

AVR ASM INTRODUCTION

AVR ASSEMBLER TUTOR

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2c. LOGARITHMS

BASIC AVR MATH III v1.2

LOGARITHMS & e

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The advantage of using integer math is the speed as versus the much slower speed and large size of floating-point math, however answers can be subject to larger rounding errors with integer math.

1. LOG BASE 2 OF A SINGLE-BYTE NUMBER

The integer value of logarithm base two of a number is useful in determining the number of bits required to store the number. The routine works by shifting the number left until a one falls out. The routine yields an error of about 1% and uses 10 to 40 clock cycles.

```
.DEF  ANSF = R0           ;Fractional Part of Answ
.DEF   ANS  = R1           ;Integer Part of Answer
```

```

.DEF      A = R16                ;Original Value
.DEF      N = R20                ;Counter/Index

      LDI A,100                  ;Load Original Value
      LDI N,7                    ;Initial log2 Value
      PUSH A                      ;Store Original Value
LOOP:   LSL A                    ;Shift Left until a one
      BRCS FINI                  ;
SKIP:   DEC N                    ;
      BRNE LOOP                  ;
FINI:   MOV ANS,N                ;Store the Integer Part
      MOV ANSF,A                ;Store Fractional Part
      POP A                      ;Restore Original Value

```

2. LOG BASE TWO OF A SIXTEEN-BIT NUMBER

We can expand the previous routine to handle 16-bit numbers. The routine uses 20 to 100 clock cycles and should have an error of about 0.1%.

```

.DEF      ANSF = R0               ;Fractional Part of Answ
.DEF      ANS = R1                ;Integer Part of Answer
.DEF      AL = R16                ;Original Value
.DEF      AH = R17                ;
.DEF      N = R20                ;Counter/Index

      LDI AL,LOW(10000)          ;Load Original Value
      LDI AH,HIGH(10000)         ;
      LDI N,15                   ;Initial log2 Value
      PUSH AL                    ;Store Original Value
      PUSH AH                    ;
LOOP:   LSL AL                   ;Shift Left until a one
      ROL AH                     ;
      BRCS FINI                  ;
SKIP:   DEC N                    ;
      BRNE LOOP                  ;
FINI:   MOV ANS,N                ;Store the Integer Part
      MOV ANSF,AH                ;Store Fractional Part
      POP AH                     ;Restore Original Value

```

```
POP AL ;
```

3. MULTIPLYING A SINGLE-BYTE NUMBER BY e

The value of e is 2.718281828. To estimate this with integer math we use the ratio 87/32 which is 2.71875 yielding an error of 0.017%. We first multiply our number by 87 then shift the result five times to the right for a division of 32. The routine is about 16 bytes long and takes about 28 clock cycles.

```
.DEF  ANSL = R0           ;Answer Low Byte
.DEF  ANSH = R1           ;Answer High Byte
.DEF  A = R16             ;Original Value
.DEF  B = R18             ;Workspace
.DEF  N = R20             ;Counter

        LDI A,100         ;Load Multiplier into A
        LDI B,87          ;Load Est of e = 87/32
        MUL A,B           ;
        LDI N,5           ;32 = 2^5
LOOP:   LSR ANSH           ;Divide result by 32
        ROR ANSL          ;
        DEC N             ;
        BRNE LOOP        ;
```

4. MULTIPLYING A SIXTEEN-BIT NUMBER BY e

To estimate the value of $e = 2.718281828$ we use the ratio 5567/2048 = 2.71826 which yields an error of 0.001%. The routine is about 40 bytes long and takes about 24 clock cycles.

```
.DEF  ANS1 = R0           ;Two Byte Answer
.DEF  ANS2 = R1           ;
.DEF  ZERO = R10          ;To hold Zero
.DEF  AL = R16            ;To hold multiplicand
.DEF  AH = R17            ;
.DEF  BL = R18            ;To hold multiplier
.DEF  BH = R19            ;
.DEF  WRK1 = R20          ;Workspace
```

```

.DEF WRK2 = R21          ;
.DEF WRK3 = R22          ;
.DEF WRK4 = R23          ;

        LDI AL,LOW(1000)  ;Load Original Value into
        LDI AH,HIGH(1000) ;
        LDI BL,LOW(5567)  ;Load multiplier into BH
        LDI BH,HIGH(5567) ;

MUL16x16:
        CLR ZERO          ;Set Zero
        MUL AH,BH          ;Multiply AH:AL by 5567
        MOVW WRK4:WRK3,R1:R0 ;
        MUL AL,BL          ;
        MOVW WRK2:WRK1,R1:R0 ;
        MUL AH,BL          ;
        ADD WRK2,R0        ;
        ADC WRK3,R1        ;
        ADC WRK4,ZERO      ;
        MUL BH,AL          ;
        ADD WRK2,R0        ;
        ADC WRK3,R1        ;
        ADC WRK4,ZERO      ;
        LSR WRK4           ;Ignore lower two bytes
        ROR WRK3           ;by 1024 and a shift make
        MOV ANS2,WRK4      ;Store Answer
        MOV ANS1,WRK3      ;By ignoring the lower two
                           ;get a division by 65536

```

5. MULTIPLYING A SINGLE-BYTE NUMBER BY

1/e

The number $1/e = 0.367879441$ can be estimated with the ratio $94/256$ which is 0.36719 with an error of 0.19% . The routine is about 6 bytes long and takes about 2 clock cycles.

```

.DEF ANSL = R0          ;Fractional Low Byte (Ignore)
.DEF ANS = R1           ;Answer
.DEF A = R16            ;Original Value
.DEF B = R18            ;Workspace
.DEF N = R20            ;Counter

```

```

LDI A,100          ;Original Value
LDI B,94           ;Load Est of e = 94/256
MUL A,B           ;Multiply Original Value

```

6. MULTIPLYING A SIXTEEN-BIT NUMBER BY 1/e

The constant $1/e = 0.367879441$ can be estimated by the ratio $24109/65536 = 0.36787$ with an error of 0.001%. The routine is about 36 bytes long and takes about 20 clock cycles.

```

.DEF ANS1 = R0      ;Two Byte Answer
.DEF ANS2 = R1
.DEF ZERO = R10     ;To hold Zero
.DEF AL = R16        ;Original Value
.DEF AH = R17        ;
.DEF BL = R18        ;To hold multiplier
.DEF BH = R19        ;
.DEF WRK1 = R20      ;Workspace
.DEF WRK2 = R21      ;
.DEF WRK3 = R22      ;
.DEF WRK4 = R23      ;

LDI AL,LOW(1000)     ;Load Original Value int
LDI AH,HIGH(1000)    ;
LDI BL,LOW(24109)    ;Load multiplier into BH
LDI BH,HIGH(24109)   ;

```

MUL16x16:

```

CLR ZERO            ;Set Zero
MUL AH,BH           ;Multiply Original Value
MOVW WRK4:WRK3,R1:R0 ;
MUL AL,BL           ;
MOVW WRK2:WRK1,R1:R0 ;
MUL AH,BL           ;
ADD WRK2,R0         ;
ADC WRK3,R1         ;
ADC WRK4,ZERO       ;
MUL BH,AL           ;

```

```

ADD WRK2,R0      ;
ADC WRK3,R1      ;
ADC WRK4,ZERO    ;
MOV ANS2,WRK4    ;Store Answer
MOV ANS1,WRK3    ;By ignoring the lower t
                  ;get a division by 65536

```

7. NATURAL LOGARITHM OF A SINGLE-BYTE NUMBER

Previously we created routines to calculate the log base two of a number. From the equations below we see that by multiplying the log₂ of a number by 0.6931472 we can calculate the natural logarithm.

$$\begin{aligned}
 \ln(x) &= \log_2(x) / \log_2(e) \\
 &= \log_2(x) * 1/1.442695 \\
 &= \log_2(x) * 0.6931472 \\
 &= C * \log_2(x) ; \text{ where } C = 0.6931472
 \end{aligned}$$

We will use the following ratios to estimate the constant above.

$$C = 177/256 = 0.69141 \text{ Error } 0.24\%$$

The routine is about 40 bytes long and uses about 50 to 80 clock cycles the error should be less than 1%.

```

.DEF ANSF = R2      ;Fractional Part of Answ
.DEF ANS = R3       ;Integer Part of Answer
.DEF A = R16        ;Original Value
.DEF N = R20        ;Counter/Index

        LDI A,250    ;Load Original Value
        LDI N,7      ;Initial log2 Value
        PUSH A       ;Store Original Value
LOOP:   LSL A         ;Shift Left until a one
        BRCS FINI    ;
SKIP:   DEC N         ;
        BRNE LOOP    ;
FINI:   MOV ANS,N     ;Store the Integer Part
        MOV ANSF,A    ;Store Fractional Part
        LDI A,177    ;Multiply by 177 then

```

```

MUL16x8:MUL ANSF,A           ;divide by 256 by ignori
      MOV ANSF,R1           ;lowest byte of the resu
      MUL ANS,A             ;
      CLR ANS               ;
      ADD ANSF,R0           ;
      ADC ANS,R1            ;
      POP A                 ;Restore Original Value

```

8. NATURAL LOGARITHM OF A SIXTEEN-BIT NUMBER

Previously we created routines to calculate the log base two of a number. From the equations below we see that by multiplying the log₂ of a number by 0.6931472 we can calculate the natural logarithm.

$$\begin{aligned}
 \ln(x) &= \log_2(x) / \log_2(e) \\
 &= \log_2(x) * 1/1.442695 \\
 &= \log_2(x) * 0.6931472 \\
 &= C * \log_2(x) ; \text{ where } C = 0.6931472
 \end{aligned}$$

We will use the following ratio to estimate the constant above.

$$C = 45426/65536 = 0.69315 \text{ Error} = 0.0004\%$$

The routine is about 70 bytes long and takes about 40 to 120 clock cycles.

```

.DEF ANSF = R2           ;Fractional Part of Answ
.DEF ANS = R3            ;Integer Part of Answer
.DEF TMP1 = R4           ;Temporary Workspace
.DEF TMP2 = R5           ;
.DEF TMP3 = R6           ;
.DEF TMP4 = R7           ;
.DEF ZERO = R10          ;Hold Zero
.DEF AL = R16            ;Original Value
.DEF AH = R17            ;
.DEF N = R20             ;Counter/Index

      LDI AL,LOW(65000)   ;Load Original Value
      LDI AH,HIGH(65000)  ;
      LDI N,15            ;Initial log2 Value

```

```

        PUSH AL                ;Store Original Value
        PUSH AH                ;
LOOP:   LSL AL                  ;Shift Left until a one
        ROL AH                  ;
        BRCS FINI              ;
SKIP:   DEC N                   ;
        BRNE LOOP              ;
FINI:   MOV ANS,N               ;Store the Integer Part
        MOV ANSF,AH            ;Store Fractional Part
        LDI AL,LOW(45426)       ;Multiply by 45426
        LDI AH,HIGH(45426)      ;Then divide by 65536 by
MUL16x16:                                ;the lowest two bytes
        CLR ZERO
        MUL ANS,AH              ;
        MOVW TMP4:TMP3,R1:R0    ;
        MUL ANSF,AL             ;
        MOVW TMP2:TMP1,R1:R0    ;
        MUL ANS,AL              ;
        ADD TMP2,R0              ;
        ADC TMP3,R1              ;
        ADC TMP4,ZERO            ;
        MUL ANSF,AH             ;
        ADD TMP2,R0              ;
        ADC TMP3,R1              ;
        ADC TMP4,ZERO            ;
        MOVW ANS:ANSF,TMP4:TMP3 ;Store Answer
        POP AH                  ;Restore Original Value
        POP AL                  ;

```

9. LOG BASE 10 OF A SINGLE-BYTE NUMBER

Previously we created routines to calculate the log base two of a number. From the equations below we see that by multiplying the log₂ of a number by 0.301030004 we can calculate the logarithm base 10.

$$\begin{aligned}
 \log_{10}(x) &= \log_2(x) / \log_2(10) \\
 &= \log_2(x) * 1/3.321928 \\
 &= \log_2(x) * 0.301030004 \\
 &= C * \log_2(x) ; \text{ where } C = 0.301030004
 \end{aligned}$$

We will use the following ratio to estimate the constant above.

$$C = 77/256 = 0.30078 \text{ Error} = 0.08\%$$

The routine is about 40 bytes long and takes about 20 to 50 clock cycles.

```
.DEF  ANSF = R2           ;Fractional Part of Answ
.DEF   ANS = R3           ;Integer Part of Answer
.DEF    A = R16           ;Original Value
.DEF    N = R20           ;Counter/Index

        LDI A,250         ;Load Original Value
        LDI N,7           ;Initial log2 Value
        PUSH A            ;Store Original Value
LOOP:   LSL A              ;Shift Left until a one
        BRCS FINI         ;
SKIP:   DEC N              ;
        BRNE LOOP        ;
FINI:   MOV ANS,N          ;Store the Integer Part
        MOV ANSF,A        ;Store Fractional Part
        LDI A,77          ;Multiply by 77 then
MUL16x8:MUL ANSF,A        ;divide by 256 by ignori
        MOV ANSF,R1       ;lowest byte of the resu
        MUL ANS,A         ;
        CLR ANS           ;
        ADD ANSF,R0       ;
        ADC ANS,R1        ;
        POP A             ;Restore Original Value
```

10. LOG BASE 10 OF A SIXTEEN-BIT NUMBER

Previously we created routines to calculate the log base two of a number. From the equations below we see that by multiplying the log2 of a number by 0.301030004 we can calculate the logarithm base 10.

$$\begin{aligned}\log_{10}(x) &= \log_2(x)/\log_2(10) \\ &= \log_2(x) * 1/3.321928 \\ &= \log_2(x) * 0.301030004 \\ &= C * \log_2(x) ; \text{ where } C = 0.301030004\end{aligned}$$

We will use the following ratio to estimate the constant above.

$$C = 19728/65536 = 0.30103 \text{ Error} = 0.00000$$

The routine is about 70 bytes long and takes about 40 to 125 clock cycles.

```
.DEF  ANSF = R2           ;Fractional Part of Answ
.DEF   ANS = R3           ;Integer Part of Answer
.DEF  TMP1 = R4           ;Workspace
.DEF  TMP2 = R5           ;
.DEF  TMP3 = R6           ;
.DEF  TMP4 = R7           ;
.DEF  ZERO = R10          ;Hold Zero
.DEF   AL = R16           ;Original Value
.DEF   AH = R17           ;
.DEF   N = R20            ;Counter/Index

                                LDI AL,LOW(65000) ;Load Original Value
                                LDI AH,HIGH(65000) ;
                                LDI  N,15         ;Initial log2 Value
                                PUSH AL           ;Store Original Value
                                PUSH AH           ;
LOOP:  LSL AL               ;Shift Left until a one
        ROL AH              ;
        BRCS FINI          ;
SKIP:  DEC N                ;
        BRNE LOOP          ;
FINI:  MOV ANS,N            ;Store the Integer Part
        MOV ANSF,AH         ;Store Fractional Part
        LDI AL,LOW(19728)   ;Multiply by 19728
        LDI AH,HIGH(19728)  ;Then divide by 65536 by
MUL16x16:                                ;the two lowest bytes
        CLR ZERO            ;
        MUL ANS,AH           ;
        MOVW TMP4:TMP3,R1:R0 ;
        MUL ANSF,AL          ;
        MOVW TMP2:TMP1,R1:R0 ;
        MUL ANS,AL           ;
        ADD TMP2,R0          ;
        ADC TMP3,R1          ;
        ADC TMP4,ZERO        ;
        MUL ANSF,AH          ;
```

```
ADD TMP2,R0      ;  
ADC TMP3,R1      ;  
ADC TMP4,ZERO    ;  
MOVW ANS:ANSF,TMP4:TMP3 ;Store Answer  
POP AH           ;Restore Original Value  
POP AL           ;
```

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