

5. Implement an algorithm to determine the maximum matching in a bipartite graph and if that matching is perfect (all nodes are matched) in either C, C++, C#, Java, or Python. Be efficient and use your max-flow implementation from the previous week.

The input will start with a positive integer, giving the number of instances that follow. For each instance, there will be 3 positive integers m , n , and q . Numbers m and n are the number of nodes in node set A and node set B . Number q is the number of edges in the bipartite graph. For each edge, there will be 2 more positive integers i , and j representing an edge between node $1 \leq i \leq m$ in A and node $1 \leq j \leq n$ in B .

A sample input is the following:

```
3
2 2 4
1 1
1 2
2 1
2 2
2 3 4
2 3
2 1
1 2
2 2
5 5 10
1 1
1 3
2 1
2 2
2 3
2 4
3 4
4 4
5 4
5 5
```

The sample input has 3 instances.

For each instance, your program should output the size of the maximum matching, followed by a space, followed by an N if the matching is not perfect and a Y if the matching is perfect. Each output line should be terminated by a newline. The correct output to the sample input would be:

```
2 Y
2 N
4 N
```