

## 2\_Entropy Production Due to Heat Flow\_Irreversible Thermodynamics

Link: [https://www.youtube.com/watch?v=yFNj6kbILDE&list=PLdBDmcnzLC\\_ZMUWMdy7SmcTgnnzyiRpql&index=3](https://www.youtube.com/watch?v=yFNj6kbILDE&list=PLdBDmcnzLC_ZMUWMdy7SmcTgnnzyiRpql&index=3)

For any natural spontaneous process, Entropy is always increased.  $\rightarrow$  we say here that the entropy is produced.

Entropy ( $S$ ) is an extensive property.



Bulk Material  $dS$

$$dS = dS_1 + dS_2 + \dots$$

$$dS \begin{cases} deS : (\text{Entropy flow due to the interaction with the exterior/environment}) \\ diS : (\text{Entropy contribution due to the change in the inside of the system}) \end{cases}$$

$$dS = diS + deS$$

$diS = 0$  for a reversible Process

$diS > 0$  for an irreversible Process

(never be negative)

$\downarrow$   
This is our entropy produced

Consider the following system:

Consider a closed system

Material System :  $\left\{ \begin{array}{l} \text{Phase I} \rightarrow \text{Temperature } T^I \\ \text{Phase II} \rightarrow \text{Temperature } T^{II} \end{array} \right.$

They react with each other.

$$dS = \frac{dq}{T}$$

$$dS = dS^I + dS^{II}$$

$$d^I q = d_e^I q + d_i^I q$$

(Since the reaction between Phase I & II could be either exothermic or endothermic)

$$d^{II} q = d_e^{II} q + d_i^{II} q$$

$$d^I S = \frac{d^I q}{T^I} = \frac{d_e^I q}{T^I} + \frac{d_i^I q}{T^I}$$

$$d^{II} S = \frac{d^{II} q}{T^{II}} = \frac{d_e^{II} q}{T^{II}} + \frac{d_i^{II} q}{T^{II}}$$

$$(d_i^I q = -d_i^{II} q)$$

Thus,

$$dS = \underbrace{\frac{d_e^I q}{T^I} + \frac{d_e^{II} q}{T^{II}}}_{d_e S} + \underbrace{d_i^I q \left( \frac{1}{T^I} - \frac{1}{T^{II}} \right)}_{d_i S \rightarrow \text{Entropy Production}}$$

$$d_i S = d_i^I q \left( \frac{1}{T^I} - \frac{1}{T^{II}} \right)$$

Arising due to the transfer of heat from Phase I to Phase II

If  $T^{II} > T^I$ , in this case  $d_i^I q > 0$ ,  $\Rightarrow d_i S > 0$

If  $T^I > T^{II}$ , in this case  $d_i^I q < 0$ ,  $\Rightarrow d_i S > 0$

$d_i S$  will be equal to 0, only when the system is under thermal equilibrium. ( $T^I = T^{II}$ )

✓ This expression can be written in the form of  $\sigma$ . (Entropy Production per unit time)

written as  $\sigma_v$  ↑ Entropy production

$$\sigma = \frac{d_i S}{dt} = \frac{d_i^I q}{dt} \left( \frac{1}{T^I} - \frac{1}{T^{II}} \right)$$

First term: rate of heat transfer  
2nd term: Difference of the state function.  
(of our temperature)  
per unit Volume per unit time.

$\frac{d_i^I q}{dt}$ : Could be considered as the microscopic force or the driving force for the heat transfer

$$J = L X \rightarrow \text{driving force}$$

↓  
Flux of the thermodynamic quantity