Research Article

Dynamic and Kinematic Models and Control for Differential Drive Mobile Robots

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Abstract

The two-wheel differential drive mobile robots, are one of the simplest and most used structures in mobile robotics applications, it consists of a chassis with two fixed and in-line with each other electric motors. This paper presents new models for differential drive mobile robots and some considerations regarding design, modeling and control solutions. The presented models are to be used to help in facing the two top challenges in developing mechatronic mobile robots system; early identifying system level problems and ensuring that all design requirements are met, as well as, to simplify and accelerate Mechatronics mobile robots design process, including proper selection, analysis, integration and verification of the overall system and sub-systems performance throughout the development process.

Keywords: Wheeled Mobile Robot, Electric motor, Differential drive, Mathematical and simulink models.

1. Introduction

Mobile robot is a platform with a large mobility within its environment (air, land, underwater) it is not fixed to one *physical location*. Mobile robots have potential application in industrial and domestic applications. Accurate designing and control of mobile robot is not a simple task in that operation of a mobile robot is essentially time-variant, where the operation parameters of mobile robot, environment and the road conditions are always varying, therefore, the mobile robot as whole including controller should be designed to make the system robust and adaptive, improving the system on both dynamic and steady state performances. one of the simplest and most used structures in mobile robotics applications, are the two-wheel differential drive mobile robots (Figure 1), it consists of a chassis with two fixed and in-lines with each other electric motors and usually have one or two additional third (or forth) rear wheel(s) as the third fulcrum, in case of one additional rear wheel, this wheel can rotate freely in all directions, because it has a very little influence over the robot's kinematics, its effect can be neglected.

Different researches studied different separate aspects of mobile robot design, modeling and control including; (Ahmad A. Mahfouz et al, 2012) studied Modeling, simulation and dynamics analysis issues of electric motor,

in terms of output speed for mechatronics applications, (Ahmad A. Mahfouz et al, 2013) introduce Mechatronics Design of a Mobile Robot System with overall system modeling and controller selection, in (Bashir M. Y. Nouri , 2005) proposed modeling and control of mobile robot, (Jaroslav Hanzel et al, 2011)studied computer aided design of mobile robotic system controlled remotely by computer, (Emese Sza´et al , 2004) addresses design and control issues of a simple two degrees of freedom positioning device. (M.B.B. Sharifian et al , 2009) present design and implementation of a PC-based DC motor velocity system using both special optimal control and PID, (Gregor Klanˇcar et al , 2005) present a control design of a nonholonomic mobile robot with a differential drive, (Tao Gong et al, 2003) discuss architecture, characteristics and principle of mobile immune-robot model are, (Aye Aye Nwe et al, 2008) introduce software implementation of obstacle detection for wheeled mobile robot, avoidance system, (Mircea Niţulescu ,2007)introduce some considerations regarding mathematical models and control solutions for two-wheel differential drive mobile robots, (J. R. Asensio et al, 2002) to control the motion, a model for motion generation of differential-drive mobile robots is introduced, the model takes into account the robot kinematic and dynamic constraint. This paper presents a new kinematics and dynamics models for differential drive mobile robots a long with main considerations regarding design, modeling and control solutions.

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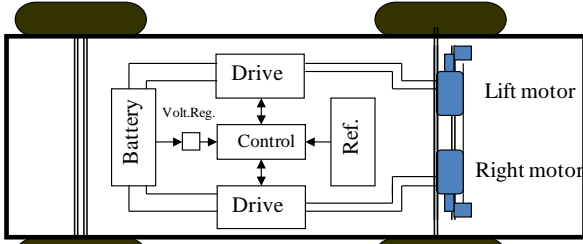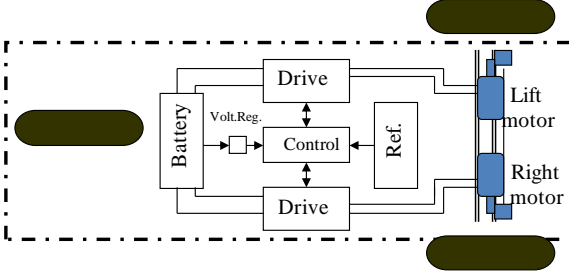
Fig.1(a)

Fig. 1 (b)

Fig. 1(a)(b) Mobile platform and circuit, one and four castor wheels; top view.

2. Mathematical modeling

The actuating machines most used in mechatronics motion control systems are DC machines (motors). The mobile platform motion control can be simplified to a DC motor motion control. In modeling DC motors and in order to obtain a linear model, the hysteresis and the voltage drop across the motor brushes is neglected, the motor input voltage, V_{in} maybe applied to the field or armature terminals (Richard C. Dorf et al , 2001), in this paper we will consider PMDC motor as electric actuator. (Ahmad A. Mahfouz et al , 2013) introduce a detailed derivation of mobile robotic platform model, including modeling of the basic electric motor modeling, as well as, simulink model and function block with its function block parameters window. Considering that system dynamics and disturbance torques depends on platform shape and dimensions, as well as, environment and the road conditions.

2.1 Basic electric motor modeling

The PMDC motor open loop transfer function without any load attached relating the input voltage, $V_{in}(s)$, to the output angular velocity, $\omega(s)$, is given by Eq(1). The total equivalent inertia, J_{equiv} and total equivalent damping, b_{equiv} at the armature of the motor are given by Eq(2), for simplicity, the mobile robot can be considered to be of cuboide shape, with the inertia calculated by Eq(3),correspondingly, the equivalent mobile robot system transfer function with gear ratio, n, is given by Eq(4):

$$G_{speed}(s) = \frac{\omega(s)}{V_{in}(s)} = \frac{K_t}{\{[(L_a s + R_a)(J_m s + b_m) + K_t K_b]\}} =$$

$$= \frac{K_t}{[(L_a J_m)s^2 + (R_a J_m + b_m L_a)s + (R_a b_m + K_t K_b)]} \quad (1)$$

$$b_{equiv} = b_m + b_{Load}\left(\frac{N_1}{N_2}\right)^2$$

$$J_{equiv} = J_m + J_{Load}\left(\frac{N_1}{N_2}\right)^2 \quad (2)$$

$$J_{load} = \frac{bh^3}{12} \quad (3)$$

$$G_{speed}(s) = \frac{\omega_{robot}(s)}{V_{in}(s)} =$$

$$= \frac{K_t / n}{[(L_a J_{equiv})s^2 + (R_a J_{equiv} + b_{equiv} L_a)s + (R_a b_{equiv} + K_t K_b)]} \quad (4)$$

2.2 Sensor modeling

Tachometer is a sensor used to measure the actual output angular speed, ω_L, Dynamics of tachometer and the transfer function can be represented using the following equation:

$$V_{out}(t) = K_{tac} * \frac{d\theta(t)}{dt} \Rightarrow V_{out}(t) = K_{tac} * \omega$$

$$K_{tac} = V_{out}(s) / \omega(s) \quad (5)$$

Tachometer constant: we are to drive our robotic platform system, with linear velocity of 0.5 m/s, the angular speed is obtained as: $\omega = V/r = 0.5/0.075 = 6.6667$ rad / s, therefore, the tachometer constant, for $\omega = 6.6667$, is given as: $K_{tac} = 12 / 6.6667 = 1.8$

2.3 Accurate dynamics modeling of mobile robotic Platform.

When deriving an accurate mathematical model for mobile system it is important to study and analyze dynamics between the road, wheel and platform considering all the forces applied upon the mobile platform system. (Farhan A. Salem , 2013) introduce accurate modeling and simulation of mobile robotic platform dynamics, including most acting forces that is categorized into road-load and tractive force. The road-load force consists of the gravitational force, hill-climbing force, rolling resistance of the tires , the aerodynamic drag force and the aerodynamics lift force, where aerodynamic drag force and rolling resistance is pure *losses*, meanwhile the forces due to climbing resistance and acceleration are conservative forces with possibility to, partly, recover. Based on equations derived by (Farhan A. Salem , 2013), that describes DC motor system dynamics and sensor modeling, the next open loop transfer function, relating the armature input terminal voltage, $V_{in}(s)$ to the output terminal voltage of the tachometer $V_{tach}(s)$, with most load torques applied are considered:

$$G_{open}(s)\frac{V_{in}(s)}{V_{tach}(s)} =$$

$$= \frac{K_{tach} * K_t}{(L_a s + R_a)(J_m s + b_m) + (L_a s + R_a)(T) + K_b K_t}$$

Where: T the disturbance torque, all torques including coulomb friction, substituting and solving gives equation (6) written in the 7th page of this paper:

2.3 Controller selection and design.

Different resources introduce different methodologies and approaches for mobile robot modeling and controller design, for instant; in (Bashir M. Y. Nouri ,2005), introduced and tested Modeling and control of mobile robot using deadbeat response, by (J. R. Asensio et al, 2002) different control strategies are used and tested for Modeling and controller design of basic used DC motor speed control. Since we are most interested in dynamics, modeling and simulation, we will apply only PID controller, this control block can be replaced with any other controller type. PID controllers are ones of most used to achieve the desired time-domain behavior of many different types of dynamic plants. The sign of the controller's output, will determine the direction in which the motor will turn. The PID gains (K_P, K_I, K_D) are to be tuned experimentally to obtain the desired overall desired response. The PID controller transfer function is given by:

$$G_{PID} = K_P + \frac{K_I}{s} + K_D = \frac{K_D s^2 + K_P s + K_I}{s} = K_D \left[s^2 + \frac{K_P}{K_D} s + \frac{K_I}{K_D} \right] / s$$

2.4 Differential drive Kinematics and dynamics modeling

To characterize the current localization of the mobile robot in its operational space of evolution a 2D plane (x,y), we must define first its position and its orientation. Assuming the angular orientation (direction) of a wheel is defined by angle θ, between the instant linear velocity of the mobile robot v and the local vertical axis as shown in Figure 2(a). The linear instant velocity of the mobile robot v , is a result of the linear velocities of the left driven wheel v_L and respectively the right driven wheel v_R . These two drive velocities v_L and v_R are permanently two parallel vectors and, in the same time, they are permanently perpendicular on the common mechanical axis of these two driven wheels.

When a wheel movement is restricted to a 2D plane (x,y), and the wheel is free to rotate about its axis (x axis), the robot exhibits preferential rolling motion in one direction (y axis) and a certain amount of lateral slip (Figure 2(a)(b)) , the wheel movement (speed) is the product of wheel's radius and angular speed and is directly proportional by the angular velocity of the wheel, and given by:

$$\dot{x} = r\dot{\varphi} \Leftrightarrow v = r\omega$$

Where: φ: wheel angular position. Referring to Figure 2(c) ,while the wheel is following a path and having no slippery conditions, the velocity of the wheel at a given time, has two velocity components with respect to coordinate axes X and Y.

$$r\omega = -\upsilon_x \sin\theta + \upsilon_y \cos\theta$$
$$0 = \upsilon_x \cos\theta + \upsilon_y \sin\theta$$
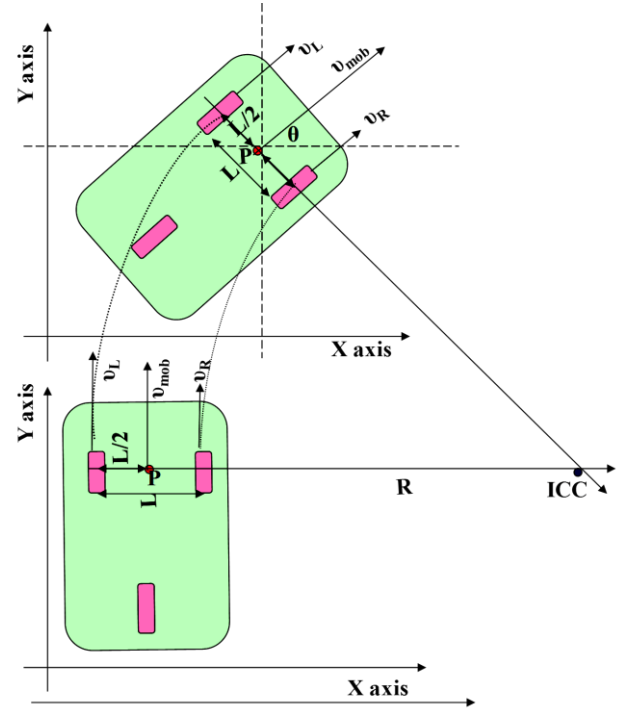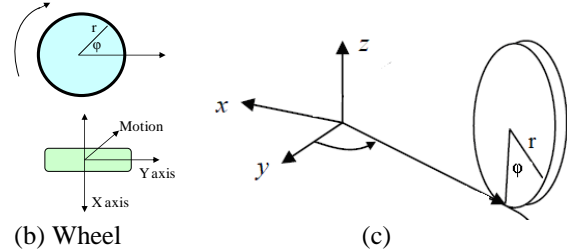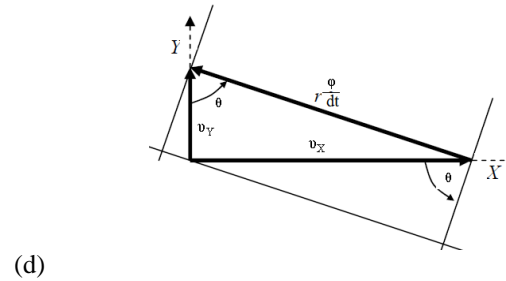

Fig.2(a) The differential drive motion

(b) Wheel   (c)

(d)

Fig. 2(a)(b)(c) Wheel movement kinematics
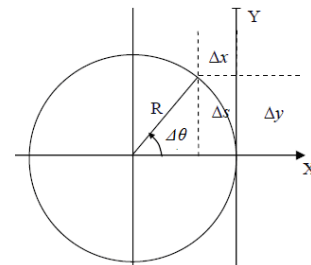

Fig. 3 circumference movement of mobile robot (Jaroslav Hanzel, 2011)

Assuming the mobile robot follows a circular trajectory shown in Figure 3, and *Δs* , *Δθ* and *R* are the arc distance traveled by the wheel, and its respective orientation with

255

respect to the global coordinates, *and R* is the circumference radius of the wheel, then the linear and angular velocities of the mobile robot are given by

$$\upsilon = \Delta s / \Delta t \iff \omega = \Delta \theta / \Delta t$$

The arc distance *Δs* traveled in time equal to *Δt*, is given by $\Delta s = R \Delta \theta$, and the curvature, that is the inverse of the radius *R* is given by $\lambda = 1/R$, referring to Figure3, the movement equation in the initial position are given by Eq.(7), these coordinate equations can be extended by their rotating, which result in Eq.(8), assuming the time is so small, then we have; $\cos(\Delta \theta) \cong 1$ and $\sin(\Delta \theta) \cong \Delta \theta$, substituting in Eq(8) , will result in Eq.(9):

$$\Delta x = R \left(\cos(\Delta \theta) - 1 \right)$$
$$\Delta y = R (\sin(\Delta \theta)) \tag{7}$$

$$\Delta x = R \left(\cos(\Delta \theta) - 1 \right) \cos \theta - R \sin(\Delta \theta) \sin \theta$$
$$\Delta y = R (\sin(\Delta \theta)) - 1) \sin \theta + R \sin(\Delta \theta) \cos \theta \tag{8}$$

$$\Delta x = -R \Delta \theta \sin(\theta)$$
$$\Delta y = R \Delta \theta \cos(\theta) \tag{9}$$

Substituting R, from the arc distance, $\Delta s = R \Delta \theta \Rightarrow R = \Delta s / \Delta \theta$, and dividing both sides by *Δt,* we have:

$$\Delta x = -\Delta s \sin(\theta) \Rightarrow \frac{\Delta x}{\Delta t} = \frac{-\Delta s \sin(\theta)}{\Delta t} \iff \upsilon_x = -\upsilon \sin(\theta)$$
$$\Delta y = \Delta s \cos(\theta) \Rightarrow \frac{\Delta y}{\Delta t} = \frac{-\Delta s \cos(\theta)}{\Delta t} \iff \upsilon_y = -\upsilon \cos(\theta) \tag{10}$$

The instantaneous center of curvature (ICC), (Figure 2(a)) is the point the robot must rotate around it, to avoid slippage and have only a pure rolling motion, ICC lies on the common axis of the two driving wheels. In case of differential drive, by changing the velocities υ_L and υ_R of the two Left and Right wheels, the ICC of rotation will move and different trajectories will be followed, at each time Left and Right wheels, moves around the ICC with the same angular speed rate, given by:

$$\omega = \frac{d\theta}{dt} \iff \omega R = \upsilon_{mob}$$

Referring to Figure 2(a) The right and left wheels linear velocities in terms of mobile angular speed are given by

$$\upsilon_L = \omega_{mob} \left(R + \frac{L}{2} \right) \iff \upsilon_R = \omega_{mob} \left(R - \frac{L}{2} \right) \tag{11}$$

Where*: R* is the distance from the ICC point to the midpoint P, between the two wheels, and can be found by:

$$R = \frac{\upsilon_R + \upsilon_L}{\upsilon_R - \upsilon_L} * \frac{L}{2} \tag{12}$$

Because the vectors for linear speed of wheels υ_L and υ_R are orthogonal on the common axis of the driven wheels,

we can write an equation to represent the angular velocity of the robot:

$$\omega = \frac{\upsilon_R - \upsilon_L}{L} = \frac{(\omega_R - \omega_L) r}{L} \tag{13}$$

The instant linear velocity of the mobile robot v_{mob} is attached and defined relative to the characteristic point *P*, this velocity is a result of the linear velocities of the left driven wheel υ_L and respectively the right driven wheel υ_R. These two drive velocities υ_L and υ_R are permanently two parallel vectors and, in the same time, they are permanently perpendicular on the common mechanical axis of these two driven wheels (Mircea Niţulescu, 2007), and given by:

$$\upsilon_{mob} = \frac{\upsilon_R + \upsilon_L}{2} = \frac{(\omega_R + \omega_L) r}{2} \tag{14}$$

A differential drive mobile robot is very sensitive to the relative velocity of the two wheels, where: for $\upsilon_R = \upsilon_L$: then the radius *R* is infinite and the robot moves in a straight line. If $\upsilon_R = -\upsilon_L$, then the radius *R* is zero and the robot rotates around robot center point P (it rotates in place). If $\upsilon_R \neq \upsilon_L$: The robot follows a curved trajectory around an ICC point located at a distance *R* from robot center point P.
The curvature, which is the inverse of the radius *R* is given by:

$$\lambda = \frac{1}{R} = \frac{\omega}{\upsilon_{mob}} = \frac{2}{L} * \frac{(\upsilon_R - \upsilon_L)}{(\upsilon_R + \upsilon_L)} \tag{15}$$

Now, substituting Eq.(14) in Eq.(10)

$$\upsilon_x = \frac{\upsilon_R + \upsilon_L}{2} \sin(\theta)$$

$$\upsilon_y = -\frac{\upsilon_R + \upsilon_L}{2} \cos(\theta)$$

The arc length, distance, traveled by the mobile robot, (point P) is the average of arcs lengths traveled by the two driven wheels and given by:

$$\Delta S_L = (R + L/2) \Delta \theta$$

$$\Delta S_R = (R - L/2) \Delta \theta \iff \Delta S = (\Delta S_L + \Delta S_R)/2$$

Correspondingly, the center orientation angle of the trajectory is given by:

$$\Delta \theta = (\Delta S_L - \Delta S_R)/R$$

2.4.1 Odometry for differential drive

To derive the expressions for the actual position of the robot, based on Figure 2(a), lets suppose that a differential drive robot is rotating around the point ICC with an angular velocity ω(t). During the infinite short time *dt* the robot center will travel the distance from the point *P(t)* to *P(t+dt)* with a linear velocity $V_{mob}(t)$. For infinite short time we can assume that the robot is moving along a straight line tangent in the point P(t) to the real trajectory

of the robot. Based on the two components of the velocity $V_{mob}(t)$, the traveled distance in each direction can be calculated (Julius Maximilian, 2003)

$$dx = \upsilon_x(t)dt$$
$$dy = \upsilon_y(t)dt \qquad (16)$$

Substituting υ_x and υ_y from Eq.(10) , gives:

$$dx = \upsilon \sin(\theta(t))dt$$
$$dy = \upsilon \cos(\theta(t))dt$$

Similarly, the angular position can be found to be :

$$d\theta = \omega(t)dt \qquad (17)$$

Integrating Eqs.(16,17) , substituting Eq.(10) and manipulating, we have:

$$x(t) = \int \upsilon \sin(\theta(t))dt + x_0$$
$$y(t) = \int \upsilon \cos(\theta(t))dt + y_0$$
$$\theta(t) = \int \omega(t)dt + \theta_0$$

Substituting Eqs.(13 and 14) and manipulating, we have:

$$x(t) = \int \left(\frac{\upsilon_R + \upsilon_L}{2}\right) \sin(\theta(t))dt + x_0$$
$$y(t) = \int \left(\frac{\upsilon_R + \upsilon_L}{2}\right) \cos(\theta(t))dt + y_0$$
$$\theta(t) = \int \frac{\upsilon_R - \upsilon_L}{L}dt + \theta_0 \qquad (18)$$

3. Simulation of overall mobile robot system response in MATLAB/simulink

The Simulation of overall mobile robot system, including the basic electric motor, controller, feedback speed sensor considering all dynamics is shown in Figure 4(a) , based on this model the sub-system model of electric motor , shown in Figure 4(b) can be built, this sub-system will be used to built another internal sub-system, shown in Figure 4(c) , in turn the last sub-system will be used in building Simulation of Differential drive and corresponding kinematics

Now , to test these sub-models, overall sub-system model shown in Figure 4(c), applying PID controller, and resulted responses, by defining used DC motor parameters,

platform shape dimensions, acting forces parameters and coefficients and speed sensor constant to be 1.8 for linear velocity of 0.5 m/s, running the model will result in response curves shown in Figure 4(c) this model allow designer to evaluate mobile system performance in terms of output speed, angle, torque, acceleration and current, this model in the form of sub-system will be used, as basis, to build the differential drive model

3.1 Simulation of Differential drive and whole system

To face the two top challenges in developing mechatronic system; early identifying system level problems and ensuring that all design requirements are met, as well as, to simplify and accelerate Mechatronics mobile robots design process, including proper selection, analysis, integration and verification of the overall system, as well as, sub-systems performance throughout the development process, and optimize system level performance to meet the design requirements. All the derived equations, including kinematics and dynamic equations, as well as, simulink sub-system model shown in Figure 4, are used to built an accurate and detailed , single input- multi-outputs dynamics and kinematics model shown in Figure 5(a), running this model will result in visual numerical values of many variables and curves of each of the following; robot linear speed υ_{mob}, robot angular speed ω_{mob}, linear speed of right wheel υ_R , linear speed of left wheel υ_L, robot center point P motion , the turning radius of mobile robot R, Robot orientation-Direction angle θ, the curvature, ,as well as, response curves in terms of linear speed/time, torque/time, angular speed/time and current/time response curves

Beside, the general model, based on derived equations given by Eqs.(11-15) additional and supporting simulink sub-models are built to return some of these output quantities, were Figure 5(b) shows additional sub-model to return robot center point P motion in X-Y coordinate (see Figures 6-7). Figure 5(c) shows additional sub-model to return each of the following , linear speed of right motor , linear speed of left motor, linear speed of whole mobile robot, curvature covered distance S, Robot orientation-Direction angle θ, to plot both linear speed of right wheel υ_R , linear speed of left motor υ_L sub-model shown in Figure 5(c) is used. A simplified version of the proposed model is shown in Figure 5(d)

$$G_{open}(s) = \frac{2K_{tach} * K_t}{2b_{equiv}L_a s^2 + r^2 M L_a s + 2b_{equiv}R_a s + r^2 M R_a s + C_r L_a s + 2J_{equiv}L_a s + 2K_b K_t + C_r R_a + 2J_{equiv}R_a}$$
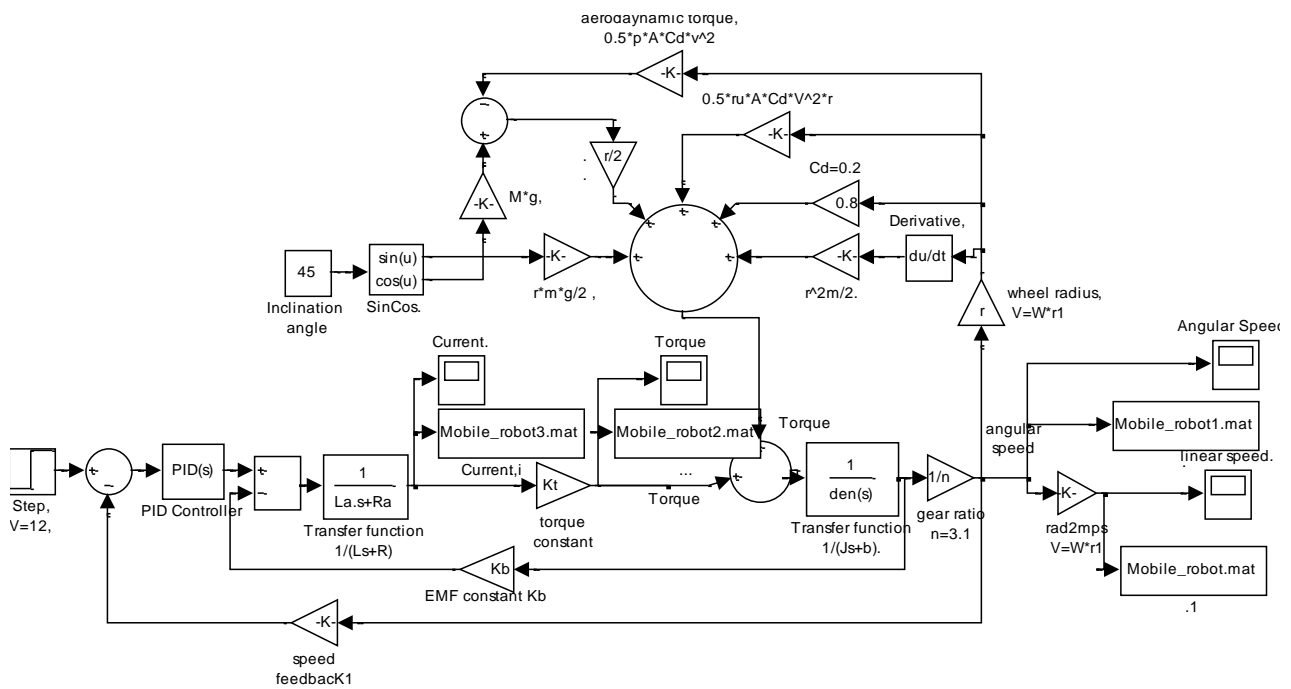
Fig. 4(a)   Accurate simulink model, of mobile robotic platform with PID controller.
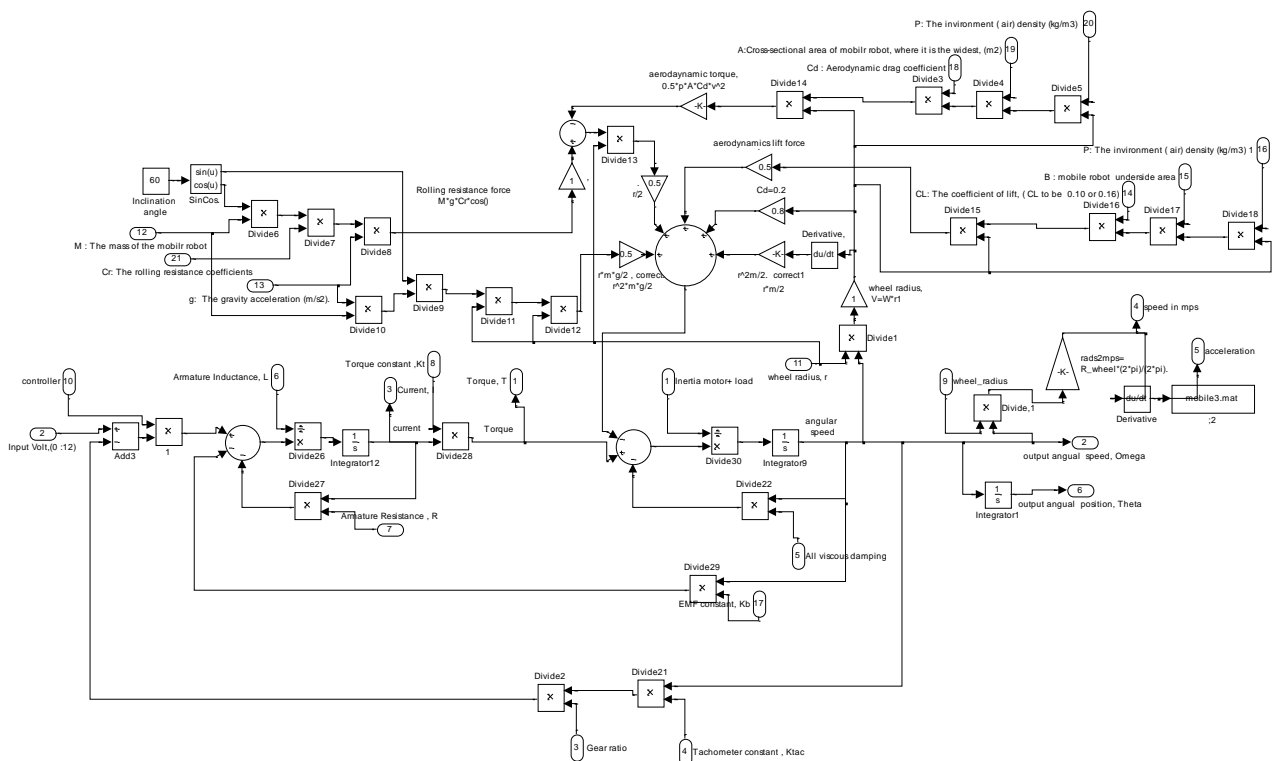

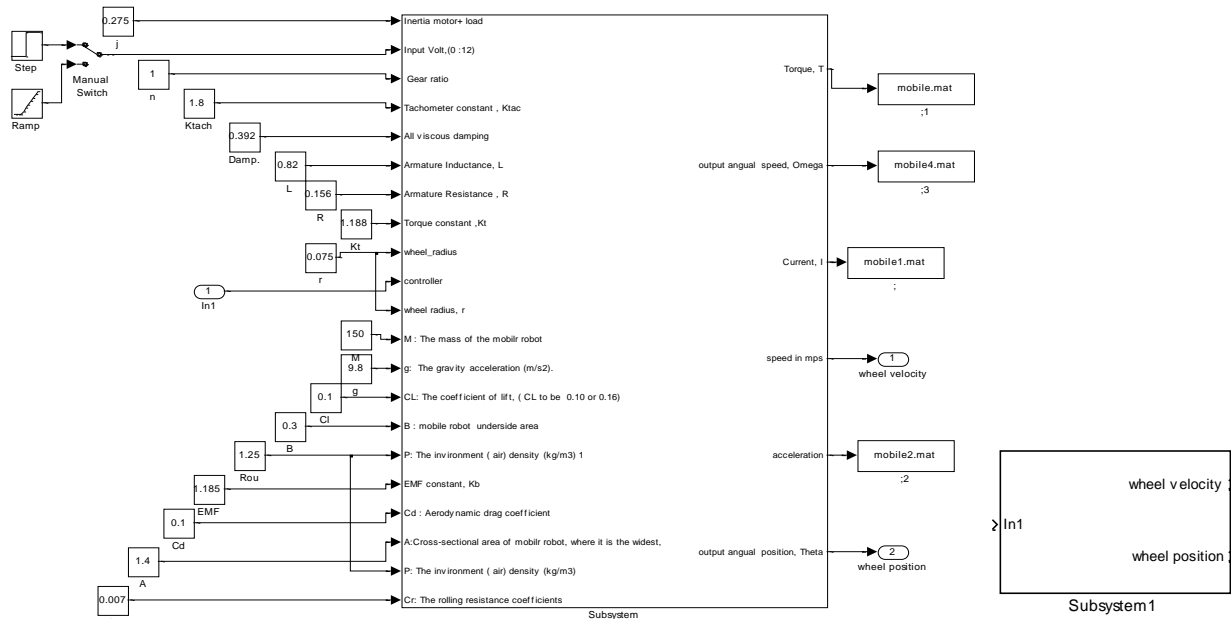Fig. 4(b) Electric motor subsystem considering all dynamics

Fig.4(c) Actuator sub-system
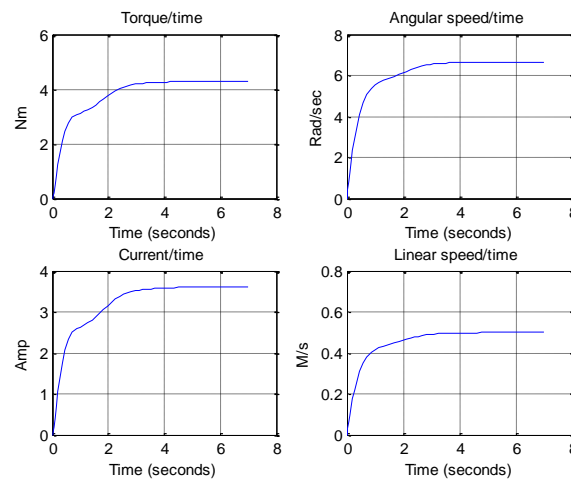
Fig. 4(d) Actuator final sub-system

Fig. 4(c) linear speed/time, torque/time, angular speed/time and current/time response curves of the accurate close loop mobile robotic platform model with PID controller.
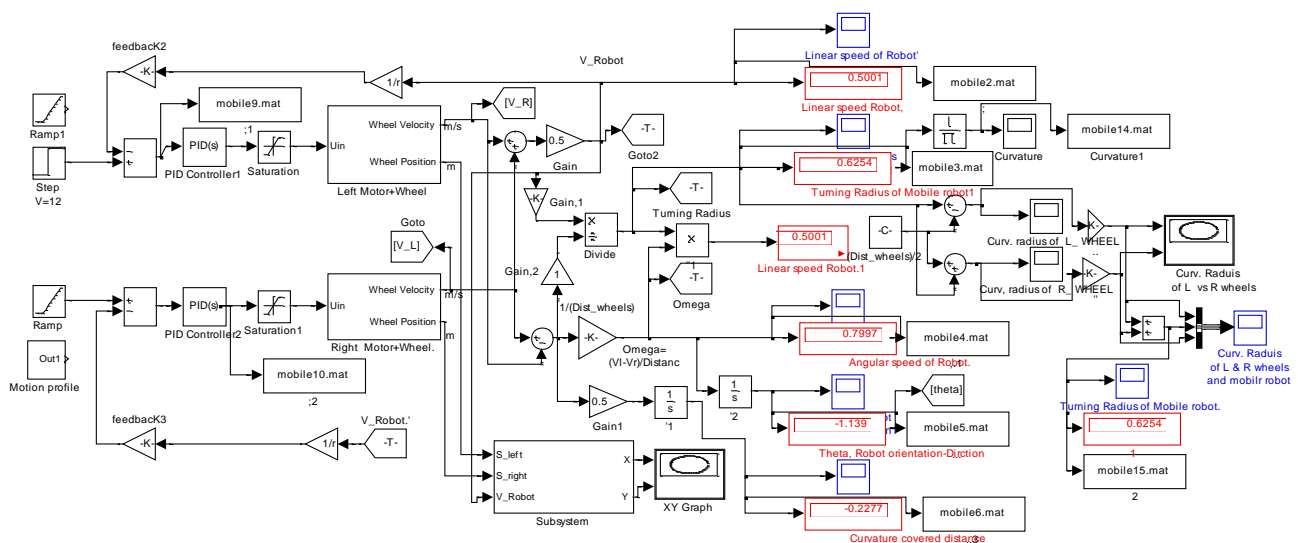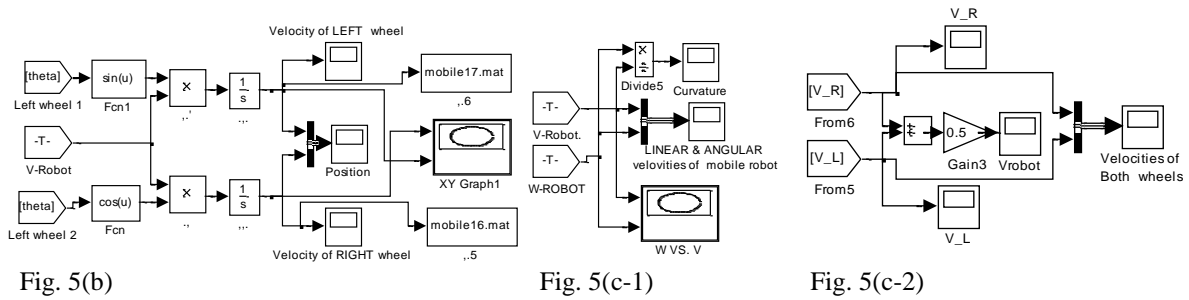

Fig. 5(a) Kinematics and dynamic simulink model

Fig. 5(b)   Fig. 5(c-1)   Fig. 5(c-2)

Fig. 5(b) additional simulink sum-model to return robot center point P motion in X-Y coordinates, velocities of right and left wheels υ_R, υ_L, Fig. 5(c-1) To return Both υ_{mobile} and ω_{mobile} curvature, and Fig. 5(c-2)To return linear speed of , mobile, and right and left wheels
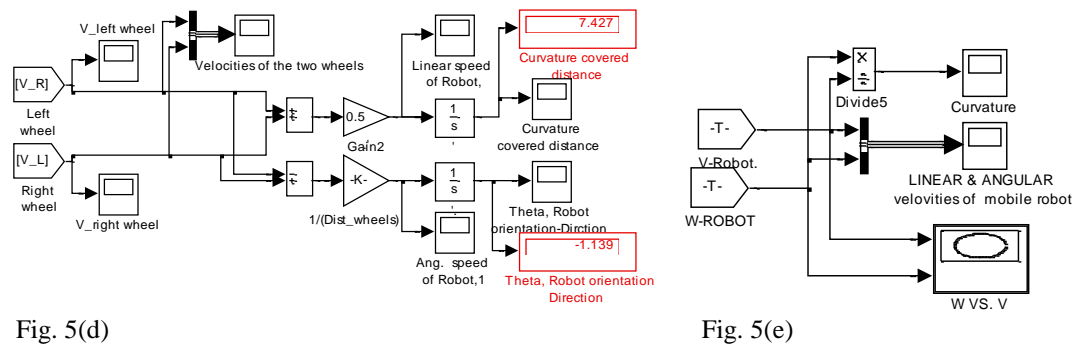

Fig. 5(d)   Fig. 5(e)

Fig. 5(d) additional simulink sub-model for odometry for differential drive to return each of the following , linear speed of right motor , linear speed of left motor, linear speed of whole mobile robot, curvature covered distance S, Robot orientation-Direction angle θ; Fig. 5(e) additional simulink to plot velocities of right and left wheels υ_R, υ_L, *as well as curvature*

Fig. 5(f) Simplified model
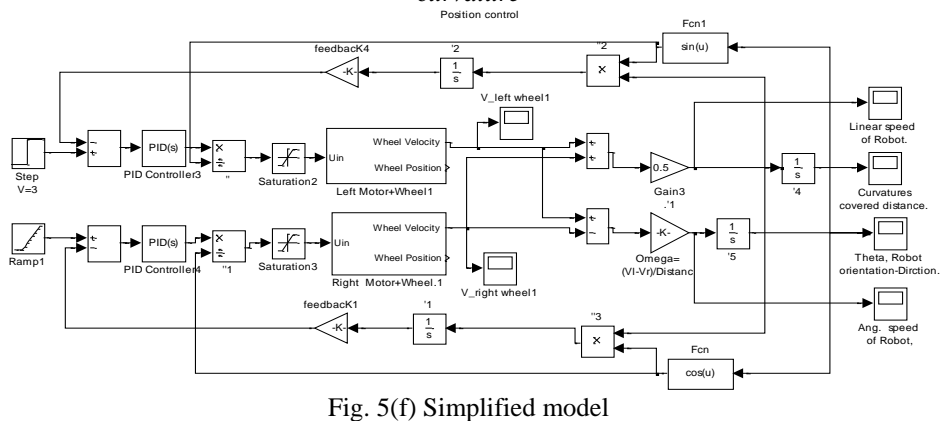
To simplify the mathematical model, we can assume that the two motors are identical in their behavior, applying similar approaches, and based on derived equations, a position control and simulation for the two-wheel differential drive mobile robot shown in Figure 5(g), is built.

Fig. 5(g) Position control and simulation
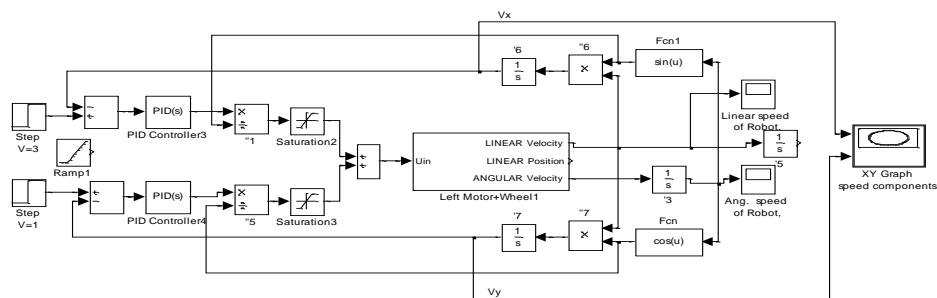
4. Testing and results

The following nominal values for the various parameters of a PMDC motor used : V_{in}=12 Volts; Motor torque constant, K_t = 1.1882 Nm/A; Armature Resistance, R_a = 0.1557 Ohms (Ω) ; Armature Inductance, L_a = 0.82 MH ;Geared-Motor Inertia: J_m = 0.271 kg.m^2, Geared-Motor Viscous damping b_m = 0.271 N.m.s; Motor back EMF constant, K_b = 1.185 rad/s/V, gear ratio, n=3, wheel radius *r =0.075 m*, mobile robot height ,h= 0.920 m, mobile robot width ,b = 0.580 m, the distance between wheels centers = 0.4 m, total mass 100 kg, the total equivalent inertia, *J_{equiv}* and total equivalent damping, *b_{equiv}* at the armature of the motor are ,J_{equiv} =0.2752 kg.m^2 , b_{equiv} = 0.3922 N.m.s. The most suitable linear output speed of suggested mobile robot is to move with 0.5 meter per second, (that is ω=V/r = 0.5/ 0.075 = 6.6667 rad/s,). Tachometer constant, K_{tac} = 12 / 6.6667=1.8 *(rad/sec)*, assuming shape of the Frontal area of mobile robot is long cylinder⬛, the aerodynamic drag coefficient, Cd =0.80, the air density (*kg/m^3*) at STP, ρ =1.25, The coefficient of lift, (C_L to be 0.10 or 0.16), the inclination angle to be 45

For model shown in Figure 5(a), when subjecting the right motor to step input with final value of 12 V, and Left motor of ramp input with slop of 7 , all the response curves shown in Figure 6 , can be obtained , as well as visual numerical values for these quantities. The sub-models can be used to return, all or only, of the required response curves.
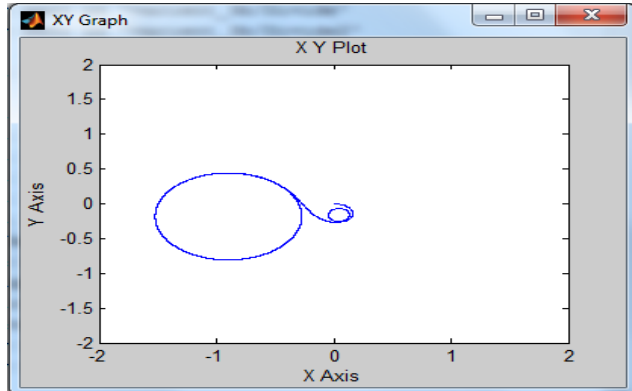

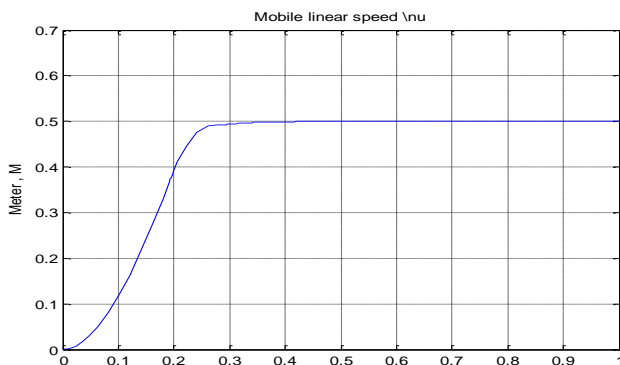Fig. 6(a) The robot center point *P* motion
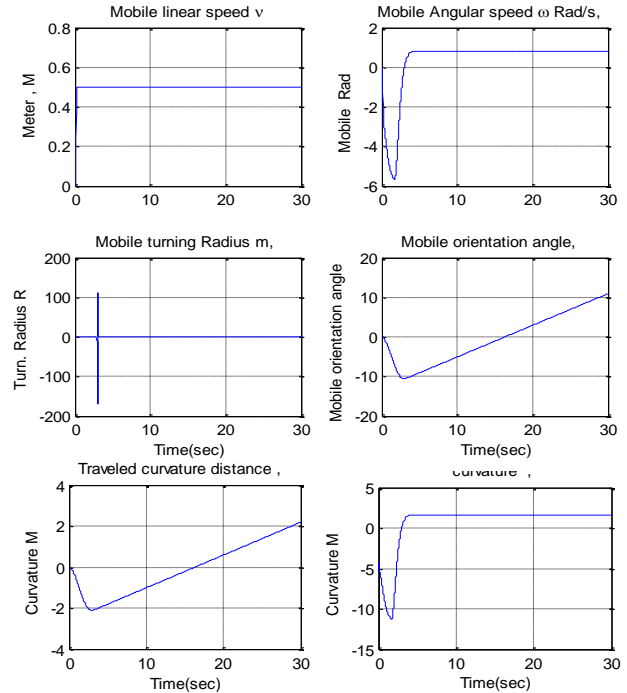

Fig. 6(b) The Mobile robot linear speed

Fig. 6(c) The mobile robot linear speed/ time, mobile robot angular speed/time, turning radius/time (final value of 0.6523), and mobile robot orientation angle. Time, traveled curvature distance/ time, and curvature/time.
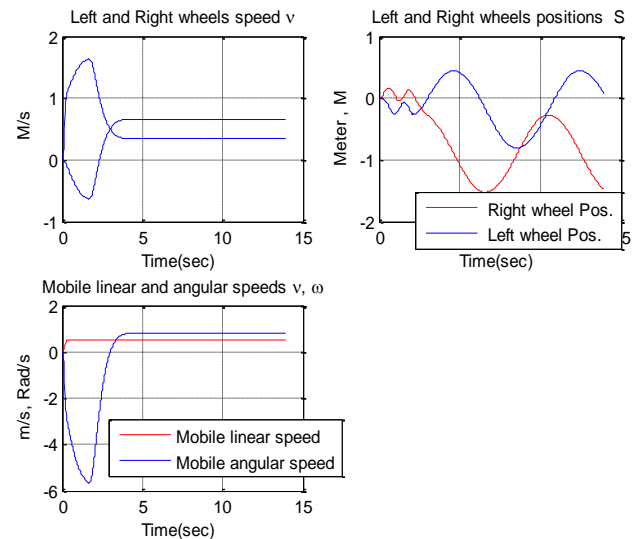

Fig. 6(d) left and right wheels linear and angular speed and position

To further test our model, (differential drive motions) shown in Figure 5(a), by defining DC parameters, platform shape dimensions, acting forces parameters and coefficients , speed sensor *constant,*, inclination angle, firstly, applying the same inputs to both motors , to have similar wheels velocities, $\upsilon_R = \upsilon_L$, result in that the radius *R* is infinite and the robot moves in a straight line motion as shown in Fig. 7(a); applying different inputs to have $\upsilon_R \neq \upsilon_L$, will result in corresponding trajectory, The robot follows a curved trajectory around an ICC point
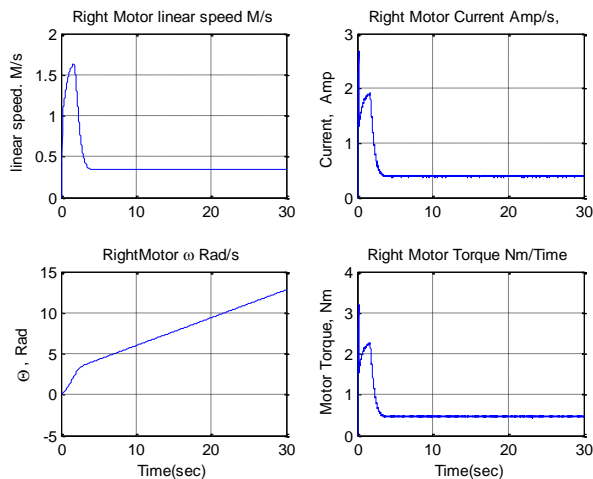
Fig. 6(e) Right motor linear speed/time, current/time, angular speed/time, torque/ time response curves.

located at a distance *R* from robot center point P. (Fig. 7(a) (b) (c)), also for each time, the model is run, we obtain response curves in terms of linear speed/time, torque/time, angular speed/time and current/time response curves.
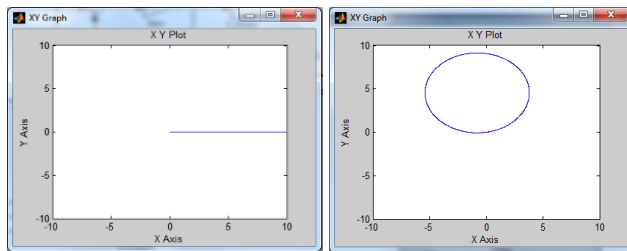

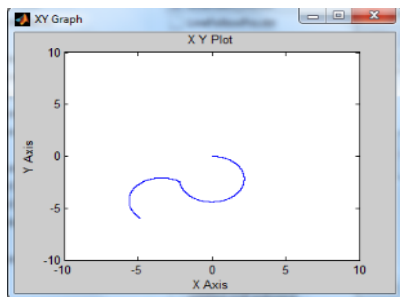Fig.7(a) straight line   Fig.7(b) circular motion

Fig. 7(c) Double-curvature

Fig.7(a)(b)(c) Three different trajectories of the central point of the mobile robot.

5. Future work; experimental testing; Mobile robot control and circuit explanation,

Wheeled mobile Robot can be designed and built using the following components (see Figure 7); chassis with two in-line with each other electric PMDC motors, a PIC microcontroller embedded on the robot and capable of controlling two drive channels (PIC16F84A), two H-bridge control circuits, corresponding sensors, The inputs

to microcontroller are sensors outputs, depending on robot application, sensors may be line detection sensor, ultrasonic range proximity sensor, temperature sensor. , PIC microcontroller is supplied with 5VDC and simple clock condition with 20 MHz crystal, The H-bridge circuit is supplied with 12VDC and the four bits outputs of microcontroller made this part to drive the desire conditions of DC Motor. A simplified algorithm for a PID control implementation loop is given next:

Read K_P, K_I, K_P
previous_error = 0;
integral = 0;
Read target_position   // the required position of robot center.
while ( )
Read current_position;   //the current position of robot center with respect to the line.
error = target_position − current_position ; // calculate error
proportional = K_P * error;   // error times proportional gain
integral = integral + error*dt;   //integral stores the accumulated error
integral = integral* K_I;
derivative = (error - previous_error)/dt; //stores change in error to derivate, dt is sampling period
derivative = K_D *derivative;
PID_action = proportional + integral + derivative;
//To add PID_action to the left and right motor speed.
//The sign of PID_action, will determine the direction in which the motor will turn.
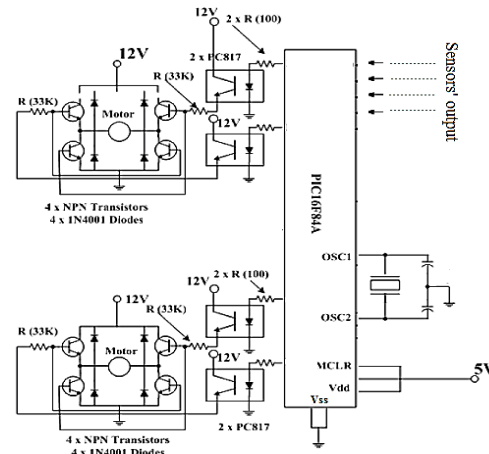previous_error =error; //Update error
end

Fig. 7 Microcontroller based DC motor control system for wheeled mobile robot

Conclusions

New models for differential drive mobile robots and some considerations regarding design, modeling and control solutions are presented. The presented models allow designer to have maximum desired informations in the form of curves and visual numerical values of all variables

required in designing and controlling of a wheeled mobile robot, that can be used to face the two top challenges in developing mechatronic system; early identifying system level problems and ensuring that all design requirements are met, as well as ,to simplify and accelerate Mechatronics mobile robots   design process, including proper selection, analysis, integration and verification of the overall system, as well as, sub-systems performance throughout the development process, and optimize system level performance to meet the design requirements. The testing results show the simplicity, accuracy and applicability of the proposed models in mechatronics design of mobile robots.

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