

$$\begin{aligned}
\ell &= \sum_u \sum_v \#Sample \cdot Sim_u(v) \cdot (\log \sigma(\vec{s}_u \cdot \vec{t}_v)) \\
&\quad + \frac{k}{|V|} \sum_n \log \sigma(-\vec{s}_u \cdot \vec{t}_n)) \\
&= \#Sample \{ \sum_u \sum_v Sim_u(v) \cdot \log \sigma(\vec{s}_u \cdot \vec{t}_v) \\
&\quad + \sum_u \sum_n \sum_v Sim_u(v) \cdot \frac{k}{|V|} \cdot \log \sigma(-\vec{s}_u \cdot \vec{t}_n) \} \\
&= \#Sample \{ \sum_u \sum_v Sim_u(v) \cdot \log \sigma(\vec{s}_u \cdot \vec{t}_v) \\
&\quad + \sum_u \sum_n \frac{k}{|V|} \cdot \log \sigma(-\vec{s}_u \cdot \vec{t}_n) \} \\
&= \#Sample \{ \sum_u \sum_v (Sim_u(v) \cdot \log \sigma(\vec{s}_u \cdot \vec{t}_v) \\
&\quad + \frac{k}{|V|} \cdot \log \sigma(-\vec{s}_u \cdot \vec{t}_v)) \}
\end{aligned}$$