code, please refer to lines 321~402.)

(g) Nevatia-Babu 5x5 Operator

100	100	100	100	100
100	100	100	100	100
0	0	0	0	0
-100	-100	-100	-100	-100
-100	-100	-100	-100	-100

0°

100	100	100	100	100
100	100	100	78	-32
100	92	0	-92	-100
32	-78	-100	-100	-100
-100	-100	-100	-100	-100

30°

100	100	100	32	-100
100	100	92	-78	-100
100	100	0	-100	-100
100	78	-92	-100	-100
100	-32	-100	-100	-100

60°

-100	-100	0	100	100
-100	-100	0	100	100
-100	-100	0	100	100
-100	-100	0	100	100
-100	-100	0	100	100

-90°

-100	32	100	100	100
-100	-78	92	100	100
-100	-100	0	100	100
-100	-100	-92	78	100
-100	-100	-100	-32	100

-60°

100	100	100	100	100
-32	78	100	100	100
-100	-92	0	92	100
-100	-100	-100	-78	32
-100	-100	-100	-100	-100

-30°

gradient magnitude: $\max_{n,n=0,\dots,5} N_n$

(For source code, please refer to lines 404~491.)

Result

(a) Robert's Operator: 12



(b) Prewitt's Edge Detector: 24



(c) Sobel's Edge Detector: 38



(d) Frei and Chen's Gradient Operator: 30



(e) Kirsch's Compass Operator: 135



(f) Robinson's Compass Operator: 43



(g) Nevatia-Babu 5x5 Operator: 12500



Reference:

1. lecture slide