

5. Implement a solution in either C, C++, C#, Java, or Python to the following problem.

Suppose you are given two sets of  $n$  points, one set  $\{p_1, p_2, \dots, p_n\}$  on the line  $y = 0$  and the other set  $\{q_1, q_2, \dots, q_n\}$  on the line  $y = 1$ . Create a set of  $n$  line segments by connecting each point  $p_i$  to the corresponding point  $q_i$ . Your goal is to develop an algorithm to determine how many pairs of these line segments intersect. Your algorithm should take the  $2n$  points as input, and return the number of intersections. Using divide-and-conquer, you should be able to develop an algorithm that runs in  $O(n \log n)$  time.

*Hint:* What does this problem have in common with the problem of counting inversions in a list?

Input should be read in from stdin. The first line will be the number of instances. For each instance, the first line will contain the number of pairs of points ( $n$ ). The next  $n$  lines each contain the location  $x$  of a point  $q_i$  on the top line. Followed by the final  $n$  lines of the instance each containing the location  $x$  of the corresponding point  $p_i$  on the bottom line. For the example shown in Fig 1, the input is properly formatted in the first test case below.

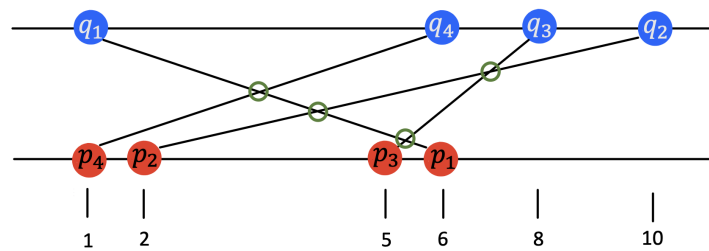


Figure 1: An example for the line intersection problem where the answer is 4

#### Constraints:

- $1 \leq n \leq 10^6$
- For each point, its location  $x$  is a positive integer such that  $1 \leq x \leq 10^6$
- No two points are placed at the same location on the top line, and no two points are placed at the same location on the bottom line.
- Note that in C\C++, the results of some of the test cases may not fit in a 32-bit integer. If you are using C\C++, make sure you use a 'long long' to store your final answer.

**Sample Test Cases:**

input:

2  
4  
1  
10  
8  
6  
6  
2  
5  
1  
5  
9  
21  
1  
5  
18  
2  
4  
6  
10  
1

expected output:

4  
7