# Imagination and Curiosity

#### **John Canny**

Spring 2018

Lecture 22 of CS194/294-129: Designing, Visualizing and Understanding Deep Neural Networks

Some slides borrowed from S. Levine et al. "Deep Reinforcement Learning"

#### Last Time: Q Functions

$$\nabla_{\theta} J(\theta) \approx \frac{1}{N} \sum_{i=1}^{N} \sum_{t=1}^{T} \nabla_{\theta} \log \pi_{\theta}(\mathbf{a}_{i,t} | \mathbf{s}_{i,t}) \left( \sum_{t'=1}^{T} \gamma^{t'-t} r(\mathbf{s}_{i,t'}, \mathbf{a}_{i,t'}) \right)$$
"reward to go"
$$\hat{Q}_{i,t}$$

Define an expected value estimator Q:

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#### Last Time: Advantage functions

$$Q(\mathbf{s}_t, \mathbf{a}_t) = \sum_{t'=t}^{T} E_{\pi_{\theta}} \left[ \gamma^{t'-t} r(\mathbf{s}_{t'}, \mathbf{a}_{t'}) | \mathbf{s}_t, \mathbf{a}_t \right] \quad \text{: true } expected \text{ reward-to-go} \\ \text{total reward from taking } \mathbf{a}_t \text{ in } \mathbf{s}_t$$

Value function 
$$V^{\pi}(\mathbf{s}_t) = E_{\mathbf{a}_t \sim \pi_{\theta}(\mathbf{a}_t | \mathbf{s}_t)}[Q^{\pi}(\mathbf{s}_t, \mathbf{a}_t)]$$
: total reward from  $\mathbf{s}_t$   
Advantage function  $A^{\pi}(\mathbf{s}_t, \mathbf{a}_t) = Q^{\pi}(\mathbf{s}_t, \mathbf{a}_t) - V^{\pi}(\mathbf{s}_t)$ : how much better  $\mathbf{a}_t$  is

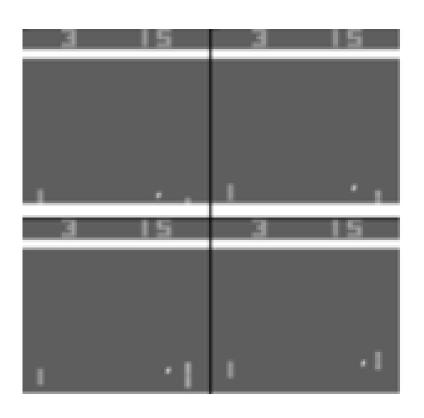
Advantage functions are typically sparse functions of state.

i.e. for many environments, most states have action advantages = 0.

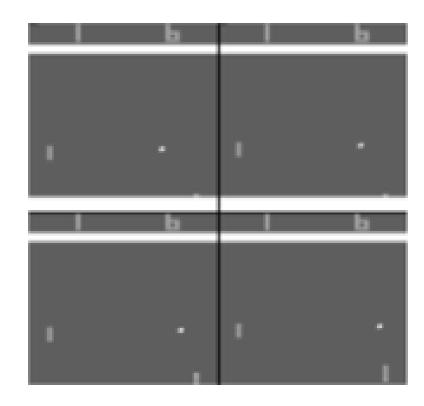
#### Advantage function Sparseness

Atari Pong, player on the right:

High advantage for some action:



Advantages close to zero (action doesn't affect reward) true for most states:



Advantage functions address the *temporal credit assignment problem*. Advantage focuses updates on actions that have high advantage, and ignores others:

#### Advantage function Sparseness

Advantage functions address the *temporal credit assignment problem*. Advantage focuses updates on actions that have high advantage, and ignores others.

Reinforce gradient: 
$$\nabla_{\theta} J(\theta) \approx \frac{1}{N} \sum_{i=1}^{N} \left( \sum_{t=1}^{T} \nabla_{\theta} \log \pi_{\theta}(\mathbf{a}_{i,t} | \mathbf{s}_{i,t}) \right) \left( \sum_{t=1}^{T} r(\mathbf{s}_{i,t}, \mathbf{a}_{i,t}) \right)$$

Actor-critic gradient:  $\nabla_{\theta} J(\theta) \approx \sum_{i} \nabla_{\theta} \log \pi_{\theta}(\mathbf{a}_{i}|\mathbf{s}_{i}) \hat{A}^{\pi}(\mathbf{s}_{i},\mathbf{a}_{i})$ 

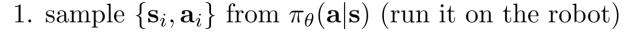
For the sequence  $(s_0, a_0, s_1, a_1, s_2, a_2, s_3, a_3, s_4, a_4, s_5, a_5, ...)$ Advantages: 0, 0, 0, 1.2, 0, 0

Backpropagated gradient

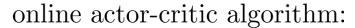
Gradients only backpropagate to actions with non-zero advantage, i.e. only actions which affect the reward are reinforced.

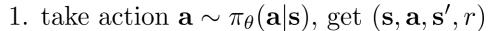
# Last Time: Actor-critic algorithms

batch actor-critic algorithm:

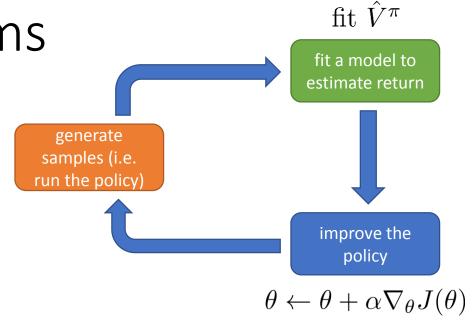


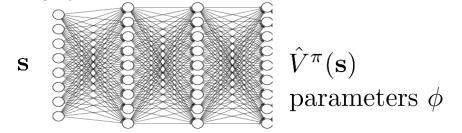
- 2. fit  $\hat{V}_{\phi}^{\pi}(\mathbf{s})$  to sampled reward sums
- 3. evaluate  $\hat{A}^{\pi}(\mathbf{s}_i, \mathbf{a}_i) = r(\mathbf{s}_i, \mathbf{a}_i) + \gamma \hat{V}_{\phi}^{\pi}(\mathbf{s}_i') \hat{V}_{\phi}^{\pi}(\mathbf{s}_i)$
- 4.  $\nabla_{\theta} J(\theta) \approx \sum_{i} \nabla_{\theta} \log \pi_{\theta}(\mathbf{a}_{i}|\mathbf{s}_{i}) \hat{A}^{\pi}(\mathbf{s}_{i},\mathbf{a}_{i})$
- 5.  $\theta \leftarrow \theta + \alpha \nabla_{\theta} J(\theta)$





- 2. update  $\hat{V}_{\phi}^{\pi}$  using target  $r + \gamma \hat{V}_{\phi}^{\pi}(\mathbf{s}')$
- 3. evaluate  $\hat{A}^{\pi}(\mathbf{s}, \mathbf{a}) = r(\mathbf{s}, \mathbf{a}) + \gamma \hat{V}_{\phi}^{\pi}(\mathbf{s}') \hat{V}_{\phi}^{\pi}(\mathbf{s})$
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"classic" deep Q-learning algorithm:



- 1. take some action  $\mathbf{a}_i$  and observe  $(\mathbf{s}_i, \mathbf{a}_i, \mathbf{s}_i', r_i)$ , add it to  $\mathcal{B}$
- 2. sample mini-batch  $\{\mathbf{s}_j, \mathbf{a}_j, \mathbf{s}'_j, r_j\}$  from  $\mathcal{B}$  uniformly
- 3. compute  $y_j = r_j + \gamma \max_{\mathbf{a}'_j} Q_{\phi'}(\mathbf{s}'_j, \mathbf{a}'_j)$  using target network  $Q_{\phi'}$   $4. \ \phi \leftarrow \phi \alpha \sum_j \frac{dQ_{\phi}}{d\phi}(\mathbf{s}_j, \mathbf{a}_j)(Q_{\phi}(\mathbf{s}_j, \mathbf{a}_j) y_j)$

4. 
$$\phi \leftarrow \phi - \alpha \sum_{j} \frac{dQ_{\phi}}{d\phi}(\mathbf{s}_{j}, \mathbf{a}_{j}) (Q_{\phi}(\mathbf{s}_{j}, \mathbf{a}_{j}) - y_{j})$$

5. update 
$$\phi'$$
: copy  $\phi$  every  $N$  steps

"classic" deep Q-learning algorithm:

#### Save to and sample from a replay buffer

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- 3. compute  $y_j = r_j + \gamma \max_{\mathbf{a}'_j} Q_{\phi'}(\mathbf{s}'_j, \mathbf{a}'_j)$  using target network  $Q_{\phi'}$  K = 14.  $\phi \leftarrow \phi \alpha \sum_j \frac{dQ_{\phi}}{d\phi}(\mathbf{s}_j, \mathbf{a}_j)(Q_{\phi}(\mathbf{s}_j, \mathbf{a}_j) y_j)$
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Use a target network, updated periodically

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#### Course Logistics

Guest lectures next week by Chelsea Finn and Andrew Critch.

Please try to attend in person.

• The course survey is on Wednesday, you can get that done as well...

# Course Logistics

M 4/23	RL Capstone: Learning to Learn. Chelsea Finn Guest Lecture.		Assignment 4 due 11pm (pdf to Gradescope & and zipfile to Bcourses)
W 4/25	Risks. Andrew Critch Guest Lecture.		
Su 4/29			Final Project Presentation due 11pm
M 4/30	Final project presentations I	4-5:30pm in 306 Soda Hall	Final Project Presentation
W 5/2	Final project presentations II	12:30-2:30pm in 306 Soda Hall	Final Project Presentation
Th 5/3	Final project poster session	3-4:30pm in Soda 5th floor atrium	Final Project Poster due
F 5/11			Final Project Report due

• Exploration vs. Exploitation

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- Exploration Methods:

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  - An imagination architecture

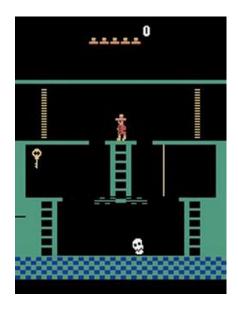
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this is impossible

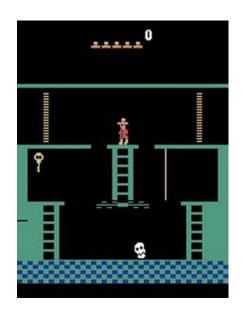


this is easy (mostly)



Why?

this is impossible







• Getting key = reward



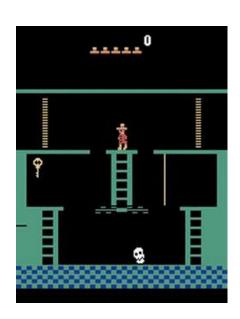
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- Getting key = reward
- Opening door = reward
- Getting killed by skull = nothing (is it good? bad?)
- Finishing the game only weakly correlates with rewarding events
- We know what to do because we **understand** what these sprites mean!

### Exploration and exploitation examples

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Restaurant selection

- Restaurant selection
  - Exploitation: go to your favorite restaurant

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  - Exploitation: go to your favorite restaurant
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- Information gain style algorithms
  - reason about information gain from visiting new states

# Optimistic exploration in RL

UCB (Upper Confidence Bound) methods for MDPs

Define N(s) as the number of times we have visited state s, or N(s, a) as the number of times we performed action a in state s.

Add an intrinsic reward of bonus for visiting rarely-visited states:

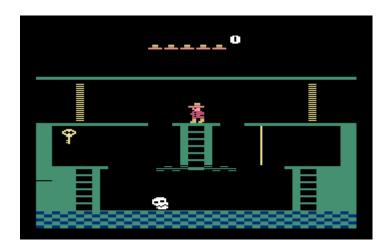
use 
$$r^+(\mathbf{s}, \mathbf{a}) = r(\mathbf{s}, \mathbf{a}) + \mathcal{B}(N(\mathbf{s}))$$
  
bonus that decreases with  $N(\mathbf{s})$ , e.g.  $\mathcal{B}(N(\mathbf{s})) = \sqrt{\frac{2 \ln T}{N(\mathbf{s})}}$   
use  $r^+(\mathbf{s}, \mathbf{a})$  instead of  $r(\mathbf{s}, \mathbf{a})$  with any model-free algorithm

- + simple addition to any RL algorithm
- need to tune bonus weight

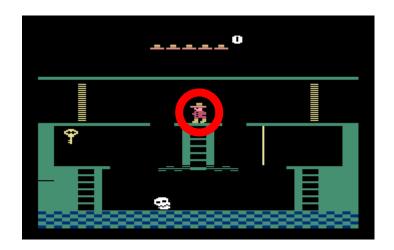
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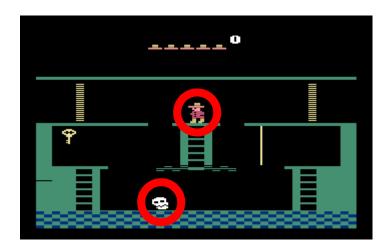
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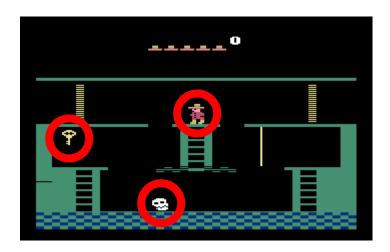
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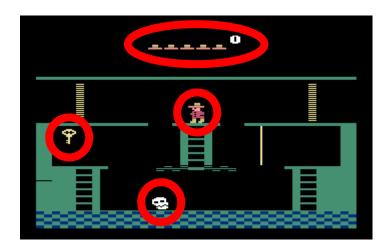
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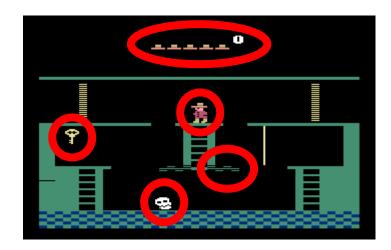
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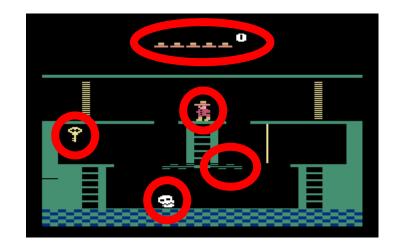
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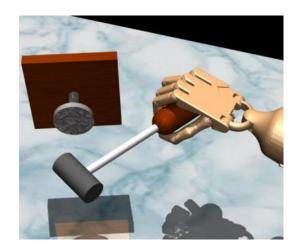


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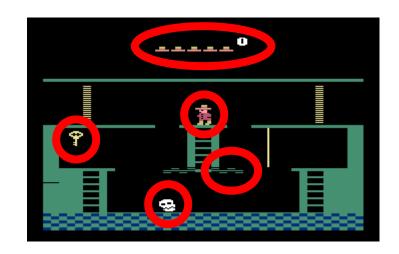
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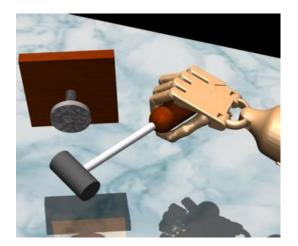




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But wait... what's a count?

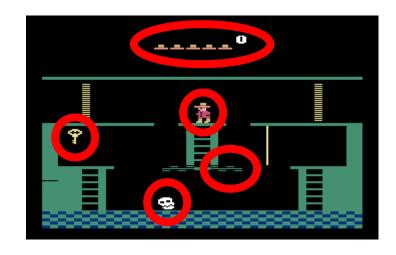


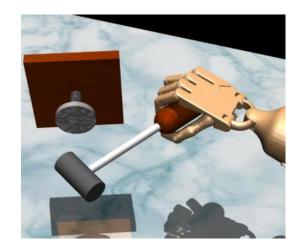


Uh oh... we never see the same thing twice!

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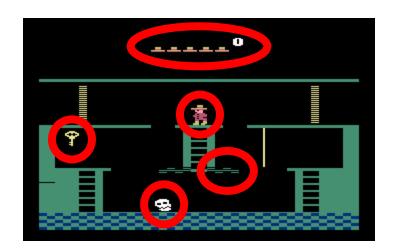
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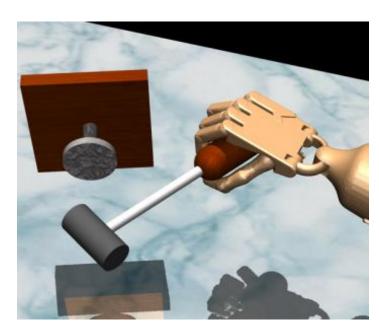


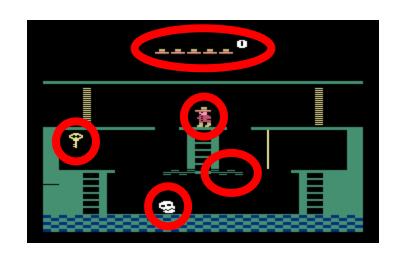
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But some states are more similar than others



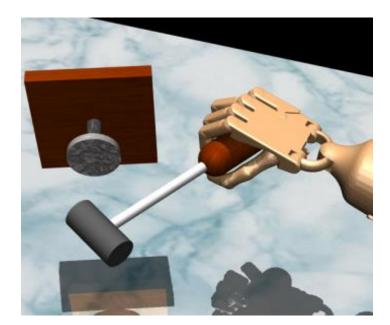
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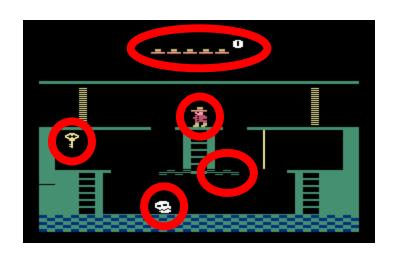




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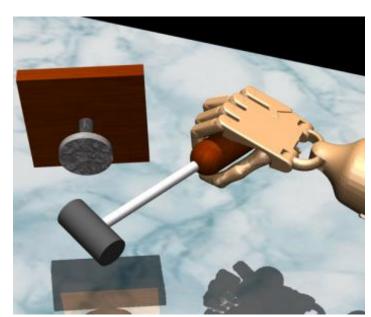


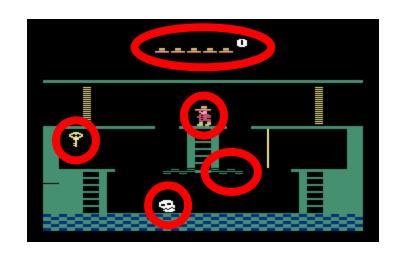


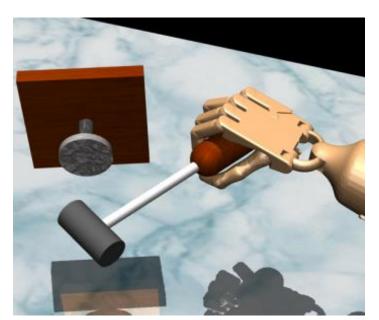
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can we use  $p_{\theta}(\mathbf{s})$  to get a "pseudo-count"?







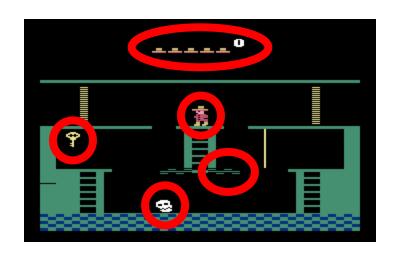
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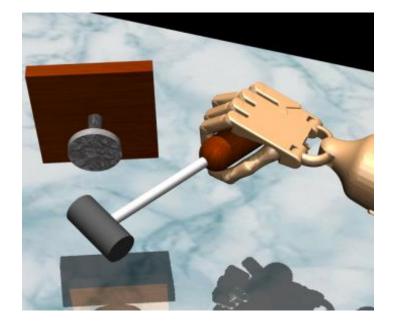
$$P(\mathbf{s}) = \frac{N(\mathbf{s})}{n}$$





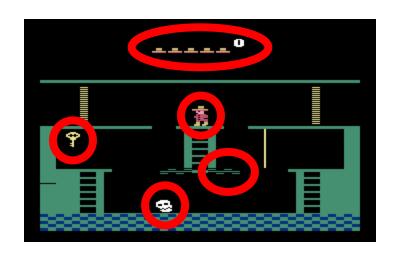
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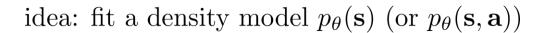
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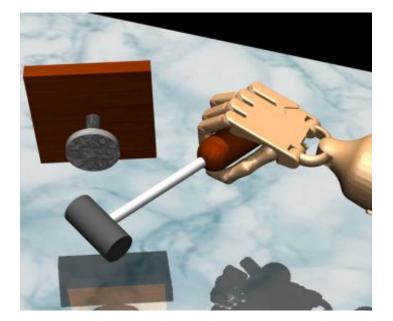
$$P(\mathbf{s}) = \frac{N(\mathbf{s})}{n}$$
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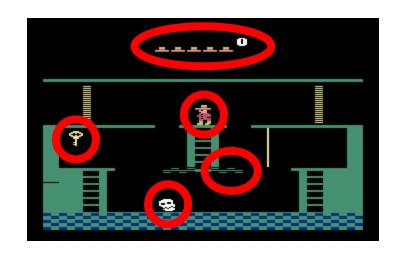
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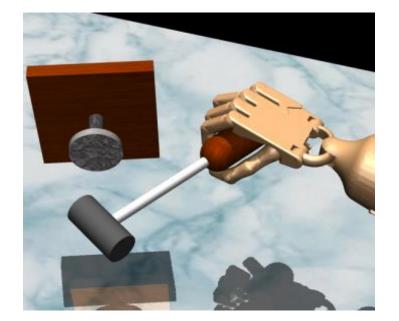
### Fitting generative models





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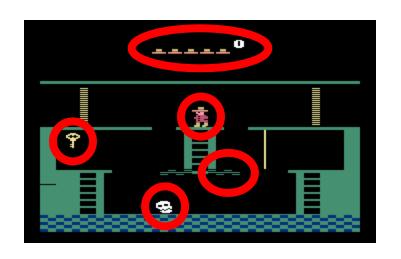
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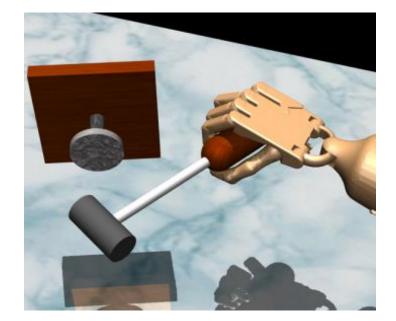
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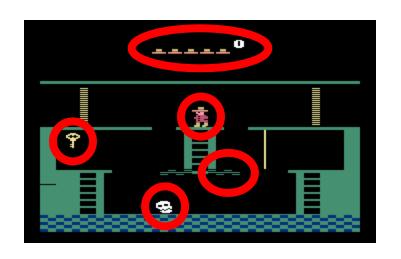
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after we see s, we have:

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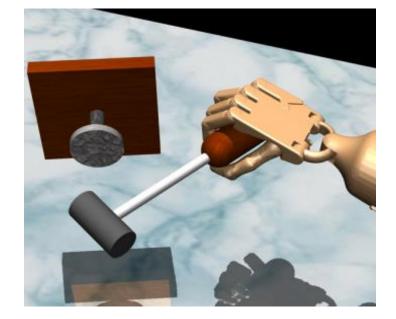
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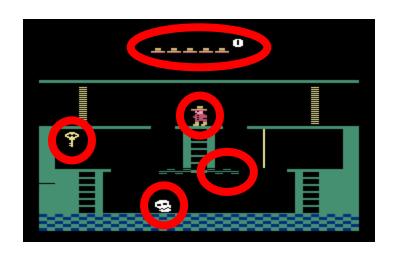
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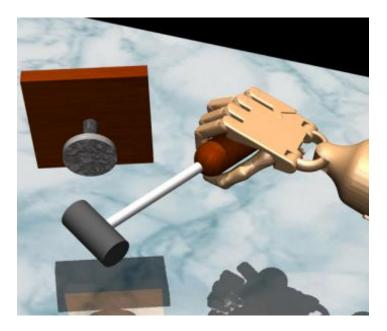
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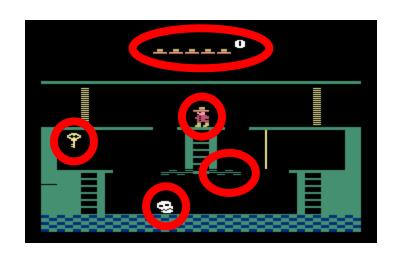
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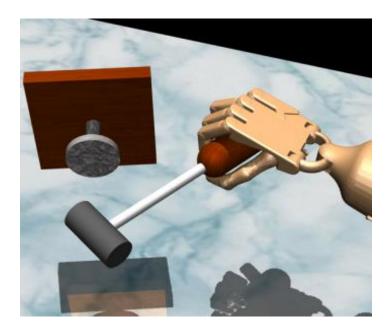
can we get  $p_{\theta}(\mathbf{s})$  and  $p_{\theta'}(\mathbf{s})$  to obey these equations?

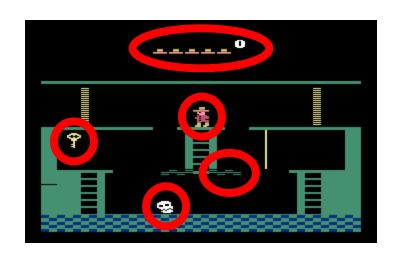




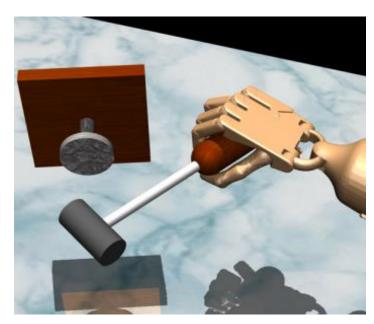


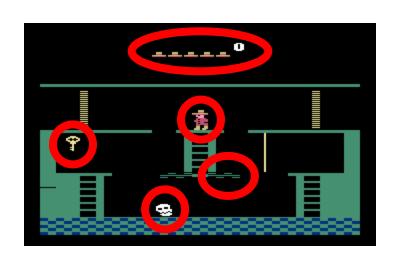
fit model  $p_{\theta}(\mathbf{s})$  to all states  $\mathcal{D}$  seen so far



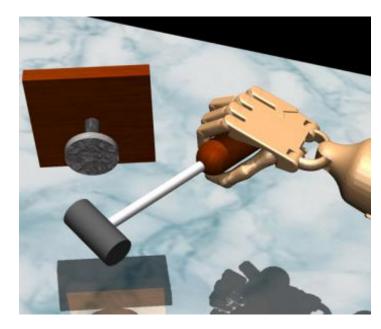


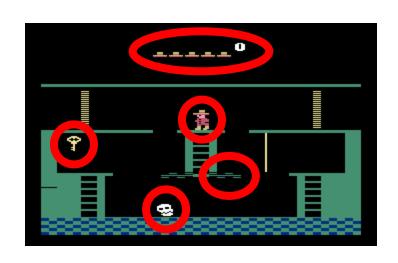
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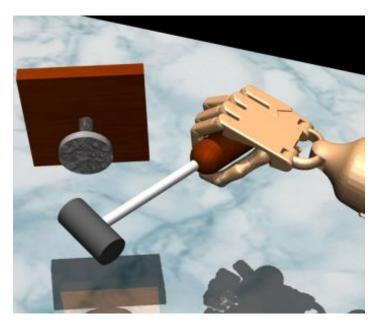


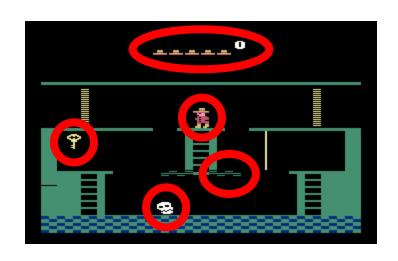
fit model  $p_{\theta}(\mathbf{s})$  to all states  $\mathcal{D}$  seen so far take a step i and observe  $\mathbf{s}_i$  fit new model  $p_{\theta'}(\mathbf{s})$  to  $\mathcal{D} \cup \mathbf{s}_i$ 

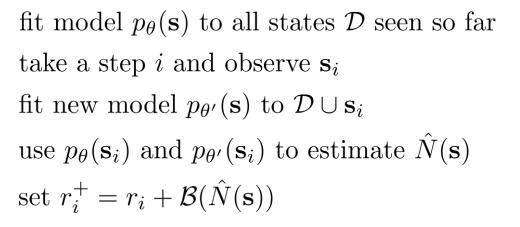


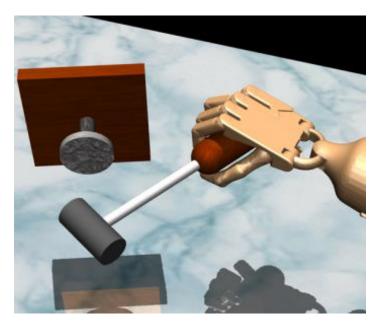


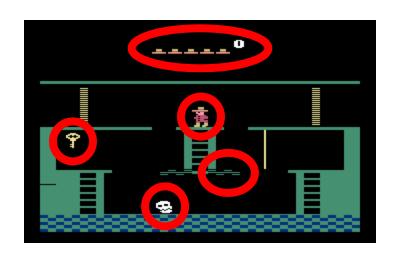
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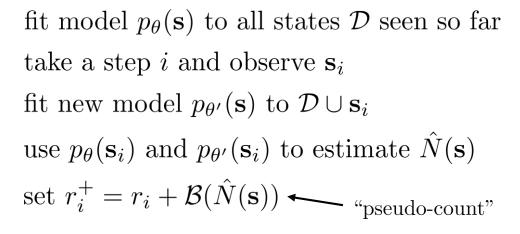


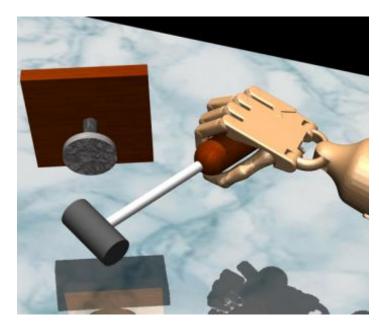


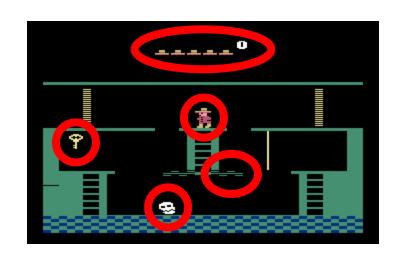


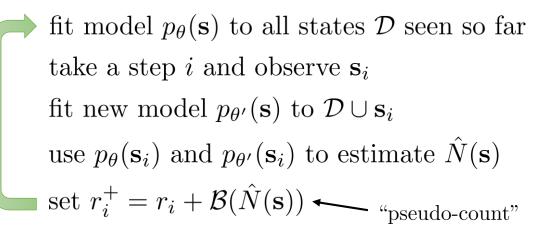


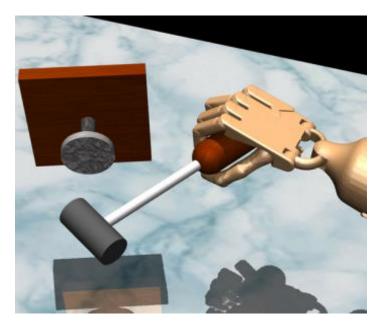


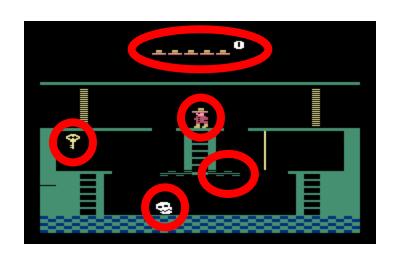


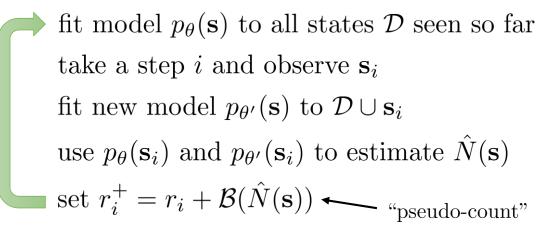


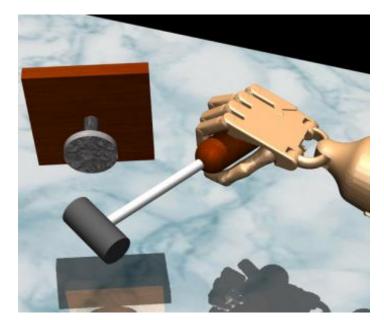




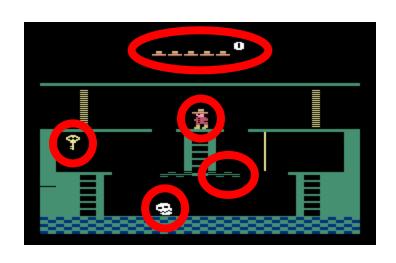


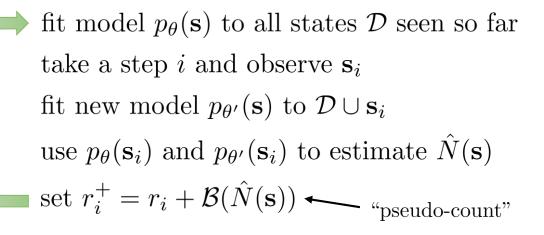


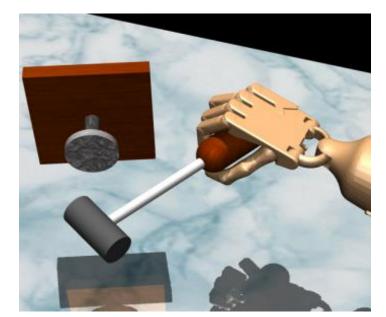




how to get  $\hat{N}(\mathbf{s})$ ? use the equations

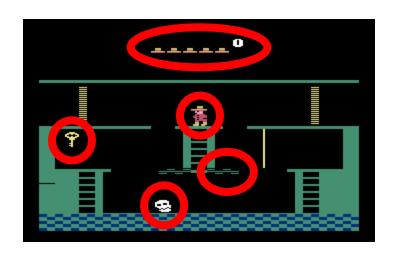


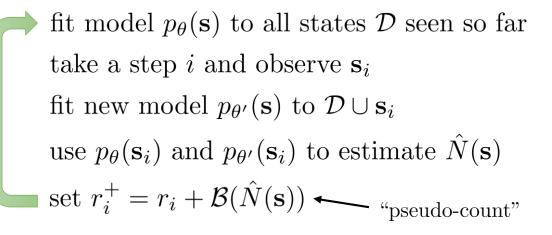


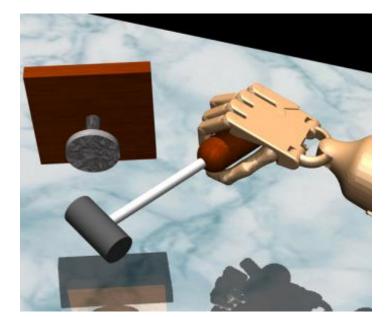


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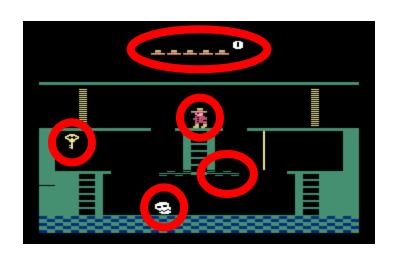


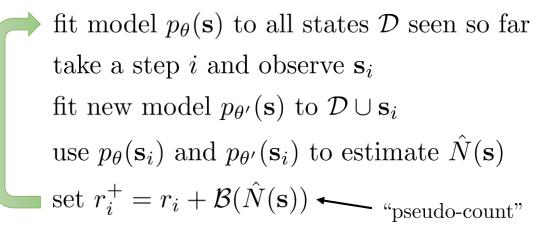


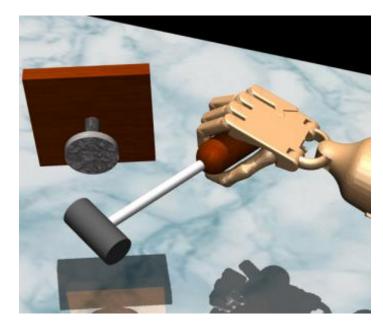
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two equations and two unknowns!

$$\hat{N}(\mathbf{s}_i) = \hat{n}p_{\theta}(\mathbf{s}_i)$$
 
$$\hat{n} = \frac{1 - p_{\theta'}(\mathbf{s}_i)}{p_{\theta'}(\mathbf{s}_i) - p_{\theta}(\mathbf{s}_i)} p_{\theta}(\mathbf{s}_i)$$

Bellemare et al. "Unifying Count-Based Exploration..."

Lots of functions in the literature, inspired by optimal methods for bandits or small MDPs

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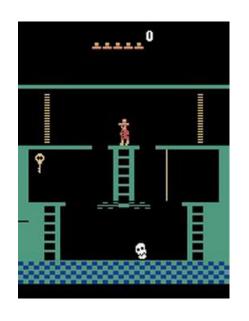
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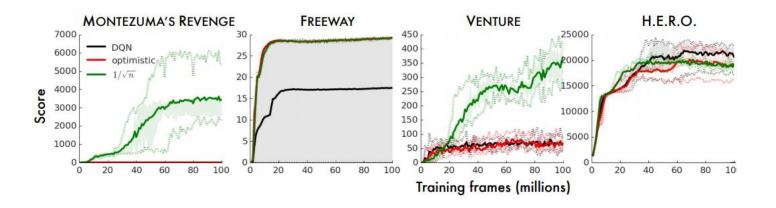
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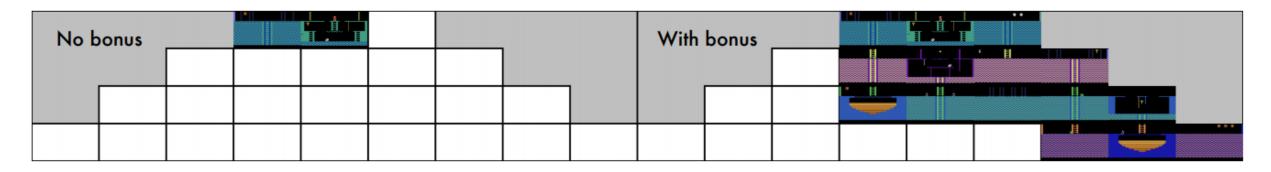
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this is the one used by Bellemare et al. '16

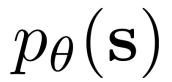
### Does it work?

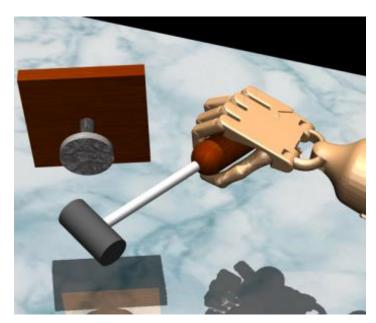


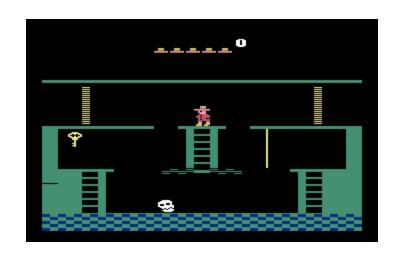


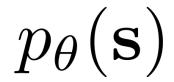




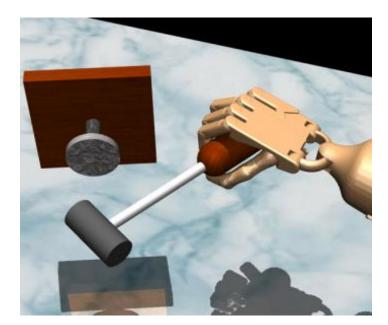


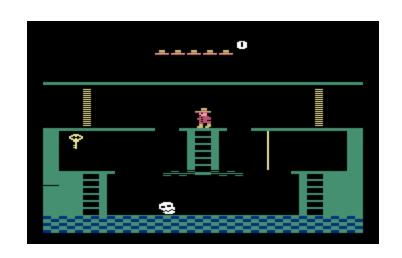


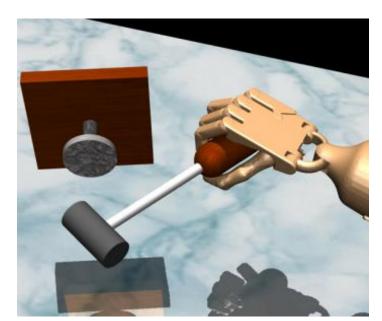




need to be able to output densities, but doesn't necessarily need to produce great samples



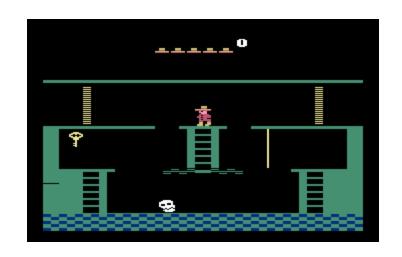


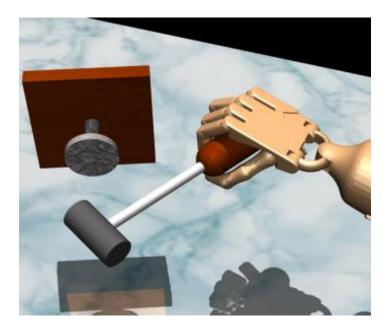


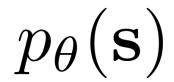
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opposite considerations from many popular generative models in the literature (e.g., GANs)





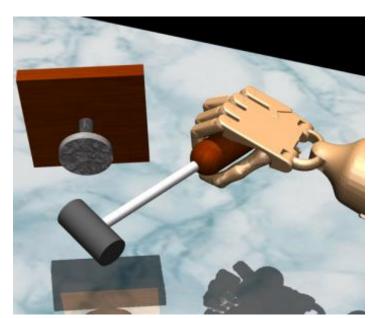


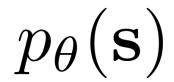
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Bellemare et al.: "CTS" model: condition each pixel on its top-left neighborhood



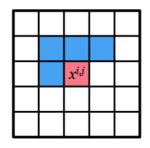


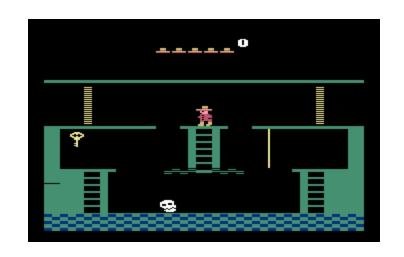


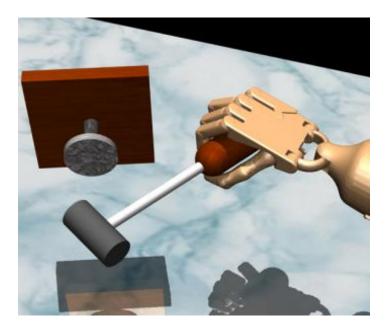
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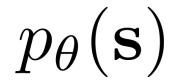
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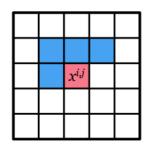


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Bellemare et al.: "CTS" model: condition each pixel on its top-left neighborhood

Other models: stochastic neural networks, compression length, EX2



Represent explicitly our uncertainty in the model parameters  $\theta$ . Then sample from it (Thompson sampling):

$$\theta_1, \dots, \theta_n \sim \hat{p}(\theta_1, \dots, \theta_n)$$

$$a = \arg\max_{a} E_{\theta_a}[r(a)]$$

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A simple and very general approach is to compute an ensemble of models, and then sample from it:

1. sample Q-function Q from p(Q)

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since Q-learning is off-policy, we don't care which Q-function was used to collect data

# Bootstrap

given a dataset  $\mathcal{D}$ , resample with replacement N times to get  $\mathcal{D}_1, \ldots, \mathcal{D}_N$ 

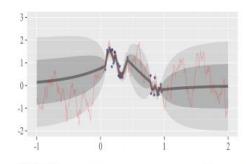
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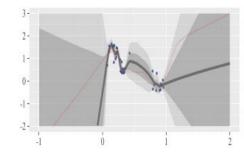
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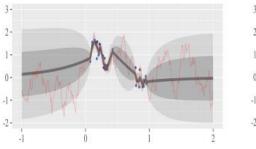
(b) Gaussian process posterior

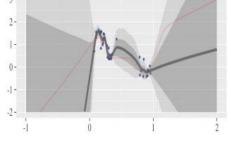
(c) Bootstrapped neural nets

given a dataset  $\mathcal{D}$ , resample with replacement N times to get  $\mathcal{D}_1, \ldots, \mathcal{D}_N$ 

train each model  $f_{\theta_i}$  on  $\mathcal{D}_i$ 

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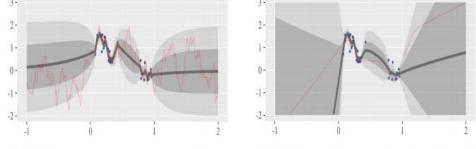
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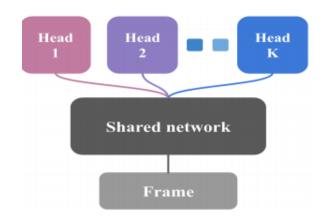
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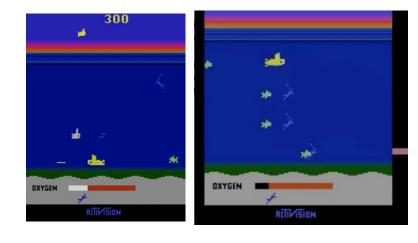


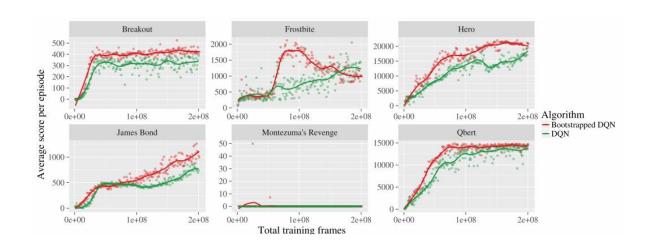
Osband et al. "Deep Exploration via Bootstrapped DQN"

# Why does this work?

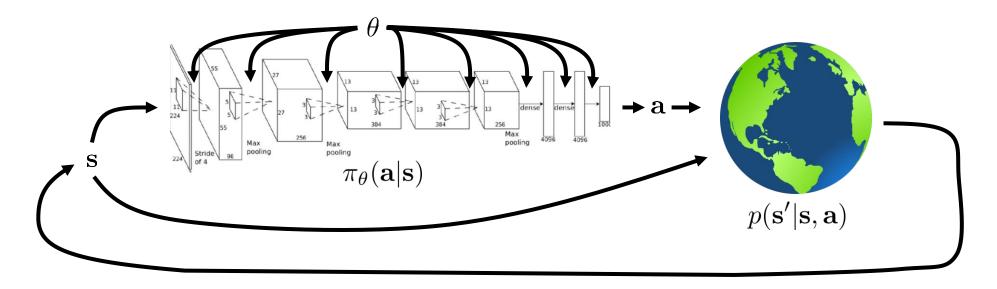
Exploring with random actions (e.g., epsilon-greedy): random walk pattern, in general  $\Omega(N^2)$  steps to visit N states.

Exploring with random Q-functions: commit to a randomized but internally consistent strategy *for an entire episode* 



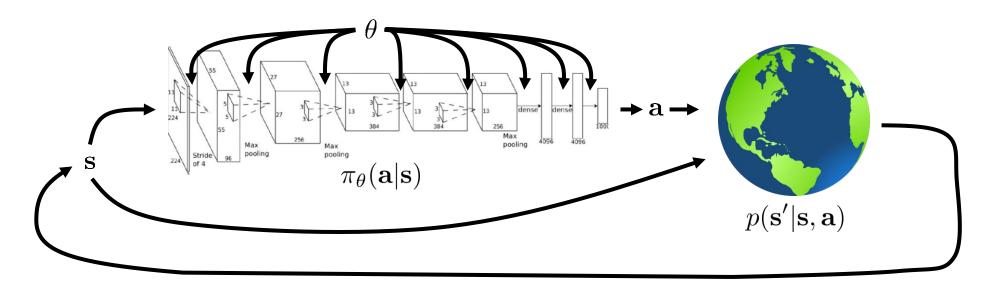


- + no change to original reward function
- very good bonuses often do better



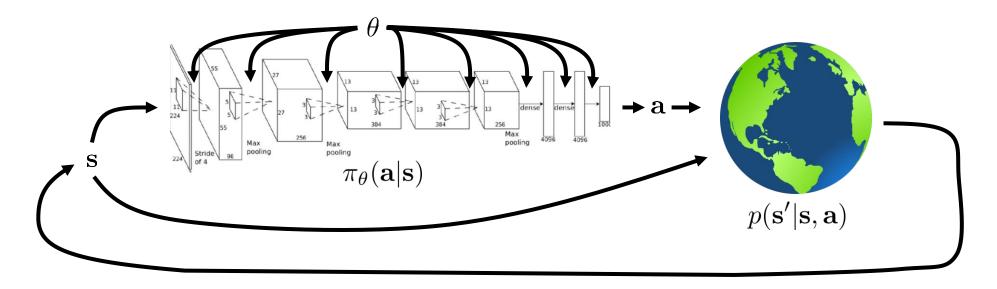
$$\underbrace{p_{\theta}(\mathbf{s}_1, \mathbf{a}_1, \dots, \mathbf{s}_T, \mathbf{a}_T)}_{\pi_{\theta}(\tau)} = p(\mathbf{s}_1) \prod_{t=1}^{T} \pi_{\theta}(\mathbf{a}_t | \mathbf{s}_t) p(\mathbf{s}_{t+1} | \mathbf{s}_t, \mathbf{a}_t)$$

$$\theta^* = \arg\max_{\theta} E_{\tau \sim p_{\theta}(\tau)} \left[ \sum_{t} r(\mathbf{s}_t, \mathbf{a}_t) \right]$$



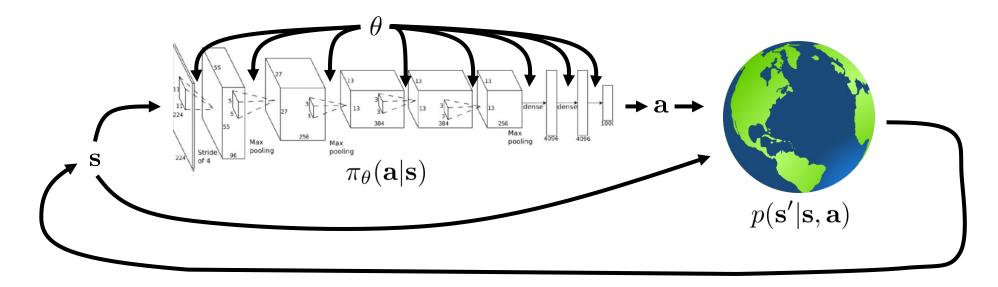
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 assume this is unknown don't even attempt to learn it

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Often we do know the dynamics

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Does knowing the dynamics make things easier?

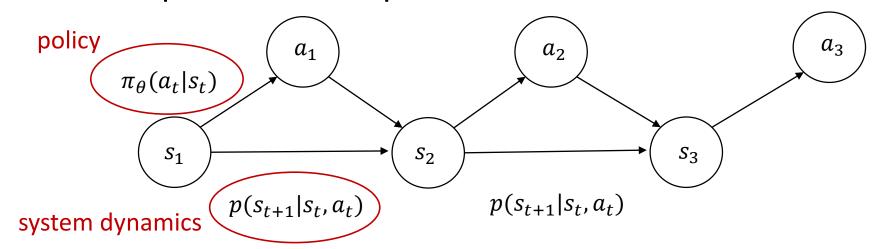
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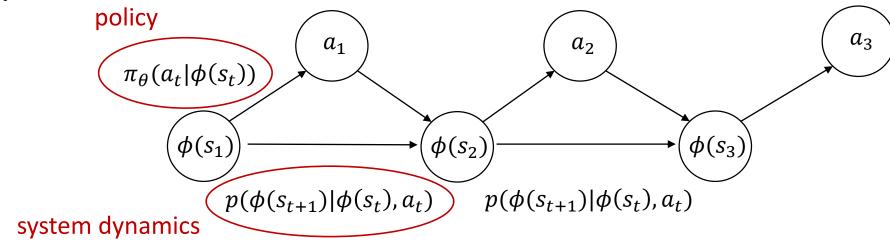
## Model-based reinforcement learning

- 1. Model-based reinforcement learning: learn the transition dynamics, then figure out how to choose actions
- 2. Advantages:
  - 1. Avoid making expensive real-world or simulator actions
  - 2. Possibly differentiate through the dynamics to optimize action choice
- 3. We then have an optimal control problem



# Simplifying Model-based reinforcement learning

- Computing a complete environment model can be very expensive (has
  to generate images for vision-based policies)
- 2. Do we really need the full state?
- 3. Is there a simplified function of the state  $\phi(s)$  that's sufficient for RL?
- 4. Should be sufficient to predict next state and for policy to choose next action.



#### Curiosity-driven Exploration by Self-supervised Prediction

Pathak et al. 2017

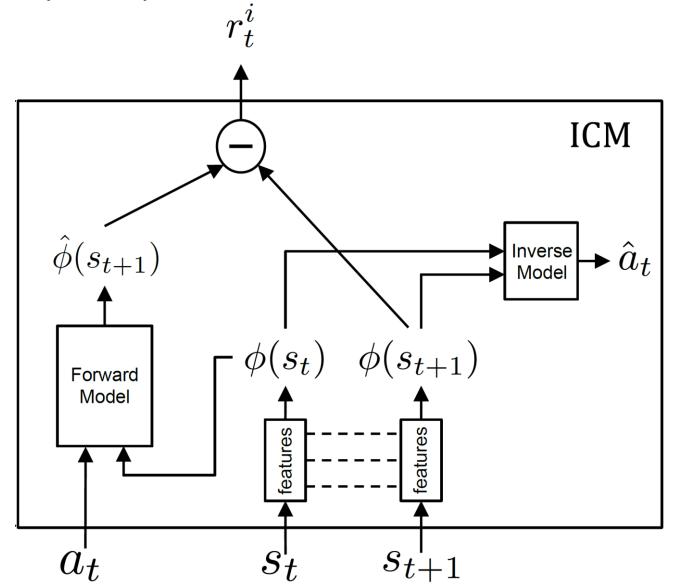
- 1. Computes a simplified environment model  $\phi(s_t)$
- 2. Uses error in the model's prediction to highlight states that need further exploration.

#### Intrinsic Curiosity Model (ICM)

1. Uses an inverse model to ensure  $\phi(s_t)$  is sufficient for action selection.

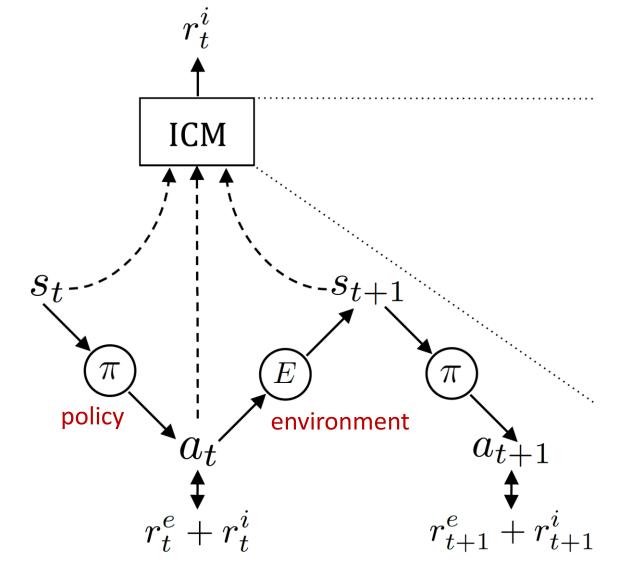
2. Estimates a forward model for next state.

3. The forward model error is the curiosity signal.



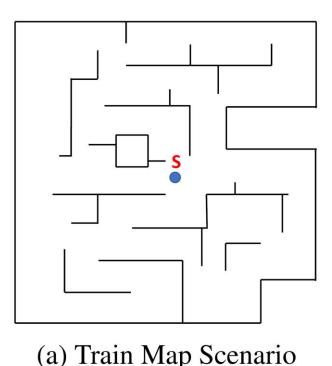
1. The ICM provides an intrinsic reward signal  $r_t^i$ .

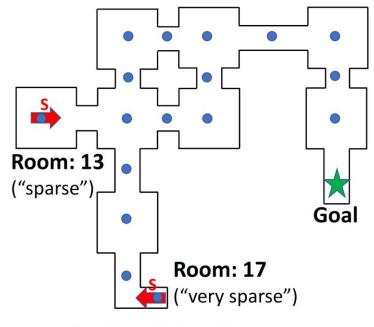
2. The policy can be trained by any RL method using the combined reward.



**Environments: Vizdoom** 



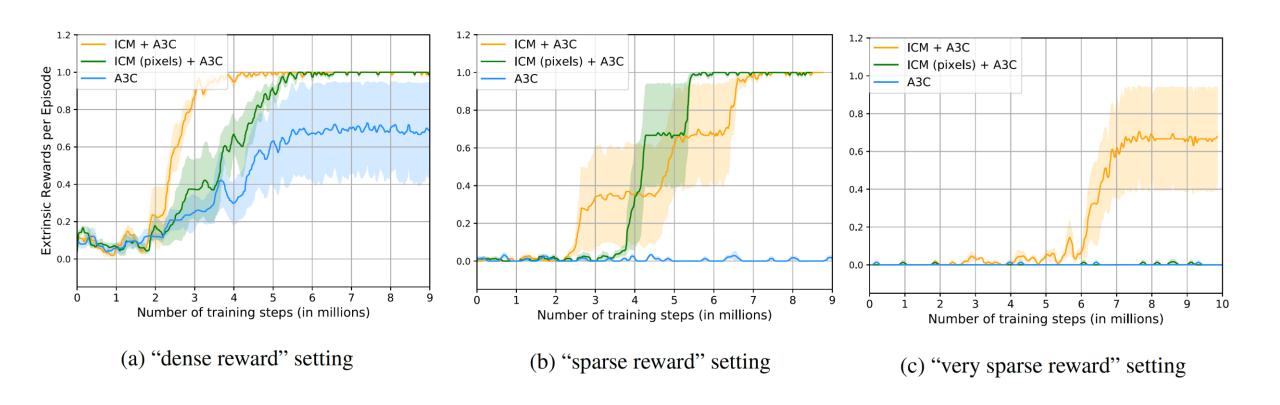




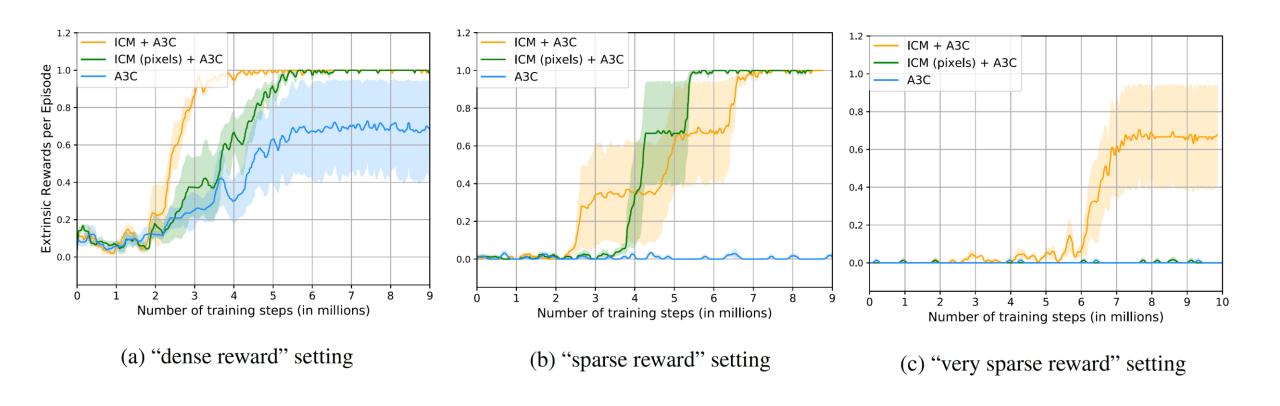
(a) Train Map Scenario

(b) Test Map Scenario

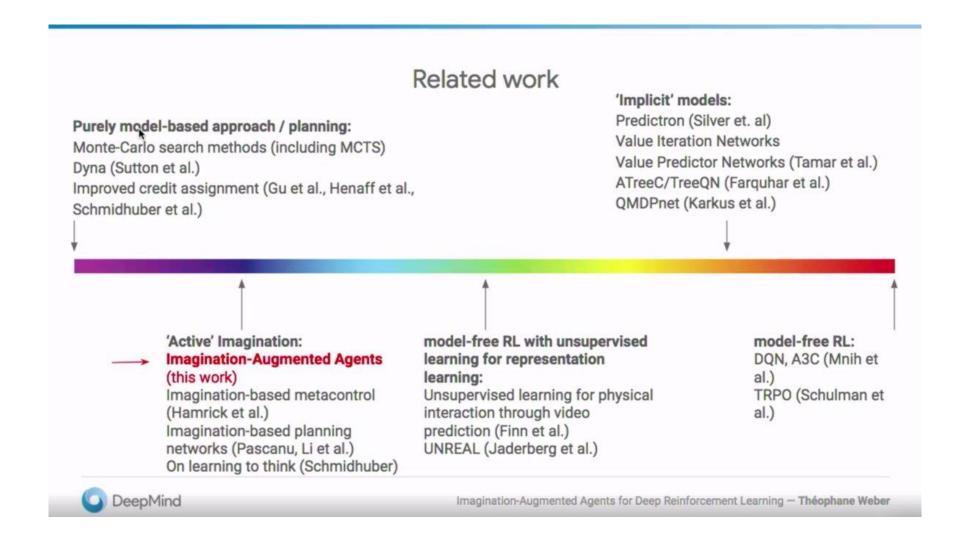
Model is trained initially without goal reward (left). Agent is randomly started on one of the blue dots in the "dense" case (right).



Relative performance improves as reward sparseness increases.



#### Model-Free vs Model-Based (Theophane Weber)

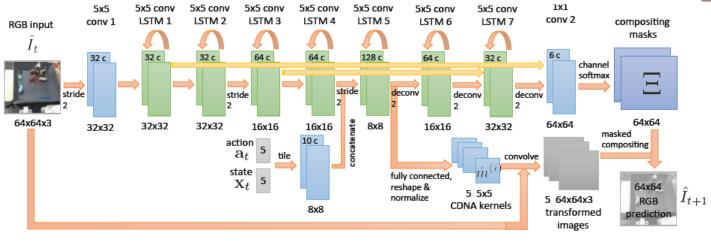


#### Model-Free vs Model-Based

Video predictive models, e.g.

"Deep Visual Foresight for Planning Robot Motion" by Finn et al.

Pixel-level recurrent image prediction:



indicated goal

Computes a flow (motion) map across the image.

Optimizes action choice using CEM (Cross-Entropy Method).

$$\mathbf{a}_1, \dots, \mathbf{a}_T = \arg \max_{\mathbf{a}_1, \dots, \mathbf{a}_T} J(\mathbf{a}_1, \dots, \mathbf{a}_T)$$

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abstract away optimal control/planning:

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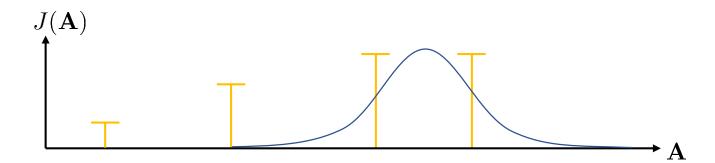
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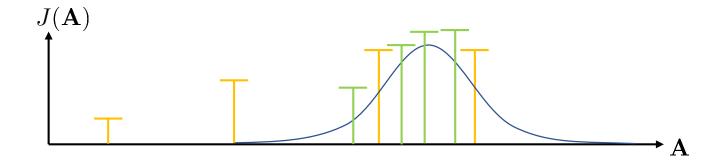
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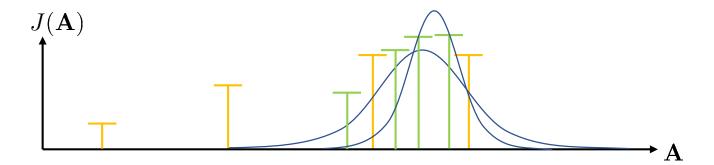
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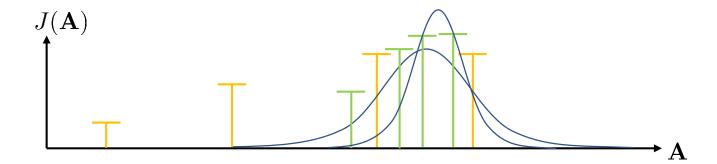
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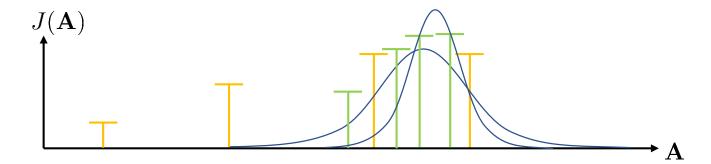
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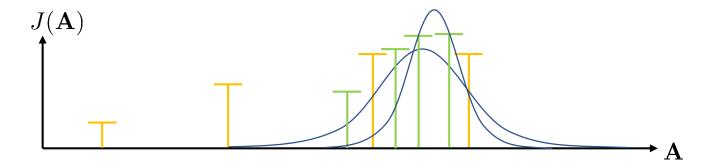
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cross-entropy method with continuous-valued inputs:

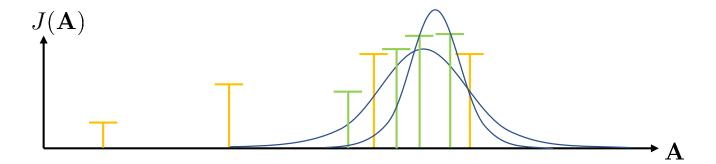
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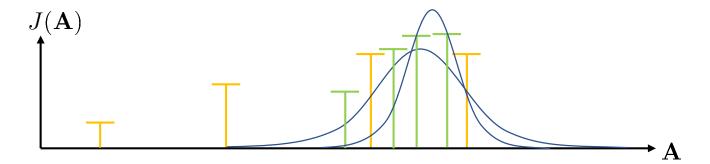
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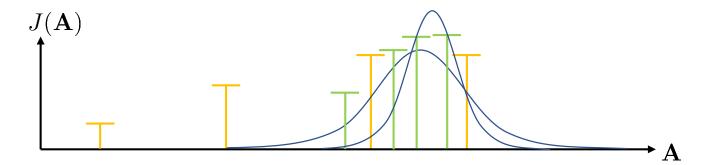
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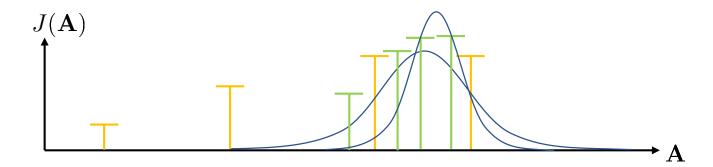
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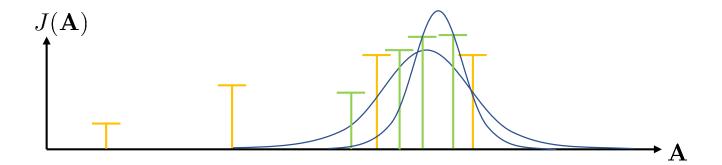


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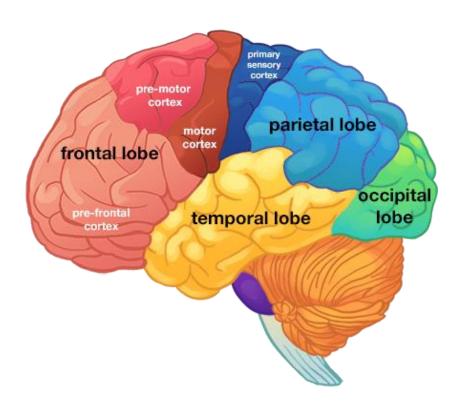
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see also: CMA-ES (sort of like CEM with momentum)

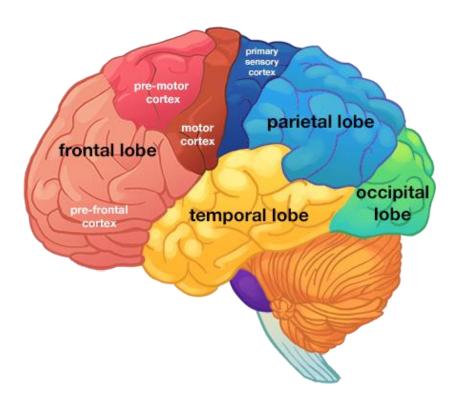
# Imagination

s or  $\phi(s)$ , that is the question...

i.e. how important is it to have an accurate facsimile of the input images, vs and embedding tailored for planning?

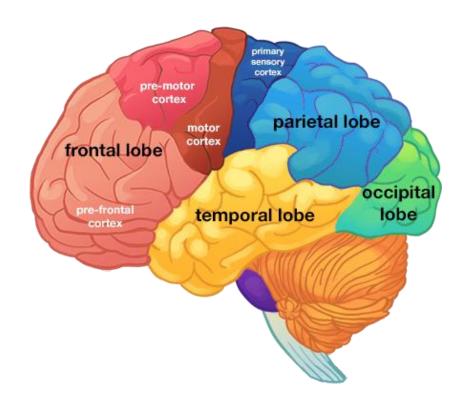


What do people do?



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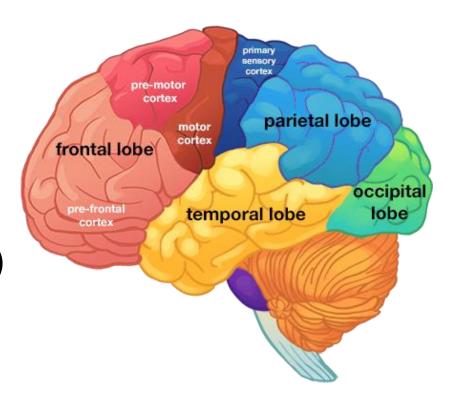
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But the results on primary visual cortex V1 (the pixels) in visual imagination experiments is mixed.

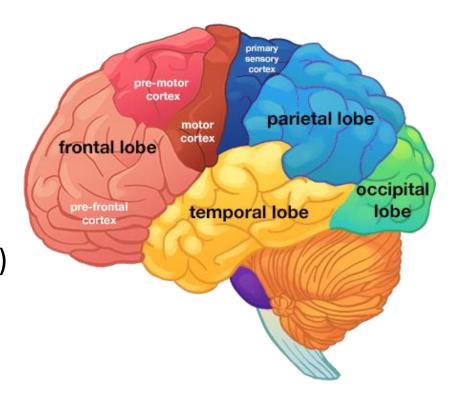


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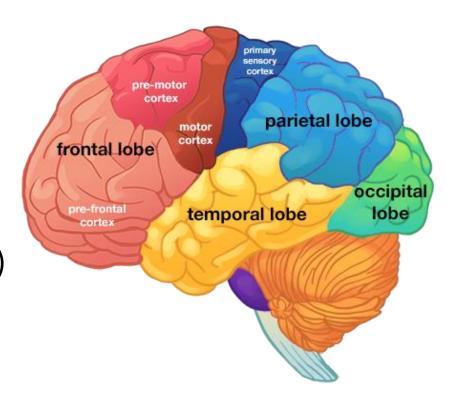
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### See this recent study:

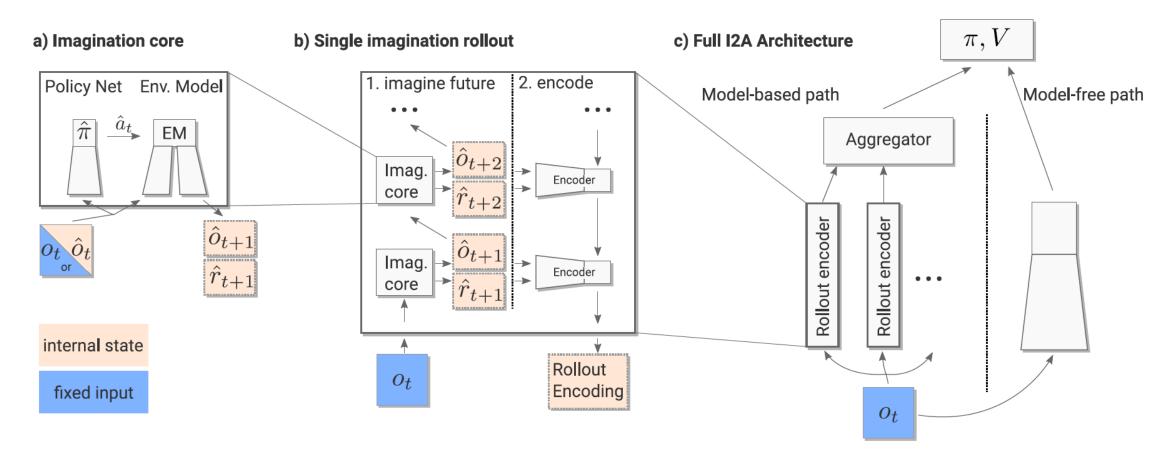
"Vivid visual mental imagery in the absence of the primary visual cortex" by Bridge et al.

"Imagination-Augmented Agents for Deep Reinforcement Learning" Weber et al

In the mean time we can build it and try it...

"Imagination-Augmented Agents for Deep Reinforcement Learning" Weber et al

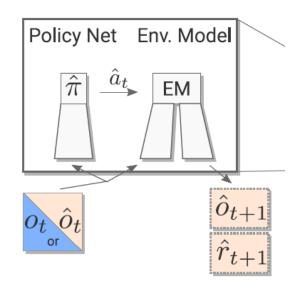
Symbols with represent imagined values



The rollout policy  $\hat{\pi}$  generates the action sequence.

Its produced by a standard policy network.

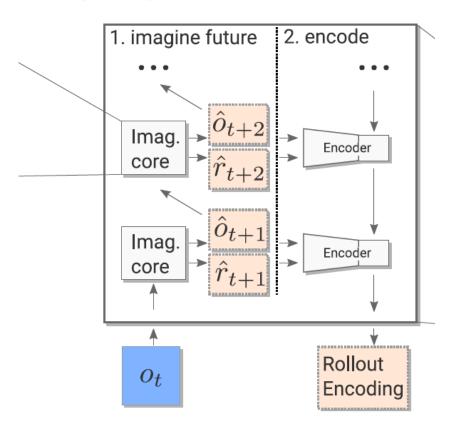
#### a) Imagination core



internal state fixed input

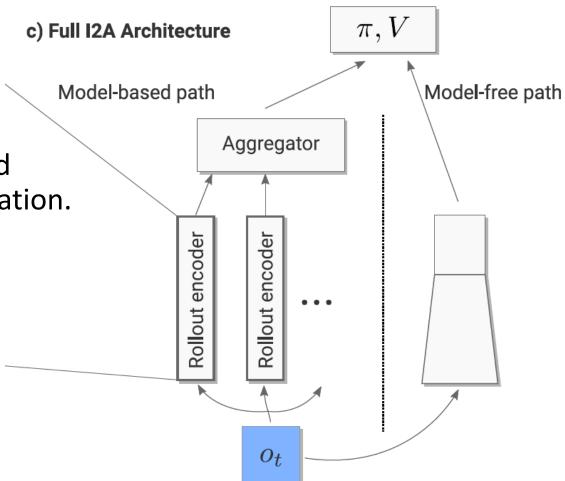
The imagination rollout block recurrently computes a sequence of observations and rewards.

#### b) Single imagination rollout

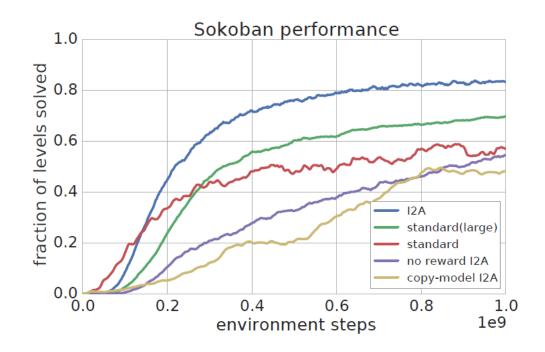


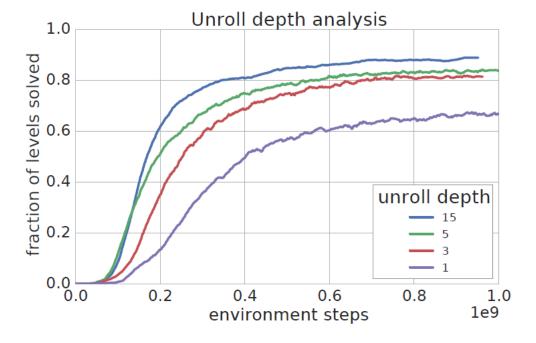
The imagined sequence forms "advice" to the final policy and value function blocks.

They are both also informed by a feed-forward network connected to the current real observation.



#### Performance on Sokoban:



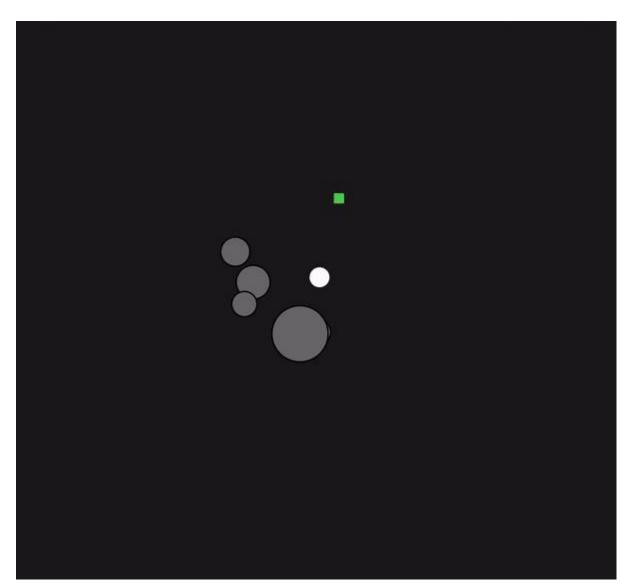




• An agent playing the spaceship game.

 Red lines are executed trajectories.

• Blue and green are imaged trajectories.



# Take-aways

• Optimistic exploration methods favor poorly-explored states, assuming their value is as high as it could be. Use counts to estimate uncertainties.



- An elegant way to model  $\theta$  uncertainty is to train an ensemble of models using bootstrap sampling. Sample from the posterior  $\rightarrow$  choose a model.
- Avoid random walks at all costs!  $\Omega(N^2)$  cost to explore N states. Simple methods: epsilon-greedy, entropy regularization and Thompson sampling all do random walks.
- Doing better requires memory (counts, environment models etc.)

# Take-aways

• Can plan and anticipate states and rewards with a simplified environment model ( $\phi(s)$  instead of s).



Human visual imagination doesn't always use pixel-level representation.

• But visual representation is the most powerful, and allows the system to use policies or other networks trained for very different tasks.

• Imagination was used as "advice" in the imagination architecture. Another network needs to learn how to use it (CEM etc.).