

# Statistical Mechanics Notes

## Pratice and Examples

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<sup>1</sup>[www.example.com](http://www.example.com)



Dedicated to Calvin and Hobbes.



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# Preface

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## Un-numbered sample section

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## Structure of book

Each unit will focus on <SOMETHING>.

## About the companion website

The website<sup>1</sup> for this file contains:

- A link to (freely downloadable) latest version of this document.
- Link to download LaTeX source for this document.
- Miscellaneous material (e.g. suggested readings etc).

## Acknowledgements

- A special word of thanks goes to Professor Don Knuth<sup>2</sup> (for T<sub>E</sub>X) and Leslie Lamport<sup>3</sup> (for L<sup>A</sup>T<sub>E</sub>X).
- I'll also like to thank Gummi<sup>4</sup> developers and LaTeXila<sup>5</sup> development team for their awesome L<sup>A</sup>T<sub>E</sub>X editors.
- I'm deeply indebted my parents, colleagues and friends for their support and encouragement.

Amber Jain

<http://amberj.devio.us/>

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<sup>1</sup><https://github.com/amberj/latex-book-template>

<sup>2</sup><http://www-cs-faculty.stanford.edu/~uno/>

<sup>3</sup><http://www.lamport.org/>

<sup>4</sup><http://gummi.midnightcoding.org/>

<sup>5</sup><http://projects.gnome.org/latexila/>

# 1

## Introductory Chapter

*“Available energy is the main object at stake in the struggle for existence and the evolution of the world.”*

– Ludwig Boltzmann

### 1.1 Boltzmann’s Distribution

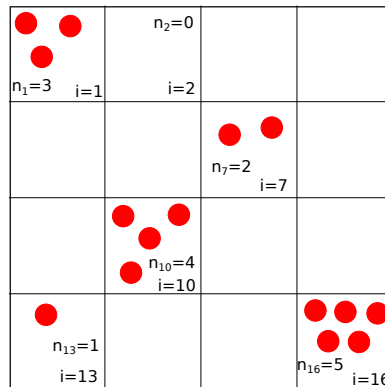
#### 1.1.1 Gas Example

$N$  Gas particles occupy small volumetric cells  $i = 1, 2, 3, \dots, s$  of phase space, with occupation number  $n_i$ . Particle number is conserved so

$$\sum_i n_i = N \quad (1.1)$$

The number of ways  $W$  that any particular distribution  $\{n_1, n_2, \dots, n_s\}$  of particles will fall within their respective volumetric cells in phase space is given by the multinomial formula

$$W = \frac{N!}{(n_1! n_2! \dots n_s!)} \quad (1.2)$$



Taking the logarithm of  $W$  and approximating the factorial for large  $N$  using Stirling's formula gives

$$\log W = \log N! - \sum_i \log n_i! \approx -N \sum_i \frac{n_i}{N} \log \left( \frac{n_i}{N} \right) = -N \sum_i p_i \log p_i \quad (1.3)$$

where  $p_i = \frac{n_i}{N}$  is taken to be the probability that a particle is in cell  $i$ , provided  $N$  is sufficiently large. The entropy  $S$  is defined by

$$S = -k_B \sum_i p_i \log p_i \quad (1.4)$$

There are two constraints

$$\sum_i p_i = 1 \quad (1.5)$$

$$\sum_i p_i \epsilon_i = \bar{\epsilon} \quad (1.6)$$

where  $\epsilon_i$  is the total energy of cell  $i$ , and  $\bar{\epsilon}$  is the average energy per particle.

## 1.2 Another section heading

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Table 1.1: Sample table

S. No.	Column#1	Column#2	Column#3
1	50	837	970
2	47	877	230
3	31	25	415
4	35	144	2356
5	45	300	556

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