

P(1)

(a).

$$P(\text{word} = \text{we}) = \frac{1}{3} \times \frac{13}{12+12+1+1+13} + \frac{1}{3} \times \frac{17}{17+17+0+0+17} + \frac{1}{3} \times \frac{15}{14+14+2+2+15}$$

(b)

$$= 0.32860422$$

$$P\left(\frac{\text{Document}=1}{\text{Word}=\text{we}}\right) = \frac{0.00854}{0.0227313} = 0.3760$$

$$P(\text{word} = \text{we}) = \frac{1}{3} \times \frac{1}{12+12+1+1+13} + \frac{1}{3} \times \frac{0}{17+17+0+0+17} + \frac{1}{3} \times \frac{2}{14+14+2+2+15}$$

$$P(\text{Word} = \text{we from Document} = 1) = \frac{1}{3} \times \frac{1}{12+12+1+1+13} = 0.0227313$$

$$= 0.00854$$

(c)

$$P\left(\frac{\text{Document} = 2}{\text{Word} = \text{am or Word} = \text{are}}\right) = 0.3310$$

$$P(\text{Document} = 2 \text{ and } (\text{Word} = \text{am or Word} = \text{are}))$$

$$= \frac{1}{3} \times \frac{12+1}{12+12+1+1+13} + \frac{1}{3} \times \frac{17+0}{17+17+0+0+17} + \frac{1}{3} \times \frac{14+2}{14+14+2+2+15} = 0.3356$$

$$P(\text{Document} = 2 \text{ and } (\text{word} = \text{am or word} = \text{are}))$$

$$= \frac{1}{3} \times \frac{17+0}{17+17+0+0+17} = 0.1111$$

(d)

$$P(\text{word} = \text{groot}) = \frac{1}{6} \times \frac{13}{12+12+1+1+13} + \frac{1}{3} \times \frac{17}{17+17+0+0+17} + \frac{1}{2} \times \frac{15}{14+14+2+2+15}$$

(e)

$$P\left(\frac{\text{Document} = 1 \text{ and Word} = \text{we}}{\text{Word} = \text{we}}\right)$$

$$= 0.3262$$

$$= 0.16436538$$

$$P(\text{doc}=1 \text{ and Word}=we)$$

$$= \frac{1}{6} \times \frac{1}{12+12+1+1+13} = 0.0042735$$

$$P(\text{Word}=we)$$

0.026

$$= \frac{1}{6} \times \frac{1}{12+12+1+1+13} + \frac{1}{3} \times \frac{0}{17+17+0+0+17} + \frac{1}{2} \times \frac{2}{14+14+2+2+15}$$

(f)

$$P\left(\frac{\text{Doc}=2 \text{ and } (\text{Word}=am \text{ or } \text{Word}=are)}{\text{Word}=am \text{ or } \text{Word}=are}\right) = 0.3298$$

$$P(\text{Doc}=2 \text{ and } (\text{Word}=am \text{ or } \text{Word}=are))$$

$$= \frac{1}{3} \times \frac{17+0}{17+17+0+0+17} = 0.1111$$

$$P(\text{Word}=am \text{ or } \text{Word}=are)$$

$$= \frac{1}{6} \times \frac{12+1}{12+12+1+1+13} + \frac{1}{3} \times \frac{17+0}{17+17+0+0+17} + \frac{1}{2} \times \frac{14+2}{14+14+2+2+15}$$

$$= 0.33687$$