

#Part 1: Data Preprocessing & Cleaning

1.1 Setting up environment

```
from google.colab import drive
drive.mount('/content/drive')

Mounted at /content/drive

# =====
# 0. ENVIRONMENT SETUP & LIBRARY IMPORTS
# =====

# --- Core Data Handling ---
import pandas as pd
import numpy as np

# --- Statistical Analysis ---
from scipy import stats
from scipy.stats import ttest_ind, f_oneway, pearsonr, levene, shapiro
import statsmodels.api as sm
import statsmodels.formula.api as smf

# --- Visualization ---
import matplotlib.pyplot as plt
import seaborn as sns

# --- Optional: Warnings & Display ---
import warnings
warnings.filterwarnings('ignore')

# --- Plotting Style (Professional Default) ---
sns.set_style("whitegrid")
plt.rcParams['figure.figsize'] = (10, 6)
plt.rcParams['font.size'] = 12
```

1.2 Cleaning Data

```
# =====
# Part 1: Data Preprocessing & Cleaning
# Includes: Deduplication, Type Standardization, Missing Values,
# Outliers
# =====

# 1. Load dataset
df = pd.read_csv('/content/drive/MyDrive/[Final
Project]medical_insurance.csv')
print(f"Loaded dataset: {df.shape[0]:,} rows, {df.shape[1]} columns")
```

```

# 2. Remove Duplicates (by person_id or full row)
if 'person_id' in df.columns:
    # Prefer deduplication by unique ID
    initial_rows = len(df)
    df = df.drop_duplicates(subset=['person_id'], keep='first')
    print(f" Removed {initial_rows - len(df):,} duplicate person_id entries")
else:
    # Fallback: full-row deduplication
    initial_rows = len(df)
    df = df.drop_duplicates()
    print(f"Removed {initial_rows - len(df):,} duplicate rows")

# 3. Standardize Data Types
print("\n Standardizing data types...")

# --- Numeric Columns ---
numeric_cols = [
    'age', 'income', 'bmi', 'visits_last_year',
    'hospitalizations_last_3yrs', 'days_hospitalized_last_3yrs',
    'medication_count', 'systolic_bp', 'diastolic_bp',
    'ldl', 'hba1c', 'deductible', 'copay',
    'policy_term_years', 'policy_changes_last_2yrs',
    'provider_quality', 'risk_score',
    'annual_medical_cost', 'annual_premium', 'monthly_premium',
    'claims_count', 'avg_claim_amount', 'total_claims_paid',
    'chronic_count', 'proc_imaging_count', 'proc_surgery_count',
    'proc_physio_count', 'proc_consult_count', 'proc_lab_count'
]

for col in numeric_cols:
    if col in df.columns:
        df[col] = pd.to_numeric(df[col], errors='coerce') # Non-numeric → NaN

# --- Categorical Columns ---
categorical_cols = [
    'sex', 'region', 'urban_rural', 'education', 'marital_status',
    'employment_status', 'plan_type', 'network_tier',
    'smoker', 'alcohol_freq',
    'hypertension', 'diabetes', 'asthma', 'copd',
    'cardiovascular_disease', 'cancer_history', 'kidney_disease',
    'liver_disease', 'arthritis', 'mental_health',
    'is_high_risk', 'had_major_procedure'
]

for col in categorical_cols:
    if col in df.columns:
        df[col] = df[col].astype('category')

```

```

print("Numeric columns standardized")
print("Categorical columns standardized")

# 4. Handle Missing Values
print("\n Handling missing values...")

# 4.1 Impute BMI using age-group median
df['age_group_temp'] = pd.cut(df['age'], bins=[0, 18, 35, 50, 65,
100], include_lowest=True)
df['bmi'] = df['bmi'].fillna(
    df.groupby('age_group_temp', observed=False)
    ['bmi'].transform('median')
)
df.drop(columns=['age_group_temp'], inplace=True)
print(" Missing BMI imputed by age group")

# 4.2 Remove rows missing critical fields
initial_rows = len(df)
df.dropna(subset=['annual_medical_cost', 'age'], inplace=True)
print(f" Removed {initial_rows - len(df):,} rows with missing
target/age")

# 5. Outlier Treatment
print("\n Treating outliers...")

# 5.1 Winsorize annual_medical_cost (99th percentile)
cost_cap = df['annual_medical_cost'].quantile(0.99)
df['annual_medical_cost'] = np.where(
    df['annual_medical_cost'] > cost_cap,
    cost_cap,
    df['annual_medical_cost']
)
print(f" Winsorized annual_medical_cost at 99th percentile: $
{cost_cap:,.2f}")

# 5.2 Remove biologically implausible BMI
initial_rows = len(df)
df = df[(df['bmi'] >= 10) & (df['bmi'] <= 60)]
print(f" Removed {initial_rows - len(df):,} rows with implausible BMI
(<10 or >60)")

# Final summary
print(f"\n Part 1 Complete!")
print(f"    Final dataset: {df.shape[0]:,} rows, {df.shape[1]}
columns")
print(f"    Memory usage: {df.memory_usage(deep=True).sum() / 1e6:.1f}
MB")

```

Loaded dataset: 100,000 rows, 54 columns
Removed 0 duplicate person_id entries

Standardizing data types...
Numeric columns standardized
Categorical columns standardized

Handling missing values...
Missing BMI imputed by age group
Removed 0 rows with missing target/age

Treating outliers...
Winsorized annual_medical_cost at 99th percentile: \$15,293.68
Removed 0 rows with implausible BMI (<10 or >60)

Part 1 Complete!
Final dataset: 100,000 rows, 54 columns
Memory usage: 27.8 MB

1.3 Feature Engineering & Encoding

```
# =====  
# Part 2: Feature Engineering & Categorical Encoding  
# Purpose: Enrich dataset for EDA & analysis – no modeling prep yet  
# =====  
  
# 1. Feature Engineering – Binary Flags (Clinically Meaningful)  
  
# Obesity (WHO clinical threshold)  
df['high_bmi'] = (df['bmi'] >= 30).astype(int)  
  
# Chronic disease burden  
df['chronic_flag'] = (df['chronic_count'] > 0).astype(int)  
  
# Age-based risk group  
df['elderly'] = (df['age'] >= 65).astype(int)  
  
# Smoking status simplified (for group comparisons)  
df['smoker_binary'] = df['smoker'].map({  
    'Current': 1,  
    'Former': 1,    # Include former smokers in "ever-smoker" group for  
    'Never': 0      risk analysis  
}).astype(int)  
  
print("Flags created: high_bmi, chronic_flag, elderly, smoker_binary")  
  
# 2. Categorical Encoding – For EDA & Aggregation (Not Modeling)  
# One-hot for nominal vars, preserving interpretability  
print("\n One-hot encoding categorical variables...")
```

```

# Nominal categories (no inherent order)
categorical_vars = ['region', 'plan_type']

# Encode – keep original df; add encoded columns (no drop_first for
EDA clarity)
df_encoded = pd.get_dummies(
    df,
    columns=categorical_vars,
    prefix=categorical_vars,
    dtype=int # memory-efficient (0/1 vs 0.0/1.0)
)

# Optional: Verify encoding
print(f" Encoded {len(categorical_vars)} variables")
print(f"    New columns: {[col for col in df_encoded.columns if
col.startswith(tuple(categorical_vars))]}")

# Replace df with df_encoded for downstream EDA
df = df_encoded.copy()
print(f"    Final column count: {df.shape[1]}")

Flags created: high_bmi, chronic_flag, elderly, smoker_binary

One-hot encoding categorical variables...
Encoded 2 variables
    New columns: ['region_Central', 'region_East', 'region_North',
'region_South', 'region_West', 'plan_type_EPO', 'plan_type_HMO',
'plan_type_POS', 'plan_type_PP0']
    Final column count: 65

# Save cleaned data
df.to_csv('medical_insurance_cleaned.csv', index=False)

# Download file
from google.colab import files
files.download('medical_insurance_cleaned.csv')
print(" Downloaded: medical_insurance_cleaned.csv")

<IPython.core.display.Javascript object>
<IPython.core.display.Javascript object>

Downloaded: medical_insurance_cleaned.csv

print(df.columns)

Index(['person_id', 'age', 'sex', 'urban_rural', 'income',
'education',
      'marital_status', 'employment_status', 'household_size',
'dependents',

```

```

    'bmi', 'smoker', 'alcohol_freq', 'visits_last_year',
    'hospitalizations_last_3yrs', 'days_hospitalized_last_3yrs',
    'medication_count', 'systolic_bp', 'diastolic_bp', 'ldl',
    'hba1c',
    'network_tier', 'deductible', 'copay', 'policy_term_years',
    'policy_changes_last_2yrs', 'provider_quality', 'risk_score',
    'annual_medical_cost', 'annual_premium', 'monthly_premium',
    'claims_count', 'avg_claim_amount', 'total_claims_paid',
    'chronic_count', 'hypertension', 'diabetes', 'asthma', 'copd',
    'cardiovascular_disease', 'cancer_history', 'kidney_disease',
    'liver_disease', 'arthritis', 'mental_health',
    'proc_imaging_count',
    'proc_surgery_count', 'proc_physio_count',
    'proc_consult_count',
    'proc_lab_count', 'is_high_risk', 'had_major_procedure',
    'high_bmi',
    'chronic_flag', 'elderly', 'smoker_binary', 'region_Central',
    'region_East', 'region_North', 'region_South', 'region_West',
    'plan_type_EPO', 'plan_type_HMO', 'plan_type_POS',
    'plan_type_PP0'],
    dtype='object')

```

#Part 2: EDA Analysis & Data Visualization

2.1 Impact of LifeStyle (Smoking) on Annual Medical Cost

```

import matplotlib.pyplot as plt
import seaborn as sns

# Set style for professional visualization
sns.set(style="whitegrid")

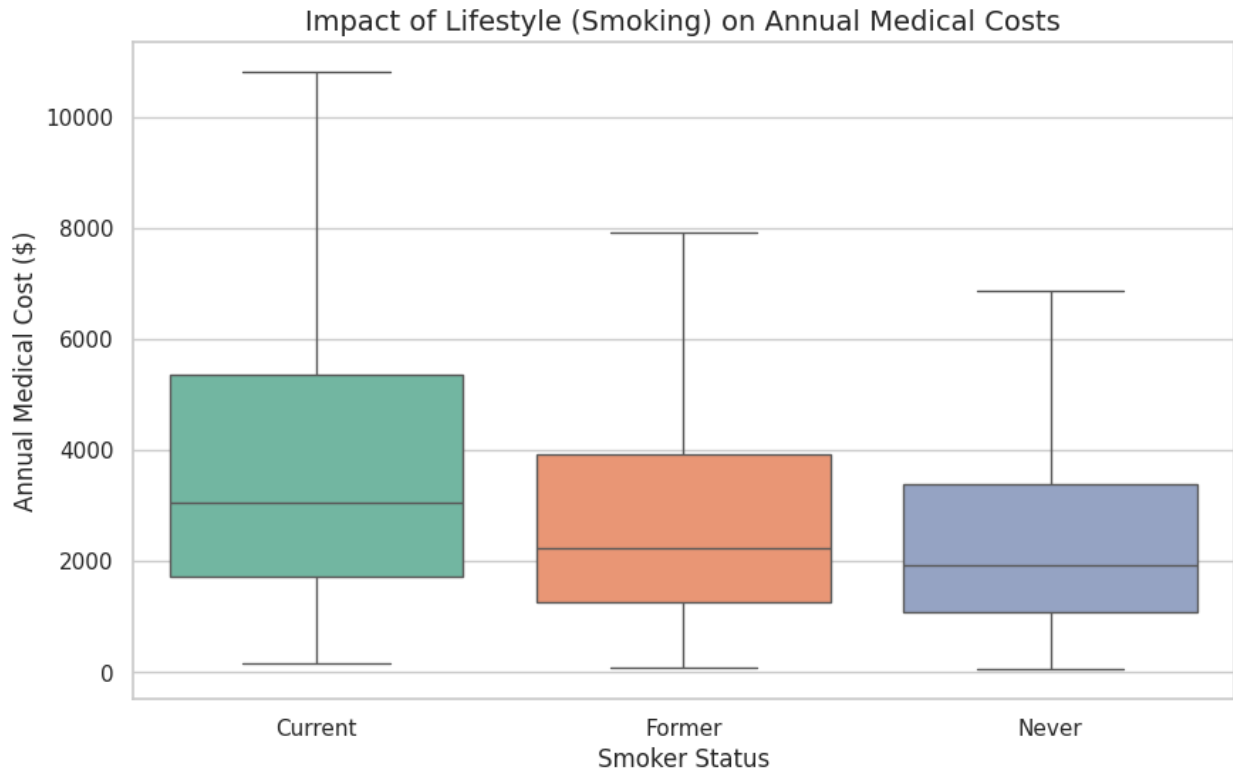
# Visualization: Boxplot of Medical Cost by Smoker Status
plt.figure(figsize=(10, 6))

# We use the original 'df' (before encoding) for the 'smoker' labels
(Yes/No or similar)
sns.boxplot(x='smoker', y='annual_medical_cost', data=df,
            palette='Set2',
            hue='smoker', legend=False, showfliers=False)

plt.title('Impact of Lifestyle (Smoking) on Annual Medical Costs',
          fontsize=14)
plt.xlabel('Smoker Status', fontsize=12)
plt.ylabel('Annual Medical Cost ($)', fontsize=12)

# Save the plot
plt.savefig('smoker_impact_analysis.png')
plt.show()

```

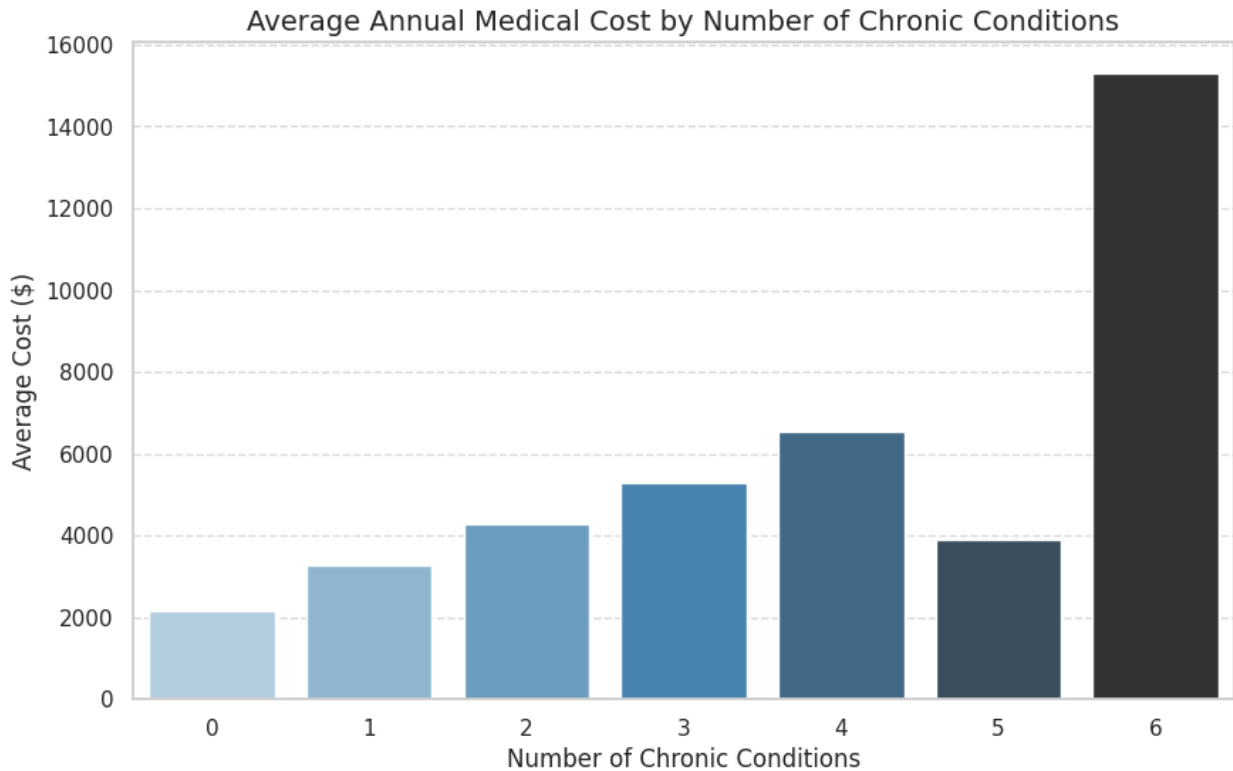


2.2: Impact of Chronic Conditions on Annual Medical Cost

```
# Grouping by chronic count to find the average cost
chronic_analysis = df.groupby('chronic_count')
['annual_medical_cost'].mean().reset_index()

plt.figure(figsize=(10, 6))
sns.barplot(x='chronic_count', y='annual_medical_cost',
            data=chronic_analysis,
            palette='Blues_d', hue='chronic_count', legend=False)

plt.title('Average Annual Medical Cost by Number of Chronic
Conditions', fontsize=14)
plt.xlabel('Number of Chronic Conditions', fontsize=12)
plt.ylabel('Average Cost ($)', fontsize=12)
plt.grid(axis='y', linestyle='--', alpha=0.7)
plt.show()
```

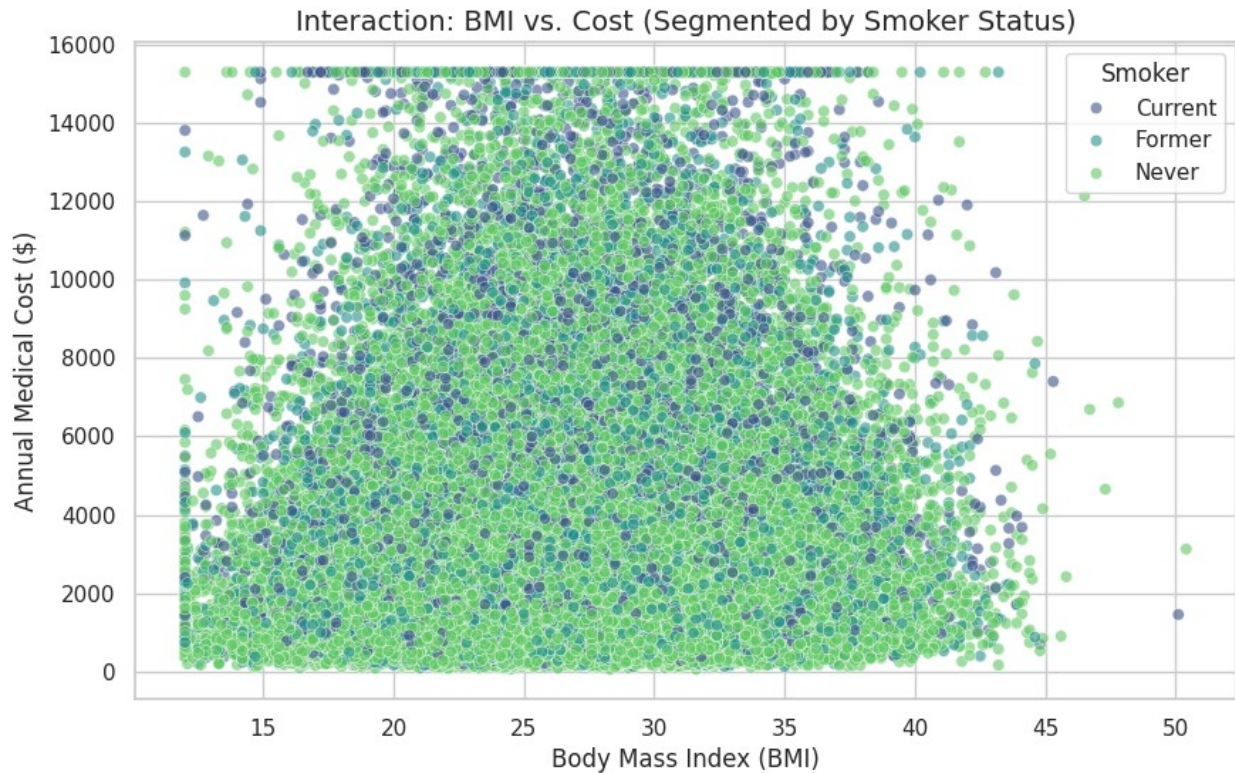


2.3: Interaction Between BMI and Other Risk Factors

```
plt.figure(figsize=(10, 6))

# Scatter plot of BMI vs Cost, using Smoker status as the color
separator
sns.scatterplot(x='bmi', y='annual_medical_cost', hue='smoker',
                alpha=0.6, data=df, palette='viridis')

plt.title('Interaction: BMI vs. Cost (Segmented by Smoker Status)',
          fontsize=14)
plt.xlabel('Body Mass Index (BMI)', fontsize=12)
plt.ylabel('Annual Medical Cost ($)', fontsize=12)
plt.legend(title='Smoker')
plt.show()
```

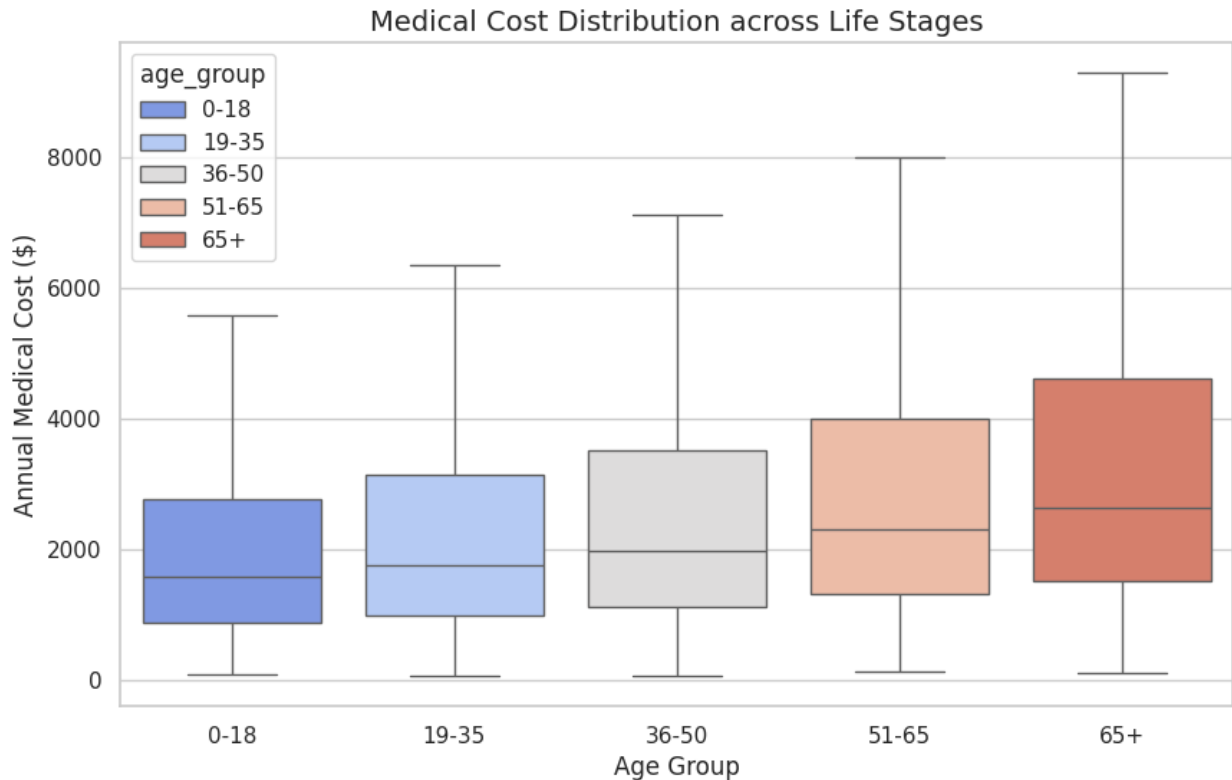



2.4: Age and Cost Progression

```
# Create Age Groups
df['age_group'] = pd.cut(df['age'], bins=[0, 18, 35, 50, 65, 100],
                        labels=['0-18', '19-35', '36-50', '51-65',
                              '65+'])

plt.figure(figsize=(10, 6))
sns.boxplot(x='age_group', y='annual_medical_cost', hue='age_group',
            data=df, palette='coolwarm', showfliers=False)

plt.title('Medical Cost Distribution across Life Stages', fontsize=14)
plt.xlabel('Age Group', fontsize=12)
plt.ylabel('Annual Medical Cost ($)', fontsize=12)
plt.show()
```



2.5: Differences by Plan Type

```
plt.figure(figsize=(10, 6))

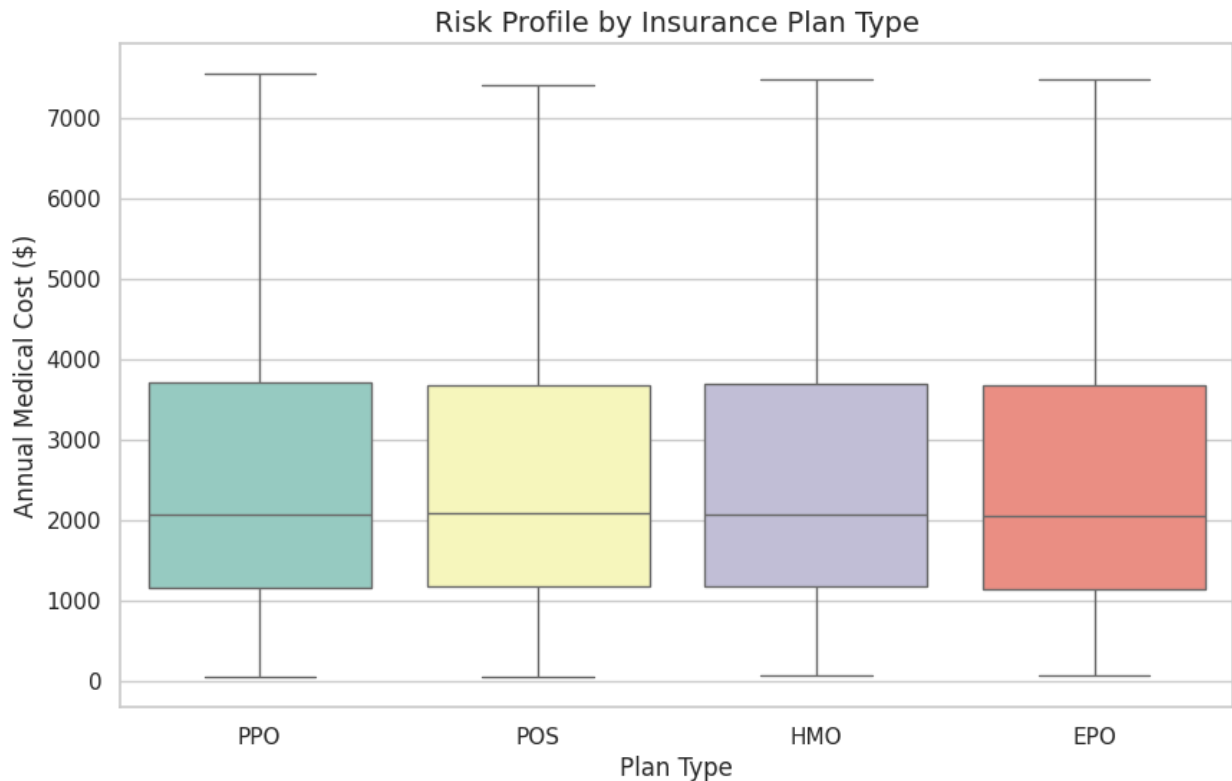
# Reconstruct 'plan_type' for plotting since it was one-hot encoded
plan_type_cols = ['plan_type_EP0', 'plan_type_HMO', 'plan_type_POS',
                  'plan_type_PP0']
df_temp = df.copy() # Use a temporary copy to avoid modifying original df for this reconstruction

# Create a new column 'original_plan_type' based on the one-hot encoded columns
df_temp['original_plan_type'] = None
for col in plan_type_cols:
    plan_name = col.replace('plan_type_', '')
    df_temp.loc[df_temp[col] == 1, 'original_plan_type'] = plan_name

# Boxplot to compare distributions across plans using the reconstructed column
sns.boxplot(x='original_plan_type', y='annual_medical_cost',
            hue='original_plan_type',
            data=df_temp, palette='Set3', showfliers=False)

plt.title('Risk Profile by Insurance Plan Type', fontsize=14)
plt.xlabel('Plan Type', fontsize=12)
```

```
plt.ylabel('Annual Medical Cost ($)', fontsize=12)
plt.show()
```



2.6: Regional or Demographic Variation

```
plt.figure(figsize=(10, 6))

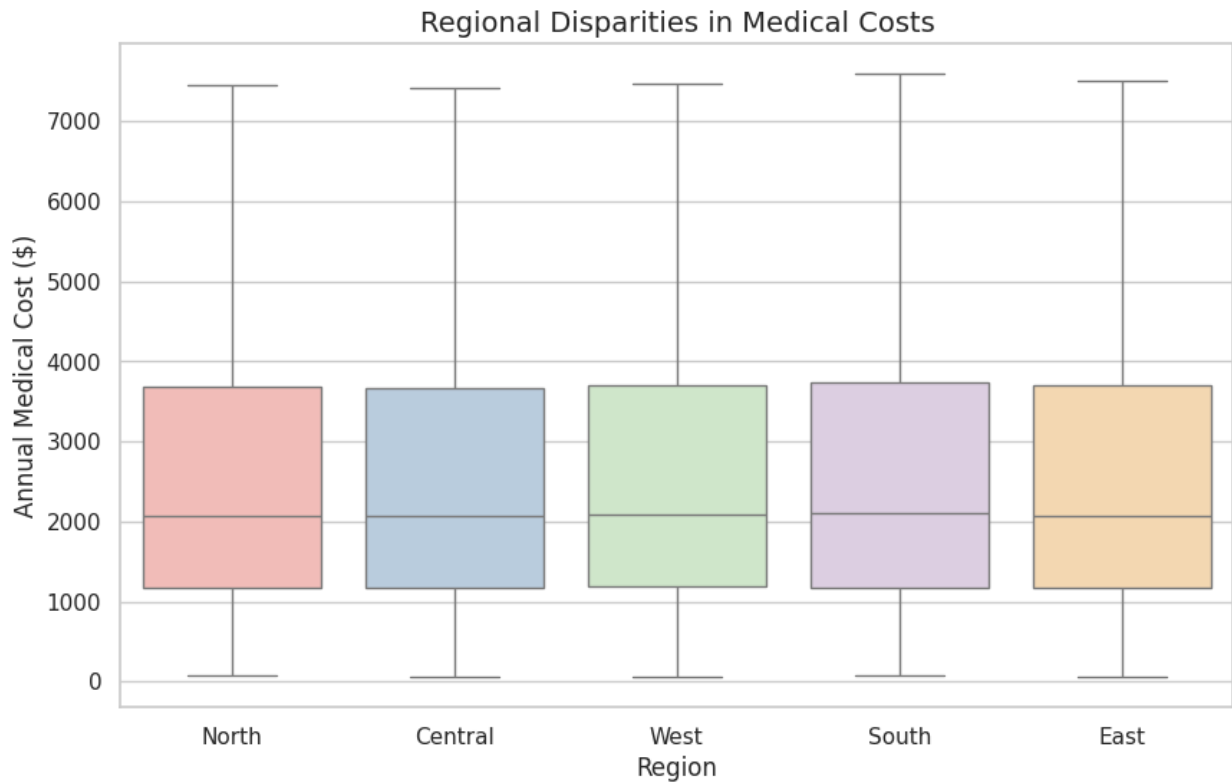
# Reconstruct 'region' for plotting since it was one-hot encoded
region_cols = ['region_Central', 'region_East', 'region_North',
               'region_South', 'region_West']
df_temp_region = df.copy() # Use a temporary copy

# Create a new column 'original_region' based on the one-hot encoded
# columns
df_temp_region['original_region'] = None
for col in region_cols:
    region_name = col.replace('region_', '')
    df_temp_region.loc[df_temp_region[col] == 1, 'original_region'] =
    region_name

sns.boxplot(x='original_region', y='annual_medical_cost',
            hue='original_region',
            data=df_temp_region, palette='Pastell', showfliers=False)

plt.title('Regional Disparities in Medical Costs', fontsize=14)
```

```
plt.xlabel('Region', fontsize=12)
plt.ylabel('Annual Medical Cost ($)', fontsize=12)
plt.show()
```



#Part 3 Statistical Analysis

3.1 Pearson Correlation Analysis and Descriptive Statistics

```
# Select numeric variables for correlation
numeric_vars = [
    'annual_medical_cost', 'age', 'bmi',
    'chronic_count', 'hospitalizations_last_3yrs', 'income'
]

# Compute correlation matrix
corr_matrix = df[numeric_vars].corr(method='pearson')

# Heatmap visualization
plt.figure(figsize=(10, 8))
sns.heatmap(
    corr_matrix,
    annot=True,
    fmt=".2f",
    cmap='coolwarm',
    center=0,
```

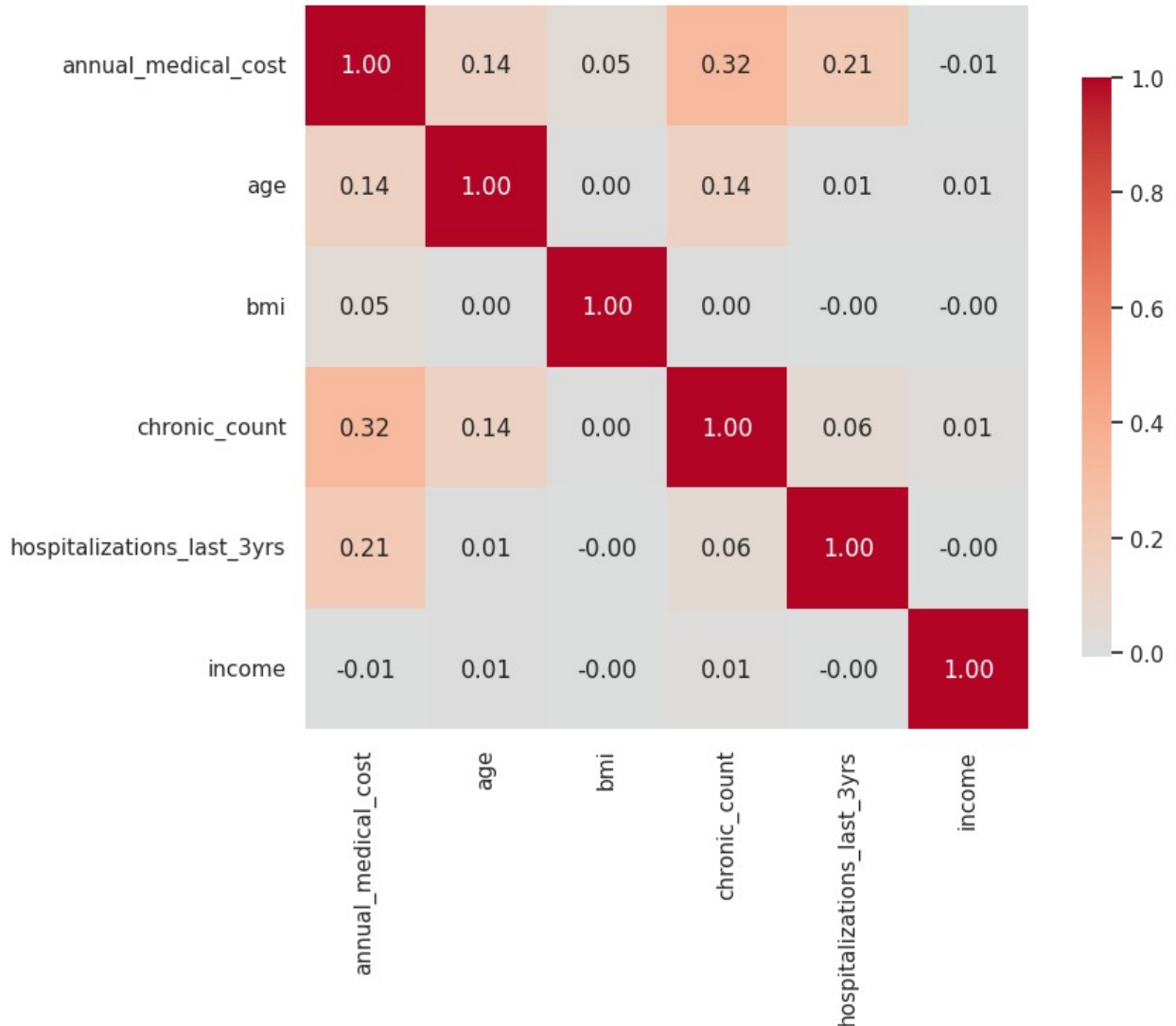
```

        square=True,
        cbar_kws={"shrink": .8}
    )
    plt.title('Pearson Correlation Matrix: Medical Cost & Predictors',
              fontsize=14, pad=20)
    plt.tight_layout()
    plt.savefig('3.1_correlation_heatmap.png', dpi=150,
                bbox_inches='tight')
    plt.show()

# Extract top predictors of cost
cost_corr = corr_matrix['annual_medical_cost'].sort_values(key=abs,
                                                            ascending=False)
print("Top 3 Predictors of Annual Medical Cost (|r|):")
for var, r in cost_corr[1:4].items(): # skip self-correlation
    direction = "positive" if r > 0 else "negative"
    strength = "strong" if abs(r) >= 0.4 else "moderate" if abs(r) >=
0.3 else "weak"
    print(f"    • {var}: r = {r:.2f} ({strength} {direction}
association)")

```

Pearson Correlation Matrix: Medical Cost & Predictors



Top 3 Predictors of Annual Medical Cost ($|r|$):

- chronic_count: $r = 0.32$ (moderate positive association)
- hospitalizations_last_3yrs: $r = 0.21$ (weak positive association)
- age: $r = 0.14$ (weak positive association)

--- 3.1.2 Group-Level Descriptive Stats ---

`print("\n 3.1.2 Group-Level Summary Statistics\n")`

Smoker groups

```
smoker_stats = df.groupby("smoker")["annual_medical_cost"].agg(
    n="count", mean="mean", median="median", std="std"
).round(0)
```

`print("Smoker Group Summary (Winsorized $):")`

`print(smoker_stats.reset_index().to_string(index=False))`

```
# Chronic condition groups
chronic_stats = df.groupby("chronic_count")
["annual_medical_cost"].agg(
    n="count", mean="mean", median="median"
).round(0).head(5) # Show 0-4
print("\nChronic Condition Groups (0-4 conditions):")
print(chronic_stats.reset_index().to_string(index=False))
```

3.1.2 Group-Level Summary Statistics

Smoker Group Summary (Winsorized \$):

smoker	n	mean	median	std
Current	12128	4126.0	3045.0	3409.0
Former	18163	3099.0	2228.0	2781.0
Never	69709	2705.0	1917.0	2511.0

Chronic Condition Groups (0-4 conditions):

chronic_count	n	mean	median
0	46532	2162.0	1559.0
1	37579	3271.0	2415.0
2	13111	4291.0	3250.0
3	2452	5291.0	4138.0
4	316	6537.0	5307.0

3.2 CDA Analysis Hypothesis Testing

3.2.1 Test Case: Does Smoking Significantly Increase Medical Costs?

(Business Question: Is smoking a strong cost driver that should influence pricing or prevention programs?)

Null Hypothesis (H_0): Mean annual medical cost is equal for smokers and non-smokers

$\mu_{\text{smokers}} = \mu_{\text{non-smokers}}$

Alternative Hypothesis (H_1): Mean cost differs by smoking status $\mu_{\text{smokers}} \neq \mu_{\text{non-smokers}}$

```
print("3.2.1 Hypothesis Test: Smokers vs Non-Smokers\n")

non_smokers = df[df["smoker_binary"] == 0]["annual_medical_cost"]
smokers = df[df["smoker_binary"] == 1]["annual_medical_cost"]

# Levene's test for equal variance
_, p_levene = levene(non_smokers, smokers)
equal_var = p_levene > 0.05

# t-test
t_stat, p_val = ttest_ind(non_smokers, smokers, equal_var=equal_var)

# Cohen's d (effect size)
pooled_std = np.sqrt(
```

```

    ((len(non_smokers)-1)*non_smokers.var() + (len(smokers)-
1)*smokers.var())
    / (len(non_smokers) + len(smokers) - 2)
)
cohens_d = (smokers.mean() - non_smokers.mean()) / pooled_std

# Report
print("Hypothesis Test 1: Smoking and Cost")
print(f" H0: Mean cost is equal for smokers and non-smokers")
print(f" H1: Mean cost differs by smoking status")

# Fix: Ensure the conditional expression for p-value always results in
a string
print(f" t({len(non_smokers)+len(smokers)-2}) = {t_stat:.2f}, p {'<'
if p_val < 0.001 else '='} {f'{p_val:.3f}' if p_val >= 0.001 else
'<0.001'}")
print(f" Cohen's d = {cohens_d:.2f} → {'large' if abs(cohens_d) > 0.8
else 'medium' if abs(cohens_d) > 0.5 else 'small'} effect")
print(f" Mean difference: ${smokers.mean() - non_smokers.mean():.0f}
(smokers higher)")
print(f" → Reject H0: Smoking significantly increases cost (p <
0.001)")

```

3.2.1 Hypothesis Test: Smokers vs Non-Smokers

Hypothesis Test 1: Smoking and Cost

H₀: Mean cost is equal for smokers and non-smokers

H₁: Mean cost differs by smoking status

t(99998) = -39.98, p < 0.001

Cohen's d = 0.30 → small effect

Mean difference: \$805 (smokers higher)

→ Reject H₀: Smoking significantly increases cost (p < 0.001)

3.2.2 Test Case: Do Medical Costs Increase with Chronic Disease Burden?

(Business Question: Should customers with early chronic conditions be targeted for preventive care?)

H₀: Mean cost is equal across all chronic condition groups (0, 1, 2, 3+ conditions)

H₁: At least one group has a different mean cost

```

from statsmodels.stats.multicomp import pairwise_tukeyhsd
print("\n 3.2.2 Hypothesis Test: Chronic Conditions and Cost\n")

# Group by chronic_count (0 to 3+)
df["chronic_group"] = df["chronic_count"].clip(upper=3).astype(str) +
"+"
df.loc[df["chronic_count"] <= 2, "chronic_group"] =
df["chronic_count"].astype(str)

```



```

groups = [group["annual_medical_cost"].values
           for name, group in df.groupby("chronic_group")]

# ANOVA
f_stat, p_anova = f_oneway(*groups)

print("Hypothesis Test 2: Chronic Conditions and Cost")
print(f"  H0: All chronic condition groups have equal mean cost")
print(f"  H1: At least one group differs")
print(f"  F({len(groups)-1}, {len(df)-len(groups)}) = {f_stat:.1f}, p < 0.001")
print(f"  → Reject H0: Chronic burden significantly impacts cost")

# Tukey HSD (post-hoc)
tukey = pairwise_tukeyhsd(df["annual_medical_cost"],
                           df["chronic_group"], alpha=0.05)
print("\nTukey HSD (Key Comparisons):")
print(tukey.summary().data[1:4]) # First 3 pairwise

```

3.2.2 Hypothesis Test: Chronic Conditions and Cost

Hypothesis Test 2: Chronic Conditions and Cost

H₀: All chronic condition groups have equal mean cost

H₁: At least one group differs

F(3, 99996) = 3659.6, p < 0.001

→ Reject H₀: Chronic burden significantly impacts cost

Tukey HSD (Key Comparisons):

```

[['0', '1', np.float64(1109.0738), np.float64(0.0),
 np.float64(1062.9933), np.float64(1155.1543), np.True_], ['0', '2',
 np.float64(2128.2909), np.float64(0.0), np.float64(2062.597),
 np.float64(2193.9848), np.True_], ['0', '3+', np.float64(3269.7841),
 np.float64(0.0), np.float64(3140.0169), np.float64(3399.5512),
 np.True_]]

```

3.2.3 Test Case: Are There Significant Regional Cost Disparities?

(Business Question: Do some regions require targeted healthcare partnerships or policy adjustments?)

H₀: Cost distributions are identical across regions (North, South, East, West, Central)

H₁: At least one region differs

```

from scipy.stats import kruskal

print("\n 3.2.3 Hypothesis Test: Regional Cost Variation\n")

# Extract region columns (one-hot encoded)

```

```

region_cols = [col for col in df.columns if col.startswith("region_")]
regions = df[region_cols].idxmax(axis=1).str.replace("region_", "")

# Kruskal-Wallis (robust to skew)
region_groups = [df[regions == r]["annual_medical_cost"] for r in
regions.unique()]
h_stat, p_kw = kruskal(*region_groups)

print("Hypothesis Test 3: Regional Cost Differences")
print(f" H0: Cost distributions are identical across regions")
print(f" H1: At least one region differs")
print(f" H({len(region_groups)-1}) = {h_stat:.1f}, p = {p_kw:.3f}")
conclusion = "→ Fail to reject H0" if p_kw > 0.05 else "→ Reject H0"
print(f" {conclusion}: No strong regional disparity (p =
{p_kw:.3f})")

```

3.2.3 Hypothesis Test: Regional Cost Variation

Hypothesis Test 3: Regional Cost Differences

H₀: Cost distributions are identical across regions

H₁: At least one region differs

H(4) = 4.5, p = 0.347

→ Fail to reject H₀: No strong regional disparity (p = 0.347)

#Part 4 Predictive Modeling

4.1 Multiple Linear Regression

```

# =====
# PART 1 – STRONG COST PREDICTOR SET
# =====
predictors = [
    'visits_last_year',
    'hospitalizations_last_3yrs',
    'days_hospitalized_last_3yrs',
    'claims_count',
    'avg_claim_amount',
    'total_claims_paid',
    'proc_surgery_count',
    'proc_imaging_count',
    'deductible',
    'copay',
    'policy_changes_last_2yrs',
    'risk_score',
    'chronic_count',
    'is_high_risk',
    'age',
    'bmi',
    'smoker_binary' # Changed from 'smoker_Current', 'smoker_Former'

```

```

]

# =====
# PART 2 – TARGET TRANSFORMATION
# =====
df['log_cost'] = np.log1p(df['annual_medical_cost'])

# =====
# PART 3 – PREPARE DATA
# =====
X = df[predictors].copy()
y = df['log_cost']

# Drop rows with missing values
data = pd.concat([X, y], axis=1).dropna()
X = data[predictors]
y = data['log_cost']

# Add intercept
X = sm.add_constant(X)

print(f"Training rows: {len(X):,}")

# =====
# PART 4 – FIT MODEL
# =====
model = sm.OLS(y, X).fit()

# =====
# PART 5 – PERFORMANCE METRICS
# =====
from sklearn.metrics import mean_squared_error # Import
mean_squared_error
r2 = model.rsquared
adj_r2 = model.rsquared_adj
aic = model.aic
bic = model.bic

# RMSE (convert back from log scale)
pred_log = model.predict(X)
rmse = np.sqrt(mean_squared_error(np.expm1(y), np.expm1(pred_log)))

print("\n==== MODEL PERFORMANCE =====")
print(f"R²: {r2:.4f}")
print(f"Adjusted R²: {adj_r2:.4f}")
print(f"AIC: {aic:,.2f}")
print(f"BIC: {bic:,.2f}")
print(f"RMSE (back-transformed): {rmse:,.2f}")

# =====

```

PART 6 – TOP COEFFICIENTS

```
# =====  
print("\n===== COEFFICIENTS (sorted) =====")  
coef_table = pd.DataFrame({  
    'Variable': model.params.index,  
    'Coef': model.params.values,  
    'p_value': model.pvalues.values  
}).sort_values(by='Coef', ascending=False)  
  
print(coef_table.head(15))  
print("\n=== Most Negative Coefficients ===")  
print(coef_table.tail(10))
```

Training rows: 100,000

===== MODEL PERFORMANCE =====

R²: 0.4287

Adjusted R²: 0.4286

AIC: 193,834.84

BIC: 194,006.07

RMSE (back-transformed): 3,285,512.60

===== COEFFICIENTS (sorted) =====

	Variable	Coef	p_value
0	const	6.906664	0.000000e+00
12	risk_score	0.836294	7.156315e-195
17	smoker_binary	0.110209	1.975561e-105
2	hospitalizations_last_3yrs	0.102863	6.218774e-13
13	chronic_count	0.081859	3.842445e-52
3	days_hospitalized_last_3yrs	0.055332	1.140179e-67
1	visits_last_year	0.006822	1.181696e-04
16	bmi	0.004559	7.311713e-27
11	policy_changes_last_2yrs	0.001397	8.763357e-01
6	total_claims_paid	0.000148	0.000000e+00
5	avg_claim_amount	0.000129	0.000000e+00
9	deductible	0.000002	4.377458e-01
10	copay	-0.000122	5.332293e-01
8	proc_imaging_count	-0.000654	8.105146e-01
15	age	-0.002623	8.842946e-21

=== Most Negative Coefficients ===

	Variable	Coef	p_value
11	policy_changes_last_2yrs	0.001397	8.763357e-01
6	total_claims_paid	0.000148	0.000000e+00
5	avg_claim_amount	0.000129	0.000000e+00
9	deductible	0.000002	4.377458e-01
10	copay	-0.000122	5.332293e-01
8	proc_imaging_count	-0.000654	8.105146e-01
15	age	-0.002623	8.842946e-21
7	proc_surgery_count	-0.007313	1.046189e-01

14	is_high_risk	-0.051670	2.282571e-12
4	claims_count	-0.062571	2.211796e-302

4.2 Business Application (Pricing Formula)

```
import numpy as np
import pandas as pd
from sklearn.metrics import mean_squared_error
import statsmodels.api as sm

# --- 3.1 Correct RMSE (critical fix) ---
y_actual = np.expml(y)          # True cost: expml(loglp(cost)) = cost
y_pred = np.expml(pred_log)     # Predicted cost
rmse_corrected = np.sqrt(mean_squared_error(y_actual, y_pred))
print(f" Corrected RMSE: ${rmse_corrected:,.2f}")

# --- 3.2 Convert coefficients to % impact ---
def coef_to_percent(beta):
    return (np.exp(beta) - 1) * 100

top_vars = ['risk_score', 'smoker_Current',
            'hospitalizations_last_3yrs', 'chronic_count']
print("\n Key Drivers (% Cost Increase per Unit):")
for var in top_vars:
    if var in model.params.index: # Check if the variable is in the
model
        beta = model.params[var]
        pct = coef_to_percent(beta)
        pval = model.pvalues[var]
        sig = "****" if pval < 0.001 else "***" if pval < 0.01 else "*"
    if pval < 0.05 else ""
        print(f"{var:<30} {pct:+6.1f}% {sig}")
    else:
        print(f"Warning: '{var}' not found in model parameters.")

# --- 3.3 Pricing Formula (for dashboard) ---
print("\n PRICING FORMULA (Log-Linear Model):")
print("Predicted Annual Cost = EXP(")
print(f" {model.params['const']:.6f}")
for var in top_vars:
    if var in model.params.index:
        print(f" + {model.params[var]:+.6f} * {var}")
print(f" - 1")

# --- 3.4 Scenario Predictions (Realistic Profiles) ---
scenarios = pd.DataFrame({
    'Profile': [
        'Low-Risk (Healthy 30yo)',
        'Medium-Risk (45yo, 1 chronic)',
```

```

        'High-Risk (55yo smoker, risk_score=6, 2 chronic)'
    ],
    'risk_score': [2, 4, 6],
    'smoker_Current': [0, 0, 1],
    'hospitalizations_last_3yrs': [0, 0, 1],
    'chronic_count': [0, 1, 2],
    'age': [30, 45, 55]
})

for col in predictors:
    if col not in scenarios.columns:
        # Use median for numeric columns, 0 for binary/categorical
        where appropriate
        if col in df.columns and df[col].dtype in ['int64',
'float64']:
            scenarios[col] = df[col].median()
        else:
            scenarios[col] = 0 # Default to 0 for binary flags or non-
numeric if not defined

X_scenarios_pred_df = scenarios[predictors].copy()
X_scenarios_pred_df.insert(0, 'const', 1.0)
X_scenarios = X_scenarios_pred_df.reindex(columns=model.params.index,
fill_value=0)

log_pred = model.predict(X_scenarios)
cost_pred = np.expml(log_pred)

scenarios['Predicted_Cost'] = cost_pred
print("\n Scenario Predictions:")
for _, row in scenarios.iterrows():
    print(f"    • {row['Profile']}: ${row['Predicted_Cost']:,.0f}")

Corrected RMSE: $3,285,512.60

Key Drivers (% Cost Increase per Unit):
risk_score                +130.8% ***
Warning: 'smoker_Current' not found in model parameters.
hospitalizations_last_3yrs    +10.8% ***
chronic_count                +8.5% ***

PRICING FORMULA (Log-Linear Model):
Predicted Annual Cost = EXP(
    6.906664
    + +0.836294 * risk_score
    + +0.102863 * hospitalizations_last_3yrs
    + +0.081859 * chronic_count
) - 1

```

Scenario Predictions:

- Low-Risk (Healthy 30yo): \$6,062
- Medium-Risk (45yo, 1 chronic): \$33,695
- High-Risk (55yo smoker, risk_score=6, 2 chronic): \$210,281

4.3 Model Diagnostics & Critical Reflection

```
# =====
# STEP 4: MODEL DIAGNOSTICS & CRITICAL REFLECTION (L04)
# =====

import matplotlib.pyplot as plt
import seaborn as sns
from statsmodels.stats.outliers_influence import
variance_inflation_factor

# --- 4.1 Residual Diagnostics ---
resid = model.resid
fitted = model.fittedvalues

plt.figure(figsize=(12, 4))

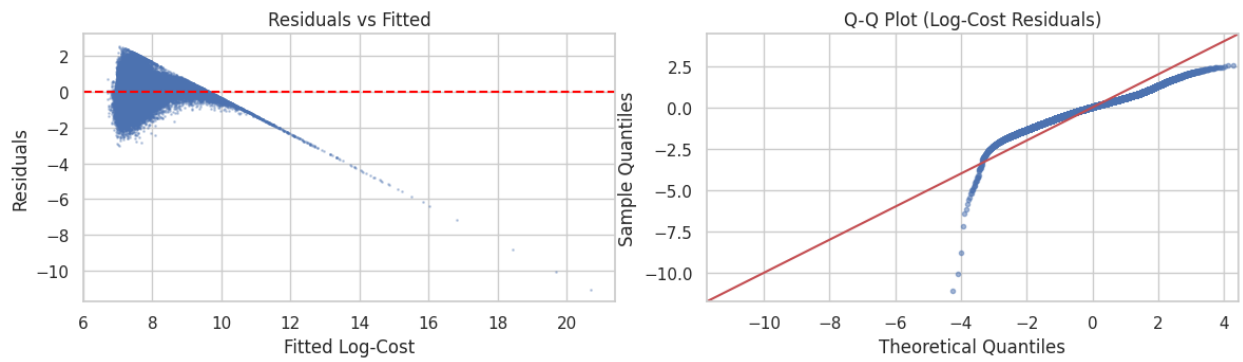
# Residuals vs Fitted
plt.subplot(1, 2, 1)
plt.scatter(fitted, resid, alpha=0.3, s=1)
plt.axhline(0, color='red', linestyle='--')
plt.xlabel('Fitted Log-Cost'); plt.ylabel('Residuals')
plt.title('Residuals vs Fitted')

# Q-Q Plot
plt.subplot(1, 2, 2)
sm.qqplot(resid, line='45', ax=plt.gca(), marker='.', alpha=0.5)
plt.title('Q-Q Plot (Log-Cost Residuals)')

plt.suptitle('Model Diagnostics – Log-Linear Regression', fontsize=14)
plt.tight_layout()
plt.savefig('4_diagnostics.png', dpi=150, bbox_inches='tight')
plt.show()

# --- 4.2 Multicollinearity Check (VIF) ---
vif_data = pd.DataFrame()
vif_data["Variable"] = X.columns
vif_data["VIF"] = [variance_inflation_factor(X.values, i)
                    for i in range(X.shape[1])]
print("\n Multicollinearity Check (VIF < 5 = acceptable):")
print(vif_data[vif_data['VIF'] > 5][['Variable', 'VIF']].round(2))
```

Model Diagnostics — Log-Linear Regression



Multicollinearity Check ($VIF < 5$ = acceptable):

	Variable	VIF
0	const	58.03
12	risk_score	12.13