# Modelling\_Assignment\_2

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# 1 Modelling Assignment 2: UBC Blue Chip Cafe

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## 1.1 Problem Statement

Model the annual revenue for Blue Chip Cafe based on temperature and precipitation data.

## 1.2 Variables and Parameters

Description	Symbol	Dimension	Type
the total daily customers	С	1	Dependent Variable
the average daily	${ m T}$	$^{\circ}\mathrm{C}$	Independent Variable
temperature			
the total daily precipitation	P	mm of water	Independent Variable
the reference number of	$C_0$	1	Parameter
customers			
the reference daily	$T_0$	$^{\circ}\mathrm{C}$	Parameter
temperature			
the reference precipitation	$P_0$	mm of water	Parameter
Rate of change of customers	a	$1/^{\circ}\mathrm{C}$	Parameter
with respect to temperature			
Rate of change of customers	b	$1/\mathrm{mm}$ of water	Parameter
with respect to precipitation			
price of one drinks	$P_d$	Dollars	Parameter
price of one cookies	$P_c$	Dollars	Parameter
cost of one drinks	$K_d$	Dollars	Parameter
cost of one cookies	$K_c$	Dollars	Parameter

## 1.3 Assumptions and Constraints

We use the online menu of Blue Chip Cafe to get the prices of products. We take averages, resulting in \$ 5.12 per drink and \$ 3.00 per cookie.

- The prices of items are the same from 1997 to 2022.
- The prices of all kinds of cookies are the same and equal to 3 dollars.
- The prices of all kinds of drinks are the same and equal to 5.12 dollars.

- Each customer only purchases 1 pastry and 1 drink, so they spend 8.12 dollars.
- There are no disruptions to service.
- The cost of making one cup of coffee is \\$1.84, including the cost of coffee, milk, water, work of an employee, electricity, and rentals. The price for cookies is \\$1.896 (Arias, 2024).
- The business always has more cookies and drinks available to sell.
- Opening hours are the same for the entire period.
- Only weather (temperature and precipitation) influences the amount of customers served.
- The number of customers has the form  $C(T,P) = \max\{C(T,P),0\}, c(T,P) = C_0 + a(T-T_0) b(P-P_0).$

# 1.4 Building Solutions

We first estimate the a and b parameters for our model. We then calculate daily revenue (money spent per customer times total customers served) and annual revenue (sum of daily revenue for every day in the year).

```
[]: #import packages
import numpy as np; import matplotlib.pyplot as plt
import pandas as pd; import statsmodels.api as sm
import scipy.stats as stats
%matplotlib inline

customer = pd.read_csv('customer.csv')
weather = pd.read_csv('vancouver_weather.csv')

T = weather['avg_temperature']; P = weather['precipitation']
T0 = np.mean(T); P0 = np.mean(P)
C0 = np.sum(customer['Monthly_Frequency_Customers'])/31 # Daily average
```

- We choose T<sub>0</sub> and P<sub>0</sub> as the mean temperature and precipitation from 1997 to 2022, as the
  mean is a representative measure of the data and centers the models around the most common
  weather conditions.
- As for  $C_0$ , we sum the customer numbers in the given data and divide by 31 to obtain the daily reference customer count, making it easier to analyze how changes in weather impact customer behavior.

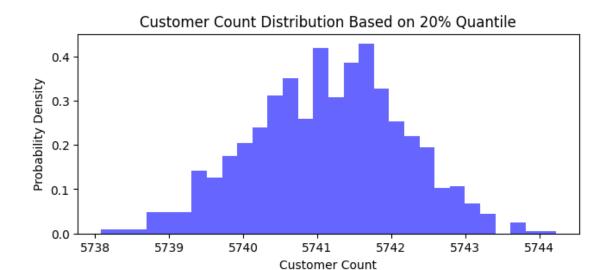
```
[]: ## Customers function
    c = lambda t,p: C0 + a*(T0 - t) - b*(p - P0)

def Customers_in_period(temp,pre):
    customs = []
    for k in range(len(temp)):
        DayCustomer = max(c(temp[k],pre[k]),0)
        customs.append(DayCustomer)
    return customs
```

### 1.4.1 Adjusting a and b

- We can find a using  $\Delta C/\Delta T$ . Given the customer count data for March 2024, we assume a 20% quantile for March and build a normal distribution based on this assumption. We consider a normal distribution appropriate because customer counts generally increase with temperature, peaking around June and July and decreasing in January and December, as shown in the graph above. Next, we calculate the difference between the tail and head values, denoted as  $\Delta C$ . Then, we group the weather data by year and month to obtain the monthly temperature difference, which we multiply by 12 to estimate the yearly temperature change,  $\Delta T$ .
- We find b in a similar way for  $\Delta C/\Delta P$ .

```
[]: # Given customer count in March
     customers march = C0*31
     # Assuming 5742.0 is the 20th percentile in a normal distribution
     quantile = 0.20
     # Calculate the mean and standard deviation for the distribution
     # We assume a standard normal distribution, then solve for the parameters
     mean, std dev = stats.norm.ppf(quantile, loc=customers_march, scale=1), 1 #__
      start with std deviation as 1
     # Adjust to reflect the assumption based on 20th quantile
     std_dev = (mean - customers_march) / stats.norm.ppf(quantile)
     # Generate a normal distribution based on these parameters
     distribution = np.random.normal(loc=mean, scale=std_dev, size=1000)
     plt.figure(figsize=(7.5, 3))
     plt.hist(distribution, bins=30, density=True, alpha=0.6, color='b')
     plt.title("Customer Count Distribution Based on 20% Quantile")
     plt.xlabel("Customer Count"); plt.ylabel("Probability Density")
     plt.show()
```



We found a and b to be approximately 2.9 and 0.99, respectively. We now use the customer data (total monthly customers and daily average) to compare the a and b parameters. We take weather data from March of 2022, as it is the most recent available.

```
[]: # Select data for period
March_22 = weather[weather['year'] == 2022]
March_22 = March_22[March_22['month'] == 3]
T_22_03 = March_22['avg_temperature']; P_22_03 = March_22['precipitation']
C_March_24 = customer['Monthly_Frequency_Customers']
T_22_03 = np.array(T_22_03.tolist()); P_22_03 = np.array(P_22_03.tolist())
C_March_24 = np.array(C_March_24.tolist())

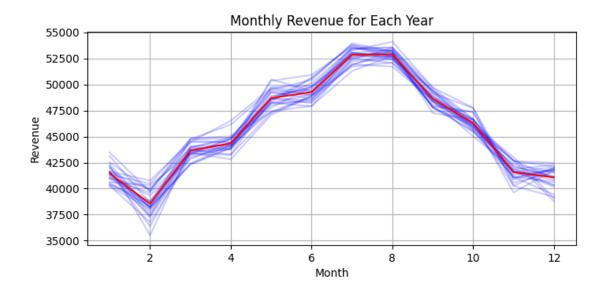
a = 2.9; b = 0.99 # Estimates for parameters

# Make simulation
Customers_tune = Customers_in_period(T_22_03,P_22_03)
Month_customs_22_03 = np.round(np.sum(Customers_tune))
Day_avg_22_03 = np.mean(Customers_tune)
print('Estimates: ', Month_customs_22_03, ',', Day_avg_22_03)
print('Actual values: ',np.sum(C_March_24),',',np.sum(C_March_24)/31)
```

Estimates: 5991.0 , 193.26674222762722 Actual values: 5742 , 185.2258064516129

#### 1.4.2 Revenue Function

```
[]: def period_revenue(data):
         T = data['avg_temperature']
         P = data['precipitation']
         c = C0 + a*(T - T0) - b * (P - P0)
         c = np.maximum(c,0)
         rev = np.sum(c) * 8.12
         return rev
     monthly_revenue = {} # Calculate revenue per month
     for year in range(1997, 2023):
         yearly_data = weather[weather['year'] == year]
         monthly_data = yearly_data.groupby('month')
         monthly_revenue[year] = {month: period_revenue(month_data) for month,_
      month_data in monthly_data}
     # Convert monthly revenue to DataFrame for easier plotting
     monly_rev_df = pd.DataFrame(monthly_revenue).T
     plt.figure(figsize=(8, 3.5)) # Plot revenue for each year
     for year in monly rev df.index:
         plt.plot(monly_rev_df.columns,monly_rev_df.loc[year],color='blue',alpha=0.2)
     ## monthly_average
     monthly_avg = [np.mean(monly_rev_df[month]) for month in monly_rev_df.columns]
     monly_rev_df.loc['Month_Average'] = monthly_avg
     plt.plot(monly_rev_df.columns, monly_rev_df.loc['Month_Average'], color = 'red')
     plt.xlabel('Month'); plt.ylabel('Revenue'); plt.grid()
     plt.title('Monthly Revenue for Each Year')
     plt.show()
```



```
[]: ## Calculate for annual revenue
monly_rev_df['annual'] = pd.DataFrame.sum(monly_rev_df,axis=1)
Ann_rev = monly_rev_df['annual']
Ann_rev = Ann_rev.tolist()
Anual_avg = Ann_rev[-1]
Annual_min = np.min(Ann_rev); Annual_max = np.max(Ann_rev)
print(Anual_avg, Annual_min, Annual_max)
```

549319.3298263026 544184.8399147275 557449.4755982199

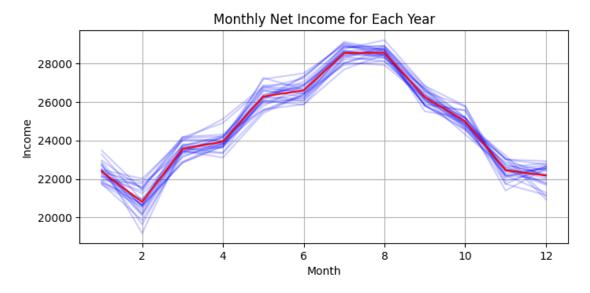
### 1.4.3 Income Function

```
monly_rev_df = pd.DataFrame(monthly_income).T

plt.figure(figsize=(8, 3.5)) # Plot revenue for each year
for year in monly_rev_df.index:
    plt.plot(monly_rev_df.columns,monly_rev_df.loc[year],color='blue',alpha=0.2)

## monthly_average
monthly_avg = [np.mean(monly_rev_df[month]) for month in monly_rev_df.columns]
monly_rev_df.loc['Month_Average'] = monthly_avg
plt.plot(monly_rev_df.columns, monly_rev_df.loc['Month_Average'], color = 'red')

plt.xlabel('Month'); plt.ylabel('Income'); plt.grid()
plt.title('Monthly Net Income for Each Year')
plt.show()
```



```
[]: ## Calculate annual profits
monly_rev_df['annual'] = pd.DataFrame.sum(monly_rev_df,axis=1)
Ann_rev = monly_rev_df['annual']
Ann_rev = Ann_rev.tolist()
Anual_avg = Ann_rev[-1]
Annual_min = np.min(Ann_rev); Annual_max = np.max(Ann_rev)
print(Anual_avg, Annual_min, Annual_max)
```

296578.31797518604 293806.1992840105 300967.79569243797

# 1.5 Analyze and Assess

# 1.5.1 Monthly Net Income and Revenue Analysis

The average monthly net income starts out at around 32,000 dollars per month in January and reaches the lowest point in Feburary at around 30,000 dollars. Feburary's net income also has more variance in revenue than revenues on other months. The net income steadily increases from the month of Feburary to August. The net income at the month of July and August is the highest point at around \$41,000. Then, the income decreases overtime from the month of August to December. The value of the income in the month of December is similar to the monthly income on January.

One reason the net revenue on December, January, Feburary are low could be due to colder weather and snow, which deters students from going to Blue Chip to buy coffee. While the month of June, July, and August, are summer time so more students would go out and buy coffee from Bluechip. The monthly revenue follows a very similar trend with the monthly net income except with higher value. This is because monthly net income is the monthly revenue prior to subtracting the operation costs. We are assuming the operation costs are constant throughout the month.

Janurary, Feburary, and December are times when the business is the least profitable while the Month of July and August is when our business is the most profitable. We could consider decreasing the price of our items on Feburary to attract more customers and increasing the price of the items on July and August to maximize profit. In addition, we could shift the price of our items up in other months where the business is profitable and decreases the price of item on months where they aren't that profitable.

For the annual revenue, the average annual revenue is 549,319.3 dollars. The maximum annual revenue is 544,184.8 dollars. The minimum annual revenue is 557,449.5 dollars. The annual profit is the annual revenue minus the operation cost. For the annual profit, the average annual profit is 296,578 dollars. The maximum annual profit is 300,967 dollars. The minimum annual profit 293,806 dollars.

#### 1.6 Conclusions

- More advanced models could include the customer choice for what and how many products to purchase, the associated costs for the cafe for each item sold (ingredients, paper cups, etc.), or varying prices for the menu items throughout time.
- For an advanced model, we could consider a more realistic menu and adding uncertainty to price of goods to show a range of the expense each customer spents at the coffee.

## 1.7 References

- 1. UBC Food services. *Blue Chip Cookies*. UBC Student Housing and Community Services. https://food.ubc.ca/places/blue-chip-cafe/
- 2. Contributor, & By. (1970, November 30). How much does your coffee cost?. Coffee Ti Magazine. http://www.coffeeteaimagazine.com/how-much-does-your-coffee-cost/#:~:text=To%20prepare%20one%20cup%20of,rise%20up%20to%2050%20cents.
- 3. Arias, T. (2024, October 14). Cheap vs. expensive ingredients in chocolate chip cookies. Handle the Heat. https://handletheheat.com/cheap-vs-expensive-cookies/

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