

Res, $SSE = \sum (y_a - y_p)^2$

$$SST = \sum (y_a - y_{mean})^2$$

$$SSR = \sum (y_p - y_{mean})^2$$

x_i	y_i	\hat{y}_i	Residuals	SSE	$\sum (y_i - \hat{y}_i)^2$
10	5	5.5	-0.5	0.25	
20	6	8	-2	4	
30	7	10	-3	9	
40	4	5	-1	1	
50	3	3.5	-0.5	0.25	
				$\sum 14.5$	
				SSE = RSS //	

KM //

x_i	y_a	y_p	(Residuals) $y_a - y_p$	SSE $\sum (y_a - y_p)^2$
	5000	5500	-500	250000
	6000	8000	-2000	400000
	7000	10000	-3000	900000
	4000	5000	-1000	100000
	3000	3500	-500	250000
				<hr/> SSE <hr/>

M/

$$\frac{K_M}{SSE} = \sum (y_a - y_p)^2 = \text{---?}$$

M

$$SSE = \sum (y_a - y_p)^2 = \text{---?}$$

Scale Variant

x_1	x_2	x_3	
1	1000	10,000	Scale Variant
2	2000	20000	
3	3000	30000	
4	4000	40000	
5	5000	50000	

$R^2_{\text{score}} = \text{Score Invariant}$

$R \times R$

$$R^2_{\text{score}} = 1 - \frac{\text{SSE}}{\text{SST}}$$

$$= \frac{\text{SST} - \text{SSE}}{\text{SST}}$$

$$R_2 \text{ score} = 1 - \frac{SSE}{SST}$$

$$\Rightarrow SSE = \text{High}, \quad SST = \text{High}$$

$$SSE \approx SST$$

$$R_2 \text{ score} \approx 0$$

$0 \Rightarrow$

Worst
score

$$\text{II} \quad \text{SSE} = \text{low}^2, \quad \text{SST} = \text{high}^2$$

$$R^2 = 1 - \text{SSE} / \text{SST}$$

$$= \frac{1 - \frac{\sum (y_a - \hat{y}_p)^2}{\sum (y_a - \bar{y}_{\text{mean}})^2}}{1}$$

$$R^2_{\text{Score}} \approx 1$$

$$1 \rightarrow \text{Best Score}$$

$$\frac{y - \bar{y}}{s} = \frac{6/9}{3} = 0.7 = \underline{\underline{70\%}}$$

$$\text{iii] } SSE = \text{High}, \quad SST = \text{low}$$

$$R^2_{\text{score}} = 1 - \frac{SSE}{SST}$$

$$= \frac{\text{low} - \text{high}}{\text{low}}$$

$$R^2_{\text{score}} = \underline{\underline{-ve}}$$

$$R^2_{\text{score}} =$$

$$1 - \frac{SSE}{SST} = \frac{SST - SSE}{SST}$$

$$= 1 - \frac{\sum (y_a - y_e)^2}{\sum (y_a - \bar{y})^2}$$

$$= 1 - \frac{\text{unexplained variation}}{\text{total variation}}$$

10 features + 1 feature

↳ Correlated
feature

$$\underline{\underline{R^2 \text{ score} = 0.85}}$$

$$\underline{\underline{R = 0.9}}$$

$$\underline{\underline{R^2 \text{ score} = 0.87}}$$

10 Features + 1 feature
↳ Non-correlated

$$\underline{\underline{R^2 \text{ score} = 0.85}}$$

$$R = 0.4$$

$$\begin{aligned} R^2 \text{ score} &= 0.85 \\ &= 0.856 \\ &= 0.8500\% \end{aligned}$$

$$\bar{R}^2 = \frac{R^2 - (K-1)(1-R^2)}{n-K}$$

N = Number of sample size

K = Number of input variables / Attributes

5 Features

+

1 Features

↳ Correlated

↓
 $R = 0.8$

$$\underline{\underline{\bar{R}^2 = 0.85}}$$

$$\underline{\underline{\bar{R}^2 = 0.87}}$$

5 features + 1 feature

↳ Non-correlated

$$\bar{R}^2 = 0.85$$

$$R = 0.7$$

$$\bar{R}^2 = 0.84$$
$$0.838$$

	R^2	\bar{R}^2
	0.85	0.85
ρ - Correlated	0.87	0.87 \rightarrow <u>Good</u>
ρ - Non correlated	0.856 σ^2 0.86	0.83 \rightarrow <u>Bad</u>