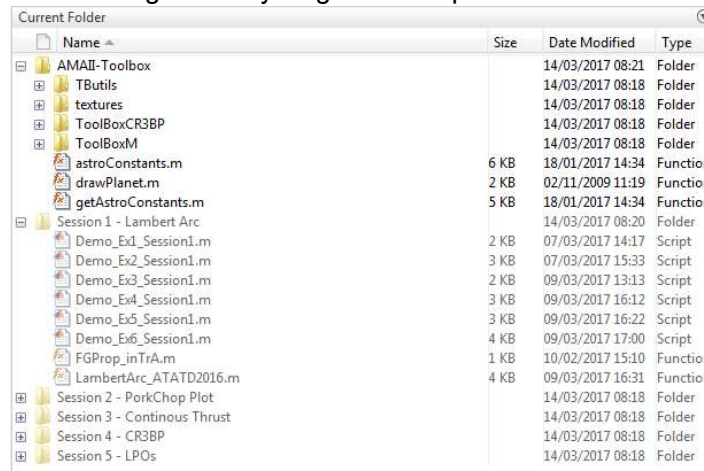


Basic Notes

The following bullet points provide some basic hints on how completing the tasks of this course.

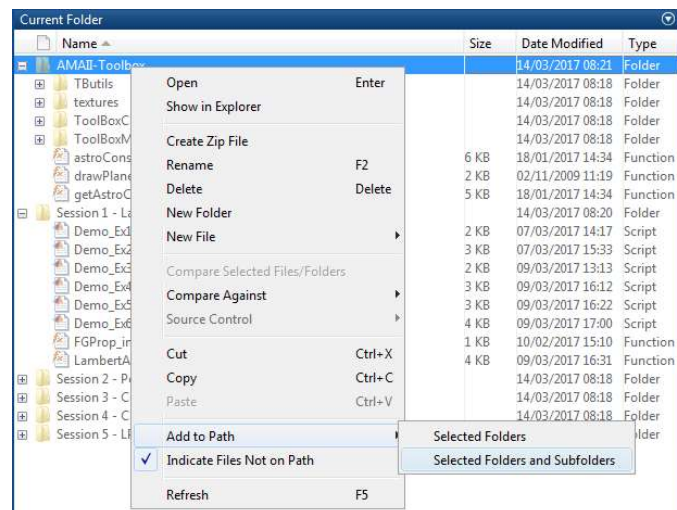
- Complete all the exercises by creating one script for each task. This way you will be able to revise easily your calculations, as well as comparing with the exercise solutions. To know more on MATLAB scripts click [here](#).
- Create a sensible working directory. A good example would be as follow:



Name	Size	Date Modified	Type
AMAIL-Toolbox		14/03/2017 08:21	Folder
TButils		14/03/2017 08:18	Folder
textures		14/03/2017 08:18	Folder
ToolBoxCR3BP		14/03/2017 08:18	Folder
ToolBoxM		14/03/2017 08:18	Folder
astroConstants.m	6 KB	18/01/2017 14:34	Function
drawPlanet.m	2 KB	02/11/2009 11:19	Function
getAstroConstants.m	5 KB	18/01/2017 14:34	Function
Session 1 - Lambert Arc		14/03/2017 08:20	Folder
Demo_Ex1_Session1.m	2 KB	07/03/2017 14:17	Script
Demo_Ex2_Session1.m	3 KB	07/03/2017 15:33	Script
Demo_Ex3_Session1.m	2 KB	09/03/2017 13:13	Script
Demo_Ex4_Session1.m	3 KB	09/03/2017 16:12	Script
Demo_Ex5_Session1.m	3 KB	09/03/2017 16:22	Script
Demo_Ex6_Session1.m	4 KB	09/03/2017 17:00	Script
FGProp_inTrA.m	1 KB	10/02/2017 15:10	Function
LambertArc_ATATD2016.m	4 KB	09/03/2017 16:31	Function
Session 2 - PorkChop Plot		14/03/2017 08:18	Folder
Session 3 - Continuous Thrust		14/03/2017 08:18	Folder
Session 4 - CR3BP		14/03/2017 08:18	Folder
Session 5 - LPOs		14/03/2017 08:18	Folder

Note that AMAIL-Toolbox is highlighted, while the other folders seem to be more shaded. This is simply because AMAIL-Toolbox is already in the path of the working environment.

- In order to add the toolbox folder in the path do as follow:
 1. Right-click over the folder you want to add into the path (AMAIL-Toolbox).
 2. Look for the option “add to path” and hover with the cursor over it.
 3. The option “select folder and subfolders” will appear. Click on it.



- Remember the rule: Never ever duplicate code sections! When another choice can be made: Choose always to group into a common function any code that repeats with only small differences due to different input parameters. If you have never created a function in Matlab, check the following tutorial:
https://uk.mathworks.com/help/matlab/matlab_prog/create-functions-in-files.html

Session 1 Lambert Arc Matlab Guide PART B

Exercise 3. “Shoot” the minimum energy orbit for a Δt equivalent to the real ExoMars TGO transfer ($\Delta t = 215$ days) and compute the $d\mathbf{x}$ error of the final position state.

- Implement algorithm in slide 48 to complete Exercise 3. Also use the code you have written to solve the minimum energy orbit to compute the departure velocity from Earth.
- Propagate for the required Δt using F and G coefficients and compute the difference between Mars at the arrival date and your position.

Exercise 4. Use the STM to correct the previous shooting and come up with a better approximation of the velocity at departure.

- Resume from script implementing Exercise 3, save it as Ex4_session1.m
- Implement the state transition matrix algorithm as described in slide 55.

Help: See code for the implementation (note nomenclature may vary slightly from the slides)

```
% This section reproduces the pseudo-code in slide 35.
%-----
% Relevant State Transition Matrix
C=sma*sqrt(sma^3/muSun)*(3*sin(DE_f)-(2+cos(DE_f))*DE_f)...
-DT*sma*(1-cos(DE_f));

dr=rf-r1;
%r2dot
% Gdot
Gdot=1-sma/norm(rf)*(1-cos(DE_f));
r2dot=1/G*(-r1+Gdot*rf);

dv=r2dot-r1dot;

drf_drdotzero=r1_n/muSun*(1-F)*(dr'*r1dot - dv'*r1)+...
C/muSun*r2dot'*r1dot+G*eye(3);
```

- Compute matrix $\frac{\partial \mathbf{r}_f}{\partial \dot{\mathbf{r}}_0}$ using the initial conditions $(\mathbf{r}_0 \quad \dot{\mathbf{r}}_0)$ as given from the minimum energy orbit.
- Compute the correction to apply to $\dot{\mathbf{r}}_0$ as:

$$\Delta \dot{\mathbf{r}}_{\text{Correction}}(t_1) = \left(\frac{\partial \mathbf{r}_f}{\partial \dot{\mathbf{r}}_0} \right)^{-1} (\mathbf{r}_{\text{Mars}} - \mathbf{r}_f)$$

Or in MATLAB code:

```
Drldot=inv(drf_drdotzero)*(rf-r2)';  
rldot_new=rldot-Drldot';
```

5. Perform the correction to the initial velocity as $\dot{\mathbf{r}}_0 + \Delta\dot{\mathbf{r}}_{\text{Correction}}$ and propagate the conditions $(\mathbf{r}_0 \quad \dot{\mathbf{r}}_0 + \Delta\dot{\mathbf{r}}_{\text{Correction}})$ for $\Delta t = 215$ days.
6. Is the final distance between \mathbf{r}_f and the position of Mars on 15/10/2016 smaller than in Exercise 3?

Exercise 5. Iterate the differential correction method until convergence to an error of below 1m.

1. Resume from script implementing Exercise 4, save it as Ex5_session1.m
2. At the end of the first “shooting” (i.e. propagation), create a new variable name Error such as:

```
Error=norm(rf-r2)
```

3. Create a [while-loop](#) after the first shooting (i.e. previous to the first correction) on which the expression that limits/stops the execution of the loop is:

```
while Error>1e-3 % 1m...
```

4. Run the script and, if done correctly, should converge in four loops.

Exercise 6. What ΔV is required to launch ExoMars Trace Gas Orbiter on 14/03/2016, and arrive at Mars on 15/10/2016.

1. Resume from script implementing Exercise 5, save it as Ex6_session1.m
2. Create [for-loop](#) just after the minimum energy trajectory has been generated, to implement a continuation method in, for example, 10 steps. The [while-loop](#) of the differential corrector should be located within this [for-loop](#).

```

% Defining the number of differential correction steps
nIterations=10; % number of Iterations until reaching the desired solution
% Start loop
for iIter=1:nIterations
    % disp(['Starting Iteration ',num2str(iIter),' in Continuation Method'])
    Lamda=iIter/nIterations;
    DT=Lamda*ToF_target+(1-Lamda)*ToF_min;
    %-----
    % STEP 4: Shooting method
    ETolerance=1e-3; % 1 m miss match are allowed
    numMaxIter=25;
    numIter=0;
    r2_iteration=0;
    while (norm(r2_iteration-r2)>ETolerance)&&(numIter<numMaxIter) ...
end

```

2. After the [while-loop](#) has concluded, you should have the initial position and velocity, as well as the final position. However, you still require the final velocity. Compute it as:

```

Gdot=1-sma/norm(rf)*(1-cos(DE_f));
vf=1/G*(-r1+Gdot*rf); % Final velocity
                        % at Mars Arrival

```

3. The difference between the velocity of the Earth on 14/03/2016 and the departure velocity of your transfer will give you the ΔV to depart the Earth.

4. The difference between the velocity of Mars on 15/10/2016 and the arrival velocity of your transfer will give you the ΔV at Mars.

Note that these are just velocity differences, but are not necessarily the ΔV -costs of the manoeuvres to complete the Earth-Mars transfer. Session 2 will elaborate on this, providing a complete explanation of how to compute realistic transfers costs.

Exercise 7. Complete Exercise 6, but this time using *LambertArc_ATD2021* function.

1. Resume from script implementing Exercise 6, save it as Ex7_session1.m

2. Implement function *LambertArc_ATD2021* as described in the class notes.

Note that this function will be used for the remaining of the course and it will be tested thoroughly. Often the inputs that may be tested may define transfers that are very far from optimal, and even with the continuation and correction procedures, it may not converge. Because of this reason, it would be good to add some extra checks and stops into your function.

3. Within the [while-loop](#) implement a safe check of the semimajor axis in case the orbit goes hyperbolic, which would make all the algorithmics not applicable.

```

while (norm(r2_iteration-r2)>ETolerance)&&(numIter<numMaxIter)
    (...)
    % checks and warnings:
    sma_seed=mu/2/(mu/r1_n-norm(r1dot_seed)^2/2);
    if sma_seed<0
        sma_seed
        warning('sma_seed error:The shooting method did not converge ')
        r1dot=[NaN NaN NaN];
        r2dot=[NaN NaN NaN];
        return
    end
end
end

```

4. Within the [for-loop](#) implement a check for the maximum number of iterations, and define a stop condition for the [while-loop](#) subject to a pre-defined number of iterations.

```
for iIter=1:nIterations
    % disp(['Starting Iteration ',num2str(iIter),' in Continuation Method'])
    Lamda=iIter/nIterations;
    DT=Lamda*ToF_target+(1-Lamda)*ToF_min;
    %-----
    % STEP 4: Shooting method
    ETolerance=1e-3; % 1 m miss match are allowed
    numMaxIter=25;
    numIter=0;
    r2_Iteration=0;
    while (norm(r2_Iteration-r2)>ETolerance)&&(numIter<numMaxIter) ...
    if numIter>numMaxIter
        numIter
        warning('numMaxIter issue:The shooting method did not converge')
        r1dot=[NaN NaN NaN];
        r2dot=[NaN NaN NaN];
        return
    end
end
end
%-----
```

5. Once the function *LambertArc_ATD2020* is implemented, proceed to compute the ΔV required to send ExoMars Trace Gas Orbiter to Mars at the required dates, and ensure it is the same as in Exercise 6.