Homework 4

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```
# libraries
library(tidyverse)
library(ggplot2)
library(dagitty)
library(tableone)
library(knitr)
library(personalized)

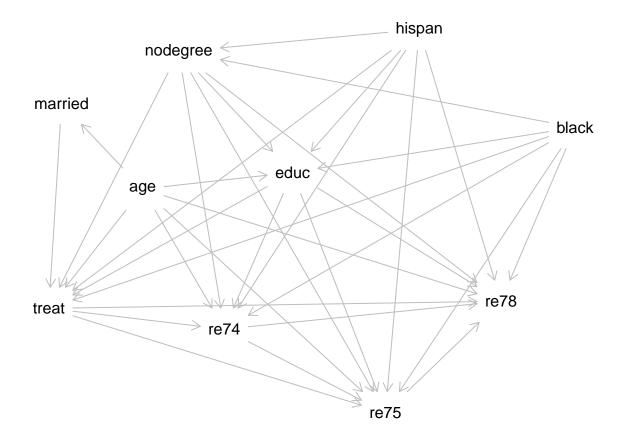
# setup plot theme
theme_set(
    theme_minimal() +
    theme(legend.position = "top")
)
```

```
# import data
df = read_csv("./data/hw4_data.csv") |>
mutate(
    treat = as.factor(treat),
    black = as.factor(black),
    hispan = as.factor(hispan),
    married = as.factor(married),
    nodegree = as.factor(nodegree)
)
```

1. DAG

```
g = dagitty('dag {
age [pos="-1.842,-0.039"]
black [pos="1.458,-0.317"]
educ [pos="-0.698,-0.114"]
hispan [pos="0.269,-0.760"]
married [pos="-2.461,-0.426"]
nodegree [pos="-1.567,-0.659"]
re74 [pos="-1.219,0.594"]
re75 [pos="0.011,0.971"]
re78 [outcome,pos="0.893,0.468"]
treat [exposure,pos="-2.558,0.500"]
age -> educ
age -> married
age -> re74
age -> re75
age -> re78
age -> treat
```

```
black -> educ
black -> nodegree
black -> re74
black -> re75
black -> re78
black -> treat
educ -> re74
educ -> re75
educ -> re78
educ -> treat
hispan -> educ
hispan -> nodegree
hispan -> re74
hispan -> re75
hispan -> re78
hispan -> treat
married -> treat
nodegree -> educ
nodegree -> re74
nodegree -> re75
nodegree -> re78
nodegree -> treat
re74 -> re75
re74 -> re78
re75 -> re78
treat -> re74
treat -> re75
treat -> re78
}')
plot(g)
```



Note of the variables in the DAG:

treat: treatment assignment (job training); exposure

- Suppose that the job training was completed before 1974, treat is likely to infludence re74, re75 and re78

age: age in years

- age may affect married, treat, educ and all the income status (re74, re75, re78)

educ: education in years

- educ may affect all the income status and treat

black, hispan: indicators for African American and hispanic

- Both of the ethnicity indicator may affect all the income status, nodegree, treat, and educ married: indicator for married
- married could influence treat

nodegree: indicator for highschool degree

- nodegree may affect treat, educ, and all the income status

re74: income in 1974

- $\tt re74$ can influence $\tt re75$ and $\tt re78$

re75: income in 1975

- re75 can influence re78

re78: income in 1978; outcome

Given the DAG, covariates that need to be adjusted in investigating the effect of exposure on the outcome are nodegree, hispan, black, educ and age.

2. I will evaluate the covariate balance using standardized mean differences.

```
cov = c("nodegree", "hispan", "black", "educ", "age")

# construct a table
tab = CreateTableOne(vars = cov, strata = "treat", data = df, test = FALSE)
print(tab, smd = TRUE)
```

```
##
                      Stratified by treat
##
                       0
                                      1
                                                     SMD
##
                         429
                                        185
##
                         256 (59.7)
                                        131 (70.8)
                                                      0.235
     nodegree = 1 (%)
##
     hispan = 1 (\%)
                          61 (14.2)
                                         11 (5.9)
                                                      0.277
     black = 1 (\%)
                          87 (20.3)
                                        156 (84.3)
##
                                                      1.671
     educ (mean (SD)) 10.24 (2.86) 10.35 (2.01)
##
                                                      0.045
     age (mean (SD)) 28.03 (10.79) 25.82 (7.16)
##
                                                      0.242
```

We can see that most covariates have SMD > 0.1 except for educ, indicating the potential imbalance between the two treatment group.

3. Propensity score estimates are calculated by fitting a logistic regression.

```
# fit PS model
ps.fit <- glm(treat ~ nodegree + hispan + black + educ + age, family = "binomial", data = df)
ps.fit |>
broom::tidy() |>
kable()
```

term	estimate	std.error	statistic	p.value
(Intercept)	-4.6689752	1.0063696	-4.6394238	0.0000035
nodegree1	0.7812141	0.3303690	2.3646714	0.0180461
hispan1	1.0760070	0.4168588	2.5812269	0.0098450
black1	3.3041742	0.2811462	11.7525129	0.0000000
educ	0.1523227	0.0643134	2.3684437	0.0178631
age	-0.0054560	0.0125728	-0.4339522	0.6643232

```
# estimate PS
df.ps <- predict(ps.fit, type = 'response')
print(df.ps[1:50])</pre>
```

```
##
                        2
                                   3
                                               4
                                                           5
                                                                                  7
            1
                                                                      6
## 0.70890885 0.17352013 0.57429368 0.72003809 0.61181465 0.66089500 0.58360334
                        9
                                  10
                                              11
                                                         12
                                                                     13
## 0.71450603 0.72158352 0.04647944 0.66455356 0.62265153 0.63106456 0.68833095
##
           15
                                                                     20
                       16
                                  17
                                              18
                                                         19
## 0.59626339 0.69761702 0.61492967 0.69299354 0.56090387 0.57962038 0.72441625
##
           22
                       23
                                  24
                                              25
                                                         26
                                                                     27
## 0.05951577 0.06156125 0.72332569 0.69876670 0.71783314 0.72223248 0.19219049
##
           29
                       30
                                  31
                                              32
                                                         33
                                                                     34
## 0.69991390 0.72332569 0.69991390 0.44122686 0.72223248 0.58757541 0.58094921
##
           36
                       37
                                  38
                                              39
                                                         40
                                                                     41
                                                                                 42
```

```
## 0.63147843 0.51040509 0.58360334 0.59484193 0.69183153 0.58625263 0.06782935

## 43 44 45 46 47 48 49

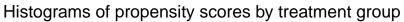
## 0.63233393 0.15559436 0.72767188 0.72223248 0.63233393 0.66698171 0.51040509

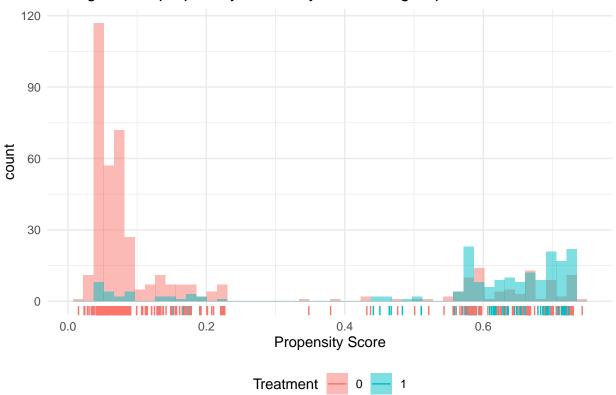
## 50

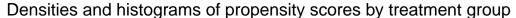
## 0.58360334
```

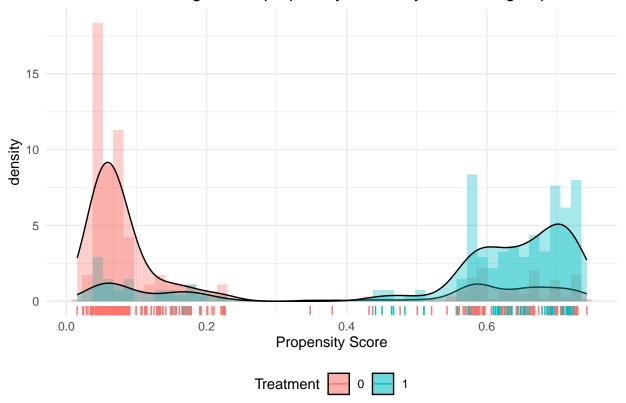
Listed values are the propensity scores for each observation in the dataset (only showing the first 50 observations out of 614).

4.









The histogram shows that the propensity score estimates does not overlap in ranges approximately [0, 0.0375] and [0.7375, 1]. I will trim the samples whose PS estimate is in these ranges.

```
# trimming
# eliminate controls for whom the P(A=1/C) is less that the min(P(A=1/C)) found in the treated group
min(df$ps.est[df$treat == 1])
## [1] 0.04528526
head(df$ps.est[which(df$treat == 0)] <= min(df$ps.est[df$treat == 1]))</pre>
##
     186
                 188
                              190
                                    191
           187
                       189
## FALSE FALSE FALSE FALSE FALSE
length(df$ps.est[which(df$treat == 0)] <= min(df$ps.est[df$treat == 1]))</pre>
## [1] 429
# eliminate treated for whom the P(A=1|C) is greater that the max(P(A=1|C)) found in the control group
max(df$ps.est[df$treat == 0])
```

[1] 0.7428825

```
head(df$ps.est[which(df$treat == 1)]>= max(df$ps.est[df$treat == 0]))

## 1 2 3 4 5 6
## FALSE FALSE FALSE FALSE FALSE FALSE
length(df$ps.est[which(df$treat == 1)]>= max(df$ps.est[df$treat == 0]))

## [1] 185

df_trim = df[df$ps.est >= min(df$ps.est[df$treat == 1]) & df$ps.est <= max(df$ps.est[df$treat == 0]),]

dim(df_trim)</pre>
```

After the trimming, sample size went down from 614 to 571, which may lead to reduced statistical power. In terms of the generalizability, trimming will disable the external validity because we are only looking at individuals with non-extreme propensity scores.

5. Here I will reevaluate the covariate balance using the trimmed sample.

```
# construct a table
tab_trim = CreateTableOne(vars = cov, strata = "treat", data = df_trim, test = FALSE)
print(tab_trim, smd = TRUE)
```

```
##
                      Stratified by treat
##
                                      1
                                                     SMD
##
                         386
                                        185
##
     nodegree = 1 (%)
                         232 (60.1)
                                        131 (70.8)
                                                      0.227
     hispan = 1 (\%)
                                         11 (5.9)
##
                          60 (15.5)
                                                      0.314
##
     black = 1 (\%)
                          87 (22.5)
                                        156 (84.3)
                                                      1.578
##
     educ (mean (SD)) 10.47 (2.63)
                                      10.35 (2.01)
                                                      0.054
##
     age (mean (SD)) 26.21 (9.28)
                                      25.82 (7.16)
                                                      0.047
```

Compared to untrimmed data, the balance of nodegree, black and age appear to be improved while educ and hispan appear to be worsened.

6. Subclassification

[1] 571 12

First I will refit the model using the trimmed data and recheck the overlap.

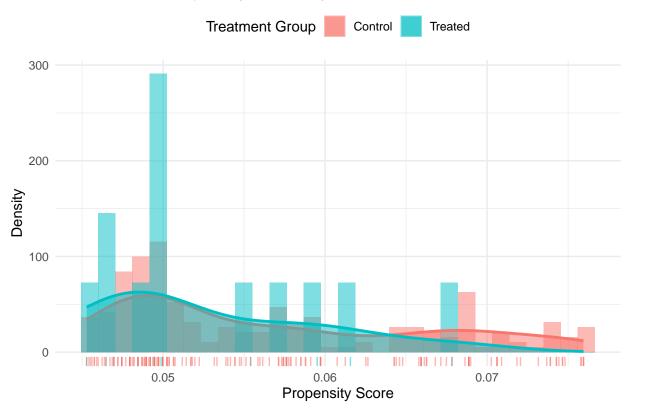
```
# fit PS model
ps.fit_trim <- glm(treat ~ nodegree + hispan + black + educ + age, family = "binomial", data = df_trim)
ps.fit_trim |>
broom::tidy() |>
kable()
```

term	estimate	std.error	statistic	p.value
(Intercept)	-4.4833461	1.0137243	-4.4226485	0.0000097
nodegree1	0.7219629	0.3302166	2.1863314	0.0287914
hispan1	0.9709541	0.4176188	2.3249772	0.0200732
black1	3.1925557	0.2824490	11.3031244	0.0000000
educ	0.1370930	0.0652493	2.1010666	0.0356351
age	-0.0008086	0.0129672	-0.0623585	0.9502774

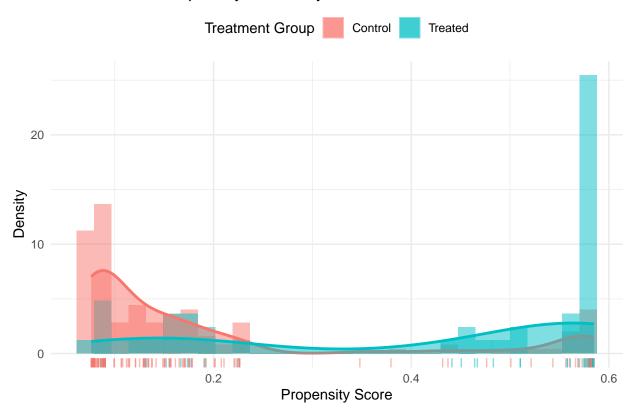
```
df.ps_trim <- predict(ps.fit_trim, type = 'response')</pre>
print(df.ps_trim[1:50])
            1
                        2
                                   3
                                                          5
## 0.71285226 0.17159272 0.58177585 0.71450459 0.62274896 0.65638382 0.58315243
##
            8
                       9
                                  10
                                             11
                                                         12
                                                                    13
## 0.71367914 0.70783841 0.05391550 0.65693075 0.61643370 0.62559424 0.68573839
                                                                    20
##
           15
                      16
                                  17
                                             18
                                                         19
                                                                                21
## 0.59316802 0.68713077 0.61528590 0.68643500 0.57980710 0.58256263 0.71516392
##
           22
                      23
                                  24
                                             25
                                                         26
                                                                    27
## 0.06931906 0.07187265 0.71499917 0.68730458 0.71417458 0.71483437 0.19133929
##
           29
                      30
                                  31
                                             32
                                                         33
                                                                    34
## 0.68747834 0.71499917 0.68747834 0.48518715 0.71483437 0.58374200 0.58275926
##
           36
                      37
                                  38
                                             39
                                                         40
                                                                    41
## 0.64440855 0.52408694 0.58315243 0.62027619 0.68626093 0.58354550 0.07290428
##
           43
                      44
                                  45
                                             46
                                                         47
                                                                    48
## 0.62578362 0.15339217 0.71565781 0.71483437 0.62578362 0.65729513 0.52408694
##
## 0.58315243
I will create three strata. The breaks are shown below.
df trim = df trim |>
  mutate(ps.strata = gtools::quantcut(ps.est, 3))
# breaks
quantile(df_trim$ps.est, probs = seq(0, 1, length.out = 4))
##
           0% 33.33333% 66.66667%
                                           100%
## 0.04528526 0.07594860 0.58492860 0.74288249
breaks = quantile(df_trim$ps.est, probs = seq(0, 1, length.out = 4))
# save dataset for each strata
df_trim1 = df_trim |>
  filter(ps.strata == "[0.0453,0.0759]")
df_trim2 = df_trim |>
  filter(ps.strata == "(0.0759, 0.585]")
df trim3 = df trim |>
 filter(ps.strata == "(0.585,0.743]")
```

Below is the histogram and density plot of the propensity scores in each stratum.

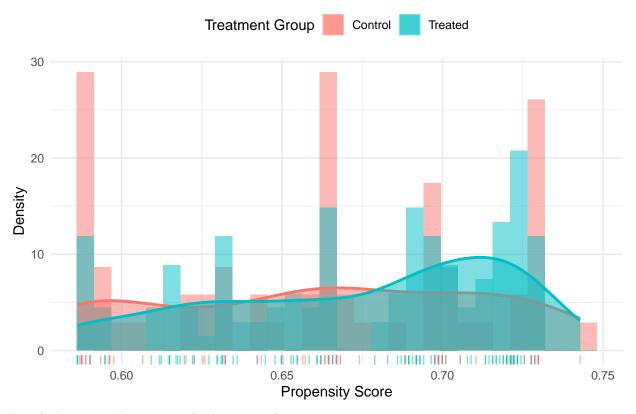
Distribution of Propensity Scores by Stratum 1



Distribution of Propensity Scores by Stratum 2



Distribution of Propensity Scores by Stratum 3



Now, let's inspect the covariate balance in each stratum.

```
# stratum 1
tab_trim1 = CreateTableOne(vars = cov, strata = "treat", data = df_trim1, test = FALSE)
print(tab_trim1, smd = TRUE)
```

```
##
                     Stratified by treat
##
                                                    SMD
##
                         180
                                        13
##
    nodegree = 1 (%)
                         80 (44.4)
                                         4 (30.8)
                                                     0.285
    hispan = 1 (\%)
                           4 (2.2)
##
                                         0 (0.0)
                                                     0.213
##
     black = 1 (\%)
                           0(0.0)
                                         0 ( 0.0)
                                                    <0.001
##
     educ (mean (SD)) 10.64 (2.68)
                                     11.08 (2.10)
                                                     0.180
##
     age (mean (SD)) 27.16 (8.63)
                                     27.85 (7.51)
                                                     0.085
```

```
# stratum 2
tab_trim2 = CreateTableOne(vars = cov, strata = "treat", data = df_trim2, test = FALSE)
print(tab_trim2, smd = TRUE)
```

```
##
                      Stratified by treat
##
                                                     SMD
##
                                         47
                         142
##
     nodegree = 1 (%)
                         105 (73.9)
                                         22 (46.8)
                                                      0.577
                          56 (39.4)
     hispan = 1 (%)
                                                      0.351
##
                                         11 (23.4)
##
     black = 1 (\%)
                          23 (16.2)
                                         31 (66.0)
                                                      1.172
     educ (mean (SD)) 10.24 (2.77)
                                    10.09 (2.76)
                                                      0.056
##
```

```
## age (mean (SD)) 25.98 (9.63) 26.38 (6.96) 0.048
```

```
# stratum 3
tab_trim3 = CreateTableOne(vars = cov, strata = "treat", data = df_trim3, test = FALSE)
print(tab_trim3, smd = TRUE)
```

```
##
                    Stratified by treat
##
                     0
                                                   SMD
                                    1
                                      125
##
                        64
    n
##
    nodegree = 1 (%)
                        47 (73.4)
                                      105 (84.0)
                                                    0.260
##
    hispan = 1 (%)
                         0 ( 0.0)
                                       0 ( 0.0)
                                                   <0.001
    black = 1 (%)
                                                  <0.001
##
                        64 (100.0)
                                      125 (100.0)
##
    educ (mean (SD)) 10.50 (2.09)
                                    10.37 (1.63)
                                                    0.070
     age (mean (SD)) 24.06 (10.01) 25.39 (7.20)
                                                    0.152
##
```

7.

8.

9. The advantage of regression based approach is that it can be applied to