

One draw means the result may be red card or blue card if the card is red.

Attachment 1.1

$$P(H_0 | \text{red}) = \frac{P(H_0) \cdot P(\text{red} | H_0)}{P(\text{red})} = \frac{0.4 \cdot 0.7}{0.4 \cdot 0.7 + 0.6 \cdot 0.3} = 0.688$$

$$P(H_1 | \text{red}) = 1 - 0.688 = 0.312$$

$$E(\text{accept } H_0) = 0.688 \cdot 5 - 0.312 \cdot 3 = 1.864$$

$$E(\text{accept } H_1) = 0.688 \cdot (-3) + 0.312 \cdot 5 = 0.136$$

Since $1.864 > 0.136$, a'' is accept H_0

$$USI = E(U(a'' | y) | y) - E(U(a' | y))$$

$$= 1.864 - 0.136 = 1.728$$

If the card is blue.

$$P(H_0 | \text{blue}) = \frac{P(H_0) \cdot P(\text{blue} | H_0)}{P(\text{blue})} = \frac{0.4 \cdot 0.3}{0.4 \cdot 0.3 + 0.6 \cdot 0.7} = 0.222$$

$$P(H_1 | \text{blue}) = 1 - 0.222 = 0.778$$

$$E(\text{accept } H_0) = 0.222 \cdot 5 - 0.778 \cdot 3 = -1.225$$

$$E(\text{accept } H_1) = -0.222 \cdot 3 + 0.778 \cdot 5 = 3.224$$

Since $3.224 > -1.225$, a'' is accept H_1

$$USI = 3.224 - (-1.225) = 4.449$$

$$EUSI = \sum_{i=1}^2 USI(y_i) \cdot P(y_i)$$

$$= 1.728 \cdot 0.6 + 4.449 \cdot 0.4 = 3.0792$$