

$$X \xrightarrow{h_1} XW_1 + b_1 \xrightarrow{X_1} \text{ReLU}(h) \xrightarrow{\text{score}} X_1W_2 + b_2 \xrightarrow{\text{prob}} \text{softmax}(\text{score})$$

$$\xrightarrow{\text{loss}} -\log(\text{prob}_{:,y_i}) \xrightarrow{\text{sum_loss}} \sum \text{loss} + R_2$$

$$\frac{\partial \text{sum_loss}}{\partial W_1} = \frac{\partial \text{sum_loss}}{\partial \text{loss}} \cdot \underbrace{\frac{\partial \text{loss}}{\partial \text{prob}} \cdot \frac{\partial \text{prob}}{\partial \text{score}} \cdot \frac{\partial \text{score}}{\partial X_1} \cdot \frac{\partial X_1}{\partial h_1} \cdot \frac{\partial h_1}{\partial W_1}}_{\text{chain rule}}$$

$$= 1 \cdot (\text{prob} \cdot W_2^T) \cdot (h_1 > 0) \cdot X^T$$