### Baryon number fluctuation and critical end point

Shi Yin,<sup>1</sup> Rui Wen,<sup>1</sup> and Wei-jie Fu<sup>1,\*</sup>

<sup>1</sup>School of Physics, Dalian University of Technology, Dalian, 116024, P.R. China

We investigate the relationship between the peak value of baryon number fluctuation kurtosis and the critical baryon chemical potential. At the same time, the freeze-out curves under different position of the critical end point. We control the position of the critical end point by a new cutoff scale which can remove the fermion vacuum fluctuation from the flow equations. This work is done under the low energy Polyakov-quark-meson model with the functional renormalization group approach.

### PACS numbers: 11.30.Rd, 11.10.Wx, 05.10.Cc, 12.38.Mh

### INTRODUCTION

The location of the critical end point (CEP) of the QCD phase diagram is a popular research direction in the field of high energy physics. However, the physical property at high baryon chemical potential that is the high density area is hard to study in both theoretical and experimental. In the experimental field, the Relativistic Heavy Ion Collider (RHIC) that provides us with a lot of experimental data at the high density part, see [1–3].

# BARYON NUMBER FLUCTUATIONS AND THE FERMION VACUUM FLUCTUATION

The kurtosis of the baryon number fluctuation is the core of our work, for the significant role it plays in the experiment area of the QCD phase structure. The calculation of the baryon number fluctuation can be done using the following formula,

$$\chi_n^B = \frac{\partial^n}{\partial (\mu_B/T)^n} \frac{p}{T^4} \,, \tag{1}$$

in which the  $\mu_B = 3\mu$  is the beryon chemical potential that is triple of the quark chemical potential. Then we can obtain the first to fourth order of the beryon number fluctuation known as the generalized susceptibilities,

$$\chi_2^B = \frac{1}{VT^3} \langle (\delta N_B)^2 \rangle \,, \tag{2}$$

$$\chi_4^B = \frac{1}{VT^3} \left( \langle (\delta N_B)^4 \rangle - 3 \langle (\delta N_B)^2 \rangle^2 \right), \tag{3}$$

The meaning of the angle brackets stands for the average value, and the  $\delta N_B$  stands for the difference between the  $N_B$  and  $\langle N_B \rangle$  which reads  $\delta N_B := N_B - \langle N_B \rangle$ .

For the purpose of comparing our calculation with the experimental results, we divide the fourth and second order of the baryon number fluctuations to get the kurtosis which is the observable in the experiments, e.g.,  $\kappa \sigma^2 = \chi_4^B/\chi_2^B$ . More details discussion about baryon number fluctuation see [4]. Here we investigate the relationship

of the maximum value of the kurtosis and the fermion vacuum fluctuation.

We find that the position of the critical end point would change with different fermion vacuum contribution we involve in our calculation. In this work we add a new cutoff scale into the functional renormalisation group flow equation to restrict the fermion vacuum fluctuation and study the behavior of the position of the critical end point under the different cutoff. From the previous work of the low energy effective theory under the FRG, the flow equation of the effective potential contain the full contribution of the fermion vacuum part throughout the integral interval which is cover from the infrared point to the ultraviolet point. The effect of the fermion vacuum contribution is studied in the mean field approximation, see [5]. We can tell that the fermion vacuum fluctuation can suppress the baryon number fluctuation at finite temperature and density. If the new cutoff scale get the value of the UV scale, the flow return to the previous which includes all the fermion vacuum term. If the cutoff scale get the value of the IR scale, the flow get the result of the mean-field approximation. The neglect of the fermion vacuum part is known as the no-sea approximation.

## POLYAKOV-QUARK-MESON MODEL AND THE CUTOFF

This work is done under the two quark flavor Polyakovquark-meson model. We give the effective action

$$\Gamma_{k} = \int_{x} \left\{ Z_{q,k} \bar{q} \left[ \gamma_{\mu} \partial_{\mu} - \gamma_{0} (\hat{\mu} + igA_{0}) \right] q \right. \\
+ \frac{1}{2} Z_{\phi,k} (\partial_{\mu} \phi)^{2} + h_{k} \bar{q} \left( T^{0} \sigma + i \gamma_{5} \vec{T} \cdot \vec{\pi} \right) q \right. \\
+ V_{k}(\rho) - c \sigma \right\}, \tag{4}$$

with the 4 dimension integral  $\int_x = \int_0^{1/T} dx_0 \int d^3x$ . The k is the FRG infrared (IR) cutoff scale which is running from the ultraviolet (UV) scale to 0. The meson field is

defined as  $\phi = (\sigma, \vec{\pi})$ , and  $\rho = \phi^2/2$ .  $\vec{T}$  is the generators of the  $SU(N_f)$  group here we have  $N_f = 2$ . The generators satisfy  $Tr(T^iT^j) = \frac{1}{2}\delta^{ij}$ ,  $T^0 = \frac{1}{\sqrt{2N_f}}\mathbb{1}_{N_f \times N_f}$ .

The  $-c\sigma$  gives the chiral symmetry breaking in our theory. In this work we get the results under the local potential approximation (LPA), under which  $\partial_t Z_{\phi,q} = 0$ ,  $\partial_t h_k = 0$ . The t is RG time with  $t = \ln(k/\Lambda)$ . We choose the UV cutoff scale  $\Lambda$  to 700MeV. The effective potential  $V_k(\rho)$  involves the infermation of the meson chiral symmetry breaking. Here we solve the flow equation of the effective potential by the Taylor expansion around the expansion point  $\kappa$ . The expansed meson potential is  $V_k(\rho) = \sum_{n=0}^{N_v} \frac{\lambda_{n,k}}{n!} (\rho - \kappa_k)^n$ . In this work, we choose  $N_v = 5$  for the good convergence of the fix expansion point  $\partial_t \kappa_k = 0$ . In order to get the pressure, the thermodynamical potential should be calculated. The definition of the thermodynamical potential is  $\Omega[T,\mu] = V_{k=0}(\rho) + V_{glue}(L,\bar{L}) - c\sigma$ . The glue potential is a function of the traced Polyakov loop Land the complex conjugate  $\bar{L}$ . They are in concerning with the gluonic background field  $A_0$  by  $L = \frac{1}{N_*} \langle \text{Tr} \mathcal{P} \rangle$ ,  $\bar{L} = \frac{1}{N_c} \langle \text{Tr} \mathcal{P}^{\dagger} \rangle \text{ with } \mathcal{P} = \mathcal{P} \exp \left( ig \int_0^{\beta} d\tau A_0(\tau) \right).$ 

In the LPA situation, we focus on the flow of effective potential. The flow equation can be written as

$$\partial_t V_k(\rho) = \frac{k^4}{4\pi^2} \left[ (N_f^2 - 1) l_0^{B,4} (\bar{m}_{\pi,k}^2, \eta_{\phi,k}; T) + l_0^{(B,4)} (\bar{m}_{\sigma,k}^2, \eta_{\phi,k}; T) - 4N_c N_f l_0^{(F,4)} (\bar{m}_{q,k}^2, \eta_{q,k}; T, \mu) \right],$$
(5)

The anomalous dimensions of the fermion and boson is all 0 here. The  $l_0^{(F,4)}$  in the flow equation stands for the fermion threshold function. The analytical form of the threshold function is

$$l_0^{(F,d)}(\bar{m}_{q,k}^2, \eta_{q,k}; T, \mu) = \frac{1}{z_q(d-1)\sqrt{1 + \bar{m}_{q,k}^2}} (1 - \frac{\eta_{q,k}}{d}) \times (1 - n_F(\bar{m}_{q,k}^2, z_q; T, \mu) - n_F(\bar{m}_{q,k}^2, z_q; T, \mu))$$
(6)

which contains all contribution of the fermion vacuum fluctuation. We take place this with another threshold function with no fermion vacuum part

$$j_0^{(F,d)}(\bar{m}_{q,k}^2, \eta_{q,k}; T, \mu) = \frac{1}{z_q(d-1)\sqrt{1+\bar{m}_{q,k}^2}} (1 - \frac{\eta_{q,k}}{d}) \times (-n_F(\bar{m}_{q,k}^2, z_q; T, \mu) - n_F(\bar{m}_{q,k}^2, z_q; T, \mu))$$
(7)

Then we devided the integral of the flow equation into two parts by the new cutoff scale  $\Lambda_2$  between the IR and UV scales. The integral between the IR scale and  $\Lambda_2$  is the flow equation with the fermion vacuum contribution the other side of the integral that between the  $\Lambda_2$  and UV

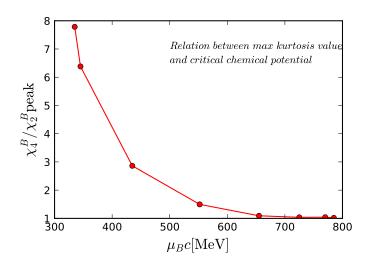


FIG. 1. The relation between the maximum baryon number fluctuation kurtosis value and the baryon chemical potential of the critical end point.

$\Lambda_2 \; ({ m MeV})$	0	100	200	300	400	500	600	700
$T_c \; (\mathrm{MeV})$	124	123	117	110	98	97	95	89
$\mu_B c \text{ (MeV)}$	335	345	435	552	655	725	770	785

TABLE I. The position of the critical point and the value of the cutoff  $\Lambda_2$ .

scale is the flow equation without the fermion vacuum contribution. Now we can control the quantity of the fermion vacuum part by changing the new cutoff  $\Lambda_2$ .

### RESULTS AND SUMMARY

### ACKNOWLEDGMENTS

The work was supported by the National Natural Science Foundation of China under Contracts Nos. 11775041.

<sup>\*</sup> wjfu@dlut.edu.cn

L. Adamczyk *et al.* (STAR), Phys. Rev. Lett. **112**, 032302 (2014), arXiv:1309.5681 [nucl-ex].

<sup>[2]</sup> X. Luo (STAR), Proceedings, 9th International Workshop on Critical Point and Onset of Deconfinement (CPOD 2014): Bielefeld, Germany, November 17-21, 2014, PoS CPOD2014, 019 (2015), arXiv:1503.02558 [nucl-ex].

<sup>[3]</sup> X. Luo and N. Xu, Nucl. Sci. Tech. 28, 112 (2017), arXiv:1701.02105 [nucl-ex].

<sup>[4]</sup> W.-j. Fu and J. M. Pawlowski, Phys. Rev. **D92**, 116006 (2015), arXiv:1508.06504 [hep-ph].

[5] V. Skokov, B. Friman, E. Nakano, K. Redlich, and B. J. Schaefer, Phys. Rev. **D82**, 034029 (2010), arXiv:1005.3166 [hep-ph].