

Supplementary Materials: Nukplex: An Efficient Local Search Algorithm for Maximum K-Plex Problem

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1 Detail Results

For each instance, *max* represents the best size found and *avg* denotes the average size. When *max=avg*, we do not report *avg*. In the tables, the bold values denote the best solution obtained among all algorithms. We only report the results for which all algorithms fail to find the same best and average values. Tables 1-6 display the detailed results corresponding to Table 2 in the main paper.

2 Comparisons against MKPP Exact Algorithms on Some Additional Large Sparse Instances

To further verify the performance of our proposed algorithm, we select two sets of large sparse graphs from KpLeX-Gap [Wang *et al.*, 2023], which have been tested in many previous k-plex related studies [Gao *et al.*, 2018; Zhou *et al.*, 2021; Jiang *et al.*, 2021; Chang *et al.*, 2022; Wang *et al.*, 2023]. The first set is the Network-Repo benchmark, which contains 139 large sparse graphs with up to 5.87×10^7 vertices from the Network Data Repository¹ [Rossi and Ahmed, 2015]. The second set is the 10th-DIMACS benchmark, which contains 84 large sparse graphs with up to 5.09×10^7 vertices². Previous works for the MKKP heuristic algorithms focus on solving some small *k* values (e.g., $k = 2, 3, 4, 5$), while in KpLeX-Gap [Wang *et al.*, 2023], the authors carry out experiments with $k = 2, 5, 10, 15, 20$. In our work, *k* is set to 2, 3, 4, 5, 10, 15, 20, and thus we consider 1561 instances in total. The time limit of the two exact algorithms KpLeX-Gap and DiseMKP is set to 1800 seconds, whereas the cutoff time of Nukplex is set to 1000 seconds with random seeds from 1 to 10.

Tables 7-8 display the results of Nukplex, KpLeX-Gap, and DiseMKP. The results indicate that Nukplex, KpLeX-Gap, and DiseMKP are able to obtain the best solutions for 1559, 1521, and 1433 instances, respectively. Nukplex only fails to obtain the best solutions for 2 instances when using 10 different seed values. However, when using 100 different seed values, Nukplex successfully obtains the best solutions for these two instances as well. Furthermore, when using a single seed value of 1, Nukplex achieves the best solutions for 1553 out

of the 1561 instances. These additional experimental results further validate the effectiveness of Nukplex.

References

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¹<http://lcs.ios.ac.cn/caisw/Resource/realworld%20graphs.tar.gz>

²<https://networkrepository.com/dimacs10.php>

Instance	k	Nukplex max(avg)	DCCplex max(avg)	KLS max(avg)	Instance	k	Nukplex max(avg)	DCCplex max(avg)	KLS max(avg)
brock400_3	2	31 (30.64)	30	31	brock800_3	3	30	30 (29.98)	30
brock400_4	2	33	33 (32.84)	33	C1000.9	3	96(95.96)	96 (94.98)	96 (95.94)
brock800_4	2	26(25.96)	26 (25.6)	26 (25.94)	C2000.5	3	23 (22.5)	23 (22.16)	23(22.99)
C1000.9	2	82(81.98)	82 (81.88)	82 (81.88)	C2000.9	3	109(108.64)	108(107.18)	109 (107.85)
C2000.5	2	20(19.78)	20 (19.68)	20 (19.68)	C4000.5	3	25(24)	24(23.32)	24
C2000.9	2	94(93.42)	94 (92.28)	93(92.06)	C500.9	3	81	81 (80.82)	81
C4000.5	2	21(20.58)	22 (20.92)	21	frb100-40	3	156 (153.06)	156(153.36)	154(152.55)
frb100-40	2	131(128.02)	130(127.52)	129(127.6)	frb35-17-2	3	55(54.32)	55 (54.02)	55(54.32)
frb40-19-1	2	55	55 (54.28)	55	frb35-17-4	3	57	57 (56.1)	57
frb40-19-3	2	53	53 (52.92)	53 (52.98)	frb35-17-5	3	56	56 (55.8)	56
frb45-21-3	2	60	60 (59.32)	60	frb40-19-1	3	66	66 (65.7)	66
frb45-21-4	2	61(60.98)	61 (60.16)	61 (60.88)	frb40-19-2	3	65	65 (64.92)	65
frb45-21-5	2	59	59 (58.70)	59 (58.98)	frb40-19-4	3	63	63 (62.94)	63
frb50-23-1	2	67	67 (66.24)	67	frb45-21-1	3	71(70.9)	71 (70.06)	71 (70.56)
frb50-23-2	2	67(66.38)	66	67 (66.35)	frb45-21-2	3	71	71 (70.46)	71
frb50-23-3	2	65(64.82)	65 (64.04)	65 (64.57)	frb45-21-3	3	72(71.74)	71(70.96)	72 (71.32)
frb50-23-4	2	67(66.02)	66(65.98)	66	frb45-21-4	3	73(72.4)	73 (71.9)	73 (72.22)
frb50-23-5	2	67(66.98)	67 (66.24)	67 (66.9)	frb45-21-5	3	71(70.74)	71 (69.94)	71 (70.54)
frb53-24-1	2	71	71 (70.88)	71 (70.71)	frb50-23-1	3	80(79.06)	79(78.96)	79
frb53-24-2	2	70	70 (69.96)	70	frb50-23-2	3	79	79 (78.96)	79
frb53-24-3	2	70	70 (69.84)	70	frb50-23-3	3	77(76.4)	76(75.80)	77(76.4)
frb53-24-4	2	70(69.98)	70 (69)	70 (69.68)	frb50-23-4	3	79	79 (78.96)	79
frb53-24-5	2	69(68.44)	68	69 (68.41)	frb50-23-5	3	80(79.4)	80 (79.16)	80 (79.38)
frb56-25-1	2	75	75 (74.28)	75 (74.47)	frb53-24-1	3	85	85 (84.2)	85
frb56-25-2	2	75	75 (74.48)	75 (74.4)	frb53-24-2	3	83(82.92)	83 (82.16)	83 (82.91)
frb56-25-3	2	74	74 (73.48)	74 (73.66)	frb53-24-3	3	84(83.18)	83(82.9)	83
frb56-25-4	2	74(73.98)	74 (72.96)	74 (73.4)	frb53-24-4	3	84(83.7)	84 (82.56)	84 (83.69)
frb56-25-5	2	74(73.98)	74 (73.1)	74 (73.64)	frb53-24-5	3	82	82 (81.52)	82 (81.94)
frb59-26-1	2	79(78.98)	78	79 (78.22)	frb56-25-1	3	90(89.46)	89(88.96)	89
frb59-26-2	2	79(78.96)	79 (78.16)	79 (78.3)	frb56-25-2	3	89	89 (88.48)	89
frb59-26-3	2	78(77.98)	78 (77.04)	78 (77.28)	frb56-25-3	3	88(87.92)	88 (87.1)	88 (87.78)
frb59-26-4	2	79(78.1)	78(77.2)	78(77.44)	frb56-25-4	3	88(87.66)	88 (86.66)	88 (87.04)
frb59-26-5	2	78	78 (77.92)	78 (77.6)	frb56-25-5	3	88(87.48)	88 (86.8)	88 (87.46)
gen400_p0.9_55	2	68(67.8)	68 (67.56)	68 (67.76)	frb59-26-1	3	94(93.44)	93(92.64)	93
gen400_p0.9_65	2	74	74 (73.08)	74	frb59-26-2	3	94(93.66)	94 (92.86)	94 (93.56)
gen400_p0.9_75	2	80	79	80 (79.99)	frb59-26-3	3	94(92.98)	94 (91.98)	94 (92.70)
MANN_a27	2	236 (235.96)	236	236 (235.96)	frb59-26-4	3	93(92.9)	93 (92.14)	93 (92.76)
san1000	2	18 (17.06)	18 (17)	18(17.28)	frb59-26-5	3	93(92.88)	93 (91.69)	93 (92.58)
san200_0.7_2	2	26 (25.4)	26	26 (25.4)	keller6	3	93	93 (91.46)	93
san400_0.5_1	2	15	15 (14.86)	15	p_hat1500-3	3	133	133 (132.98)	133
san400_0.7_1	2	42 (41.14)	42 (41.06)	42	san1000	3	25	25 (24.96)	25
san400_0.7_2	2	33(32.46)	32(32)	33 (32.07)	san200_0.7_1	3	46	46 (45.94)	46
san400_0.7_3	2	28	28 (27.02)	28 (27.87)	san400_0.5_1	3	22	22 (21.84)	22
san400_0.9_1	2	103(102.98)	103 (102.12)	103 (102.46)	san400_0.7_2	3	47 (46.1)	47 (46.22)	47
brock800_1	3	30(29.9)	30 (29.32)	30 (29.84)	san400_0.7_3	3	39(38.36)	39 (38.02)	39 (38.34)

Table 1: Experimental results of Nukplex, DCCplex and KLS on classic instances I. All algorithms are executed for 100 independent runs, with a cutoff time of 1000 seconds for each run.

Instance	k	Nukplex max(avg)	DCCplex max(avg)	KLS max(avg)	Instance	k	Nukplex max(avg)	DCCplex max(avg)	KLS max(avg)
brock800_1	4	34	34 (33.88)	34	brock400_4	5	46	46 (45.98)	46
brock800_2	4	34	34 (33.06)	34	brock800_2	5	38	38 (37.08)	38
brock800_3	4	34	34 (33.78)	34	C1000.9	5	122(121.26)	121(119.88)	122 (121.24)
brock800_4	4	34 (33.08)	33	34(33.98)	C2000.5	5	28	28	29(28.11)
C1000.9	4	110(109.28)	109(107.96)	110 (109.26)	C2000.9	5	137(136.34)	136(134.20)	137 (136.01)
C2000.5	4	26 (25.08)	25	26(25.74)	C4000.5	5	30(29.94)	30 (29.08)	30 (29.92)
C2000.9	4	123(122.62)	123 (121.20)	123 (122.02)	C500.9	5	104(103.62)	103(102.78)	104 (103.56)
C4000.5	4	28 (26.70)	27(26.08)	28(27.02)	c-fat200-2	5	24	24 (23.99)	24
C500.9	4	93(92.9)	93 (92.18)	93(92.9)	c-fat200-5	5	58	58 (57.94)	58
c-fat200-5	4	58	58 (57.94)	58	DSJC1000.5	5	27	27 (26.64)	27
c-fat500-5	4	64	64 (63.98)	64	frb100-40	5	202(199.28)	201(198.98)	200(198.59)
DSJC1000.5	4	24(23.82)	24 (23.74)	24 (23.8)	frb30-15-5	5	63	63 (62.98)	63
frb100-40	4	179(176.9)	178(176.48)	177(175.82)	frb35-17-1	5	73	73 (72.98)	73
frb30-15-2	4	55(54.68)	55 (54.12)	55 (54.58)	frb35-17-2	5	72(71.82)	72 (71.14)	72 (71.78)
frb30-15-4	4	56(55.88)	56 (55.34)	56 (55.78)	frb35-17-4	5	74	74 (73.94)	74
frb30-15-5	4	56	56 (55.94)	56	frb35-17-5	5	74(73.7)	74 (73.04)	74 (73.36)
frb35-17-3	4	67	67 (66.22)	67	frb40-19-1	5	88	88 (87.92)	88
frb35-17-4	4	66(65.26)	65	66 (65.06)	frb40-19-2	5	85(84.66)	84	85 (84.48)
frb40-19-1	4	77	77 (76.96)	77	frb40-19-3	5	83(82.66)	82(81.98)	83 (82.38)
frb40-19-2	4	75(74.98)	75 (74.12)	75 (74.94)	frb40-19-4	5	81	81 (80.86)	81
frb40-19-4	4	73(72.98)	73 (72.08)	73 (72.94)	frb40-19-5	5	83(82.7)	83 (82.02)	83 (82.48)
frb40-19-5	4	74	74 (73.62)	74 (73.96)	frb45-21-1	5	93(92.68)	92(91.68)	93 (92.58)
frb45-21-1	4	82	82 (81.04)	82 (81.94)	frb45-21-2	5	92(91.88)	92 (91.04)	92 (91.7)
frb45-21-2	4	82(81.12)	81(80.76)	82 (81.06)	frb45-21-3	5	94(93.28)	94 (92.82)	94 (93.22)
frb45-21-3	4	83(82.98)	83 (82.44)	83 (82.80)	frb45-21-4	5	94	94 (93.84)	94
frb45-21-4	4	84(83.18)	84 (83.04)	84 (83.08)	frb45-21-5	5	92	92 (91.52)	92
frb45-21-5	4	82(81.66)	82 (80.78)	82 (81.52)	frb50-23-1	5	104(103.56)	103(102.48)	103
frb50-23-1	4	92	92 (91.22)	92	frb50-23-2	5	104(103.6)	104 (102.32)	103
frb50-23-2	4	92(91.7)	92 (90.7)	92 (91.68)	frb50-23-3	5	99	99 (98.14)	99
frb50-23-3	4	88	88 (87.4)	88	frb50-23-4	5	104(103.28)	104 (102.42)	103
frb50-23-4	4	92(91.2)	91(90.78)	92 (91.18)	frb50-23-5	5	104	104 (102.98)	103
frb50-23-5	4	92	92 (91.04)	92	frb53-24-1	5	112	112 (110.98)	111
frb53-24-1	4	99(98.98)	99 (97.96)	99(98.98)	frb53-24-2	5	108(107.76)	107(106.60)	107
frb53-24-2	4	96(95.5)	96 (94.66)	96 (95.48)	frb53-24-3	5	110(109.1)	109(108.14)	109
frb53-24-3	4	97(96.84)	97 (96.02)	97 (96.82)	frb53-24-4	5	109	109 (107.94)	109
frb53-24-4	4	97(96.32)	96(95.54)	96	frb53-24-5	5	107(106.28)	106(105.12)	105
frb53-24-5	4	94	94 (93.67)	94	frb56-25-1	5	118(117.34)	117(116.24)	117
frb56-25-1	4	104(103.88)	104 (103.05)	104 (103.86)	frb56-25-2	5	117(116.32)	116(115)	115
frb56-25-2	4	104(103.04)	103(102.84)	103(102.89)	frb56-25-3	5	114	114 (112.82)	114 (113.89)
frb56-25-3	4	101(100.98)	101 (100.06)	101 (100.97)	frb56-25-4	5	114(113.2)	113(112.14)	113
frb56-25-4	4	101(100.52)	101 (99.73)	101 (100.5)	frb56-25-5	5	115(114.12)	114(112.86)	114
frb56-25-5	4	102(101.04)	101(100.08)	101	frb59-26-1	5	122(121.8)	122 (120.8)	121
frb59-26-1	4	108(107.92)	108 (106.96)	108 (107.69)	frb59-26-2	5	122(121.78)	122 (120.3)	121
frb59-26-2	4	108(107.96)	108 (106.8)	108 (107.73)	frb59-26-3	5	121(120.96)	121 (119.76)	120
frb59-26-3	4	108(107.12)	107(106.12)	107(106.98)	frb59-26-4	5	122(120.86)	121(119.18)	119
frb59-26-4	4	107(106.96)	107 (105.84)	107 (106.49)	frb59-26-5	5	120(119.98)	120 (118.54)	119
frb59-26-5	4	107(106.64)	106(105.48)	107 (106.2)	hamming10-2	5	521(516.98)	515(514.48)	515(512.64)
hamming10-4	4	69(68.08)	69(68.04)	70(69.05)	hamming10-4	5	80 (79.02)	79(78.88)	80
hamming8-2	4	130	130 (129.32)	130	keller6	5	125	125	126(125.12)
keller6	4	117 (113.40)	117 (114.66)	117 (114.49)	p_hat1500-2	5	117	117 (116.48)	117
p_hat1500-2	4	107	107 (106.82)	107	p_hat1500-3	5	165(164.9)	164(163.98)	165 (164.88)
san1000	4	33	33 (32.94)	33	p_hat500-3	5	90	90 (89.12)	90
san400_0.5_1	4	29	29 (28.58)	29	san1000	5	41	41 (40.92)	41
san400_0.7_1	4	81(80.82)	81 (80.8)	81 (80.8)	san400_0.5_1	5	36 (35.28)	36 (35.14)	36
san400_0.7_3	4	50(49.82)	50 (49.78)	50 (49.78)					

Table 2: Experimental results of Nukplex, DCCplex and KLS on classic instances II. All algorithms are executed for 100 independent runs, with a cutoff time of 1000 seconds for each run.

Instance	timelimit	k	Nukplex max(avg)	DCCplex max(avg)	KLS max(avg)	Instance	timelimit	k	Nukplex max(avg)	DCCplex max(avg)	KLS max(avg)
rt-retweet-crawl	100	2	14	14 (13.3)	14	soc-orkut	100	3	59	58(53.1)	59
soc-digg	100	2	57	57 (55.3)	57 (56.8)	rt-retweet-crawl	100	4	16	16 (15.5)	16
socfb-A-anon	100	2	28	28 (27.3)	28	soc-digg	100	4	69	69 (68.7)	69
socfb-B-anon	100	2	27	27 (26.6)	27	socfb-A-anon	100	4	35(34.88)	34	34
soc-FourSquare	100	2	35	35 (34.9)	35	socfb-B-anon	100	4	33	33 (32.96)	33
soc-gowalla	100	2	30	30 (29.3)	30	soc-pokec	100	4	32 (31.6)	32 (30.4)	32
soc-pokec	100	2	31(30.8)	26(25.7)	26	soc-orkut	100	4	62	60(48.7)	61
soc-orkut	100	2	52	52 (49.3)	52	cage15	100	5	11	11	11 (10.98)
audikw1	100	3	39	39	39 (38.71)	soc-digg	100	5	72	72 (71.4)	72 (71.4)
rt-retweet-crawl	100	3	15	15 (14.4)	15	socfb-B-anon	100	5	35(34.88)	35 (34.5)	35 (34.5)
soc-digg	100	3	63	63 (61.8)	63	soc-orkut	100	5	67(66.2)	66(49.9)	63
socfb-A-anon	100	3	32	32 (31.2)	32	soc-orkut	1000	2	52	52 (51.7)	52
socfb-B-anon	100	3	30	30 (29)	30	soc-orkut	1000	3	59	59 (58.6)	59
soc-FourSquare	100	3	39	39 (38.7)	39	soc-orkut	1000	4	63(62.6)	61	62(61.4)
soc-pokec	100	3	32(31.12)	29(28.8)	29	soc-orkut	1000	5	68(66.8)	66(64.5)	63

Table 3: Experimental results of Nukplex, DCCplex and KLS on large sparse instances.

Instance	k	Nukplex max(avg)	KpLeX-Gap max	DiseMKP max	Instance	k	Nukplex max(avg)	KpLeX-Gap max	DiseMKP max	Instance	k	Nukplex max(avg)	KpLeX-Gap max	DiseMKP max
frb100-40	2	131(128.02)	82	93	san1000	2	18(17.06)	10	16	johnson16-2-4	3	16	8	16
frb30-15-1	2	40	25	34	san200.0.7.1	2	31	30	30	johnson32-2-4	3	32	16	32
frb30-15-2	2	39	26	33	san200.0.7.2	2	26(25.4)	15	24	keller5	3	45	24	35
frb30-15-3	2	40	26	35	san200.0.9.2	2	71	51	70	keller6	3	93	50	64
frb30-15-4	2	39	26	34	san200.0.9.3	2	54	35	48	p_hat1000-1	3	15	9	15
frb30-15-5	2	40	26	34	san400.0.5.1	2	15	13	14	p_hat1000-2	3	67	44	64
frb35-17-1	2	46	29	38	san400.0.7.1	2	42(41.14)	40	40	p_hat1000-3	3	98	62	94
frb35-17-2	2	46	30	39	san400.0.7.2	2	33(32.46)	18	30	p_hat1500-1	3	17	11	16
frb35-17-3	2	47	31	40	san400.0.7.3	2	28	16	24	p_hat1500-2	3	93	60	90
frb35-17-4	2	47	31	40	san400.0.9.1	2	103(102.98)	99	100	p_hat1500-3	3	133	88	127
frb35-17-5	2	46	31	40	sanr200.0.9	2	51	38	49	p_hat300-3	3	52	33	51
frb40-19-1	2	55	35	43	sanr400.0.5	2	15	12	15	p_hat500-1	3	14	9	14
frb40-19-2	2	54	34	46	sanr400.0.7	2	26	19	24	p_hat500-2	3	50	34	49
frb40-19-3	2	53	34	42	frb100-40	3	156(153.06)	82	118	p_hat500-3	3	72	47	70
frb40-19-4	2	52	35	45	frb30-15-1	3	48	25	44	p_hat700-1	3	15	14	15
frb40-19-5	2	53	35	48	frb30-15-2	3	48	26	42	p_hat700-2	3	62	41	60
frb45-21-1	2	59	38	50	frb30-15-3	3	48	26	44	p_hat700-3	3	89	60	88
frb45-21-2	2	59	39	44	frb30-15-4	3	47	26	42	san1000	3	25	10	24
frb45-21-3	2	60	38	47	frb30-15-5	3	48	26	44	san200.0.7.1	3	46	30	45
frb45-21-4	2	61(60.98)	39	51	frb35-17-1	3	55	29	49	san200.0.7.2	3	37	15	36
frb45-21-5	2	59	39	48	frb35-17-2	3	55(54.32)	30	47	san200.0.9.3	3	73	35	72
frb50-23-1	2	67	44	55	frb35-17-3	3	57	31	50	san400.0.5.1	3	22	13	21
frb50-23-2	2	67(66.38)	44	55	frb35-17-4	3	57	31	51	san400.0.7.1	3	61	40	60
frb50-23-3	2	65(64.82)	44	51	frb35-17-5	3	56	31	49	san400.0.7.2	3	47(46.1)	18	45
frb50-23-4	2	67(66.02)	43	53	frb40-19-1	3	66	35	59	san400.0.7.3	3	39(38.36)	16	36
frb50-23-5	2	67(66.98)	42	50	frb40-19-2	3	65	34	57	san400.0.9.1	3	150	99	150
frb53-24-1	2	71	45	54	frb40-19-3	3	63	34	55	sanr200.0.7	3	26	16	26
frb53-24-2	2	70	45	53	frb40-19-4	3	63	35	54	sanr200.0.9	3	61	38	57
frb53-24-3	2	70	45	56	frb40-19-5	3	63	35	54	sanr400.0.5	3	18	12	18
frb53-24-4	2	70(69.98)	45	58	frb45-21-1	3	71(70.9)	38	60	sanr400.0.7	3	30	19	28
frb53-24-5	2	69(68.44)	45	53	frb45-21-2	3	71	39	59	frb100-40	4	179(176.9)	82	142
frb56-25-1	2	75	48	59	frb45-21-3	3	72(71.74)	38	61	frb30-15-1	4	55	25	51
frb56-25-2	2	75	47	58	frb45-21-4	3	73(72.4)	39	64	frb30-15-2	4	55(54.68)	26	49
frb56-25-3	2	74	48	57	frb45-21-5	3	71(70.74)	39	62	frb30-15-3	4	56	26	51
frb56-25-4	2	74(73.98)	48	58	frb50-23-1	3	80(79.06)	44	66	frb30-15-4	4	56(55.88)	26	49
frb56-25-5	2	74(73.98)	48	56	frb50-23-2	3	79	44	67	frb30-15-5	4	56	26	51
frb59-26-1	2	79(78.98)	51	62	frb50-23-3	3	77(76.4)	44	62	frb35-17-1	4	64	29	57
frb59-26-2	2	79(78.96)	49	59	frb50-23-4	3	79	43	65	frb35-17-2	4	63	30	56
frb59-26-3	2	78(77.98)	50	60	frb50-23-5	3	80(79.4)	42	66	frb35-17-3	4	67	31	61
frb59-26-4	2	79(78.1)	50	62	frb53-24-1	3	85	45	69	frb35-17-4	4	66(65.26)	31	60
frb59-26-5	2	78	50	57	frb53-24-2	3	83(82.92)	45	72	frb35-17-5	4	65	31	60
brock200.1	2	26	20	25	frb53-24-3	3	84(83.18)	45	68	frb40-19-1	4	77	35	71
brock400.1	2	30	23	28	frb53-24-4	3	84(83.7)	45	68	frb40-19-2	4	75(74.98)	34	67
brock400.2	2	30	23	29	frb53-24-5	3	82	45	66	frb40-19-3	4	74	34	64
brock400.3	2	31(30.64)	22	28	frb56-25-1	3	90(89.46)	48	76	frb40-19-4	4	73(72.98)	35	65
brock400.4	2	33	23	28	frb56-25-2	3	89	47	76	frb40-19-5	4	74	35	65
brock800.1	2	25	19	23	frb56-25-3	3	88(87.92)	48	73	frb45-21-1	4	82	38	73
brock800.2	2	25	19	23	frb56-25-4	3	88(87.66)	48	73	frb45-21-2	4	82(81.12)	39	71
brock800.3	2	25	19	23	frb56-25-5	3	88(87.48)	48	72	frb45-21-3	4	83(82.98)	38	72
brock800.4	2	26(25.96)	18	23	frb59-26-1	3	94(93.44)	51	80	frb45-21-4	4	84(83.18)	39	75
C1000.9	2	82(81.98)	60	66	frb59-26-2	3	94(93.66)	49	77	frb45-21-5	4	82(81.66)	39	74
C125.9	2	43	33	42	frb59-26-3	3	94(92.98)	50	74	frb50-23-1	4	92	44	79
C2000.5	2	20(19.78)	15	17	frb59-26-4	3	93(92.9)	50	75	frb50-23-2	4	92(91.7)	44	82
C2000.9	2	94(93.42)	68	74	frb59-26-5	3	93(92.88)	50	78	frb50-23-3	4	88	44	74
C250.9	2	55	41	50	brock200.1	3	30	20	29	frb50-23-4	4	92(91.2)	43	77
C4000.5	2	21(20.58)	15	18	brock200.3	3	20	13	20	frb50-23-5	4	92	42	77
C500.9	2	69	50	61	brock200.4	3	23	15	23	frb53-24-1	4	99(98.98)	45	86
DSJC1000.5	2	18	14	16	brock400.1	3	36	23	32	frb53-24-2	4	96(95.5)	45	82
DSJC500.5	2	16	12	16	brock400.2	3	36	23	34	frb53-24-3	4	97(96.84)	45	80
gen200.p0.9.44	2	53	38	50	brock400.3	3	36	22	33	frb53-24-4	4	97(96.32)	45	84
gen200.p0.9.55	2	57	40	52	brock400.4	3	36	23	33	frb53-24-5	4	94	45	79
gen400.p0.9.55	2	68(67.8)	47	56	brock800.1	3	30(29.9)	19	26	frb56-25-1	4	104(103.88)	48	91
gen400.p0.9.65	2	74	48	64	brock800.2	3	30	19	28	frb56-25-2	4	104(103.04)	47	90
gen400.p0.9.75	2	80	47	74	brock800.3	3	30	19	26	frb56-25-3	4	101(100.98)	48	87
hamming10-4	2	48	36	41	brock800.4	3	29	18	25	frb56-25-4	4	101(100.52)	48	85
johnson16-2-4	2	10	8	10	C1000.9	3	96(95.96)	60	83	frb56-25-5	4	102(101.04)	48	85
johnson32-2-4	2	21	16	21	C125.9	3	51	33	50	frb59-26-1	4	108(107.92)	51	92
keller5	2	31	24	30	C2000.5	3	23(22.5)	15	20	frb59-26-2	4	108(107.96)	49	93
keller6	2	63	50	62	C2000.9	3	109(108.64)	68	88	frb59-26-3	4	108(107.12)	50	90
MANN_a27	2	236(235.96)	236	234	C250.9	3	65	41	59	frb59-26-4	4	107(106.96)	50	90
MANN_a45	2	662	342	660	C4000.5	3	25(24)	15	20	frb59-26-5	4	107(106.64)	50	91
MANN_a81	2	2162	1096	2160	C500.9	3	81	50	73	brock200.1	4	35	20	33
p_hat1000-2	2	56	44	55	c-fat500-10	3	126	126	0	brock200.2	4	18	10	18
p_hat1000-3	2	82	62	78	DSJC1000.5	3	21	14	20	brock200.3	4	23	13	23
p_hat1500-1	2	14	11	14	DSJC500.5	3	19	12	18	brock200.4	4	26	15	26
p_hat1500-2	2	80	60	74	gen200.p0.9.44	3	66	38	64	brock400.1	4	41(40.98)	23	36
p_hat1500-3	2	114	88	109	gen200.p0.9.55	3	64	40	62	brock400.2	4	41(40.98)	23	39
p_hat300-3	2	44	33	43	gen400.p0.9.55	3	87	47	82	brock400.3	4	41	22	38
p_hat500-2	2	42	34	42	gen400.p0.9.65	3	101	48	96	brock400.4	4	41	23	37
p_hat500-3	2	62	47	60	gen400.p0.9.75	3	114	47	111	brock800.1	4	34	19	31
p_hat700-2	2	52	49	50	hamming10-4	3	64	36	51	brock800.2	4	34	19	30
p_hat700-3	2	76	60	73	hamming8-4	3	20	16	20	brock800.3	4	34	19	30

Table 4: Experimental results of Nukplex, KpLeX-Gap and DiseMKP on classic instances I. Nukplex is executed for 100 independent runs, with a cutoff time of 1000 seconds for each run, whereas the two exact algorithms are executed with a cutoff time of 1800 seconds.

Instance	k	Nukplex max(avg)	KpLeX-Gap max	DiseMKP max	Instance	k	Nukplex max(avg)	KpLeX-Gap max	DiseMKP max	Instance	k	Nukplex max(avg)	KpLeX-Gap max	DiseMKP max
brock800.4	4	34(33.08)	18	29	frb30-15-1	5	63	25	59	C1000.9	5	122(121.26)	60	106
C1000.9	4	110(109.28)	60	96	frb30-15-2	5	62	26	57	C125.9	5	65	33	64
C125.9	4	58	33	58	frb30-15-3	5	63	26	58	C2000.5	5	28	15	24
C2000.5	4	26(25.08)	15	22	frb30-15-4	5	62	26	57	C2000.9	5	137(136.34)	68	116
C2000.9	4	123(122.62)	68	102	frb30-15-5	5	63	26	57	C250.9	5	84	41	80
C250.9	4	75	41	69	frb35-17-1	5	73	29	65	C4000.5	5	30(29.94)	15	25
C4000.5	4	28(26.7)	15	22	frb35-17-2	5	72(71.82)	30	64	C500.9	5	104(103.62)	50	94
C500.9	4	93(92.9)	50	84	frb35-17-3	5	75	31	69	DSJC1000.5	5	27	14	23
DSJC1000.5	4	24(23.82)	14	21	frb35-17-4	5	74	31	68	DSJC500.5	5	24	12	22
DSJC500.5	4	21	12	20	frb35-17-5	5	74(73.7)	31	68	gen200.p0.9.44	5	84	38	79
gen200.p0.9.44	4	76	38	74	frb40-19-1	5	88	35	81	gen200.p0.9.55	5	80	40	79
gen200.p0.9.55	4	73	40	72	frb40-19-2	5	85(84.66)	34	77	gen400.p0.9.55	5	124	47	119
gen400.p0.9.55	4	112	47	106	frb40-19-3	5	83(82.66)	34	74	gen400.p0.9.65	5	138	48	131
gen400.p0.9.65	4	132	48	123	frb40-19-4	5	81	35	73	gen400.p0.9.75	5	136	47	134
gen400.p0.9.75	4	136	47	134	frb40-19-5	5	83(82.7)	35	73	hamming10-2	5	521(516.98)	512	512
hamming10-4	4	69(68.08)	36	63	frb45-21-1	5	93(92.68)	38	83	hamming10-4	5	80(79.02)	36	73
hamming8-2	4	130	128	128	frb45-21-2	5	92(91.88)	39	81	hamming8-2	5	152	128	134
hamming8-4	4	25	16	25	frb45-21-3	5	94(93.28)	38	84	hamming8-4	5	32	16	32
johnson16-2-4	4	19	8	19	frb45-21-4	5	94	39	85	johnson16-2-4	5	24	8	24
johnson32-2-4	4	38	16	38	frb45-21-5	5	92	39	82	johnson32-2-4	5	48	16	48
keller4	4	23	11	22	frb50-23-1	5	104(103.56)	44	93	keller4	5	28	11	27
keller5	4	53	24	46	frb50-23-2	5	104(103.6)	44	93	keller5	5	61	24	54
keller6	4	117(113.4)	50	93	frb50-23-3	5	99	44	87	keller6	5	125	50	119
p_hat1000-1	4	18	9	17	frb50-23-4	5	104(103.28)	43	89	p_hat1000-1	5	20	9	20
p_hat1000-2	4	76	44	73	frb50-23-5	5	104	42	92	p_hat1000-2	5	84	44	84
p_hat1000-3	4	111	62	106	frb53-24-1	5	112	45	98	p_hat1000-3	5	122	62	116
p_hat1500-1	4	19	11	18	frb53-24-2	5	108(107.76)	45	94	p_hat1500-1	5	21	11	20
p_hat1500-2	4	107	60	103	frb53-24-3	5	110(109.1)	45	94	p_hat1500-2	5	117	112	114
p_hat1500-3	4	150	88	143	frb53-24-4	5	109	45	96	p_hat1500-3	5	165(164.9)	88	158
p_hat300-2	4	41	25	41	frb53-24-5	5	107(106.28)	45	94	p_hat300-3	5	65	33	64
p_hat300-3	4	59	33	58	frb56-25-1	5	118(117.34)	48	106	p_hat500-1	5	18	9	18
p_hat500-1	4	16	14	16	frb56-25-2	5	117(116.32)	47	99	p_hat500-2	5	62	60	61
p_hat500-2	4	57	56	56	frb56-25-3	5	114	48	99	p_hat500-3	5	90	47	87
p_hat500-3	4	81	47	79	frb56-25-4	5	114(113.2)	48	97	p_hat700-1	5	19	17	18
p_hat700-1	4	17	16	17	frb56-25-5	5	115(114.12)	48	100	p_hat700-2	5	79	73	76
p_hat700-2	4	70	67	69	frb59-26-1	5	122(121.8)	51	110	p_hat700-3	5	109	60	107
p_hat700-3	4	100	60	98	frb59-26-2	5	122(121.78)	49	106	san1000	5	41	10	40
san1000	4	33	10	32	frb59-26-3	5	121(120.96)	50	105	san200.0.7.1	5	75	30	75
san200.0.7.1	4	60	30	60	frb59-26-4	5	122(120.86)	50	103	san200.0.7.2	5	60	15	60
san200.0.7.2	4	49	15	48	frb59-26-5	5	120(119.98)	50	104	san200.0.9.2	5	105	51	103
san200.0.9.2	4	105	105	103	brock200.1	5	39	20	37	san200.0.9.3	5	100	35	95
san200.0.9.3	4	96	35	95	brock200.2	5	20	10	20	san400.0.5.1	5	36(35.28)	13	35
san400.0.5.1	4	29	13	28	brock200.3	5	26	13	25	san400.0.7.1	5	100	40	100
san400.0.7.1	4	81(80.82)	40	80	brock200.4	5	30	15	29	san400.0.7.2	5	76	18	75
san400.0.7.2	4	61	18	60	brock400.1	5	46(45.68)	23	42	san400.0.7.3	5	61	16	60
san400.0.7.3	4	50(49.82)	16	48	brock400.2	5	45	23	43	san400.0.9.1	5	200	99	193
san400.0.9.1	4	200	99	193	brock400.3	5	46(45.98)	22	43	sanr200.0.7	5	33	16	31
sanr200.0.7	4	30	16	29	brock400.4	5	46	23	42	sanr200.0.9	5	77	38	74
sanr200.0.9	4	69	38	65	brock800.1	5	37	19	34	sanr400.0.5	5	24	12	22
sanr400.0.5	4	21	12	21	brock800.2	5	38	19	33	sanr400.0.7	5	39	19	36
sanr400.0.7	4	35	19	32	brock800.3	5	38	19	33					
frb100-40	5	202(199.28)	82	170	brock800.4	5	37	18	33					

Table 5: Experimental results of Nukplex, KpLeX-Gap and DiseMKP on classic instances II. Nukplex is executed for 100 independent runs, with a cutoff time of 1000 seconds for each run, whereas the two exact algorithms are executed with a cutoff time of 1800 seconds.

Instance	k	Nukplex max(avg)	KpLeX-Gap max	DiseMKP max	Instance	k	Nukplex max(avg)	KpLeX-Gap max	DiseMKP max	Instance	k	Nukplex max(avg)	KpLeX-Gap max	DiseMKP max
333SP	2	5	5	4	soc-orkut	3	59	59	31	as-22july06	5	24	24	23
kron.*-logn16	2	140	136	138	soc-buzznet	3	41	27	41	cit-Patents	5	31	8	31
rgg_n.2.17_s0	2	16	16	15	soc-flickr	3	77	76	77	audikw1	5	45	45	33
soc-flickr	2	68	64	66	audikw1	4	45	45	33	kron.*-logn16	5	152	136	23
soc-digg	2	57	57	25	cit-Patents	4	26	6	26	WikiTalk	5	44	44	42
soc-orkut	2	52	52	27	kron.*-logn16	4	148	146	147	soc-buzznet	5	50	48	49
audikw1	3	39	39	36	WikiTalk	4	41	40	39	soc-flickr	5	90	89	89
eu-2005	3	390	390	389	soc-buzznet	4	46	27	45	tech-as-skitter	5	75	75	72
kron.*-logn16	3	144	136	143	soc-orkut	4	63(62.6)	63	34	soc-digg	5	72	71	36
WikiTalk	3	36	35	35	soc-flickr	4	85	56	84	soc-orkut	5	68(66.8)	68	37
tech-as-skitter	3	71	71	67	tech-as-skitter	4	74	74	69					
soc-digg	3	63	59	29	soc-digg	4	69	66	33					

Table 6: Experimental results of Nukplex, KpLeX-Gap and DiseMKP on large sparse instances. Nukplex is executed for 100 independent runs, with a cutoff time of 1000 seconds for each run, whereas the two exact algorithms are executed with a cutoff time of 1800 seconds.

Instance	k	Nukplex max(avg)	DiseMKP max	KpLeX-Gap max	Instance	k	Nukplex max(avg)	DiseMKP max	KpLeX-Gap max	Instance	k	Nukplex max(avg)	DiseMKP max	KpLeX-Gap max
sec_retweet	2	166	165	166	soc-digg	10	87	53	87	soc-twitter-follows	15	30	26	30
soc-BlogCatalog	2	54	54	52	socfb-A-anon	10	47	43	47	soc-youtube	15	43	41	43
soc-digg	2	57	25	57	socfb-Duke14	10	60	59	60	soc-youtube-snap	15	43	42	43
soc-flickr	2	68	66	64	socfb-MIT	10	57	56	57	tech-as-skitter	15	95	89	95
soc-FourSquare	2	35	33	35	socfb-Stanford3	10	75	57	75	tech-internet-as	15	37	36	37
soc-orkut	2	52	27	52	socfb-UCLA	10	67	66	67	web-spam	15	47	45	47
soc-BlogCatalog	3	60	58	58	socfb-Ullinois	10	82	47	82	web-wikipedia2009	15	37	35	35
soc-buzznet	3	41	41	27	soc-flickr	10	114	113	56	ia-enron-large	15	45	42	45
soc-digg	3	63	29	59	soc-FourSquare	10	53	49	53	ia-wiki-Talk	20	51	22	50
soc-flickr	3	77	77	76	soc-gowalla	10	42	39	42	sc-reality	20	1251 (1248.9)	1248	1251
soc-FourSquare	3	39	36	39	soc-LiveMocha	10	41	25	41	sc-msdoor	20	45	40	45
soc-orkut	3	59	31	59	soc-orkut	10	89 (88.2)	51	89	sc-pkustk11	20	56 (55.3)	56	56
tech-as-skitter	3	71	67	71	soc-youtube-snap	10	35	34	35	sc-pkustk13	20	55	54	55
soc-orkut	4	63 (62.6)	63	34	tech-as-skitter	10	84	80	84	sc-pwtk	20	46	38	46
soc-buzznet	4	46	45	27	web-spam	10	40	39	40	sc-shipsec5	20	44	42	44
soc-digg	4	69	33	66	web-wikipedia2009	10	33	26	33	soc-BlogCatalog	20	123	123	41
socfb-Duke14	4	45	43	45	ia-enron-large	10	38	36	38	soc-buzznet	20	89	88	88
socfb-Indiana	4	57	56	57	ia-wiki-Talk	15	44	42	44	soc-delicious	20	49	48	49
soc-flickr	4	85	84	56	sc-pkustk13	15	50	45	50	soc-digg	20	109	81	109
soc-karate	4	8	7	8	sc-pwtk	15	38	36	38	socfb-A-anon	20	61	58	61
tech-as-skitter	4	74	69	74	soc-BlogCatalog	15	109	109	41	socfb-B-anon	20	64	52	64
soc-BlogCatalog	4	66	64	61	soc-buzznet	15	78	77	76	socfb-CMU	20	67	66	67
soc-buzznet	5	50	49	48	soc-delicious	15	43	42	43	socfb-Stanford3	20	77	75	77
soc-digg	5	72	36	71	soc-digg	15	100	68	100	socfb-Texas84	20	94	93	94
socfb-Duke14	5	48	46	48	socfb-A-anon	15	54	52	54	socfb-Ullinois	20	96	65	96
socfb-Stanford3	5	67	65	67	socfb-B-anon	15	57	45	57	soc-flickr	20	153	152	150
soc-flickr	5	90	89	89	socfb-CMU	15	62	60	62	soc-FourSquare	20	65	54	65
soc-FourSquare	5	44	38	44	socfb-Stanford3	15	77	67	77	soc-LiveMocha	20	60	41	60
soc-orkut	5	68 (66.2)	37	68	socfb-Ullinois	15	89	57	89	soc-orkut	20	108 (100.5)	73	111
tech-as-skitter	5	75	72	75	socfb-Wisconsin87	15	67	65	67	soc-pokec	20	55	49	55
soc-BlogCatalog	5	72	69	70	soc-flickr	15	135	133	56	soc-slashdot	20	68	67	68
ia-wiki-Talk	10	35	34	35	soc-FourSquare	15	59	49	59	soc-youtube	20	50	48	50
sc-pkustk11	10	48 (43.8)	48	48	soc-gowalla	15	49	47	49	soc-youtube-snap	20	51	48	51
sc-pwtk	10	33 (31.8)	33	33	soc-LiveMocha	15	52	34	52	tech-as-skitter	20	104	102	104
soc-BlogCatalog	10	93	90	90	soc-orkut	15	99 (96.4)	63	101	ia-enron-large	20	51	49	51
soc-buzznet	10	65	64	64	soc-pokec	15	49	42	49	web-wikipedia2009	20	46	44	45

Table 7: Experimental results of Nukplex, KpLeX-Gap and DiseMKP on the Network-Repo instances. Nukplex is executed for 10 independent runs, with a cutoff time of 1000 seconds for each run, whereas the two exact algorithms are executed with a cutoff time of 1800 seconds.

Instance	k	Nukplex max(avg)	KpLeX-Gap max	DiseMKP max	Instance	k	Nukplex max(avg)	KpLeX-Gap max	DiseMKP max	Instance	k	Nukplex max(avg)	KpLeX-Gap max	DiseMKP max
333SP	2	5	5	4	audikw1	5	45	45	33	kron *-logn16	15	182	180	178
kron *-logn16	2	140	136	138	cit-Patents	5	31	8	31	Slashdot0902	15	61	61	60
rgg n 2 17 s0	2	16	16	15	kron *-logn16	5	152	136	23	web-Stanford	15	74	72	74
audikw1	3	39	39	36	WikiTalk	5	44	44	42	WikiTalk	15	70	69	70
eu-2005	3	390	390	389	audikw1	10	48	48	45	Wiki-Vote	15	47	47	46
kron *-logn16	3	144	136	143	Email-EuAll	10	36	36	35	audikw1	20	60 (58)	60	54
WikiTalk	3	36	35	35	kron *-logn16	10	168	165	164	Slashdot0811	20	68	68	67
audikw1	4	45	45	33	WikiTalk	10	58	56	57	lashdot0902	20	69	69	68
cit-Patents	4	26	6	26	audikw1	15	52	52	45	web-Stanford	20	82	82	48
kron *-logn16	4	148	146	147	cit-Patents	15	63	63	62	WikiTalk	20	81	79	79
WikiTalk	4	41	40	39	cond-mat-2005	15	38	38	31					

Table 8: Experimental results of Nukplex, KpLeX-Gap and DiseMKP on the 10th-DIMACS instances. Nukplex is executed for 10 independent runs, with a cutoff time of 1000 seconds for each run, whereas the two exact algorithms are executed with a cutoff time of 1800 seconds.