

Baryon number fluctuation and critical end point

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We investigate the relationship between the peak value of baryon number fluctuation kurtosis and the critical baryon chemical potential. At the same time, the freeze-out curves under different position of the critical end point. We control the position of the critical end point by include the fermion vacuum fluctuation gradually. This work is done under the low energy Polyakov-quark-meson model with the functional renormalization group approach.

PACS numbers: 11.30.Rd, 11.10.Wx, 05.10.Cc, 12.38.Mh

INTRODUCTION

The location of the critical end point (CEP) of the QCD phase diagram is a popular research direction in the field of high energy physics. However, the physical property at high baryon chemical potential is hard to study in both theoretical and experimental. In the experimental field, the Relativistic Heavy Ion Collider (RHIC) that provides us with a lot of experimental data [1–3].

BARYON NUMBER FLUCTUATIONS AND THE FERMION VACUUM FLUCTUATION

The kurtosis of the baryon number fluctuation is the core of our work, for the significant role it play in the experiment area of the QCD phase structure. The calculation of the baryon number fluctuation can be done using the following formula,

$$\chi_n^B = \frac{\partial^n}{\partial(\mu_B/T)^n} \frac{p}{T^4}, \quad (1)$$

In which the $\mu_B = 3\mu$ is the beryon chemical potential that is triple of the quark chemical potential. Then we can obtain the first to fourth order of the beryon number distribution,

$$\chi_1^B = \frac{1}{VT^3} \langle N_B \rangle, \quad (2)$$

$$\chi_2^B = \frac{1}{VT^3} \langle (\delta N_B)^2 \rangle, \quad (3)$$

$$\chi_3^B = \frac{1}{VT^3} \langle (\delta N_B)^3 \rangle, \quad (4)$$

$$\chi_4^B = \frac{1}{VT^3} \left(\langle (\delta N_B)^4 \rangle - 3 \langle (\delta N_B)^2 \rangle^2 \right), \quad (5)$$

The meaning of the angle brackets stands for the average value, and the δN_B stands for the difference between the N_B and $\langle N_B \rangle$ which reads $\delta N_B := N_B - \langle N_B \rangle$.

For the purpose of comparing our calculation with the experimental results, we divide the fourth and second order of the baryon number fluctuations to get the kurtosis

which is the observable in the experiments, e.g., $\kappa\sigma^2 = \chi_4^B/\chi_2^B$. More details discussion about baryon number fluctuation see [4]. Here we investigate the relationship of the maximum value of the kurtosis and the fermion vacuum fluctuation.

We find that the position of the critical end point would change with different fermion vacuum contribution we involve in our calculation. In this work we add a new cutoff scale into the functional renormalisation group flow equation to restrict the fermion vacuum fluctuation and study the behavior of the position of the critical end point under the different cutoff. From the previous work of the low energy effective theory under the FRG, the flow equation of the effective potential contain the full contribution of the fermion vacuum part throughout the integral interval which is cover from the infrared point to the ultraviolet point. The effect of the fermion vacuum contribution is studied in the mean field approximation, see [5].

POLYAKOV-QUARK-MESON MODEL AND THE CUTOFF

This work is done under the two quark flavor Polyakov-quark-meson model. We give the effective action

$$\begin{aligned} \Gamma_k = \int_x \Big\{ & Z_{q,k} \bar{q} \left[\gamma_\mu \partial_\mu - \gamma_0 (\hat{\mu} + i g A_0) \right] q \\ & + \frac{1}{2} Z_{\phi,k} (\partial_\mu \phi)^2 + h_k \bar{q} (T^0 \sigma + i \gamma_5 \vec{T} \cdot \vec{\pi}) q \\ & + V_k(\rho) - c\sigma \Big\}, \end{aligned} \quad (6)$$

with the 4 dimension integral $\int_x = \int_0^{1/T} dx_0 \int d^3x$. The k is the FRG infrared (IR) cutoff scale which is running from the ultraviolet (UV) scale to 0. The meson field is defined as $\phi = (\sigma, \vec{\pi})$, and $\rho = \phi^2/2$. \vec{T} is the generators of the $SU(N_f)$ group here we have $N_f = 2$. The generators satisfy $\text{Tr}(T^i T^j) = \frac{1}{2} \delta^{ij}$, $T^0 = \frac{1}{\sqrt{2N_f}} \mathbb{1}_{N_f \times N_f}$. The $-c\sigma$ gives the chiral symmetry breaking in our theory. In this work we get the results under the local potential

Λ_2 (MeV)	0	100	200	300	400	500	600	700
T_c (MeV)	124	123	117	110	98	97	95	89
μ_{BC} (MeV)	335	345	435	552	655	725	770	785

TABLE I. The position of the critical point and the value of the cutoff Λ_2 .

approximation (LPA), under which $\partial_t Z_{\phi,q} = 0$, $\partial_t h_k = 0$. The t is RG time with $t = \ln(k/\Lambda)$. We choose the UV cutoff scale Λ to 700 MeV. In the LPA situation, we focus on the flow of effective potential. The flow equation can be written as

$$\begin{aligned} \partial_t V_k(\rho) = & \frac{k^4}{4\pi^2} [(N_f^2 - 1)l_0^{B,4}(\bar{m}_{\pi,k}^2, \eta_{\phi,k}; T) \\ & + l_0^{(B,4)}(\bar{m}_{\sigma,k}^2, \eta_{\phi,k}; T) \\ & - 4N_c N_f l_0^{(F,4)}(\bar{m}_{q,k}^2, \eta_{q,k}; T, \mu)], \end{aligned} \quad (7)$$

The anomalous dimensions of the fermion and boson is all 0 here. The $l_0^{(F,4)}$ in the flow equation stands for the fermion threshold function. The analytical form of the threshold function is

$$\begin{aligned} l_0^{(F,d)}(\bar{m}_{q,k}^2, \eta_{q,k}; T, \mu) = & \frac{1}{z_q(d-1)\sqrt{1+\bar{m}_{q,k}^2}}(1 - \frac{\eta_{q,k}}{d}) \\ & \times (1 - n_F(\bar{m}_{q,k}^2, z_q; T, \mu) - n_F(\bar{m}_{q,k}^2, z_q; T, \mu)) \end{aligned} \quad (8)$$

which contains all contribution of the fermion vacuum fluctuation. We take place this with another threshold function with no fermion vacuum part

$$\begin{aligned} j_0^{(F,d)}(\bar{m}_{q,k}^2, \eta_{q,k}; T, \mu) = & \frac{1}{z_q(d-1)\sqrt{1+\bar{m}_{q,k}^2}}(1 - \frac{\eta_{q,k}}{d}) \\ & \times (-n_F(\bar{m}_{q,k}^2, z_q; T, \mu) - n_F(\bar{m}_{q,k}^2, z_q; T, \mu)) \end{aligned} \quad (9)$$

And we divided the integral of the flow equation into two parts by the new cutoff scale Λ_2 between the IR and UV scales. The integral between the IR scale and Λ_2 is the flow equation with the fermion vacuum contribution the other side of the integral that between the Λ_2 and UV

scale is the flow equation without the fermion vacuum contribution. Now we can control the quantity of the fermion vacuum part by changing the new cutoff Λ_2 .

RESULTS AND SUMMARY

ACKNOWLEDGMENTS

The work was supported by the National Natural Science Foundation of China under Contracts Nos. 11775041.

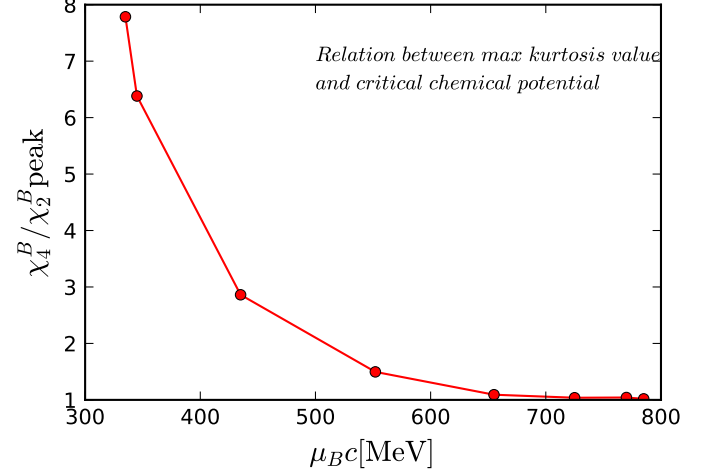


FIG. 1. The relation between the maximum baryon number fluctuation kurtosis value and the baryon chemical potential of the critical end point.

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