
Algorithm 5: Levenberg-Marquardt algorithm

input : $f : \mathbb{R}^n \rightarrow \mathbb{R}$ a function such that $f(\mathbf{x}) = \sum_{i=1}^m (f_i(\mathbf{x}))^2$
where all the f_i are differentiable functions from \mathbb{R}^n to \mathbb{R}
 $\mathbf{x}^{(0)}$ an initial solution

output: \mathbf{x}^* , a local minimum of the cost function f .

```
1 begin
2    $k \leftarrow 0$  ;
3    $\lambda \leftarrow \max \text{diag}(\mathbf{J}^T \mathbf{J})$  ;
4    $\mathbf{x} \leftarrow \mathbf{x}^{(0)}$  ;
5   while STOP-CRIT and  $(k < k_{max})$  do
6     Find  $\delta$  such that  $(\mathbf{J}^T \mathbf{J} + \lambda \text{diag}(\mathbf{J}^T \mathbf{J}))\delta = \mathbf{J}^T \mathbf{f}$  ;
7      $\mathbf{x}' \leftarrow \mathbf{x} + \delta$  ;
8     if  $f(\mathbf{x}') < f(\mathbf{x})$  then
9        $\mathbf{x} \leftarrow \mathbf{x}'$  ;
10       $\lambda \leftarrow \frac{\lambda}{\nu}$  ;
11    else
12       $\lambda \leftarrow \nu \lambda$  ;
13     $k \leftarrow k + 1$  ;
14  return  $\mathbf{x}$ 
15 end
```
