$VING KIT HUI 2993849 Growdnate Level $ RIa. To sum up, we get $C_0 = 2 = 9^{2} (14u - 12) \qquad (1)$ $C_0 = 1.5 = 9^{2} (14u - 13.5) \qquad (2)$ (1) $C_0 = 1.5 = 12u - 12$ (2) (1) $C_0 = 1.5 = 12u - 12$ (2) (1) $C_0 = 1.5 = 12u - 12$ (2) $C_1 = 1.5 = 12u - 12$ $C_2 = 12u - 12$ $C_3 = 12u - 12$ $C_4 = \frac{4}{5}(3.5 - 12 = 6)$ $C_6 = \frac{3}{12}(14u - 13.5) = 12u - 12$ $C_7 = \frac{3}{5}(14u - 13.5) = 12u - 12$ $C_8 = \frac{3}{5}(14u - 13.5) = 12u - 12$ $C_9 = \frac{3}{5}(14u - 12.5) = 12u - 12$ $C_9 = \frac{3}{5}(14u - 12.5) = 12u - 12$ $C_9 = \frac{3}{5}(14u - 12.5) = 12u - 12$		
	4	VING KIT HULL 20933849 Grandwate Level
	RIa.	
	1.0	Co = 2 = 2 (1du-12) (1)
		$C_0 = 1.5 = 2^4 ((au - 13.5)$ (2)
		(1) => d = lan - (d
	-	=> { (du -13.5) = 120 -12
		=) ((\frac{1}{12} = 12 = (
	C	=> u = 3/2
	5	7 hus by (1) 2 = 2 (1d. 3 -(2)
		=> 4* 1
	•	
	•	Also $g^* = \frac{1-\alpha}{q-d} = \frac{1}{2-d} = \frac{1}{3}$
		=> 3(1-d) = \frac{2}{2} - d
	· •	
	~	
	~	max (15-124,0) = max (15-12-3,0) = max (15-16,0)=0
	•	
		= mx((5-1da,0) = max((5-(d-7,0) = max(15-9,0) =6
	Lee .	By risk - neutral valuation,
	æ	
	1 20	
		$=$ $(1-3^4)\cdot (=\frac{2}{3}\cdot 6=4)$
	4111	
Alloy		n strike price of \$15 so \$4.
Millory Millory	11	
Action Action	<u> </u>	
Hillory		
		Hillion

QIL) Let Tt denote our portfolio at time t.
	let 1/4 and 84 to denote the amount of
	bond and stock that we hold at time t.
	Thedas a short position in the next online
	To hedge a whost position in the put option
	sperified in (a) amounts to find yo, so site
	the portfelio To = -Po + 70 + 80 So
	short houd stock
	has the value $\Pi_T = 0$ at espiny time T .
	So m want TTT = -PT + 10 et + So ST =0
	(0 0 1 0 0
	(=> no ett & SoST = PT.
	That is , we want to replicate the payoff PT,
	thus amounts to solve the following Chared on our
	binomial model)
	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$
	(8)
	noting that et = e = 1.
	6
	(#) =) yo + 3.12.80 = 0
	ho + 3/4.1d. So = 6
	=) (2(3/4) So = -6
4 (M () () () () () ()	$\delta_0 = -\frac{2}{3}$
	=> $\eta_0 = -\frac{1}{2} \cdot a \cdot \delta_0 = -\frac{3}{2} \cdot a \cdot (-\frac{7}{3}) = 12$
	-1 10 - 1 - 2 - 73) - 186
	Thus, So 1/2 unit of the underlying is required at
	t=0 to heave. That is, we need to short
	2/2 we went to short
	is ant of the stock and long ld dollars of bone
	to hedge. Hillory
500	

(B)	
65	
(5)	
	, D
alc alc	We use the notation $E(\cdot)$ and $E^{\alpha}(\cdot)$ for
7	expendation where outreal mobability to and under
100	expectation under actual publishing p and under risk neutral expectation of respectively.
<u></u>	Kish heartan dependency of the second had again
0	Then, using actual probability p, the expected appear
(3)	payobs for the lampean put in (a) is
73	10
	(PT) = p.0 + (1-p).6 = 6(1-p)
	Priving this put option at this expected payoff value will
40	come and free it has a
-10	Now we demostrate how to construct artitrage
	Now we demostrate now to constitute of PIP)
(i)	assuming p = g* and suppose Po is given by EP(PT)
***	(ax): p>g*, equivalently 1-p<1-g*.
**	
-3	Then Po = EP(PT) = (1-p)6 < (1-2*)6 = EQ(PT)=4
	So instrictly, this put is unobeapsived.
	Construct protholio by
-	Contract porterio by
	To = Po - (Mo + So So) < 0
-	ζΨ = Ψ
49	
49	(note that $y_0 + \delta_0 S_0 = a + \frac{3}{2} \cdot a = 4.$)
4	
4	and TIT = PT - (no + 8.0 ST)
-	= P _T - P _T = 0
	since ho, so are chosen s.t.
	η o t δoST = PT under each
	svenario in Linounial model).
	This is an arbitrage since To <0, TT =0.
10	Kilroy
Lo	

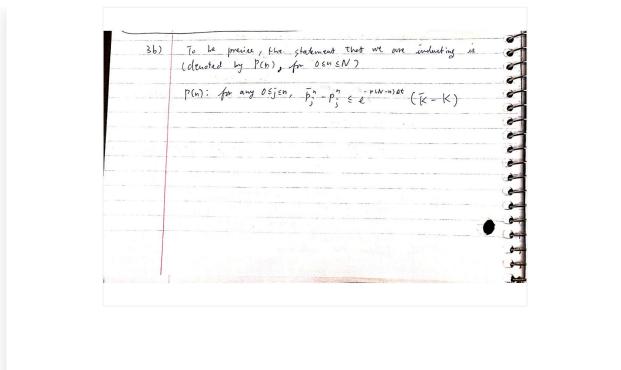
Cased:	p < g * , equivalently 1-p > 1- & *.
	So Po = EP(PT) = 6(1-p) > 6(1-g*) = 4=1
	So, intuitively, this put is orrespoised.
	Construct prontfolio by
	X-4 = 4
	Then TT = -PT + (40 + SO ST)
	$=$ $-P_T + P_T = 0$ So To < 0 , $T_{T} = 0$, this is an arbitrage.
	So To CO, TT = 0, this is an arbitrage.
	Hilton
	Stephen State of the Control of the

	**
49)	E[S(++0+)[S(+)]
	= 5(t)u. g + 5(t).d (1-g)
	Note 44 (1-2)
	Note $\frac{\sqrt{2} + o(1-2)}{e^{-\sqrt{16}\epsilon} - e^{-\sqrt{16}\epsilon}} + e^{-\sqrt{16}\epsilon} \left(\frac{e^{-\sqrt{16}\epsilon} - e^{-\sqrt{16}\epsilon}}{e^{-\sqrt{16}\epsilon} - e^{-\sqrt{16}\epsilon}} \right) = 0$
	= constant color+rat
	= e - e - e - e
	= erec
	Heure [[sittaer sit]] = 5(4) 2 . 4 . 5(4) . d(1-2)
	= S(+) e rat
b)	Var [51++0+) 5(+)]
	Note E[Sitemen Site] - E[Scetaen Sites]
	E[S(++0+) S(+)] = S(t)u · g + S(+)·d (1-g) Note ug + d(1-g) = e ^{-lot} (e ^{-nt} - e ^{-lot}) + e ^{-lot} (e ^{-lot} - e ^{-lot}) = e ^{-lot} (e ^{-nt} - e ^{-lot}) + e ^{-lot} (e ^{-lot} - e ^{-lot}) = e ^{-lot} (e ^{-nt} - e ^{-lot}) + e ^{-lot} (e ^{-lot} - e ^{-lot}) = e ^{-lot} - e ^{-lot} = e ^{-lot} - e ^{-lot} = e ^{-lot} - e ^{-lot} = s(+) u · g + S(+)·d(1-g) Note [S(++0+)]S(+)] = S(+) u · g + S(+)·d(1-g) = S(+) u · g + S(+)·d(1-g) Note [S(++0+)]S(+)] = S(+) u · g + S(+)·d(1-g)
	and riz + da (1-8)
	e e lat (e e e e late e e e e e e e e e e e e e e e e e e
	e star - e star
	= -e te terot (errot - zrot) e cot - e tot
	= -1 + e rat (e rate + e rate)
	$= e^{\frac{2\sigma Tat}{e^{\frac{\sigma Tat}{e^{-\frac{\sigma Tat}{e^$

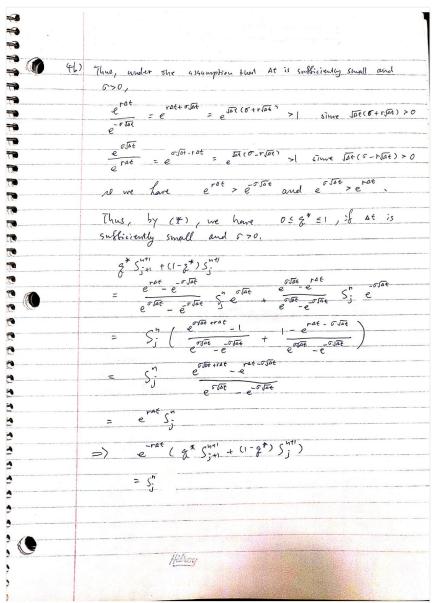
2	
€	
2	
3 6	2. \ \ \[\(\(\lambda \) \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \
3	Heme, Vour [Sit+10t) 2 Sit) = Sit) (-1+erot (e or to +e or face))
≥	= 5(t) (-1+e (e +e))
≩	- sitize wat
⊋	ant)2
≆	but $e^{rot} = \left[+ rot + \frac{(rot)^2}{2} + \dots \right]$
₹	= 1 + r D + O (D 6 2)
€	1 law Town or expansion?
3	Similarly e otat = 1 + otat + (tag) +
€	5 (mileny e = (+ 6) se + 2
	$= 1 + c \sqrt{50c} + \frac{c^2 at}{2} + \frac{c^3 (at)^{3/2}}{6} + O(cat^2)$
4	$\frac{2}{624t} = \frac{634t}{634t} = \frac{34t}{640t^2}$
\$	e 1 - 0/0+ + = - 6 + 00000)
4	$= \frac{e^{-r_{1}at}}{e^{-r_{1}at}} = \frac{e^{-r_{1}at}}{e^{-r_{1}at}} + \frac{e^{-r_{1}at}}{e^{-r_{1}a$
\$	- (1+rAt + (2(At2)) (e 1 + e -)
\$	C18t _ 18t
4	T(AF -0 170)
4 FB	+ (rat + 0 (at2))(e 1 + e = e riot + e -riot + (rat + 0 (at2))(2 + (0 (at2)) = e riot + e -riot + 2 + 0 (at2)
4 6	Flat - That 3 - At + (O(At2)
•	
· Su,	5/5(6)=5(6)2(-1+ e olac + e olac + 2rat + ()(a+2)) -5(6)e iran
4 Vour Sittat	[] [S(B)] = > (E) (-1 + & +E + C+BC + O(1-0)
(by (*)	= 514)2 (-1+2+ 52At + 21At + ()(At21)
4	- 700, 4
4	= 5(t)2 (1+ 2rac + 62 st + 0(4t2))
4 (Taylor expansion	= 5/6/2 (1+ 2rst + (0 (pt2))
(Taylor expansion for expansion)	= S(t)2 (02 At + (0(At2)) = S(t)2 [01 At + (0(At)2]
4	
4	noting that e lat + e - lat = +0 lot + 62 At + 63(At) 1/2 + (6(At))
4	+1 - otat + \frac{7}{2} - \frac{03}{4} (at) \frac{1}{4} + \text{(Cat}^2
4	+1-1106+ = -6 +000
4	$= \lambda + \sigma^2 \Delta t + (0(\Delta t^2))$
4	
4	and $O(\Delta t^2) = O(\Delta t)^2$
* (AND THE RESERVE AND ADDRESS OF THE PARTY OF
# (()	Hilroy -
4	

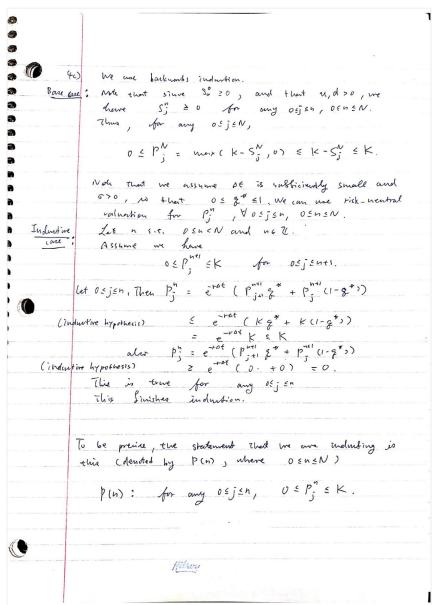
	Construct a partfelix by $ \overline{\Pi}_{0} = e^{-rT}(E-K) - (\overline{P}_{0} - \overline{P}_{0}) $ $ = e^{-rT}(T_{0} - K) - \overline{P}_{0} + \overline{P}_{0} $ This lead short lang puts $ \overline{\Pi}_{0} = e^{-rT-E}(E-K) - \overline{P}_{0} + \overline{P}_{0} $ Will lead short lang puts $ \overline{\Pi}_{0} = e^{-rT-E}(E-K) - \overline{P}_{0} + \overline{P}_{0} $ With $\overline{\Pi}_{T} = \overline{K} - K - \overline{P}_{T} + \overline{P}_{T}$ Let SCT be the mice of undanging at expiry T . If SCT is \overline{K} , then $ \overline{P}_{T} = unix(\overline{K} - SCT), 0) = 0 $ $ \overline{P}_{T} = unix(\overline{K} - SCT), 0) = 0 $ and so $\overline{\Pi}_{T} = \overline{K} - K - (\overline{K} - SCT) + 0$ $ = SCT) - \overline{K} \geq 0 $ If SCT is \overline{K} , then $ \overline{P}_{T} = \overline{K} - SCT $ and so $\overline{\Pi}_{T} = \overline{K} - K - (\overline{K} - SCT) + K - SCT $ ound $\overline{N}_{T} = \overline{K} - SCT $ ound $\overline{N}_{T} = \overline{K} - K - (\overline{K} - SCT) + K - SCT $ Thus, we we shall in any case. $ \overline{\Pi}_{T} = 0 $
Q3a	Construct a portfolio by
	1, = e ⁻¹ (E-K) - (p, -p,)
	= e (1x-1x) - Po +10
	full hand short lang put
	10 Te = e (F-k) - Pe+Pe for 0665T.
	Note TTT = K-K-PT+PT.
	Let SCT) be the price of underlying at expiry T.
	14 S(T) > k, then
	PT = max (K-SCT), 0) = 0 , PT = max (K-SCT), 0) = 0
	and No 11 = k-K >0.
	18 Kissit) (K, then
7,17	$\bar{P}_{T} = \bar{k} - sc\tau$
	$P_{T} = 0$ and so $T_{T} = \overline{k} - k - (\overline{k} - S(T)) + 0$
	= SCT) -K ≥0
	9
	If ScT) < K, then
	PT = K - S(T)
	$P_{T} = \left(\frac{1}{2} \cdot S(T) \right)$
	and $\overline{M} = \overline{K} - K - (\overline{K} - S(T)) + K - S(T)$ $= 0.$
	Thus, we see that in any case,
	Tip 20.
	Thus, no arbitrage implies that
	The 20 , for all 056 21.
	Otherwise if It <0 for some 05 t<1, Then we
	can love this portfolio (obtaining with - Te) and short
	this protetion at time T, 6 htmining Tit 20, this is an arbitrage.
	3

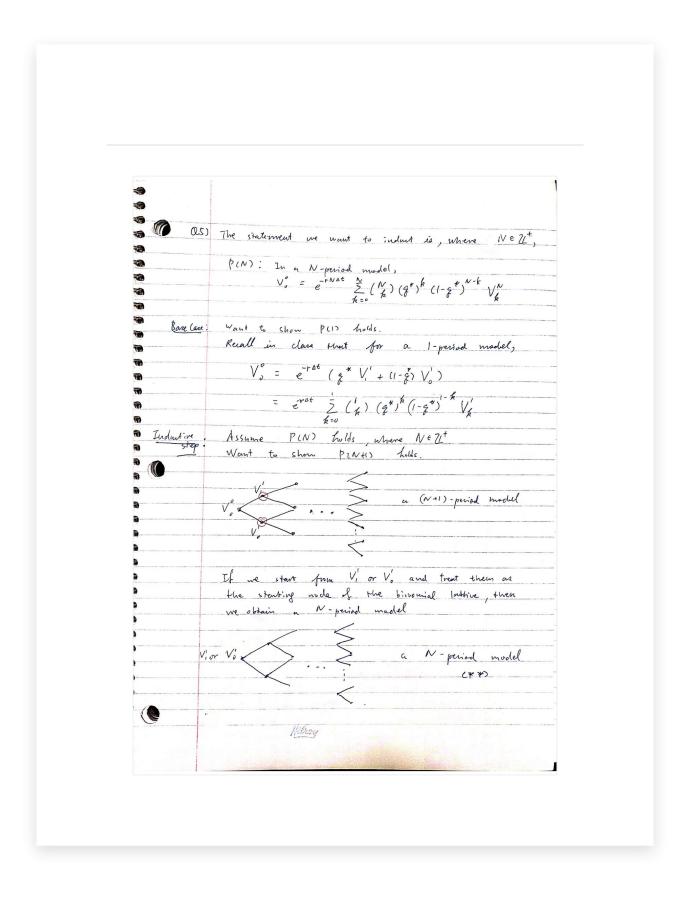
5	
) B	
	Tto for OileT implies
	the story of the supplies
	$T_{l_{\xi}} = e^{-r(T-t)} (\bar{k} - k) - (\bar{p}_{\xi} - p_{\xi}) \ge 0$
	$=) \qquad \stackrel{\text{Pe}}{=} \stackrel{\text{Pe}}{=} e^{-r(T-\ell)} \left(\stackrel{\text{F}}{=} -k \right).$
	36) We me back wards and time Evenley St introling for militing
Q.	as in fernie
	Base Cone: P" = max (K-5",0) - max(K-5",0)
- -	5-1; = max (K-), ,0) - mex(K-5;,0)
	(E-K of si ck
	= { \vec{k} - \vec{k} \ \vec{s} \ \vec{k} \ \vec{s} \ \vec{k} \ \vec{s} \ \vec{k} \ \vec{s} \ \v
	\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \
	(o if K =).
)	r(N-N) 4 t
	< k-K= e (F-K)
)	hoting that if $K \leq S_{j}^{N} < \widehat{K}$, then
	K-SM 5 K-K
	K-SN = K-K. (which is equivalent to SN ≥ K.)
	Industive care: Let n s.t. Osn < N, n & 2 and Osjen.
	1554me we have P-1 p not se (K-(K-)) St (K-(K))
	for 05 = n+1.
	Let go = erat_d. (We use risk-neutral valuation.)
	Let g = u-d, (ve wa pill-neutral valuerion.)
))	7 / 0/569
· · · · · · · · · · · · · · · · · · ·	Then for DSj En,
;	P; -P; = e (& P;+++ (1-8") P; - & P;++- (1-8") P;
	1; -1; = e (\f \mu_{j+1} + (1-\f _2) \mu_{j} - \f \mu_{j+1} - (1-\f _2) \mu_{j} - \f \mu_{j+1} - (1-\f _2) \mu_{j} - \f \mu_{j} - (1-\f _2) \mu_{
	= e rec (2 ([] 1 - [] 1) + (1-2) ([] 1 - [] 1))
	TPT W n.N.n-12Af -
	(industrie 3 e (q e rando)
//•	mypothesis/ + (1-5") e (F-K))
	(industrie $\leq e^{-r(N-n-1)\Delta t}$ (\bar{k} - k) hypothesis) $+ (1-\xi^{\theta}) e^{-r(N-n-1)\Delta t}$ (\bar{k} - k)) $= e^{-r(N-n)\Delta t}$ (\bar{k} - k).
	This finishes the industion.
,	(with finishers have become

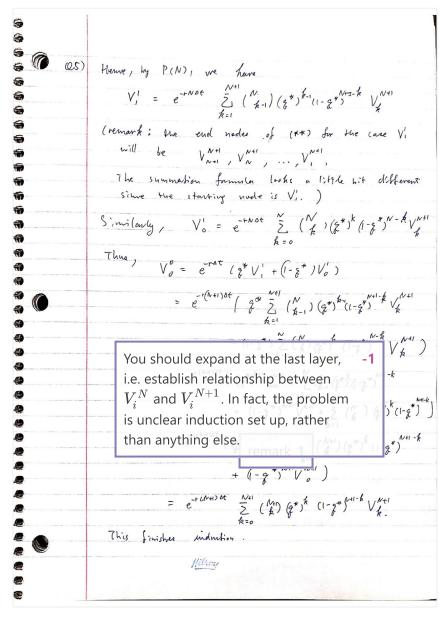


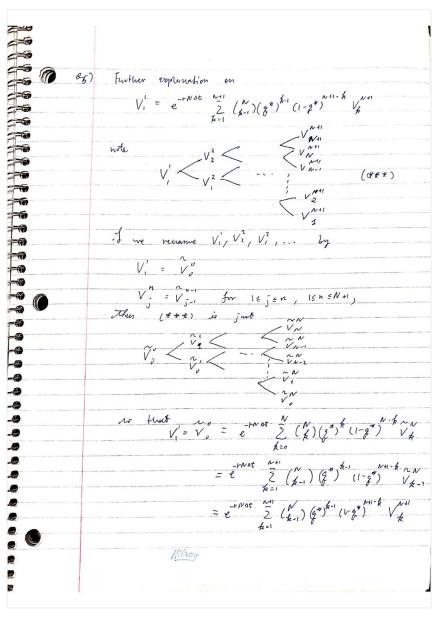
1	
	u.
	$S_{j+1}^{n+1} = u S_{j}^{n}$ $S_{j}^{n+1} = d S_{j}^{n}$
	S; 5, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1,
	Note that SN = dN So = (e stat) NS.
	$= S, e^{-sN\sqrt{\frac{1}{N}}}$
	= So e-ORIT
	hating that $\Delta t = \frac{T}{N}$. Thus, $\Delta t > \frac{T}{N} \to 0$ iff $N \to \infty$.
	Thus, $\Delta t > \overline{\lambda} \rightarrow 0$ iff $N \rightarrow \infty$.
	Thus we me that $S_0^N = S_0 e^{-c \sqrt{N} \sqrt{T}} \longrightarrow 0 \text{ as } N \longrightarrow \infty$ Thus
	Thus PN = max (K-SN,0) -> K as N-20.
	Since $S_0^{\prime\prime} \rightarrow 0$ and $K \ge 0$.
	b> Recall that $g^2 = \frac{e^{rat} \cdot d}{n-d} = \frac{e^{rat} - e^{-rat}}{e^{-rat}}$, Assume $s > 0$.
	Then, we me p & g & s1
	ill 0 = erot = rote = 1
	(*) if (e-out erot and erot erot)
	Note in (6+ rot) = 6.
	and lim (0-150) = 0. Hence if st is sufficiently small and 0 = 0, thou we have
A THE REAL PROPERTY OF THE PARTY OF THE PART	6+ rlat > 0 and 6-rlat > 0,
0	and so sate (6+rsat) >0 and sate (6-rsat) >0.











79		
	6. Consider G(Z,t); IR → IR defined by	
-	$G(s,t) = \frac{1}{2} z^2 - \frac{t}{3}$	
	Thun 24 = 3 34 = 1	
-	$\frac{\partial^2 \theta_1}{\partial z^2} = 1$	
-10	by Ho's Lemma, $d G(\xi(t),t) = \frac{\partial G}{\partial \xi}(\xi(t),t) \cdot d\xi(t) + \frac{\partial G}{\partial \xi}(\xi(t),t) dt$	
(note (d 20	22/2 2. 2	
	$= \xi(\xi) d\xi(\xi) - \frac{1}{2}d\xi + \frac{1}{2}d\xi$	
	= \frac{2}{2}c(4) \text{A}\frac{2}{3}(4)	
	Heme G(Z(T),T)-G(Z(0),0) = JT Z(+) dZ(+)	
~~ ~	$=) \int_{0}^{T} z(t) dz(t) = G_{1}(z(\tau), T)$ $= \frac{1}{2} z(\tau)^{2} - \frac{T}{2}$	
-3	$\frac{2^{2(1)}-2}{\sin \omega} = \frac{1}{2} \cdot 0^{2} - \frac{\omega}{2} = 0$	
	Milroy	
40		