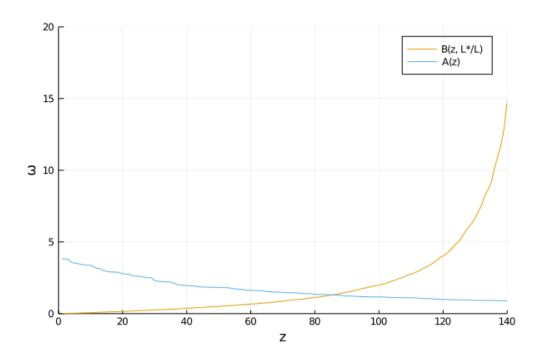
Assignment 1 Writeup

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1 Figure 1



2 Solving for Equilibrium

Table 1: Equilibrium ω and Specialization

Var	g = 1	g = 0.9
\bar{z}^*	86	72
\bar{z}	86	95
ω	1.306	1.314

3 Calculating Welfare

From class, we can calculate welfare using:

$$\ln(U/L) = \ln w - \int_0^1 b(z) \ln p(z) dz$$

Reformulating this equation, setting w=1 and $L=L^*=1$, Home's welfares in autarky and trade are:

$$\ln(U^a/L) = \ln w - \int_0^1 b(z) \ln(a(z)wL) dz$$

$$= -\int_0^1 b(z) \ln(a(z)) dz$$

$$\ln(U^t/L) = \ln w - \int_0^{\bar{z}} b(z) \ln(wa(z)) dz - \int_{\bar{z}}^1 b(z) \ln\left(a^*(z)\frac{w^*L^*}{g}\right) dz$$

$$= -\int_0^{\bar{z}} b(z) \ln(a(z)) dz - \int_{\bar{z}}^1 b(z) \ln\left(\frac{a^*(z)}{\bar{\omega}g}\right) dz$$

Similarly, Foreign's welfares are:

$$\ln(U^{*a}/L^*) = \ln\left(\frac{1}{\bar{\omega}}\right) - \int_0^1 b(z) \ln(w * a^*(z)) dz$$
$$\ln(U^{*t}/L^*) = \ln\left(\frac{1}{\bar{\omega}}\right) - \int_{\bar{z}^*}^1 b(z) \ln\left(\frac{a^*(z)}{\bar{\omega}}\right) dz - \int_0^{\bar{z}^*} b(z) \ln\left(\frac{a(z)}{g}\right) dz$$

Table 2: Welfare

Var	g = 1	g = 0.9
Home - Autarky	0.421	0.421
Home - Trade	0.527	0.487
Foreign - Autarky	0	0
Foreign - Trade	0.26	0.202

4 Volume of Trade and Gains from Trade

Table 3: Changing b(z)

Var	Economy 1	Economy2	Economy 3
$\overline{\overline{z}}$	72	75	67
$ar{z}^*$	95	102	90
ω	1.314	1.28	1.364
Volume	0.734	0.734	0.734
Gains - Home	0.066	0.068	0.073
Gains - Foreign	0.475	0.449	0.527