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In [4]: # Import libraries
         import os
         import sys
         import numpy as np
         import pandas as pd
         import matplotlib.pyplot as plt
         import seaborn as sns
         import plotly.graph_objects as go
         import plotly.express as px
         import warnings
         from scipy.integrate import odeint
         from IPython.display import Image
         from statistics import mode
         from scipy.stats import pearsonr, spearmanr
         from sklearn.feature_selection import mutual_info_regression
         import statsmodels.api as sm
         import pingouin as pg
         from sklearn.neural_network import MLPRegressor
         from sklearn.metrics import mean_squared_error
         # Suppress warnings
         warnings.filterwarnings('ignore')
         # Set number of decimals for np print options
         np.set_printoptions(precision=3)
         # Set the current working directory
         os.chdir(sys.path[0])
 In [3]: df = pd.read_csv('fish_river.csv')
         print(df.shape)
         df
        (2192, 4)
 Out[3]:
                 datetime year
                                 rainfall runoff
            0 2016-01-01 2016 0.000675 1720.0
            1 2016-01-02 2016 0.144395 1680.0
            2 2016-01-03 2016 2.918217 1640.0
            3 2016-01-04 2016 0.000000 1580.0
            4 2016-01-05 2016 0.000000 1520.0
          2187 2021-12-27 2021 0.000000 989.0
          2188 2021-12-28 2021 3.711825 972.0
         2189 2021-12-29 2021 0.018728 947.0
          2190 2021-12-30 2021 0.000000 928.0
          2191 2021-12-31 2021 0.030013 902.0
         2192 rows × 4 columns
In [14]: df['datetime'] = pd.to_datetime(df['datetime'])
         df['month'] = df['datetime'].dt.month
         df['runoff_shifted'] = df['runoff'].shift(2)
         from sklearn.model_selection import train_test_split
         from sklearn.metrics import mean_squared_error, r2_score
         # Drop rows with missing runoff values after the shift
         df.dropna(subset=['runoff_shifted'], inplace=True)
         # Extract rainfall as the input (X) and runoff_shifted as the target (y)
         X = df[['rainfall', 'runoff_shifted']]
         y = df['runoff']
         # get the training data and testing data
         train_data = df[(df['month'] >= 9) | (df['month'] <= 3)]</pre>
         test_data = df[(df['month'] >= 4) & (df['month'] <= 8)]</pre>
         # split the data into training and testing
         X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.3, random_state=42)
         # Initialize the MLPRegressor model with one hidden layer of 10 nodes
         mlp = MLPRegressor(hidden_layer_sizes=(10,), max_iter=1000, random_state=42)
         # Train the model
         mlp.fit(X_train, y_train)
         # Make predictions on the test set
         y_pred = mlp.predict(X_test)
         # Compute the RMSE
         rmse = np.sqrt(mean_squared_error(y_test, y_pred))
         print(f"Test RMSE: {rmse}")
        Test RMSE: 430.5003056633389
In [32]: # Prepare yearly average streamflow
         yearly_avg_streamflow = df.groupby('year')['runoff'].mean()
         # Initialize dictionary to store RMSE for each year
         yearly_rmse = {}
         # Loop through each year, train on the other years, and test on the current year
         for year in range(2016, 2022):
             # Split into train and test (current year)
             train_data = df[df['year'] == year]
             test_data = df[df['year'] != year]
             X_train_custom = train_data[['rainfall', 'runoff_shifted']]
             y_train_custom = train_data['runoff']
             X_test_custom = test_data[['rainfall', 'runoff_shifted']]
             y_test_custom = test_data['runoff']
             # Train the LinearRegression model
             model_custom = LinearRegression()
             model_custom.fit(X_train_custom, y_train_custom)
             # Predict on the test data and calculate RMSE
             y_pred_custom = model_custom.predict(X_test_custom)
             rmse_custom = np.sqrt(mean_squared_error(y_test_custom, y_pred_custom))
             # Store the RMSE for the current year
             yearly_rmse[year] = rmse_custom
         X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.3, random_state=42)
         # Train the model on train_test_split
         #model_split = LinearRegression()
         #model_split.fit(X_train, y_train)
         #y_pred_split = model_split.predict(X_test)
         #rmse_split = np.sqrt(mean_squared_error(y_test, y_pred_split))
         #print("Train-Test Split RMSE:", rmse_split)
         years = sorted(yearly rmse.keys())
         rmse_values = [yearly_rmse[year] for year in years]
         avg_streamflow_values = [yearly_avg_streamflow[year] for year in years]
         plt.figure(figsize=(10, 6))
         plt.scatter(avg_streamflow_values, rmse_values, color='blue', label='RMSE per Year')
         # Add labels and title
         plt.xlabel('Yearly Average Daily Streamflow')
         plt.ylabel('RMSE')
         plt.title('RMSE vs. Yearly Average Daily Streamflow')
         # Optional: Add grid and legend
         plt.grid(True)
         plt.legend()
         # Show the plot
         plt.show()
                                          RMSE vs. Yearly Average Daily Streamflow
```

