P-adic Numbers

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8 Talk 8 - Elementary Analysis in Qp

8.1 TODO p-adic mean value theorem

8.2 Problems with derivatives:

- There exist Injektive Functions with derivative zero at some points, so the zero derivative does not imply that a function is locally constant in Q_p

9 Talk 9 - Strassman's Theorem and the Logarithm Function