1. 作業概述

本作業的目標是開發一個 Flask 網頁應用程式,實作一個網格地圖(Gridworld),允許使用者指定維度(範圍從 5 到 9),並透過互動設定起始格、終點格及障礙物。此外,還需顯示策略矩陣(Policy Matrix)及價值矩陣(Value Matrix),並利用策略評估推導各狀態的價值。

本作業分為兩個部分:

- HW1-1: 網格地圖開發(60%)
- HW1-2: 策略顯示與價值評估(40%)

2. HW1-1 網格地圖開發

2.1 功能實作

(1) 網格生成與動態設定

- 使用者可以輸入數值(介於5到9),生成對應大小的網格。
- 使用 AJAX 進行非同步請求,後端 Flask 會根據使用者輸入更新網格大小。

(2) 起始點、終點與障礙物設置

- 點擊一個單元格可將其標記為起始格(綠色)。
- 再次點擊另一單元格可將其標記為終點格(紅色)。
- 使用者最多可標記 個障礙物(灰色)。
- 單元格可以重複點擊來取消設定。

2.2 程式碼設計

後端 (Flask) 設計

- set_size() 方法處理網格大小變更。
- 變數 GRID_SIZE 、 START_CELL 、 END_CELL 、 OBSTACLES 負責存儲當前的網格設定。

前端 (HTML + JavaScript) 設計

- generateGrid() 負責創建網格。
- handleCellClick() 處理單元格點擊事件,根據不同條件更新格子顏色。
- startGame() 發送請求到 Flask,取得策略與價值矩陣。

3. HW1-2 策略顯示與價值評估

3.1 功能實作

(1) 策略矩陣 (Policy Matrix) 生成

- 針對非終點與障礙物的單元格,隨機選擇一組合法動作(↑ ↓ ← →)。
- 確保選擇的動作不會超出網格範圍或進入障礙物。

(2) 價值矩陣 (Value Matrix) 計算

- 終點格的獎勵設為 1.0 ,障礙物的價值設為 -1.0 。
- 其他格子的初始值在 [-0.5, 0.5] 之間隨機分配。

4. 成果截圖與程式碼

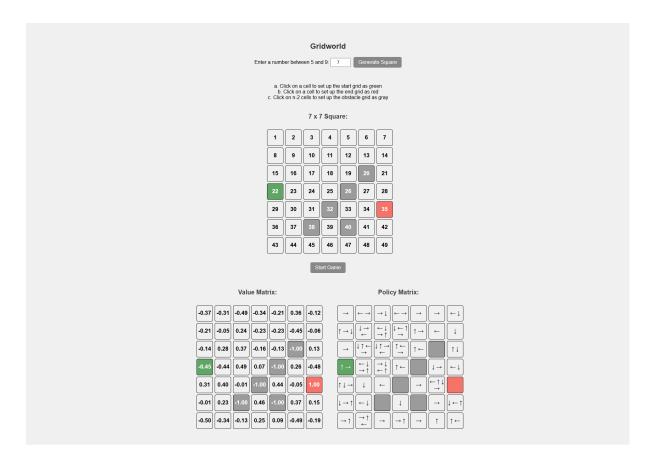
4.1成果截圖

以下為 Gridworld 介面執行結果的截圖:

HW1-1: Result

Gridworld							
Enter a number between 5 and 9: 7 Generate Square							
a. Click on a cell to set up the start grid as green b. Click on a cell to set up the end grid as red c. Click on a cell to set up the obstacle grid as gray							
c. Click on n-2 cells to set up the obstacle grid as gray							
7 x 7 Square:							
	<u> </u>	\neg		_			1
1	<u>ן</u>	2	3	4	5	6	7
8	в	9	10	11	12	13	14
15	5	16	17	18	19	20	21
22	2	23	24	25	26	27	28
29	9	30	31	32	33	34	35
36	6	37	38	39	40	41	42
43	3	44	45	46	47	48	49
Start Game							
Value Matrix: Policy Matrix:							

HW1-2: Result



4.2 程式碼

後端程式碼 (Flask - app.py)

```
from flask import Flask, render_template, request, jsonify import numpy as np import random

app = Flask(__name__)

GRID_SIZE = 5
START_CELL = None
END_CELL = None
OBSTACLES = set()

ACTIONS = {
  "↑": (-1, 0),
  "↓": (1, 0),
  "¢": (0, -1),
  "→": (0, 1)
}

@app.route('/')
```

```
def index():
  return render_template('index.html', grid_size=GRID_SIZE)
@app.route('/set_size', methods=['POST'])
def set_size():
  global GRID_SIZE, START_CELL, END_CELL, OBSTACLES
    data = request.get_json()
    size = data.get("size")
    if 5 <= size <= 9:
      GRID_SIZE = size
      START_CELL = None
      END_CELL = None
      OBSTACLES = set()
      return jsonify({"status": "success", "grid_size": GRID_SIZE})
    return jsonify({"status": "error", "message": "Grid size must be between 5 and 9"}),
400
  except Exception as e:
    return jsonify({"status": "error", "message": str(e)}), 500
@app.route('/find_best_path', methods=['POST'])
def find_best_path():
  """隨機產生 Value Matrix 和 Policy Matrix,並確保不會超出範圍"""
  global GRID_SIZE, START_CELL, END_CELL, OBSTACLES
  try:
    data = request.get_json()
    if not data or 'start' not in data or 'end' not in data or 'obstacles' not in data or 'grid_s
ize' not in data:
      return jsonify({"status": "error", "message": "Missing required parameters"}), 400
    start = tuple(data['start'])
    end = tuple(data['end'])
    obstacles = set(tuple(obs) for obs in data['obstacles'])
    GRID_SIZE = data['grid_size'] # 讀取前端傳來的 grid_size
    # 產生隨機 Value Matrix
    values = np.random.uniform(-0.5, 0.5, (GRID_SIZE, GRID_SIZE))
    values[end] = 1.0 # 設定終點獎勵
    for obs in obstacles:
      values[obs] = -1.0 # 設定障礙物
```

```
#產生隨機 Policy Matrix,確保不會超出範圍
    policy = np.full((GRID_SIZE, GRID_SIZE), " ", dtype=object)
    for r in range(GRID_SIZE):
       for c in range(GRID_SIZE):
         if (r, c) == end or (r, c) in obstacles:
           continue
         valid_actions = []
         for action, (dr, dc) in ACTIONS.items():
           nr, nc = r + dr, c + dc
           if 0 <= nr < GRID_SIZE and 0 <= nc < GRID_SIZE and (nr, nc) not in obstacles:
              valid_actions.append(action)
         if valid_actions:
           num_actions = random.randint(1, len(valid_actions)) # 隨機選擇 1~所有合法動
作
           policy[r, c] = "".join(random.sample(valid_actions, num_actions))
    return jsonify({
       "status": "success",
       "value_matrix": values.tolist(),
       "policy_matrix": policy.tolist()
    })
  except Exception as e:
    return jsonify({"status": "error", "message": str(e)}), 500
if __name__ == '__main__':
  app.run(debug=True)
```

前端程式碼 (index.html)

```
h2 {
  font-size: 24px;
  font-weight: bold;
  color: #333;
}
h3 {
  font-size: 20px;
  font-weight: bold;
  color: #444;
input[type="number"] {
  width: 50px;
  text-align: center;
  padding: 5px;
  margin-right: 5px;
button {
  font-size: 16px;
  background-color: #888888;
  color: white;
  border: none;
  padding: 8px 15px;
  cursor: pointer;
  border-radius: 5px;
  transition: background 0.3s ease;
button:hover {
  background-color: #5a5a5a;
.grid-container {
  display: grid;
  column-gap: 18px; /* 只調整水平間距 */
  row-gap: 5px; /* 可選:控制垂直間距 */
  margin-top: 10px;
  padding: 10px;
  border-collapse: collapse;
```

```
.grid-item {
  width: 50px;
  height: 50px;
  display: flex;
  justify-content: center;
  align-items: center;
  border: 1px solid black;
  font-size: 18px;
  cursor: pointer;
  font-weight: bold;
  transition: all 0.2s ease;
  border-radius: 5px; /* 設置圓角,數值越大圓角越明顯 */
.grid-item:hover {
  transform: scale(1.1);
#grid-container {
  display: flex;
  justify-content: center;
  margin-top: 20px;
#matrix-container {
  display: flex;
  justify-content: center;
  align-items: flex-start;
  gap: 40px;
  margin-top: 30px;
@media (max-width: 768px) {
  #matrix-container {
    flex-direction: column;
    align-items: center;
.start {
  background-color: #64a866;
  color: white;
.end {
  background-color: #f5736a;
```

```
color: white;
    .obstacle {
      background-color: #9E9E9E;
      color: white;
    }
  </style>
</head>
<body>
<h2>Gridworld</h2>
Enter a number between 5 and 9:
  <input type="number" id="grid-size" min="5" max="9">
  <button onclick="generateGrid()">Generate Square</button>
<br>
>
  a. Click on a cell to set up the start grid as green <br/> <br/>br>
  b. Click on a cell to set up the end grid as red <br>
  c. Click on n-2 cells to set up the obstacle grid as gray
<!-- Gridworld 區域 →
<div id="grid-container">
  <div>
    <h3><span id="grid-title">5 × 5 Square:</span></h3>
    <div id="grid" class="grid-container"></div><br>
    <button id="start-game" onclick="startGame()">Start Game</button>
  </div>
</div>
<!-- Value Matrix 和 Policy Matrix →
<div id="matrix-container">
  <div>
    <h3>Value Matrix:</h3>
    <div id="value-matrix" class="grid-container"></div>
  </div>
  <div>
    <h3>Policy Matrix:</h3>
    <div id="policy-matrix" class="grid-container"></div>
  </div>
</div>
<script>
```

```
let gridSize = 5;
let startCell = null:
let endCell = null;
let obstacles = new Set();
function generateGrid() {
  gridSize = parseInt(document.getElementById("grid-size").value);
  if (gridSize < 5 | gridSize > 9 | isNaN(gridSize)) {
     alert("Please enter a valid number between 5 and 9.");
     return;
  $.ajax({
     url: "/set_size",
     type: "POST",
     contentType: "application/json",
     data: JSON.stringify({ size: gridSize }),
     success: function(response) {
       if (response.status === "success") {
          startCell = null;
          endCell = null;
          obstacles.clear();
          renderGrid();
       } else {
          alert(response.message);
    },
     error: function(xhr) {
       console.log("AJAX Error:", xhr.responseText);
       alert("Error setting grid size.");
  });
function renderGrid() {
  let grid = document.getElementById("grid");
  grid.innerHTML = "";
  grid.style.gridTemplateColumns = \( \)repeat(\( \){\( \)gridSize\\), \( \)40px\( \);
  for (let row = 0; row < gridSize; row++) {
    for (let col = 0; col < gridSize; col++) {
       let cell = document.createElement("div");
       cell.classList.add("grid-item");
       cell.textContent = row * gridSize + col + 1;
       cell.dataset.row = row;
```

```
cell.dataset.col = col;
       cell.addEventListener("click", () ⇒ handleCellClick(cell));
       grid.appendChild(cell);
  document.getElementById("grid-title").textContent = `${gridSize} x ${gridSize} Square:';
function handleCellClick(cell) {
  let row = parseInt(cell.dataset.row);
  let col = parseInt(cell.dataset.col);
  let cellPos = [row, col];
  if (startCell && startCell[0] === row && startCell[1] === col) {
     startCell = null;
     cell.className = "grid-item";
  } else if (endCell && endCell[0] === row && endCell[1] === col) {
     endCell = null;
     cell.className = "grid-item";
  } else if (obstacles.has(JSON.stringify(cellPos))) {
     obstacles.delete(JSON.stringify(cellPos));
     cell.className = "grid-item";
  } else if (!startCell) {
     startCell = cellPos;
     cell.className = "grid-item start";
  } else if (!endCell) {
     endCell = cellPos:
     cell.className = "grid-item end";
  } else if (obstacles.size < gridSize - 2) {
     obstacles.add(JSON.stringify(cellPos));
     cell.className = "grid-item obstacle";
  } else {
     alert('You can only place up to ${gridSize - 2} obstacles.');
function startGame() {
  if (!startCell | !endCell) {
     alert("Please select both a start and end cell.");
     return;
  let obstacleList = Array.from(obstacles).map(JSON.parse);
  $.ajax({
```

```
url: "/find_best_path",
     type: "POST",
     contentType: "application/json",
     data: JSON.stringify({
       start: startCell,
       end: endCell,
       obstacles: obstacleList.
       grid_size: gridSize // 🗸 傳遞最新 gridSize
    }),
     success: function(response) {
       if (response.status === "success") {
         renderMatrix("value-matrix", response.value_matrix, false);
         renderMatrix("policy-matrix", response.policy_matrix, true);
       } else {
         alert(response.message);
    },
    error: function(xhr) {
       alert("Error calculating matrices.");
  });
function renderMatrix(id, matrix, isPolicy) {
  let container = document.getElementById(id);
  container.innerHTML = "";
  container.style.gridTemplateColumns = 'repeat(${gridSize}, 40px)';
  for (let row = 0; row < gridSize; row++) {
    for (let col = 0; col < gridSize; col++) {
       let cell = document.createElement("div");
       cell.classList.add("grid-item");
       // W 保留格子顏色 (start, end, obstacle)
       let cellPos = JSON.stringify([row, col]);
       if (startCell && startCell[0] === row && startCell[1] === col) {
         cell.classList.add("start");
       } else if (endCell && endCell[0] === row && endCell[1] === col) {
         cell.classList.add("end");
       } else if (obstacles.has(cellPos)) {
         cell.classList.add("obstacle");
       // 🗸 設定數值或箭頭
       if (isPolicy) {
```