

yyang3
1503849

Exercise 1 p.305 6.7

Part b

Script:

```
H1=[-6 6;6 0];  
H2=[6 -6;-6 0];  
H3=[-6 6;6 -12];  
H4=[6 -6;-6 12];  
res = [eig(H1) eig(H2) eig(H3) eig(H4)];  
result:
```

(0,0) H1	(0,-1) H2	(-1,-1) H3	(1,0) H4
-9.70820393249937	-3.70820393249937	-15.7082039324994	2.29179606750063
3.70820393249937	9.70820393249937	-2.29179606750063	15.7082039324994
Not definite	not definite	negative definite	positive definite
saddle point	saddle point	local maximum	local minimum

Exercise 2

Part a

$P_k = r P_{k-1}$

$P_k = r^2 P_{k-2}$

$P_k = r^3 P_{k-3}$

.....

So let $P_k = P_0 \cdot r^k$

We use Gauss-Newton Method to do non linear least square fit.

The main part of the script is as follows:

```
r=2; p0=0.1; % I take initial as 2 and 0.1 based on observation  
for i=1:30 % loop to update p0 and r, until converge  
    d=Jaco(p0,r)\error(p0,r); % Jaco is a 2d array of partial derivative of r^k and p0  
    % [ -k*p0*r^k -r^k ] where k =1,2,3,4..8  
    % error is p0*r^k-Pk where k=1,2,..8 Pk = 0.19,0.36,0.69,1.3,....14  
    r=r+d(1) % update  
    p0=p0+d(2)  
    if norm(error)<0.0001 % determine if converge  
        %converge  
    end end
```

Finally, we have $p_0 = 0.1616$, $r = 1.7494$

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Part b

```
k = [1 1;1 2;1 3 ;1 4; 1 5; 1 6; 1 7 ; 1 8;];
```

```
p = log[0.19 0.36 0.69 1.3 2.5 4.7 8.5 14]^T;
```

```
res = k/p;
```

```
p0=exp(res(1));
```

```
r = exp(res(2));
```

We get $p_0 = 0.1058$, $r = 1.8642$

Compare to the non linear fit, the linear fit has a slightly smaller p_0 and a slightly larger r . The difference is acceptable and both models work.