## Assignemt 5

# 1.(u1, y1)

a) The selected model structure: oe323

**b)** 0e323 =

Discrete-time OE model: y(t) = [B(z)/F(z)]u(t) + e(t)

 $\mathsf{B}(\mathsf{z}) = 1.242 \; (+/-\; 0.03715) \; \mathsf{z}^{\mathsf{A}} - 3 \; + \; 0.75 \; (+/-\; 0.06609) \; \mathsf{z}^{\mathsf{A}} - 4 \; + \; 0.9234 \; (+/-\; 0.06609) \; \mathsf{z}^{\mathsf{A}} - \mathsf{z}^{\mathsf{A}} + \; 0.9234 \; (+/-\; 0.06609) \; \mathsf{z}^{\mathsf{A}} - \mathsf{z}^{\mathsf{A}} + \; 0.9234 \; (+/-\; 0.06609) \; \mathsf{z}^{\mathsf{A}} - \mathsf{z}^{\mathsf{A}} + \; 0.9234 \; (+/-\; 0.06609) \; \mathsf{z}^{\mathsf{A}} - \mathsf{z}^{\mathsf{A}} + \; 0.9234 \; (+/-\; 0.06609) \; \mathsf{z}^{\mathsf{A}} - \mathsf{z}^{\mathsf{A}} + \; 0.9234 \; (+/-\; 0.06609) \; \mathsf{z}^{\mathsf{A}} - \mathsf{z}^{\mathsf{A}} + \; 0.9234 \; (+/-\; 0.06609) \; \mathsf{z}^{\mathsf{A}} - \mathsf{z}^{\mathsf{A}} + \; 0.9234 \; (+/-\; 0.06609) \; \mathsf{z}^{\mathsf{A}} - \mathsf{z}^{\mathsf{A}} + \; 0.9234 \; (+/-\; 0.06609) \; \mathsf{z}^{\mathsf{A}} - \mathsf{z}^{\mathsf{A}} + \; 0.9234 \; (+/-\; 0.06609) \; \mathsf{z}^{\mathsf{A}} - \mathsf{z}^{\mathsf{A}} + \; 0.9234 \; (+/-\; 0.06609) \; \mathsf{z}^{\mathsf{A}} - \mathsf{z}^{\mathsf{A}} + \; 0.9234 \; (+/-\; 0.06609) \; \mathsf{z}^{\mathsf{A}} - \mathsf{z}^{\mathsf{A}} + \; 0.9234 \; (+/-\; 0.06609) \; \mathsf{z}^{\mathsf{A}} - \mathsf{z}^{\mathsf{A}} + \; 0.9234 \; (+/-\; 0.06609) \; \mathsf{z}^{\mathsf{A}} - \mathsf{z}^{\mathsf{A}} + \; 0.9234 \; (+/-\; 0.06609) \; \mathsf{z}^{\mathsf{A}} - \mathsf{z}^{\mathsf{A}} + \; 0.9234 \; (+/-\; 0.06609) \; \mathsf{z}^{\mathsf{A}} - \mathsf{z}^{\mathsf{A}} + \; 0.9234 \; (+/-\; 0.06609) \; \mathsf{z}^{\mathsf{A}} - \; 0.9234 \; \mathsf{z}^{\mathsf{A}} - \; 0.9234 \; \mathsf{z}^{\mathsf{A}} - \; 0.9234 \; \mathsf{z}^{\mathsf{A}} - \; 0$ 

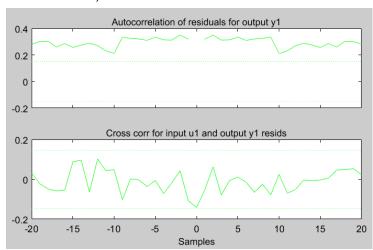
0.04139) z^-5

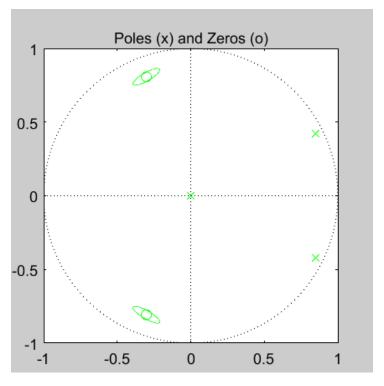
 $F(z) = 1 - 1.699 (+/- 0.0006168) z^{-1} + 0.8988 (+/- 0.0005557) z^{-2}$ 

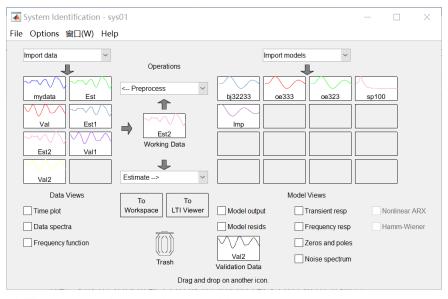
Name: oe323

Polynomial Orders: nb=3 nf=2 nk=3

Fit to estimation data: 93.1% FPE: 0.9434, MSE: 0.93







## c) The alternative model could be:

oe333 =

Discrete-time OE model: y(t) = [B(z)/F(z)]u(t) + e(t)

 $B(z) = 1.24 (+/-0.0369) z^{-3} + 0.681 (+/-0.06856) z^{-4} + 0.6648 (+/-0.1056) z^{-5}$ 

 $F(z) = 1 - 1.821 (+/- 0.04367) z^{-1} + 1.106 (+/- 0.07432) z^{-2} - 0.1094 (+/- 0.03928) z^{-3}$ 

Name: 0e333

Polynomial orders: nb=3 nf=3 nk=3

Fit to estimation data: 93.1% FPE: 0.9434, MSE: 0.93

#### 2.(u2,y2)

a) The selected model structure: arx224

**b)** arx224 =

Discrete-time ARX model: A(z)y(t) = B(z)u(t) + e(t)

 $A(z) = 1 - 1.326 (+/-0.01737) z^{-1} + 0.4265 (+/-0.01689) z^{-2}$ 

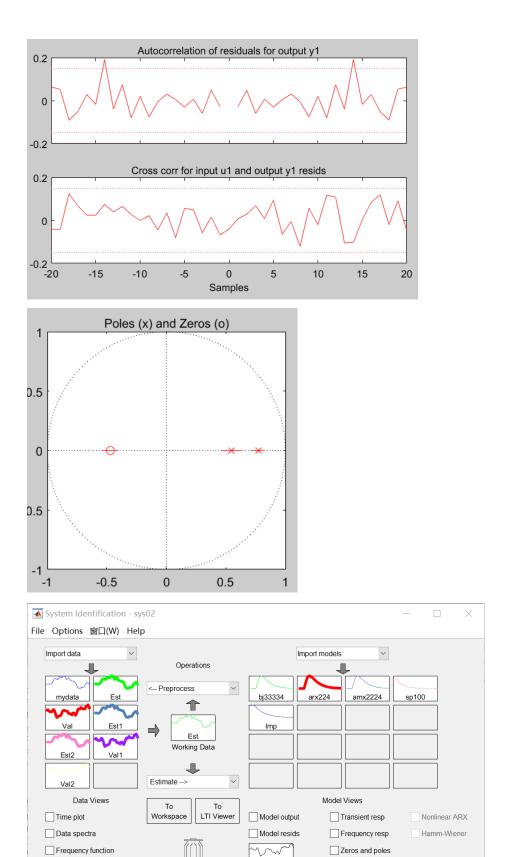
 $B(z) = 1.972 (+/-0.03796) z^{-4} + 0.9275 (+/-0.05068) z^{-5}$ 

Name: arx224

Polynomial Orders: nb=3 nf=2 nk=3

Fit to estimation data: 89.31% (prediction focus)

FPE: 1.009, MSE: 0.9915



c) The alternative model could be amx 2224

Trash

Val2

Validation Data

Noise spectrum

## 3.(u3,y3)

a) The selected model structure: amx2222

**b)** amx2222 =

Discrete-time ARMAX model: A(z)y(t) = B(z)u(t) + C(z)e(t)

 $A(z) = 1 - 1.507 (+/-0.01223) z^{-1} + 0.6971 (+/-0.01039) z^{-2}$ 

 $B(z) = 0.9862 (+/-0.03881) z^{-2} + 0.4697 (+/-0.05153) z^{-3}$ 

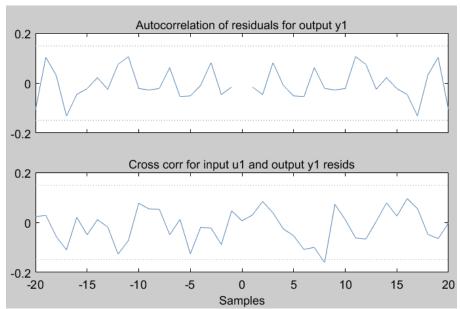
 $C(z) = 1 - 1.008 (+/-0.03981) z^{-1} + 0.2093 (+/-0.03877) z^{-2}$ 

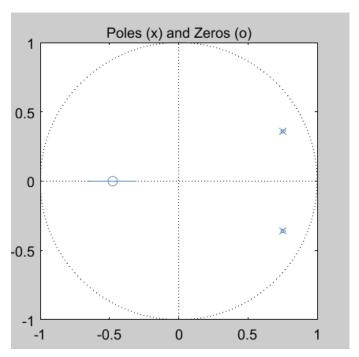
Name: amx2222

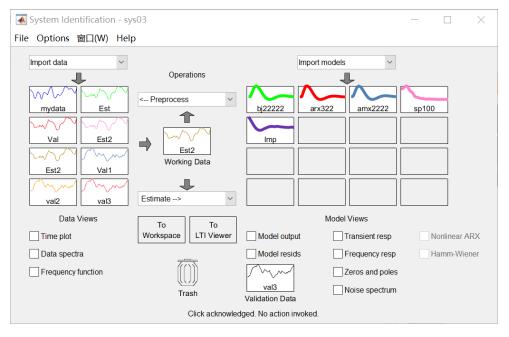
Polynomial Orders: na=2 nb=2 nc=2 nk=2

Fit to estimation data: 76.78% (prediction focus)

FPE: 1.005, MSE: 0.9881







c) The alternative model could be is bj22222

# 4.(u4,y4)

a) The selected model structure: amx2211

**b)** amx2211 =

Discrete-time ARMAX model: A(z)y(t) = B(z)u(t) + C(z)e(t)

 $A(z) = 1 - 1.112 (+/-0.03271) z^{-1} + 0.2905 (+/-0.02673) z^{-2}$ 

 $B(z) = 1.069 (+/-0.06149) z^{-1} + 0.4038 (+/-0.08782) z^{-2}$ 

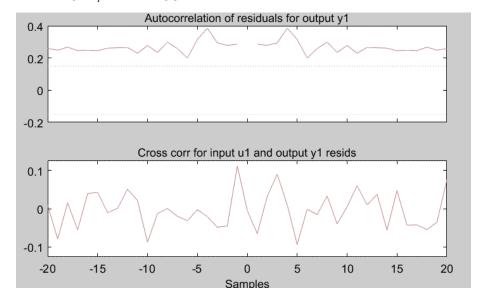
 $C(z) = 1 - 0.9897 (+/- 0.005488) z^{-1}$ 

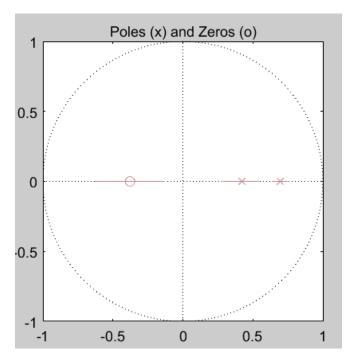
Name: amx2211

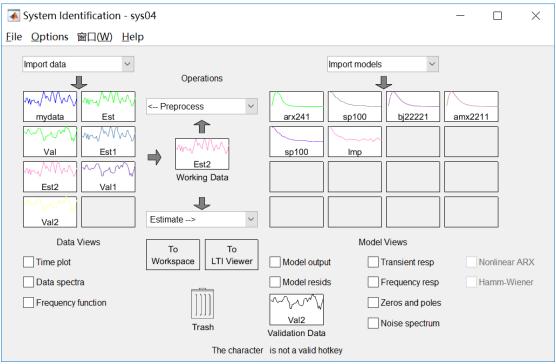
Polynomial Orders: na=2 nb=2 nc=1 nk=1

Fit to estimation data: 50.07% (prediction focus)

FPE: 2.617, MSE: 2.58







## c) No alternative models

#### 5. (u5,y5)

a) The selected model structure: bj11221

**b)** bj11221 =

Discrete-time BJ model: y(t) = [B(z)/F(z)]u(t) + [C(z)/D(z)]e(t)

 $B(z) = 1.304 (+/-0.005434) z^{-1}$ 

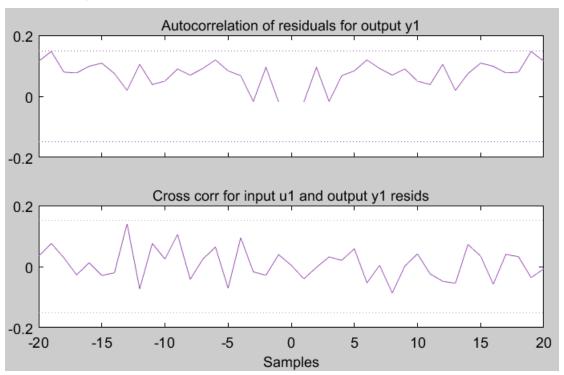
 $C(z) = 1 - 0.7385 (+/- 0.02653) z^{-1}$ 

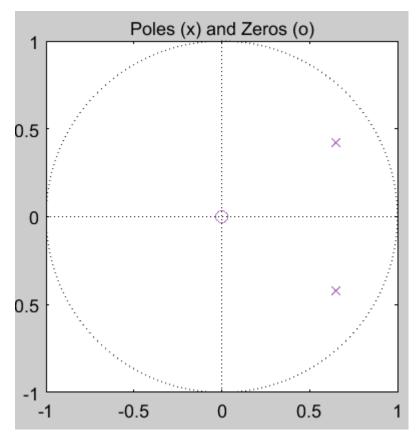
 $D(z) = 1 + 1.685 (+/-0.02434) z^{-1} + 0.7881 (+/-0.02434) z^{-2}$ 

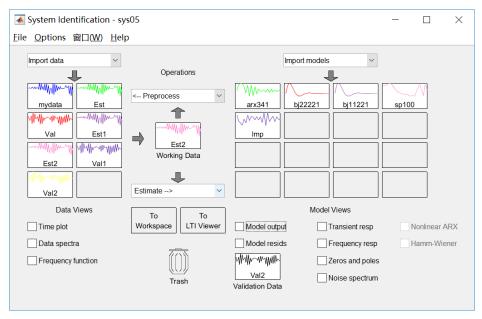
 $F(z) = 1 - 1.295 (+/-0.002506) z^{-1} + 0.5959 (+/-0.002065) z^{-2}$ 

Polynomial Orders: na=1 nb=1 nc=2 nd=2 nk=1 Fit to estimation data: 88.36% (prediction focus)

FPE: 1.565, MSE: 1.538







c) The alternative model for the data could be bj22221